Nonlinear, interacting responses to climate limit grassland production under global change

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Global changes in climate, atmospheric composition, and pollutants are altering ecosystems and the goods and services they provide. Among approaches for predicting ecosystem responses, long-term observations and manipulative experiments can be powerful approaches for resolving single-factor and interactive effects of global changes on key metrics such as net primary production (NPP). Here we combine both approaches, developing multidimensional response surfaces for NPP based on the longest-running, best-replicated, most-multifactor global-change experiment at the ecosystem scale—a 17-y study of California grassland exposed to full-factorial warming, added precipitation, elevated CO2, and nitrogen deposition. Single-factor and interactive effects were not time-dependent, enabling us to analyze each year as a separate realization of the experiment and extract NPP as a continuous function of global-change factors. We found a ridge-shaped response surface in which NPP is humped (unimodal) in response to temperature and precipitation when CO2 and nitrogen are ambient, with peak NPP rising under elevated CO2 or nitrogen but also shifting to lower temperatures. Our results suggest that future climate change will push this ecosystem away from conditions that maximize NPP, but with large year-to-year variability.

California grassland | climate change | ecosystem ecology | global change experiment | Jasper Ridge

Across the globe, terrestrial ecosystems are experiencing simultaneous changes in climate, atmospheric composition, pollutant deposition, and broad-scale changes in land use, biological invasions, and disturbance regimes, including wildfire. How ecosystems respond will have profound consequences for the goods and services they provide for humans, including feedbacks to atmospheric composition and climate. Predicting ecosystem responses to these global changes is challenging due to the number of factors and the possibility of interactive effects across physiological, ecological, and biogeochemical aspects of ecosystem function. Manipulative experiments, which can resolve single-factor and interactive effects, can effectively address these challenges, especially when focused on metrics such as net primary production (NPP) that integrate across many levels of biological organization (e.g., ambient and +2 °C warming, making it difficult to connect experimental results to real-world responses). All experiments involve only two levels of each factor (e.g., ambient and 1647 7 g m–2·yr–1, commensurate with variation in ANPP (173–784 g m–2·yr–1)). Using several approaches, we tested for but found no consistent year-to-year temporal trends in the signs, magnitudes, or significance of single-factor or interactive effects of the global change factors on NPP or its components (Methods and SI Text). In addition, there

Significance

Global environmental change involves many factors that occur simultaneously, yet they are usually studied in isolation. Here we report a long-term global change experiment that subjected California grassland to multiple individual and simultaneous changes in temperature, precipitation, carbon dioxide, and nitrogen. Our analysis revealed nonlinear and interactive effects of temperature and precipitation on grassland net primary production (NPP), which defined a ridge-shaped NPP response surface to these two variables. Added nitrogen raised the peak of the NPP response surface, and added CO2 shifted the peak to lower temperatures. Our approach was validated by tests showing an absence of progressive effects over the years. In other ecosystems, our approach may be similarly powerful for probing the effects of multifactor global change.

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were no consistent year-to-year trends in the relative abundance of the major plant functional groups (Fig. S1). The absence of time dependence opens a novel path for analyzing primary production—treating years as independent realizations of the experiment, and analyzing NPP, ANPP, and BNPP as continuous functions of each of the four global change factors. This approach takes advantage of 17 y of natural variation in temperature and precipitation as well as the treatments, which together filled the environmental space nearly uniformly across a 3.6 °C range in mean temperature during the growing season and a sixfold variation in precipitation (240–1,379 mm). CO₂ and nitrogen levels remain nearly categorical owing to background variation and trends that are small relative to the magnitude of the treatments (Fig. 1). This approach allows consideration of many sources of variation, including fires in 2003 and 2011 that are not discussed here (Methods). Although the analytical model tests simultaneously for single-factor and interaction effects, we start by discussing the single-factor responses of NPP, ANPP, and BNPP. Then, we explore combined single-factor and interactive effects of the continuous factors and test for progressive

![Graphs showing NPP, ANPP, and BNPP responses to temperature, precipitation, CO₂, and nitrogen across experimental (treatment) and natural (year) variation. Each symbol represents the average production (mean ± SE) in the ambient (open circle) or elevated (filled triangle) treatment in 1 y.](image-url)
effects. Finally, we use the results of the continuous model to create temperature-by-precipitation response surfaces for NPP under the four factorial combinations of CO2 and nitrogen.

