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In the first part of the book we introduce the fundamental suite of algorithmic tools that make up the modern neural language model that is the heart of end-to-end NLP systems. We begin with tokenization and preprocessing, as well as useful algorithms like computing edit distance, and then proceed to the tasks of classification, logistic regression, neural networks, proceeding through feedforward networks, recurrent networks, and then transformers. We’ll also see the role of embeddings as a model of word meaning.
La dernière chose qu’on trouve en faisant un ouvrage est de savoir celle qu’il faut mettre la première.

[The last thing you figure out in writing a book is what to put first.]

Pascal
The dialogue above is from **ELIZA**, an early natural language processing system that could carry on a limited conversation with a user by imitating the responses of a Rogerian psychotherapist (Weizenbaum, 1966). ELIZA is a surprisingly simple program that uses pattern matching to recognize phrases like “I need X” and translate them into suitable outputs like “What would it mean to you if you got X?”. This simple technique succeeds in this domain because ELIZA doesn’t actually need to know anything to mimic a Rogerian psychotherapist. As Weizenbaum notes, this is one of the few dialogue genres where listeners can act as if they know nothing of the world. ELIZA’s mimicry of human conversation was remarkably successful: many people who interacted with ELIZA came to believe that it really understood them and their problems, many continued to believe in ELIZA’s abilities even after the program’s operation was explained to them (Weizenbaum, 1976), and even today such **chatbots** are a fun diversion.

Of course modern conversational agents are much more than a diversion; they can answer questions, book flights, or find restaurants, functions for which they rely on a much more sophisticated understanding of the user’s intent, as we will see in Chapter 15. Nonetheless, the simple pattern-based methods that powered ELIZA and other chatbots play a crucial role in natural language processing.

We’ll begin with the most important tool for describing text patterns: the **regular expression**. Regular expressions can be used to specify strings we might want to extract from a document, from transforming “I need X” in ELIZA above, to defining strings like $199 or $24.99 for extracting tables of prices from a document.

We’ll then turn to a set of tasks collectively called **text normalization**, in which regular expressions play an important part. Normalizing text means converting it to a more convenient, standard form. For example, most of what we are going to do with language relies on first separating out or **tokenizing** words from running text, the task of **tokenization**. English words are often separated from each other by whitespace, but whitespace is not always sufficient. *New York* and *rock ‘n’ roll* are sometimes treated as large words despite the fact that they contain spaces, while sometimes we’ll need to separate *I’m* into the two words *I* and *am*. For processing tweets or texts we’ll need to tokenize **emoticons** like :) or **hashtags** like #nlproc.
Some languages, like Japanese, don’t have spaces between words, so word tokenization becomes more difficult.

Another part of text normalization is lemmatization, the task of determining that two words have the same root, despite their surface differences. For example, the words sang, sung, and sings are forms of the verb sing. The word sing is the common lemma of these words, and a lemmatizer maps from all of these to sing. Lemmatization is essential for processing morphologically complex languages like Arabic. Stemming refers to a simpler version of lemmatization in which we mainly just strip suffixes from the end of the word. Text normalization also includes sentence segmentation: breaking up a text into individual sentences, using cues like periods or exclamation points.

Finally, we’ll need to compare words and other strings. We’ll introduce a metric called edit distance that measures how similar two strings are based on the number of edits (insertions, deletions, substitutions) it takes to change one string into the other. Edit distance is an algorithm with applications throughout language processing, from spelling correction to speech recognition to coreference resolution.

### 2.1 Regular Expressions

One of the unsung successes in standardization in computer science has been the regular expression (often shortened to regex), a language for specifying text search strings. This practical language is used in every computer language, word processor, and text processing tools like the Unix tools grep or Emacs. Formally, a regular expression is an algebraic notation for characterizing a set of strings. Regular expressions are particularly useful for searching in texts, when we have a pattern to search for and a corpus of texts to search through. A regular expression search function will search through the corpus, returning all texts that match the pattern. The corpus can be a single document or a collection. For example, the Unix command-line tool grep takes a regular expression and returns every line of the input document that matches the expression.

A search can be designed to return every match on a line, if there are more than one, or just the first match. In the following examples we generally underline the exact part of the pattern that matches the regular expression and show only the first match. We’ll show regular expressions delimited by slashes but note that slashes are not part of the regular expressions.

Regular expressions come in many variants. We’ll be describing extended regular expressions; different regular expression parsers may only recognize subsets of these, or treat some expressions slightly differently. Using an online regular expression tester is a handy way to test out your expressions and explore these variations.

