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# <span id="page-0-0"></span>Self-Enforcing Voluntary Disclosures (Gigler '94)

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### <span id="page-1-0"></span>**Background**

- $\triangleright$  Previous literature suggests firms withhold private information in order to avoid proprietary costs (Verrecchia '83, Dye '85, etc.). Is this always the case?
- $\triangleright$  This paper shows that proprietary costs can actually increase voluntary disclosure, when such disclosure generates credibility.
- $\triangleright$  Does so by introducing tension in the form of a second (entrant) firm; the incumbent firm wishes to mislead the entrant downward while simultaneously misleading the market upward.
- $\triangleright$  Model only has cheap-talk equilibria rather than exact disclosures, unlike most previous voluntary disclosure models.
	- $\triangleright$  Extends Newman and Sansing, one such paper that did use cheap-talk equilibria, by allowing shareholders to sell their shares and by making the proprietary cost dependent upon the firm's private information. メロメ メ母メ メミメ メミメ Ε

### <span id="page-2-0"></span>**Motivation**

- $\triangleright$  Previous voluntary-disclosure models assume that firms would truthfully disclose all private information in the absence of proprietary costs, i.e., that these costs are the friction preventing full (truthful) disclosure.
- $\triangleright$  By contrast, in this setting firms wish to mislead the capital market to believe that profitability is higher than it actually is; since there is no cost of disclosure, any disclosure made by the firm in the absence of other tensions is unlikely to be credible ("cheap talk").
- $\triangleright$  The friction leading to an equilibrium in this case is the second firm. Firms play a Cournot game in the final stage, and Firm 1 has the opportunity to mislead Firm 2 about the total market demand. As such, Firm 1 would like to send Firm 2 a negative signal about the market, so that Firm [2 u](#page-1-0)[nd](#page-3-0)[e](#page-1-0)[rpr](#page-2-0)[o](#page-3-0)[d](#page-0-0)[u](#page-1-0)[c](#page-2-0)[e](#page-3-0)[s.](#page-0-0) Ε

### <span id="page-3-0"></span>Model Setup

- $\blacktriangleright$  Two firms and the market
- $\blacktriangleright$  Firms compete in a Cournot fashion, with market demand parameter  $t$ ; i.e., the market demand function is given by

$$
P=t-q_1-q_2
$$

- $\triangleright$  Firm 1 (the firm of interest) has a first-mover advantage in the sense that before firms make output decisions, it observes a private signal about  $t$ . After observing  $t$ , Firm 1 sends a signal  $m(t)$ , seen by both the market and the second firm.
- $\triangleright$  Cournot profits are  $\pi_1 = q_1(t q_1 q_2)$  and  $\pi_2 = q_2(t - q_1 - q_2).$

### <span id="page-4-0"></span>Model Setup

**Capital market pays K to buy a share**  $\alpha$  **of the firm. K is** assumed to be fixed, so that  $\alpha$  is a function of K and the firm's expected terminal value. That is,

$$
\alpha \cdot \mathbb{E}[\pi_1(q_1, q_2, t) | m] = K
$$

 $\triangleright$  Note that this doesn't affect the firm's output decision; by assumption that firm values its current owners and future shareholders equally, firm maximizes the following with respect to  $q_1$ :

$$
(1-\alpha)\pi_1(m) + K = \pi_1(q_1, q_2(m), t)
$$

 $\triangleright$  Other equilibrium conditions: firm 2 maximizes  $\mathbb{E}[\pi_2(q_2,q_1(m,t),t)|m]$  and the market sets

$$
\alpha(m)=\frac{\mathcal{K}}{\mathbb{E}[\pi_1(q_1(m,t),q_2(m),t)|m]}\Big|_{s\;\mathbb{R}^m\times\;\mathbb{R}^m\times\;\mathbb{R}^m\times\;\mathbb{R}^m\times\mathbb{R}^n\times\mathbb{
$$

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### <span id="page-5-0"></span>Key Assumption

At each period of time, firm only maximizes over *current* shareholders. So before selling equity, in stage 1 the firm maximizes  $(1 - \alpha) \mathbb{E}[\pi_1|m]$ . This means that when making its reporting decision, the firm maximizes

 $(1 - \alpha(m)) \mathbb{E}[\pi_1|m]$ 

for each t, given the following equilibrium beliefs by the other parties:

$$
f(t|m) = \frac{f(t)}{\int_{T(m)} f(\tau) d\tau}
$$
 for  $m(t) = m$ 

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(and zero otherwise).