Single-factor responses vary in form and magnitude across the global change factors (Fig. 1). Warming generally had negative effects on production, with a slightly hump-shaped (unimodal) response for BNPP. Responses to precipitation are hump-shaped, peaking when precipitation is near (ANPP) or slightly above (BNPP and NPP) the 40-y mean growing season precipitation at Jasper Ridge (590 mm). Elevated CO2 had no significant impact, tending to increase ANPP and decrease BNPP, summing to no response for NPP. Nitrogen addition increased ANPP by 38%, BNPP by 4%, and NPP by 23% (Fig. 1).

We developed linear mixed-effects models (Methods and SI Text) that provide results for both the main and interactive effects as standardized coefficients (Fig. 2 and Table S1). These coefficients indicate the proportional change in NPP in response to one SD change in an environmental factor. The model fit to observations is good, with 54–68% agreement, and the residuals do not show time dependence, providing additional evidence of a lack of progressive effects (Methods and SI Text). The main effects from the joint model reinforce the patterns in the single-factor plots (Figs. 1 and 2). The quadratic coefficients for temperature and precipitation are negative for production components that have hump-shaped responses to those factors, and the temperature and precipitation coefficients are negative for production terms that decline linearly or peak at low values. BNPP, the only term that peaks at higher levels of precipitation, has a positive precipitation coefficient. Main effects of nitrogen are positive and substantial for NPP and ANPP, corresponding to more than a 20% increase in both ANPP and NPP at the elevated treatment level. Elevated CO2 has no consistent effect on NPP (Fig. 2). In addition to the main effects, five interactions are significant. The temperature–precipitation interaction is positive for NPP, indicating that the negative effects of warming and precipitation are intensified when combined. Other two-way interactions involve factors whose main effects are opposite in sign; their interpretation is aided by the response surfaces that follow.

The modeled main effects and interactions define multidimensional response surfaces in which the response of NPP to temperature and precipitation is basically a ridge, with maximum NPP occurring at intermediate levels of precipitation and

![Fig. 2.](image-url) Main effects and interactions of temperature (T), precipitation (P), CO2 (C), and nitrogen (N), and quadratic effects of temperature (T^2) and precipitation (P^2), on primary production. Coefficients are summarized as point estimates (circles) and 95% confidence intervals (CIs, lines) for NPP and its components (colors), highlighting significant coefficients (filled circles) whose 95% CIs do not overlap zero (bold lines). Coefficients are standardized as proportional change in primary production with respect to one SD change in T, P, C, and N (T: 0.99 °C, P: 289 mm, C: 148 μmol·mol⁻¹, and N: 3.55 g·m⁻²·y⁻¹).
temperature (Fig. 3). When CO2 or nitrogen deposition is elevated, the peak of the NPP ridge is higher and displaced to cooler temperatures, sloping downward as temperature increases. The precipitation that maximizes NPP drops from about 800 mm at ambient CO2 to about 600 mm at elevated CO2 (Fig. 3). The response surfaces are similar for the above- and belowground components of NPP (Figs. S3 and S4), but with ANPP reaching its maximum under drier conditions, and BNPP under wetter conditions.

The responses of NPP to nitrogen deposition parallel results from other studies. Like grasslands globally (10–12), California annual grassland is nitrogen-limited, and nitrogen deposition relieves some of this limitation (13–15). The absence of single-factor effects of elevated CO2—with trends toward a small positive effect on ANPP and a slight negative effect on BNPP—are consistent with earlier results from Jasper Ridge (14–16) and confirm earlier results indicating lower CO2 sensitivity than reported for other grasslands (12, 17). The shift of maximum NPP to drier conditions under elevated CO2 (Fig. 3) is consistent with improved water-use efficiency in plants with C3 photosynthesis growing under elevated CO2 (18).