#### 2.1.1 Basic Regular Expression Patterns

The simplest kind of regular expression is a sequence of simple characters; putting characters in sequence is called concatenation. To search for woodchuck, we type `/woodchuck/`. The expression `/Buttercup/` matches any string containing the substring `Buttercup`; `grep` with that expression would return the line `I’m called little Buttercup`. The search string can consist of a single character (like `/!/`) or a sequence of characters (like `/urg1/) (see Fig. 2.1).

Regular expressions are case sensitive; lower case `/s/` is distinct from upper
Chapter 2 • Regular Expressions, Text Normalization, Edit Distance

<table>
<thead>
<tr>
<th>Regex</th>
<th>Example Patterns Matched</th>
</tr>
</thead>
<tbody>
<tr>
<td>/woodchucks/</td>
<td>“interesting links to woodchucks and lemurs”</td>
</tr>
<tr>
<td>/a/</td>
<td>“Mary Ann stopped by Mona’s”</td>
</tr>
<tr>
<td>/1/</td>
<td>“You’ve left the burglar behind again!” said Nori</td>
</tr>
</tbody>
</table>

Figure 2.1 Some simple regex searches.

case /S/ (/s/ matches a lower case s but not an upper case S). This means that the pattern /woodchucks/ will not match the string Woodchucks. We can solve this problem with the use of the square braces [ and ]. The string of characters inside the braces specifies a disjunction of characters to match. For example, Fig. 2.2 shows that the pattern /[wW]/ matches patterns containing either w or W.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
<th>Example Patterns</th>
</tr>
</thead>
<tbody>
<tr>
<td>/[wW]oodchuck/</td>
<td>Woodchuck or woodchuck</td>
<td>“Woodchuck”</td>
</tr>
<tr>
<td>/[abc]/</td>
<td>‘a’, ‘b’, or ‘c’</td>
<td>“In uomini, in soldati”</td>
</tr>
<tr>
<td>/[1234567890]/</td>
<td>any digit</td>
<td>“plenty of 7 to 5”</td>
</tr>
</tbody>
</table>

Figure 2.2 The use of the brackets [ ] to specify a disjunction of characters.

The regular expression /[1234567890]/ specifies any single digit. While such classes of characters as digits or letters are important building blocks in expressions, they can get awkward (e.g., it’s inconvenient to specify

/ABCDEFGHIJKLMNOPQRSTUVWXYZ/  

to mean "any capital letter"). In cases where there is a well-defined sequence associated with a set of characters, the brackets can be used with the dash (-) to specify any one character in a range. The pattern /[2-5]/ specifies any one of the characters 2, 3, 4, or 5. The pattern /[b-g]/ specifies one of the characters b, c, d, e, f, or g. Some other examples are shown in Fig. 2.3.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
<th>Example Patterns Matched</th>
</tr>
</thead>
<tbody>
<tr>
<td>/[A-Z]/</td>
<td>an upper case letter</td>
<td>“we should call it ‘Drenched Blossoms’”</td>
</tr>
<tr>
<td>/[a-z]/</td>
<td>a lower case letter</td>
<td>“my beans were impatient to be hoed!”</td>
</tr>
<tr>
<td>/[0-9]/</td>
<td>a single digit</td>
<td>“Chapter 1: Down the Rabbit Hole”</td>
</tr>
</tbody>
</table>

Figure 2.3 The use of the brackets [ ] plus the dash – to specify a range.

The square braces can also be used to specify what a single character cannot be, by use of the caret ^. If the caret ^ is the first symbol after the open square brace [, the resulting pattern is negated. For example, the pattern /[^a]/ matches any single character (including special characters) except a. This is only true when the caret is the first symbol after the open square brace. If it occurs anywhere else, it usually stands for a caret; Fig. 2.4 shows some examples.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match (single characters)</th>
<th>Example Patterns Matched</th>
</tr>
</thead>
<tbody>
<tr>
<td>/[^A-Z]/</td>
<td>not an upper case letter</td>
<td>“Oyfn prietchik”</td>
</tr>
<tr>
<td>/[^Ss]/</td>
<td>neither ‘S’ nor ‘s’</td>
<td>“I have no exquisite reason for’t”</td>
</tr>
<tr>
<td>/[^-]/</td>
<td>not a period</td>
<td>“our resident Djinn”</td>
</tr>
<tr>
<td>/[^e~]/</td>
<td>either ‘e’ or ‘’’</td>
<td>“look up _ now”</td>
</tr>
<tr>
<td>/a~^b/</td>
<td>the pattern ‘a~b’</td>
<td>“look up a~ b now”</td>
</tr>
</tbody>
</table>

Figure 2.4 The caret ^ for negation or just to mean ^. See below re: the backslash for escaping the period.