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### <span id="page-6-0"></span>Second-Stage Equilibrium (Lemma 1)

Given a disclosure strategy  $m(t)$ , the stage-2 equilibrium in product and capital markets is given by

$$
q_2(m) = \frac{\mathbb{E}[t|m]}{3}
$$
  
\n
$$
q_1(m,t) = \frac{t - q_2(m)}{2} = \frac{3t - \mathbb{E}[t|m]}{6}
$$
  
\n
$$
\pi_1(q_1, q_2, t) = \frac{(t - q_2(m))^2}{4}
$$
  
\n
$$
\alpha(m) = \frac{36K}{4(\mathbb{E}[t|m])^2 + 9\text{Var}[t|m]}
$$

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### Supporting Result: Proposition 1

- $\triangleright$  Proposition 1: there can be no information disclosed privately to either the competitor or the capital market in equilibrium.
- $\triangleright$  Sketch of proof: show that if private disclosure to market, firm has incentive to inflate as much as possible (disclosure is costless) so market ignores the disclosure and uses its prior for  $\alpha$ ; similarly, if privately disclosing to Firm 2, Firm 1 has incentive to deflate as much as possible and so Firm 2 also ignores any disclosure.

### <span id="page-8-0"></span>Supporting Results: Propositions 2 and 3

- $\triangleright$  These propositions also exist to set up the main result of the paper.
- **Proposition 2:** Any equilibrium strategy  $m(t)$  results in a nondecreasing outcome; i.e., if  $t'' > t$  then  $(\alpha(t''), q_2(t'')) \geq (\alpha(t'), q_2(t')).$
- $\triangleright$  Follows from Lemmas 2 (game is a cheap-talk game) and 3 (set of equilibrium outcomes are completely ordered). Useful for Proposition 4 (the main result).
- $\triangleright$  Proposition 3: There are no full disclosure intervals in a public disclosure equilibrium.

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## <span id="page-9-0"></span>Main Result: Partition Equilibria (Proposition 4)

 $\triangleright$  Proposition 4: All public disclosure equilibria are partition equilibria. That is, equilibrium outcomes are characterized by

$$
q_2(t) = \frac{\mathbb{E}[t|t \in (t_i, t_{i+1})]}{3}
$$
  
\n
$$
\alpha(t) = \frac{36K}{4 \{\mathbb{E}[t|t \in (t_i, t_{i+1})]\}^2 + 9\text{Var}[t|t \in (t_i, t_{i+1})]}
$$

for all  $t \in (t_i, t_{i+1})$ .

 $\triangleright$  The partition is defined implicitly by

$$
(1-\alpha(t'))\frac{(t_i-q_2(t'))^2}{4}=(1-\alpha(t''))\frac{(t_i-q_2(t''))^2}{4}
$$

for  $t' \in (t_{i-1}, t_i)$ ,  $t'' \in (t_i, t_{i+1})$ , and  $i = 1, ...N - 1$ .

 $\triangleright$  Corollary 2: The literal reporting strategy that supports the equ[i](#page-14-0)librium above is  $m(t)=(t_i,t_{i+1})$  f[or](#page-8-0) a[ll](#page-10-0)  $t\in (t_i,t_{i+1}).$  $t\in (t_i,t_{i+1}).$ 

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#### <span id="page-10-0"></span>Proof of Proposition 4