The response of NPP to temperature points to effects of multiple controls on photosynthesis and growth. Under ambient nitrogen deposition, the effects of warming on NPP depend on precipitation—NPP declines with rising temperature at low precipitation but increases with temperature at high precipitation. With elevated nitrogen deposition, warming leads to decreased NPP at all precipitation levels. Under ambient nitrogen, the optimum temperature for NPP is close to the long-term average, 9.94 °C, but it drops to about 1 °C lower with nitrogen deposition (dashed lines in Fig. 3). The negative effect of warming likely is influenced by NPP gains in winter outweighed by losses in spring. Gains in NPP from warmer winter temperatures are small because plant growth in winter is also limited by low irradiance and short days (16). In spring, when conditions are consistent with rapid biomass accumulation by vegetative plants, warming decreases NPP through accelerated phenology: Warming hastens flowering (6) and senescence (5) in the JRGCE, effectively wasting part of the growing season.

Elevated CO2 has subtle effects on the response surface (compare left and right panels in Fig. 3), shifting peak NPP to lower temperatures. Because this is opposite the response expected based on the physiology of C3 photosynthesis (19), it may reflect a temperature sensitivity of autotrophic respiration or exudation larger than that of photosynthesis.

The hump-shaped response of NPP to precipitation helps unify divergent results about the dependence of California grassland NPP on the amount and timing of precipitation (20–22). Had our experiment spanned significantly less than a sixfold range in precipitation, we would have concluded that NPP increased,

Fig. 3. Modeled and observed NPP in four-dimensional temperature–precipitation–CO2–nitrogen space. Axes are continuous gradients for temperature (8.69–12.28 °C) and precipitation (240–1,380 mm), as well as categorical levels for CO2 (ambient 409 μmol·mol−1, elevated 680 μmol·mol−1) and nitrogen (ambient 0.25 g·m−2·y−1, elevated 7.25 g·m−2·y−1). Observed values (bubbles) are the average NPP in the corresponding environmental conditions. Modeled values (surfaces with contour lines) are predictions from models fitted with observations spanning the environmental space. Dashed lines are references of long-term averages of temperature and precipitation at Jasper Ridge.
decreased, or was unaffected by variation in annual precipitation. Had our precipitation treatment significantly altered the seasonal distribution of rainfall, rather than amplifying natural variation, shifts in plant community composition likely would have altered the NPP response (22).

Nonlinear responses of ANPP to precipitation occur in other grasslands and other biomes (23–25) but tend to be saturating rather than the symmetrical NPP response we observe. Decreasing NPP at high precipitation input at Jasper Ridge may be related to generally cloudy growing seasons in the wettest years or to nutrient leaching, especially with the highest (manipulated) inputs. Evidence that extremely high rainfall can be detrimental to grassland NPP is supported by measurements of ecosystem carbon balance. The wettest year during the JRGCE (2004; 20°C growing season) had the lowest ANPP, and, based on CO2 balance, the grassland was a net carbon source (16). The next year was dry, ANPP doubled, and the ecosystem was a net carbon sink (16).

At Jasper Ridge and in grasslands globally, year-to-year variation in temperature and precipitation is substantial, often dramatic. In the JRGCE, the combination of single-factor and interactive effects results in NPP peaking under conditions close to the historic averages and falling off when a year is, as a result of either natural variability or experimental manipulation, substantially different from the average. If this kind of response is typical across grasslands and other ecosystems adapted to nonconstant climates, future climate variability, future climate change will tend to erode NPP as conditions diverge from historic. Changes in disturbance, herbivory, pests, pathogens, or other agents that alter plant community composition and function potentially can, of course, lead to additional layers of responses.

Many papers have discussed the expected role of progressive effects (26), but their absence in the NPP responses of the JRGCE is not entirely surprising. First, the large interannual variation in climate may act as an effective reset mechanism. Second, the species mix is largely reset annually, based on natural variability, future climate change will tend to erode NPP as conditions diverge from historic. Vegetation changes in disturbance, herbivory, pests, pathogens, or other agents that alter plant community composition and function potentially can, of course, lead to additional layers of responses.

Methods

Experiment. The JRGCE is located in the Jasper Ridge Biological Preserve, San Mateo, California (37°24’N, 122°14’W). The site occupies ~0.75 ha within a 4.5-ha stand of California annual and perennial grassland and has a Mediterranean climate with cool, wet winters and warm, dry summers. Over the period from 1998 to 2014, annual precipitation, which occurs almost entirely from November through April, varied from 240 to 1,280 mm. In summer 1997, we established 36 circular plots 2 m in diameter, subdivided into four equal-sized subplots. The 1997–1998 growing season (year 1) was a pre-treatment year, after which treatments were applied for 16 consecutive growing seasons (years 2–17), from the time of germination (November) to plant senescence (June).