How can we talk about optional elements, like an optional s in woodchuck and woodchucks? We can’t use the square brackets, because while they allow us to say
“s or S”, they don’t allow us to say “s or nothing”. For this we use the question mark `/?/`, which means “the preceding character or nothing”, as shown in Fig. 2.5.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
<th>Example Patterns Matched</th>
</tr>
</thead>
<tbody>
<tr>
<td>/woodchucks?/</td>
<td>woodchuck or woodchucks</td>
<td>“woodchuck”</td>
</tr>
<tr>
<td>/colou?r/</td>
<td>color or colour</td>
<td>“color”</td>
</tr>
</tbody>
</table>

Figure 2.5 The question mark ? marks optionality of the previous expression.

We can think of the question mark as meaning “zero or one instances of the previous character”. That is, it’s a way of specifying how many of something that we want, something that is very important in regular expressions. For example, consider the language of certain sheep, which consists of strings that look like the following:

baa!
baaa!
baaaa!
...

This language consists of strings with a b, followed by at least two a’s, followed by an exclamation point. The set of operators that allows us to say things like “some number of as” are based on the asterisk or *, commonly called the Kleene * (generally pronounced “cleany star”). The Kleene star means “zero or more occurrences of the immediately previous character or regular expression”. So /a*/ means “any string of zero or more as”. This will match a or aaaaaa, but it will also match the empty string at the start of Off Minor since the string Off Minor starts with zero a’s. So the regular expression for matching one or more a is /aa*/. meaning one a followed by zero or more as. More complex patterns can also be repeated. So /[ab]*/ means “zero or more a’s or b’s” (not “zero or more right square braces”). This will match strings like aaaa or ababab or bbbb.

For specifying multiple digits (useful for finding prices) we can extend /\[0-9]/, the regular expression for a single digit. An integer (a string of digits) is thus /\[0-9]\[0-9]*/. (Why isn’t it just /\[0-9]*/?)

Sometimes it’s annoying to have to write the regular expression for digits twice, so there is a shorter way to specify “at least one” of some character. This is the Kleene +, which means “one or more occurrences of the immediately preceding character or regular expression”. Thus, the expression /\[0-9]+/ is the normal way to specify “a sequence of digits”. There are thus two ways to specify the sheep language: /baaa*/ or /baa+!/.

One very important special character is the period (\./), a wildcard expression that matches any single character (except a carriage return), as shown in Fig. 2.6.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
<th>Example Matches</th>
</tr>
</thead>
<tbody>
<tr>
<td>/beg.n/</td>
<td>any character between beg and n</td>
<td>begin, beg’n, begun</td>
</tr>
</tbody>
</table>

Figure 2.6 The use of the period . to specify any character.

The wildcard is often used together with the Kleene star to mean “any string of characters”. For example, suppose we want to find any line in which a particular word, for example, aardvark, appears twice. We can specify this with the regular expression /aardvark.*aardvark/.

Anchors are special characters that anchor regular expressions to particular places
in a string. The most common anchors are the caret \(^\wedge\) and the dollar sign \(\$\). The caret
\(^\wedge\) matches the start of a line. The pattern \(^/\wedge\text{The}/\) matches the word \text{The} only at the
start of a line. Thus, the caret \(^\wedge\) has three uses: to match the start of a line, to in-
dicate a negation inside of square brackets, and just to mean a caret. (What are the
contexts that allow grep or Python to know which function a given caret is supposed
to have?) The dollar sign \(\$\) matches the end of a line. So the pattern \(^\wedge\text{The}\$\) is a useful
pattern for matching a space at the end of a line, and \(^/\wedge\text{The dog}\.\text{.}\$\) matches a
line that contains only the phrase \text{The dog}. (We have to use the backslash here since
we want the . to mean “period” and not the wildcard.)

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
</tr>
</thead>
<tbody>
<tr>
<td>(^\wedge)</td>
<td>start of line</td>
</tr>
<tr>
<td>($)</td>
<td>end of line</td>
</tr>
<tr>
<td>(\backslash b)</td>
<td>word boundary</td>
</tr>
<tr>
<td>(\backslash B)</td>
<td>non-word boundary</td>
</tr>
</tbody>
</table>

Figure 2.7 Anchors in regular expressions.