- $\triangleright$  Since any monotonic, bounded function is discontinuous at most countably many times, we can enumerate the points of discontinuity of  $q_2(t)$ .
- Gorollary 1 and Proposition 3:  $q_2(t)$  cannot be strictly increasing on any interval  $\Rightarrow$  it can only be increasing at the points of discontinuity, i.e., it must be a step function
- $\triangleright$  Now let  $m_i$  be a message inducing the equilibrium outcome on  $t_i, t_{i+1}$  and let  $M(m_i)$  be the set of all messages which induce the same outcome as  $m_i$ . Since  $q_2$  is monotonic,

 $m(t) \in M \Leftrightarrow t \in (t_i, t_{i+1})$ 

Eletting  $g(m)$  be the marginal density of  $f(t, m)$ , since  $q_2 \equiv \mathbb{E}[t|m]/3$  we have

$$
\int_M q_2(m)g(m)dm = \int_M \frac{\mathbb{E}[t|m]}{3}g(m)dm
$$

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#### Proof of Proposition 4

- ► Since  $q_2$  is locally constant on M, this gives  $q_2 = \frac{\mathbb{E}[t|m \in M(m_i)]}{3}$ 3 for all  $m \in M(m_i)$ .
- ▶ This is equivalent to (since  $m(t) \in M(m_i) \Leftrightarrow t \in (t_i, t_{i+1}))$

$$
q_2(t) = \frac{\mathbb{E}[t|t \in (t_i, t_{i+1})]}{3} \forall t \in (t_i, t_{i+1})
$$

 $\triangleright$  Finally, to prove Eq. (14) (the cutoff equation) by contradiction, suppose there were strict inequality. Then by continuity we would have  $\hat{t} \in (t_i,t_{i+1})$  such that the inequality is satisfied with  $t_i$  is replaced with  $\hat{t}$ ; but then  $q_2(\hat{t})\neq q_2(t'').$ 

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### Proposition 5 (Informative Equilibria)

- $\triangleright$  Proposition 4 alone admits the possibility of unique noninformative equilibria. The goal of Proposition 5 is to establish when these equilibria are informative:
- $\triangleright$  Proposition 5: There exists an informative disclosure equilibrium when  $K$  is neither too small nor too large. That is, whenever  $K < K < \overline{K}$ , there is an informative disclosure; further,  $K$  and  $\overline{K}$  are bounded above and below by  $K$  and  $\overline{K}$ , which in turn are bounded below by 0 and above by  $\frac{4\mu^2+9\sigma^2}{36}$ . K and  $\overline{K}$  are defined by

$$
\frac{K}{K} = \frac{(\mu - \underline{t})(5\underline{t} - \mu)}{3(\mu - \underline{t})(3\underline{t} + \mu) + 9\sigma^2} \frac{4\mu^2 + 9\sigma^2}{36}
$$
\n
$$
\overline{K} = \frac{(\mu - \overline{t})(5\overline{t} - \mu)}{3(\mu - \overline{t})(3\overline{t} + \mu) + 9\sigma^2} \frac{4\mu^2 + 9\sigma^2}{36}
$$

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### Proposition 5

- $\triangleright$  Sketch of proof: Recall from Crawford and Sobel that if there is a partition equilibrium with  *subintervals, then there is* also a partition equilibrium for each size  $n = 1, 2, ...N$ . Therefore, to find "informative" equilibria, it suffices to find two-element partition equilibria.
- Given this, compute expressions for  $K(t)$  and  $K(\bar{t})$  and derive conditions for t,  $\overline{t}$  such that  $K(\overline{t}) > K(\underline{t})$ ; then apply the intermediate value theorem.

### <span id="page-14-0"></span>Proposition 5

- $\triangleright$  Proposition 5 (and Corollary 3, for uniform distributions) generalize Proposition 1, in the sense that if  $K$  is sufficiently large, the capital market effect is too dominant whereas if  $K$  is sufficiently small, the product market effect is too dominant.
- $\triangleright$  Considering the special case of the two-element equilibrium, as  $K$  increases, higher firm types disclose more precise information while lower tpyes make their disclosures noisier.
- $\blacktriangleright$  Equivalently (again in the two-element equilibrium), as the relative level of proprietary costs increases, lower types disclose more precise information while higher types disclose less precise information.