Treatments consisted of four global change factors—temperature, precipitation, CO2, and nitrogen—at either ambient or an elevated level, applied in a complete factorial, randomized block design with eight replicates. Factorial combinations of CO2 (via free-air CO2 enrichment) and warming (via heaters suspended above the plot) were applied at the whole-plot level. The CO2 treatment was targeted at +300 μmol mol−1 over background via free-air CO2 enrichment; the ambient enrichment was +275.3 μmol mol−1 over the level measured in low plots, which averaged +32.8 μmol mol−1 higher than the CO2 concentration measured at the Mauna Loa observatory (28). The warming treatment increased from +30 W m−2 (years 2–5), to +100 W m−2 (years 6–12), to +250 W m−2 (years 13–17). Within each plot, the four subplots received factorial combinations of precipitation (via emitters mounted outside the plot perimeter) and nitrogen deposition (via nitrogen addition). The precipitation treatment was +50% of ambient rainfall, plus two 10-mm additions after the last rainfall event. The nitrogen treatment was +2 g N m−2 y−1 as nitrate solution in November and +5 g N m−2 y−1 as nitrate pellets in late January or early February. An additional four plots (controls for the treatment infrastructure and received no treatments. A wildfire spread into the JRGCE in July 2003, affecting two blocks of the experiment. In July 2011, replicate prescribed burns were carried out across four of the blocks, including the two blocks that burned in 2003. The ecosystem responses included NPP (grams per square meter per year) and its components ANPP and BNPP, which were measured as dry biomass. For aboveground biomass, we harvested all plant matter in a 141-cm2 area as each subplot at the peak of standing biomass. In years 1-3 we harvested biomass once (in May), and in years 4–17 we harvested from each subplot twice: the first one timed to peak biomass in the phenologically most advanced plots (mid-April to early May), and the second one 3 wk later at the peak of less advanced plots (early to late May). The locations selected each year to avoid harvesting the same spot for at least three years. In both harvests, we separated out the litter and weighed the oven-dried biomass (70 °C). In this study, we analyzed the aboveground biomass from the single harvest (years 1–3) and the maximum of the two harvests (years 4–17). After the first aboveground harvest we took four soil cores from the harvested area, two shallow (0–15 cm) and two deeper (15–30 cm), and the cores from a given depth were combined and weighed. Roots were removed by a combination of washing and hand-picking, and then were dried and weighed. This procedure was applied to the entire soil sample at each depth except for the 0–3-cm depth, which was sampled as nitrate pellets in late January or early February. Evidence that extremely high rainfall can be detrimental to grassland NPP is supported by measurements of atmospheric nitrogen deposition (29). The nitrogen treatment was determined ambient nitrogen deposition from annual maps from the National Atmospheric Deposition Program (29). We used a pneumatic corer that removed multiple cores simultaneously, and in 2004–2007 we used a single-core pneumatic corer. To account for possible differences in these cores, we calculated an area-based mean of biomass from the same cores in the same season. We did not show trends in the sign, magnitude, or significance over 17 y. Both findings are consistent with Dukes et al. (14). The absence of time dependence leads us to integrate experimental treatment and natural variation over 17 y, by quantifying the current environment each plot experienced.