There are also two other anchors: \(\backslash b\) matches a word boundary, and \(\backslash B\) matches
a non-boundary. Thus, \(^/\backslash b\text{he}\backslash b/\) matches the word \text{the} but not the word \text{other}.
More technically, a “word” for the purposes of a regular expression is defined as any
sequence of digits, underscores, or letters; this is based on the definition of “words”
in programming languages. For example, \(^/\backslash b99\backslash b/\) will match the string \text{99} in
\text{There are 99 bottles of beer on the wall} (because \text{99} follows a space) but not \text{99} in
\text{There are 299 bottles of beer on the wall} (since \text{99} follows a number). But it will
match \text{99} in \$\text{99} (since \text{99} follows a dollar sign (\$), which is not a digit, underscore,
or letter).

2.1.2 Disjunction, Grouping, and Precedence

Suppose we need to search for texts about pets; perhaps we are particularly interested
in cats and dogs. In such a case, we might want to search for either the string \text{cat} or
the string \text{dog}. Since we can’t use the square brackets to search for “cat or dog” (why
can’t we say \(^/\text{[catdog]}?/\)\), we need a new operator, the \textbf{disjunction} operator, also
called the \textbf{pipe} symbol \(|\). The pattern \(^/\text{cat}|\text{dog}/\) matches either the string \text{cat} or
the string \text{dog}.

Sometimes we need to use this disjunction operator in the midst of a larger se-
quence. For example, suppose I want to search for information about pet fish for
my cousin David. How can I specify both \text{guppy} and \text{guppies}? We cannot simply
say \(^/\text{guppy}|\text{ies}/\), because that would match only the strings \text{guppy} and \text{ies}. This
is because sequences like \text{guppy} take \textbf{precedence} over the disjunction operator \(|\).
To make the disjunction operator apply only to a specific pattern, we need to use the
parenthesis operators ( and ). Enclosing a pattern in parentheses makes it act like a
single character for the purposes of neighboring operators like the pipe \(|\) and the
Kleene\(^*\). So the pattern \(^/\text{gupp(y|ies)}/\) would specify that we meant the disjunc-
tion only to apply to the suffixes \text{y} and \text{ies}.

The parenthesis operator ( is also useful when we are using counters like the
Kleene\(^*\). Unlike the \(|\) operator, the Kleene\(^*\) operator applies by default only to
a single character, not to a whole sequence. Suppose we want to match repeated
instances of a string. Perhaps we have a line that has column labels of the form
\text{Column 1 Column 2 Column 3}. The expression \(^/\text{Column}_{\{0-9\}+\text{\text{.}}}/\text{\text{.}}^*/\) will not
match any number of columns; instead, it will match a single column followed by
any number of spaces! The star here applies only to the space \( \omega \) that precedes it, not to the whole sequence. With the parentheses, we could write the expression \(/(\text{Column}_\omega[0-9]+,*\omega\star\omega*)/*/\) to match the word Column, followed by a number and optional spaces, the whole pattern repeated zero or more times.

This idea that one operator may take precedence over another, requiring us to sometimes use parentheses to specify what we mean, is formalized by the operator precedence hierarchy for regular expressions. The following table gives the order of RE operator precedence, from highest precedence to lowest precedence.

<table>
<thead>
<tr>
<th>Operator Precedence</th>
<th>Precedence</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parenthesis ()</td>
<td></td>
</tr>
<tr>
<td>Counters * + ? {}</td>
<td></td>
</tr>
<tr>
<td>Sequences and anchors the <code>my</code> end $</td>
<td></td>
</tr>
<tr>
<td>Disjunction</td>
<td></td>
</tr>
</tbody>
</table>

Thus, because counters have a higher precedence than sequences, /the*/ matches theeee but not thethe. Because sequences have a higher precedence than disjunction, /the|any/ matches the or any but not thany or theyn.

Patterns can be ambiguous in another way. Consider the expression \(/[a-z]*/\) when matching against the text once upon a time. Since \(/[a-z]*/\) matches zero or more letters, this expression could match nothing, or just the first letter o, on, onc, or once. In these cases regular expressions always match the largest string they can; we say that patterns are greedy, expanding to cover as much of a string as they can.

There are, however, ways to enforce non-greedy matching, using another meaning of the ? qualifier. The operator *? is a Kleene star that matches as little text as possible. The operator +? is a Kleene plus that matches as little text as possible.

