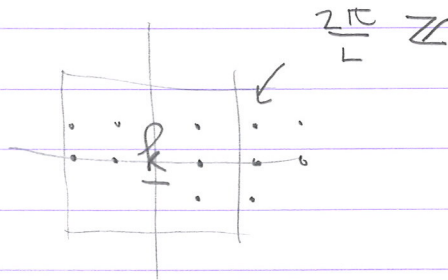
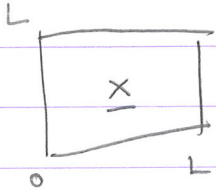


(1)

CONTINUOUS



$$\hat{f}(\underline{k}) = \int_{[0,L]^3} f(\underline{x}) e^{-i\underline{k}\underline{x}} d\underline{x} \quad \underline{k} \in \frac{2\pi}{L} \mathbb{Z}$$

$$f(\underline{x}) = \frac{1}{L^3} \sum_{\underline{k} \in \frac{2\pi}{L} \mathbb{Z}} \hat{f}(\underline{k}) e^{i\underline{k}\underline{x}} \quad \underline{x} \in [0,L]^3$$

Parseval

$$\int_{[0,L]^3} |f(\underline{x})|^2 d\underline{x} = \frac{1}{L^3} \sum_{\underline{k} \in \frac{2\pi}{L} \mathbb{Z}} |\hat{f}(\underline{k})|^2$$

MATLAB

$$\text{IFFTN}(m+1) = \sum_{n=0}^{N-1} \text{FFTN}(n+1) e^{-2\pi i \frac{1}{N} nm}$$

$$\text{FFTN}(n+1) = \frac{1}{N^3} \sum_{m=0}^{N-1} \text{IFFTN}(m+1) e^{2\pi i \frac{1}{N} nm}$$

Parseval

$$n, m \in [0, \dots, N-1]$$

$$\sum_{n=0}^{N-1} |\text{IFFTN}(n+1)|^2 = \frac{1}{N^3} \sum_{m=0}^{N-1} |\text{FFTN}(m+1)|^2$$

(2)

DISCRETE

$$X_n = \frac{n}{N} L \quad k_m = \frac{2\pi}{L} \left(m - \frac{N}{2} \right) \quad m, n \in [0, N-1]$$

$$X_n = \{ 0, \Delta x, 2\Delta x, \dots, L - \Delta x \}$$

$$k_m = \left\{ -\frac{2\pi}{2\Delta x}, \dots, 0, \dots, \frac{2\pi}{2\Delta x} - \frac{2}{N} \frac{2\pi}{2\Delta x} \right\}$$

$$f(x_n) = \text{IFFTN}(n+1)$$

$$\underbrace{\hat{f}(k)}_{\text{extral}} \approx \sum_n \Delta x^3 f(x_n) e^{-i k_m x_n}$$

$$= L^3 \sum_n \frac{1}{N^3} \text{IFFTN}(n+1) e^{-i \frac{2\pi}{L} \left(m - \frac{N}{2} \right) \frac{n}{N} L}$$

$$= L^3 \sum_n \frac{1}{N^3} \text{IFFTN}(n+1) e^{-2\pi i m n / N} \underbrace{e^{+2\pi i \frac{n}{2}}}$$

$$= \underbrace{\frac{L^3}{N^3} \text{FFTN}(k+1)}_{\text{internal}} = \Delta x^3 \text{FFTN}(k+1) \quad \begin{array}{l} \text{nicht ein} \\ \text{muss ein-oren} \\ \text{wird anders X} \\ \text{nicht das!} \end{array}$$

(3)

Parseval

$$\int_{[0,L]^3} |f(x)|^2 dx = \sum_n \Delta x^3 |FFTN(n+1)|^2$$

$$= \left(\frac{\Delta x}{N}\right)^3 \sum_{m=0}^{N-1} |FFTN(m+1)|^2$$

$$= \frac{1}{L^3} (N\Delta x)^3 \left(\frac{\Delta x}{N}\right)^3 \sum_{m=0}^{N-1} |FFTN(m+1)|^2$$

$$= \frac{1}{L^3} \sum_{m=0}^{N-1} |\Delta x^3 FF TN(m+1)|^2$$

$$\approx \frac{1}{L^3} \sum_{m=0}^{N-1} |\hat{f}(k)|^2$$

so $E_k = \int_{[0,L]^3} \frac{1}{2} |u_i(x)|^2 dx$

$$\approx \frac{1}{L^3} \sum_{m=0}^{N-1} \frac{1}{2} |\Delta x^3 \hat{u}_i(m+1)|^2$$

$$= \frac{1}{2L^3} \Delta x^6 \sum_{m=0}^{N-1} (|\hat{u}(m+1)|^2 + |\hat{v}(m+1)|^2 + |\hat{w}(m+1)|^2)$$

$$k = \frac{2\pi}{L} m = dk \cdot m$$

$$\frac{E}{k} = \frac{E}{m} \frac{m}{k} = \frac{E}{m} \frac{1}{dk} \quad \left(\frac{E}{m} \right) = dk \left(\frac{E}{k} \right)$$

$$\frac{1}{(k - m)^2} = \frac{1}{(m - m)^2} \left(\frac{m}{k - m} \right)^2 = \frac{1}{m^2} \frac{1}{(dk)^2}$$

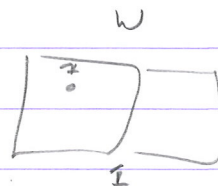
$$\Rightarrow \frac{1}{m^2} = \frac{dk^2}{k}$$

gedan,
D ift du die

D
to do.

D kay procedure...

wn mag. ~ desired... energy
old enyy



Wyke [u(1), u(2), u(3)]

Jane [u(0), u(1), u(2)]

energy data