We characterized the environment in terms of four continuous variables and two factor variables. For temperature (T), we used data from a Jasper Ridge weather station to calculate the average ambient air temperature during the growing season, defined as the period from the mean date of germination in fall to the mean midpoint between the two harvest dates; for warmed plots we added the mean effect of the warming treatments (1 °C, 1.5 °C, and 2 °C for the three successive generations of heaters). For precipitation (P), we summed rainfall from the first germinating event until the harvest date. For aboveground biomass, we harvested all plant matter in a 141-cm2 area as each subplot at the peak of standing biomass. In years 1-3 we harvested biomass once (in May), and in years 4–17 we harvested from each subplot twice: the first one timed to peak biomass in the phenologically most advanced plots (mid-April to early May), and the second one 3 wk later at the peak of less advanced plots (early to late May). The locations selected each year to avoid harvesting the same spot for at least three years. In both harvests, we separated out the litter and weighed the oven-dried biomass (70 °C). In this study, we analyzed the aboveground biomass from the single harvest (years 1–3) and the maximum of the two harvests (years 4–17). After the first aboveground harvest we took four soil cores from the harvested area, two shallow (0–15 cm) and two deeper (15–30 cm), and the cores from a given depth were combined and weighed. Roots were removed by a combination of washing and hand-picking, and then were dried and weighed. This procedure was applied to the entire soil sample at each depth except for the 0–3-cm depth, which was sampled as nitrate pellets in late January or early February. Evidence that extremely high rainfall can be detrimental to grassland NPP is supported by measurements of atmospheric nitrogen deposition (29). The nitrogen treatment was determined ambient nitrogen deposition from annual maps from the National Atmospheric Deposition Program (29). We used a pneumatic corer that removed multiple cores simultaneously, and in 2004–2007 we used a single-core pneumatic corer. To account for possible differences in these cores, we calculated an area-based mean of biomass from the same cores in the same season. We did not show trends in the sign, magnitude, or significance over 17 y. Both findings are consistent with Dukes et al. (14). The absence of time dependence leads us to integrate experimental treatment and natural variation over 17 y, by quantifying the current environment each plot experienced.

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To understand ecosystem responses to multifactor global changes, we used linear mixed-effects models to analyze NPP, with main and interactive global change factors (T, P, C, and N) with random effects (33). For main-effects terms, we used linear functions for T, P, C, N, F03, and B11, as well as quadratic functions for T² and P². Our choice of quadratic functions was motivated by the pairwise relationships in Fig. 1 and verified by model comparison (next paragraph). For interaction terms, we used full factorial combinations of global change factors (TP, TC, CN, PC, PN, CN, TPC, TCP, PCN, and TPNC). NPP variables (NPP, ANPP, and BNPP) were log-transformed to satisfy normality of fit (likelihood) variances on e-1 (number of parameters). A lower AIC indicates a preferred model. Table S2 shows the AIC values of linear and nonlinear models for NPP, ANPP, and BNPP. In all cases, nonlinear models have lower AIC than linear models. This comparison (next paragraph). For interaction terms, we used full factorial combinations of global change factors (T, P, C, and N) in Fig. 2 and the estimated coefficients of global change factors. Because of the log-scale NPPs and standardized environmental variables, the estimated fixed effects (main and interaction terms) should be interpreted as proportional change in production (d log y) with respect to an SD change in environment (dx, where x is a SD of T, P, C, or N): d log y/dx = (dy/y)/dx. Likewise, the fire effects should be interpreted as proportional change in production with respect to whether or not the plot-subplot had burned in the wildfire (F03) or prescribed burn (B11). We summarized the estimated coefficients of global change factors (T, P, C, and N) in Table S1. Our analysis controls for fire effects but focuses on environmental effects.

To verify the model’s nonlinear terms, we used an information-theoretic approach as a sensitivity analysis. We separately fitted (i) linear model, with predictors of linear and interaction terms of global change factors, and (ii) nonlinear model, with the same linear predictors as in (i) plus quadratic temperature (T²) and precipitation (P²) terms. We calculated our Akaike information criterion (AIC) values respectively. AIC measures the relative quality of models for a given set of data, by estimating the information lost when the model represents the process that generates the data. Practically, AIC uses a “likelihood” (likelihood of model parameters) plus an “information term” (number of parameters). A lower AIC indicates a preferred model. Table S2 shows the AIC values of linear and nonlinear models for NPP, ANPP, and BNPP. In all cases, nonlinear models have lower AIC than linear models. This comparison verifies the use of quadratic temperature (T²) and precipitation (P²) terms.

To synthesize joint multifactor global change effects, we used the fitted models to predict primary production in the four-dimensional environment space (T, P, C, and N) without fires, spanning the entire experiment. We set up continuous gradients for temperature (8.69−12.28 °C) and precipitation (240−1,380 mm), as well as categorical levels for CO₂ (ambient 409 μmol·mol⁻¹, elevated 680 μmol·mol⁻¹) and nitrogen (ambient 0.25 g·m⁻²·y⁻¹, elevated 7.25 g·m⁻²·y⁻¹). We visualized our predictions by temperature and precipitation interaction at different CO₂ and nitrogen level combinations. We summarized the modeled NPP, overlaid with observed NPP in Fig. S3. We included similar surfaces for ANPP and BNPP in Figs. S3 and S4.