### 2.1.3 A Simple Example

Suppose we wanted to write a RE to find cases of the English article the. A simple (but incorrect) pattern might be:

/\text{the}/

One problem is that this pattern will miss the word when it begins a sentence and hence is capitalized (i.e., The). This might lead us to the following pattern:

/\text{[tT]he}/

But we will still incorrectly return texts with the embedded in other words (e.g., other or theology). So we need to specify that we want instances with a word boundary on both sides:

/\text{\b[tT]he}\b/\text{\b}/

Suppose we wanted to do this without the use of /\b/. We might want this since /\b/ won’t treat underscores and numbers as word boundaries; but we might want to find the in some context where it might also have underlines or numbers nearby (the_ or the25). We need to specify that we want instances in which there are no alphabetic letters on either side of the the:

/\text{[^a-zA-Z] [tT]he[^a-zA-Z]}/

But there is still one more problem with this pattern: it won’t find the word the when it begins a line. This is because the regular expression [^a-zA-Z], which
we used to avoid embedded instances of the, implies that there must be some single
(although non-alphabetic) character before the the. We can avoid this by specifying
that before the the we require either the beginning-of-line or a non-alphabetic
character, and the same at the end of the line:

```
/(^|[a-zA-Z]) the([a-zA-Z]|\$)/
```

The process we just went through was based on fixing two kinds of errors: false
positives, strings that we incorrectly matched like other or there, and false negatives,
strings that we incorrectly missed, like The. Addressing these two kinds of
takes up again and again in implementing speech and language processing
systems. Reducing the overall error rate for an application thus involves two antag-
onistic efforts:

- Increasing precision (minimizing false positives)
- Increasing recall (minimizing false negatives)

We’ll come back to precision and recall with more precise definitions in Chapter 4.

### 2.1.4 More Operators

Figure 2.8 shows some aliases for common ranges, which can be used mainly to
save typing. Besides the Kleene * and Kleene + we can also use explicit numbers as
counters, by enclosing them in curly brackets. The regular expression `/{3}/`
means “exactly 3 occurrences of the previous character or expression”. So `/a\{24\}z/`
will match `a` followed by 24 dots followed by `z` (but not `a` followed by 23 or 25 dots
followed by a `z`).

<table>
<thead>
<tr>
<th>Regex</th>
<th>Expansion</th>
<th>Match</th>
<th>First Matches</th>
</tr>
</thead>
<tbody>
<tr>
<td>\d</td>
<td>[0-9]</td>
<td>any digit</td>
<td>Party_of_5</td>
</tr>
<tr>
<td>\D</td>
<td>[^0-9]</td>
<td>any non-digit</td>
<td>Blue_moon</td>
</tr>
<tr>
<td>\w</td>
<td>[a-zA-Z0-9_]</td>
<td>any alphanumeric/underscore</td>
<td>Daiyu</td>
</tr>
<tr>
<td>\W</td>
<td>[^\w]</td>
<td>a non-alphanumeric</td>
<td>!!!</td>
</tr>
<tr>
<td>\s</td>
<td>[\r\n\f]</td>
<td>whitespace (space, tab)</td>
<td>in_Concord</td>
</tr>
<tr>
<td>\S</td>
<td>[^\s]</td>
<td>Non-whitespace</td>
<td>in_Concord</td>
</tr>
</tbody>
</table>

**Figure 2.8** Aliases for common sets of characters.

A range of numbers can also be specified. So `/\{n,m\}/` specifies from `n` to `m`
occurrences of the previous char or expression, and `/\{n\}/` means at least `n`
occurrences of the previous expression. REs for counting are summarized in Fig. 2.9.

<table>
<thead>
<tr>
<th>Regex</th>
<th>Match</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>*</code></td>
<td>zero or more occurrences of the previous char or expression</td>
</tr>
<tr>
<td><code>+</code></td>
<td>one or more occurrences of the previous char or expression</td>
</tr>
<tr>
<td><code>?</code></td>
<td>zero or one occurrence of the previous char or expression</td>
</tr>
<tr>
<td><code>{n}</code></td>
<td>exactly <code>n</code> occurrences of the previous char or expression</td>
</tr>
<tr>
<td><code>{n,m}</code></td>
<td>from <code>n</code> to <code>m</code> occurrences of the previous char or expression</td>
</tr>
<tr>
<td><code>{n,}</code></td>
<td>at least <code>n</code> occurrences of the previous char or expression</td>
</tr>
<tr>
<td><code>{,m}</code></td>
<td>up to <code>m</code> occurrences of the previous char or expression</td>
</tr>
</tbody>
</table>

**Figure 2.9** Regular expression operators for counting.

Finally, certain special characters are referred to by special notation based on the
newline character (`\`) (see Fig. 2.10). The most common of these are the newline character
2.1.5 A More Complex Example

Let’s try out a more significant example of the power of REs. Suppose we want to build an application to help a user buy a computer on the Web. The user might want “any machine with at least 6 GHz and 500 GB of disk space for less than $1000”. To do this kind of retrieval, we first need to be able to look for expressions like 6 GHz or 500 GB or Mac or $999.99. In the rest of this section we’ll work out some simple regular expressions for this task.