To assess model performance, we compared modeled vs. observed primary production, summarized by goodness-of-fit measures. The modeled values were calculated as the expected (or fitted) primary production given environmental variables at unique temperature–precipitation–CO₂–nitrogen combinations. These modeled values were then compared with the observed primary production. Fig. S5A shows how the modeled and observed NPP, ANPP, and BNPP are close to the 1:1 reference line. We then summarized their goodness of fit by Pearson correlation coefficient, which is a measure between −1 and +1, where a higher value indicates a better fit. For all groups, the modeled and observed primary production are highly correlated (rNPP = 0.64, rANPP = 0.68, and rBNPP = 0.54). This assessment validates that the model can predict the data well.

Model assumptions, we performed residual diagnostics, focusing on progressive (year-dependent) effects. Progressive year effects would result in model residuals (unexplained component of observed data) that correlate with year. Residual diagnostics in Fig. S5B show that the residuals are not correlated with year, providing additional evidence of the absence of progressive effects. Fig. S5C validates the normality assumption of the model residuals, supporting log-transformed NPP variables.

All analyses were performed in R version 3.2.4 (34). All data and code are available upon request.

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Supporting Information

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SI Text

Here we show the mathematical details of the analyses.

**Exploratory Analysis.** For plot $i$, year $t$, the response variable NPP (or ANPP, BNPP) is $y_{it}$. To test for year-dependent treatment effects, we first performed standard ANOVAs separately for each year,

$$\log(y_{it}) = Z_{it} \gamma_t + \delta_{it}, \quad [S1]$$

where $Z_{it}$ is the design matrix with main and interaction terms ($0$: plot with ambient treatment; $1$: plot with elevated treatment), $\gamma_t$’s are treatment effects (ANOVA coefficients) across years ($t$), and $\delta_{it}$ is random error. Across all of the single-factor and interactive effects, there are no consistent temporal trends in the treatment effects ($\gamma_t$) that are significant at $P < 0.05$ (Fig. S2).

To integrate the experimental treatments and natural variation, we plotted the response variable NPP (or ANPP, BNPP) $y_{it}$ against actual temperature $T_{it}$, precipitation $P_{it}$, CO$_2$ $C_{it}$, and nitrogen $N_{it}$. Fig. 1 shows the pairwise relationships between the responses (averaged on log scale, mean $\pm$ SE) and each of the predictors: $y_{it}$ vs. $T_{it}$, $y_{it}$ vs. $P_{it}$, $y_{it}$ vs. $C_{it}$, and $y_{it}$ vs. $N_{it}$. Note that these are marginal relationships that do not account for interactions among predictors. We fitted these marginal relationships with linear and quadratic functions, which motivates our functional choice in the joint modeling.

**Joint Modeling.** We developed the following linear mixed-effects model to jointly quantify how NPP and its components respond to global changes across experimental manipulation and natural variation:

$$\log(y_{it}) = X_{it} \beta + b_i + e_{it}, \quad [S2]$$

where the response $\log(y_{it})$ is log-transformed NPP (or ANPP, BNPP), a design matrix $X_{it}$ includes global changes across treatment and year, a fixed effect $\beta$ quantifies main and interactive environmental effects, a random effect $b_i$ quantifies the plot-specific effect on NPP, and random error $e_{it}$ is assumed to be independent and normally distributed with mean 0 and variance $\sigma^2$,

$$e_{it} \sim N(0, \sigma^2). \quad [S3]$$

The design matrix is

$$X_{it} = [T^2, P^2, T, P, C, N, TPC, TPN, TCN, PCN, TPCN, F03, B11]_{it}, \quad [S4]$$

where $T$ is standardized temperature, $P$ is standardized precipitation, $C$ is standardized CO$_2$, $N$ is standardized nitrogen, $F03$ is a factor variable denoting whether or not the plot was burned in the 2003 wildfire, and $B11$ is a factor variable denoting whether or not the plot was burned in the 2011 control burn. Correspondingly, the estimated environmental effects are

$$\beta = [\beta_T, \beta_P, \beta_C, \beta_N, \beta_{TP}, \beta_{TC}, \beta_{PN}, \beta_{PC}, \beta_{PNC}, \beta_{TCN}, \beta_{P TCN}, \beta_{TPCN}, \beta_{F03}, \beta_{B11}], \quad [S5]$$

Because we focus on environmental effects in this analysis, we presented only $T$, $P$, $C$, and $N$ coefficients in the main text but included $F03$ and $B11$ coefficients in Table S1. The estimated $\beta$’s are plotted in Fig. 2 (except fire effects are presented in Table S1).