First, let’s complete our regular expression for prices. Here’s a regular expression for a dollar sign followed by a string of digits:

/\$(\[0-9\]\+)/

Note that the $ character has a different function here than the end-of-line function we discussed earlier. Most regular expression parsers are smart enough to realize that $ here doesn’t mean end-of-line. (As a thought experiment, think about how regex parsers might figure out the function of $ from the context.)

Now we just need to deal with fractions of dollars. We’ll add a decimal point and two digits afterwards:

/\$(\[0-9\]\+\.[0-9][0-9])/\n
This pattern only allows $199.99 but not $199. We need to make the cents optional and to make sure we’re at a word boundary:

/(\^|\W)\$(\[0-9\]\+\.[0-9][0-9])?\b/\n
One last catch! This pattern allows prices like $199999.99 which would be far too expensive! We need to limit the dollars:

/(\^|\W)\$(\[0-9\]\{0,3\}\.[0-9][0-9])?\b/\n
Further fixes (like avoiding matching a dollar sign with no price after it) are left as an exercise for the reader.

How about disk space? We’ll need to allow for optional fractions again (5.5 GB); note the use of ? for making the final s optional, and the use of /\w/ to mean “zero or more spaces” since there might always be extra spaces lying around:

/\b[0-9]\+\.(\[0-9\]\+)?\w*(GB\|Gg)abytes?\b/

Modifying this regular expression so that it only matches more than 500 GB is left as an exercise for the reader.
2.1.6 Substitution, Capture Groups, and ELIZA

An important use of regular expressions is in substitutions. For example, the substitution operator `s/regexp1/pattern/` used in Python and in Unix commands like `vim` or `sed` allows a string characterized by a regular expression to be replaced by another string:

`s/colour/color/`

It is often useful to be able to refer to a particular subpart of the string matching the first pattern. For example, suppose we wanted to put angle brackets around all integers in a text, for example, changing the 35 boxes to the `<35>` boxes. We’d like a way to refer to the integer we’ve found so that we can easily add the brackets. To do this, we put parentheses around the first pattern and use the number operator \1 in the second pattern to refer back. Here’s how it looks:

`s/([0-9]+)/<\1>/`

The parenthesis and number operators can also specify that a certain string or expression must occur twice in the text. For example, suppose we are looking for the pattern “the Xer they were, the Xer they will be”, where we want to constrain the two X’s to be the same string. We do this by surrounding the first X with the parenthesis operator, and replacing the second X with the number operator \1, as follows:

`/the (.*)er they were, the \1er they will be/`

Here the \1 will be replaced by whatever string matched the first item in parentheses. So this will match the `bigger they were, the bigger they will be` but not the `bigger they were, the faster they will be`.

This use of parentheses to store a pattern in memory is called a capture group. Every time a capture group is used (i.e., parentheses surround a pattern), the resulting match is stored in a numbered register. If you match two different sets of parentheses, \2 means whatever matched the second capture group. Thus

`/the (.*)er they (.*), the \1er we \2/`

will match the `faster they ran, the faster we ran` but not the `faster they ran, the faster we ate`. Similarly, the third capture group is stored in \3, the fourth is \4, and so on.

Parentheses thus have a double function in regular expressions; they are used to group terms for specifying the order in which operators should apply, and they are used to capture something in a register. Occasionally we might want to use parentheses for grouping, but don’t want to capture the resulting pattern in a register. In that case we use a non-capturing group, which is specified by putting the special commands `?` after the open parenthesis, in the form `(?: pattern )`.

`/(?:some|a few) (people|cats) like some \1/`

will match some cats like some cats but not some cats like some some.