The nonlinear (quadratic) terms $T^2$ and $P^2$ are justified by comparing a quadratic model with design matrix $S4$ vs. a linear model with the following design matrix:

$$X_{it} = [T, P, C, N, TP, TC, TN, PC, PN, CN, TPC, TPN, TCN, PCN, TPCN, F03, B11]_{it}. \quad [S6]$$

We then calculated the AICs for both models and found that nonlinear models always have lower AICs (Table S2).

**Response Surface Analysis.** The multidimensional surfaces were model predictions based on setting all possible combinations of $T$, $P$, $C$, and $N$ and setting $F03$ and $B11$ to ambient levels:

$$\log(\hat{y}) = X_{it} \hat{\beta}, \quad [S7]$$

where $\hat{y}$ is predicted NPP (or ANPP, BNPP), $\hat{X}$ includes standardized $T$ and $P$ gradients, $C$ and $N$ levels, and ambient $F03$ and $B11$. $\hat{\beta}$ is estimated environmental effects in Fig. 2 and Table S1. Fig. 3 and Figs. S3 and S4 present the predicted $\hat{y}$ (surfaces and contour lines) as well as the observed $y_{it}$ (bubbles).

**Model Assessment.** We performed in-sample prediction to assess model performance,

$$\log(\hat{y}_{it}) = X_{it} \hat{\beta} + \hat{b}_i, \quad [S8]$$

where $\hat{y}_{it}$ is fitted (modeled) NPP (or ANPP, BNPP), $X_{it}$ is the observed environment, $\hat{\beta}$ is estimated fixed effect, and $\hat{b}_i$ is estimated random effect. We first compared modeled ($\hat{y}_{it}$) vs. observed ($y_{it}$) NPP and its components in Fig. S5A. We also calculated the correlation between $\hat{y}_{it}$ and $y_{it}$.

We then performed residual diagnostics to check whether the model assumption $S3$ has been satisfied. The estimated residual is

$$\hat{e}_{it} = \log(y_{it}) - \log(\hat{y}_{it}). \quad [S9]$$

The plot of residuals against year in Fig. S5B shows independence of year (no progressive year effect). The histogram of residuals in Fig. SSC shows normality.
Fig. S1. Total ANPP (black line) and the component from annual plants (red line) and perennials (blue line) averaged across all treatments, from 1998 through 2014.
Fig. S2. ANOVA coefficients across years to test treatment effects over years. Filled symbols are significant at $P < 0.05$; unfilled symbols are nonsignificant.
Fig. S3. Modeled and observed ANPP in four-dimensional temperature–precipitation–CO$_2$–nitrogen space. Symbols follow Fig. 3.
Fig. S4. Modeled and observed BNPP in four-dimensional temperature–precipitation–CO₂–nitrogen space. Symbols follow Fig. 3.
Fig. S5. Model assessment. (A) Modeled vs. observed NPP, where each crosshair is NPP (mean ± SE) in a unique temperature–precipitation–CO$_2$–nitrogen–fire combination. (B) Residuals over years to test for progressive effects. (C) Residual distribution to test for normality assumption.
Table S1. Model coefficients (mean and 95% confidence intervals)

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>NPP</th>
<th>ANPP</th>
<th>BNPP</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T^2$</td>
<td>$-0.008 (-0.023, 0.008)$</td>
<td>$-0.002 (-0.021, 0.017)$</td>
<td>$-0.033 (-0.054, -0.011)$</td>
</tr>
<tr>
<td>$P^2$</td>
<td>$-0.053 (-0.069, -0.037)$</td>
<td>$-0.036 (-0.055, -0.017)$</td>
<td>$-0.054 (-0.076, -0.031)$</td>
</tr>
<tr>
<td>$T$</td>
<td>$-0.027 (-0.046, -0.005)$</td>
<td>$-0.028 (-0.054, -0.002)$</td>
<td>$-0.065 (-0.095, -0.033)$</td>
</tr>
<tr>
<td>$P$</td>
<td>$-0.016 (-0.036, 0.004)$</td>
<td>$-0.080 (-0.103, -0.056)$</td>
<td>$0.042 (0.013, 0.071)$</td>
</tr>
<tr>
<td>$C$</td>
<td>$-0.000 (-0.021, 0.020)$</td>
<td>$0.017 (-0.011, 0.044)$</td>
<td>$-0.028 (-0.063, 0.007)$</td>
</tr>
<tr>
<td>$N$</td>
<td>$0.101 (0.081, 0.122)$</td>
<td>$0.141 (0.113, 0.169)$</td>
<td>$0.021 (-0.015, 0.057)$</td>
</tr>
<tr>
<td>$TP$</td>
<td>$0.020 (0.002, 0.038)$</td>
<td>$0.022 (-0.001, 0.044)$</td>
<td>$0.013 (-0.013, 0.039)$</td>
</tr>
<tr>
<td>$TC$</td>
<td>$-0.013 (-0.031, 0.005)$</td>
<td>$-0.007 (-0.031, 0.016)$</td>
<td>$-0.019 (-0.046, 0.008)$</td>
</tr>
<tr>
<td>$PC$</td>
<td>$-0.003 (-0.024, 0.018)$</td>
<td>$-0.003 (-0.026, 0.021)$</td>
<td>$-0.045 (-0.075, -0.014)$</td>
</tr>
<tr>
<td>$PN$</td>
<td>$-0.008 (-0.027, 0.010)$</td>
<td>$-0.016 (-0.038, 0.006)$</td>
<td>$0.005 (-0.022, 0.032)$</td>
</tr>
<tr>
<td>$CN$</td>
<td>$-0.002 (-0.022, 0.018)$</td>
<td>$0.018 (-0.009, 0.044)$</td>
<td>$-0.021 (-0.055, 0.014)$</td>
</tr>
<tr>
<td>$TNC$</td>
<td>$0.009 (-0.009, 0.028)$</td>
<td>$0.007 (-0.017, 0.030)$</td>
<td>$0.017 (-0.010, 0.044)$</td>
</tr>
<tr>
<td>$TPN$</td>
<td>$-0.016 (-0.033, 0.001)$</td>
<td>$-0.014 (-0.035, 0.007)$</td>
<td>$-0.018 (-0.042, 0.006)$</td>
</tr>
<tr>
<td>$TCN$</td>
<td>$0.002 (-0.015, 0.020)$</td>
<td>$0.000 (-0.022, 0.023)$</td>
<td>$0.001 (-0.025, 0.028)$</td>
</tr>
<tr>
<td>$PCN$</td>
<td>$0.005 (-0.016, 0.026)$</td>
<td>$0.028 (0.004, 0.052)$</td>
<td>$-0.009 (-0.039, 0.021)$</td>
</tr>
<tr>
<td>$TPCN$</td>
<td>$0.003 (-0.015, 0.022)$</td>
<td>$0.000 (-0.023, 0.024)$</td>
<td>$0.001 (-0.025, 0.028)$</td>
</tr>
<tr>
<td>$F03$</td>
<td>$0.154 (0.005, 0.302)$</td>
<td>$0.299 (0.112, 0.485)$</td>
<td>$0.047 (-0.163, 0.256)$</td>
</tr>
<tr>
<td>$B11$</td>
<td>$0.274 (0.147, 0.401)$</td>
<td>$0.361 (0.201, 0.519)$</td>
<td>$0.138 (-0.040, 0.317)$</td>
</tr>
</tbody>
</table>

Notations follow Fig. 2.

Table S2. Comparison of the linear vs. nonlinear model based on AIC for NPP, ANPP, and BNPP data

<table>
<thead>
<tr>
<th>Model</th>
<th>NPP</th>
<th>ANPP</th>
<th>BNPP</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear model</td>
<td>1,857</td>
<td>3,718</td>
<td>3,254</td>
</tr>
<tr>
<td>Nonlinear model</td>
<td>1,817</td>
<td>3,168</td>
<td>3,226</td>
</tr>
</tbody>
</table>

Nonlinear models are preferred due to lower AIC.