Substitutions and capture groups are very useful in implementing simple chatbots like ELIZA (Weizenbaum, 1966). Recall that ELIZA simulates a Rogerian psychologist by carrying on conversations like the following:
ELIZA works by having a series or cascade of regular expression substitutions each of which matches and changes some part of the input lines. After the input is uppercased, substitutions change all instances of MY to YOUR, and I’M to YOU ARE, and so on. That way when ELIZA repeats back part of the user utterance, it will seem to be referring correctly to the user. The next set of substitutions matches and replaces other patterns in the input. Here are some examples:

```regex
s/.*/ YOU ARE (depressed|sad) .*/I AM SORRY TO HEAR YOU ARE \1/
s/.*/ YOU ARE (depressed|sad) .*/WHY DO YOU THINK YOU ARE \1/
s/.*/ all .*/IN WHAT WAY/
s/.*/ always .*/CAN YOU THINK OF A SPECIFIC EXAMPLE/
```

Since multiple substitutions can apply to a given input, substitutions are assigned a rank and applied in order. Creating patterns is the topic of Exercise 2.3, and we return to the details of the ELIZA architecture in Chapter 15.

### 2.1.7 Lookahead Assertions

Finally, there will be times when we need to predict the future: look ahead in the text to see if some pattern matches, but not yet advance the pointer we always keep to where we are in the text, so that we can then deal with the pattern if it occurs, but if it doesn’t we can check for something else instead.

These lookahead assertions make use of the (?) syntax that we saw in the previous section for non-capture groups. The operator (?= pattern) is true if pattern occurs, but is zero-width, i.e. the match pointer doesn’t advance. The operator (?! pattern) only returns true if a pattern does not match, but again is zero-width and doesn’t advance the pointer. Negative lookahead is commonly used when we are parsing some complex pattern but want to rule out a special case. For example suppose we want to match, at the beginning of a line, any single word that doesn’t start with “Volcano”. We can use negative lookahead to do this:

```regex
/\W*(?!Volcano)[A-Za-z]+/
```

### 2.2 Words

Before we talk about processing words, we need to decide what counts as a word. Let’s start by looking at one particular corpus (plural corpora), a computer-readable collection of text or speech. For example the Brown corpus is a million-word collection of samples from 500 written English texts from different genres (newspaper, fiction, non-fiction, academic, etc.), assembled at Brown University in 1963–64 (Kučera and Francis, 1967). How many words are in the following Brown sentence?

User$_1$: Men are all alike.
ELIZA$_1$: IN WHAT WAY
User$_2$: They’re always bugging us about something or other.
ELIZA$_2$: CAN YOU THINK OF A SPECIFIC EXAMPLE
User$_3$: Well, my boyfriend made me come here.
ELIZA$_3$: YOUR BOYFRIEND MADE YOU COME HERE
User$_4$: He says I’m depressed much of the time.
ELIZA$_4$: I AM SORRY TO HEAR YOU ARE DEPRESSED
He stepped out into the hall, was delighted to encounter a water brother.

This sentence has 13 words if we don’t count punctuation marks as words, 15 if we count punctuation. Whether we treat period (‘.’), comma (‘,’), and so on as words depends on the task. Punctuation is critical for finding boundaries of things (commas, periods, colons) and for identifying some aspects of meaning (question marks, exclamation marks, quotation marks). For some tasks, like part-of-speech tagging or parsing or speech synthesis, we sometimes treat punctuation marks as if they were separate words.

The Switchboard corpus of American English telephone conversations between strangers was collected in the early 1990s; it contains 2430 conversations averaging 6 minutes each, totaling 240 hours of speech and about 3 million words (Godfrey et al., 1992). Such corpora of spoken language introduce other complications with regard to defining words. Let’s look at one utterance from Switchboard; an utterance is the spoken correlate of a sentence:

I do uh main- mainly business data processing

This utterance has two kinds of disfluencies. The broken-off word main- is called a fragment. Words like uh and um are called fillers or filled pauses. Should we consider these to be words? Again, it depends on the application. If we are building a speech transcription system, we might want to eventually strip out the disfluencies.

But we also sometimes keep disfluencies around. Disfluencies like uh or um are actually helpful in speech recognition in predicting the upcoming word, because they may signal that the speaker is restarting the clause or idea, and so for speech recognition they are treated as regular words. Because people use different disfluencies they can also be a cue to speaker identification. In fact Clark and Fox Tree (2002) showed that uh and um have different meanings. What do you think they are?

Perhaps most important, in thinking about what is a word, we need to distinguish two ways of talking about words that will be useful throughout the book. Word types are the number of distinct words in a corpus; if the set of words in the vocabulary is \( V \), the number of types is the vocabulary size \( |V| \). Word instances are the total number \( N \) of running words.

If we ignore punctuation, the following Brown sentence has 16 instances and 14 types:

They picnicked by the pool, then lay back on the grass and looked at the stars.

We still have decisions to make! For example, should we consider a capitalized string (like They) and one that is uncapitalized (like they) to be the same word type? The answer is that it depends on the task! They and they might be lumped together as the same type in some tasks, like speech recognition, where we might just care about getting the words in order and don’t care about the formatting, while for other tasks, such as deciding whether a particular word is a noun or verb (part-of-speech tagging) or whether a word is a name of a person or location (named-entity tagging), capitalization is a useful feature and is retained. Sometimes we keep around two versions of a particular NLP model, one with capitalization and one without capitalization.

How many words are there in English? When we speak about the number of words in the language, we are generally referring to word types. Fig. 2.11 shows the rough numbers of types and instances computed from some English corpora.

---

1. In earlier tradition, and occasionally still, you might see word instances referred to as word tokens, but we now try to reserve the word token instead to mean the output of word tokenization algorithms.
2.3 Corpora

Words don’t appear out of nowhere. Any particular piece of text that we study is produced by one or more specific speakers or writers, in a specific dialect of a specific language, at a specific time, in a specific place, for a specific function.

Perhaps the most important dimension of variation is the language. NLP algorithms are most useful when they apply across many languages. The world has 7097...
languages at the time of this writing, according to the online Ethnologue catalog (Simons and Fennig, 2018). It is important to test algorithms on more than one language, and particularly on languages with different properties; by contrast there is an unfortunate current tendency for NLP algorithms to be developed or tested just on English (Bender, 2019). Even when algorithms are developed beyond English, they tend to be developed for the official languages of large industrialized nations (Chinese, Spanish, Japanese, German etc.), but we don’t want to limit tools to just these few languages. Furthermore, most languages also have multiple varieties, often spoken in different regions or by different social groups. Thus, for example, if we’re processing text that uses features of African American English (AAE) or African American Vernacular English (AAVE)—the variations of English used by millions of people in African American communities (King 2020)—we must use NLP tools that function with features of those varieties. Twitter posts might use features often used by speakers of African American English, such as constructions like iont (I don’t) in Mainstream American English (MAE), or talmbout corresponding to MAE talking about, both examples that influence word segmentation (Blodgett et al. 2016, Jones 2015).

It’s also quite common for speakers or writers to use multiple languages in a single communicative act, a phenomenon called code switching. Code switching is enormously common across the world; here are examples showing Spanish and (transliterated) Hindi code switching with English (Solorio et al. 2014, Jurgens et al. 2017):

(2.2) Por primera vez veo a @username actualmente siendo elocuente! ¡esto fue lindo!:)
[For the first time I get to see @username actually being hateful! it was beautiful:) ]

(2.3) dost tha or ra- hega ... dont worry ... but dherya rakhe
[“he was and will remain a friend ... don’t worry ... but have faith”]

Another dimension of variation is the genre. The text that our algorithms must process might come from newswire, fiction or non-fiction books, scientific articles, Wikipedia, or religious texts. It might come from spoken genres like telephone conversations, business meetings, police body-worn cameras, medical interviews, or transcripts of television shows or movies. It might come from work situations like doctors’ notes, legal text, or parliamentary or congressional proceedings.

Text also reflects the demographic characteristics of the writer (or speaker): their age, gender, race, socioeconomic class can all influence the linguistic properties of the text we are processing.

And finally, time matters too. Language changes over time, and for some languages we have good corpora of texts from different historical periods.

Because language is so situated, when developing computational models for language processing from a corpus, it’s important to consider who produced the language, in what context, for what purpose. How can a user of a dataset know all these details? The best way is for the corpus creator to build a datasheet (Gebru et al., 2020) or data statement (Bender et al., 2021) for each corpus. A datasheet specifies properties of a dataset like:

Motivation: Why was the corpus collected, by whom, and who funded it?

Situation: When and in what situation was the text written/spoken? For example, was there a task? Was the language originally spoken conversation, edited text, social media communication, monologue vs. dialogue?

Language variety: What language (including dialect/region) was the corpus in?
2.4 Simple Unix Tools for Word Tokenization

Before almost any natural language processing of a text, the text has to be normalized, a task called text normalization. At least three tasks are commonly applied as part of any normalization process:

1. Tokenizing (segmenting) words
2. Normalizing word formats
3. Segmenting sentences

In the next sections we walk through each of these tasks, but we’ll first start with an easy, if somewhat naive version of word tokenization and normalization (and frequency computation) that can be accomplished for English solely in a single UNIX command-line, inspired by Church (1994). We’ll make use of some Unix commands: tr, used to systematically change particular characters in the input; sort, which sorts input lines in alphabetical order; and uniq, which collapses and counts adjacent identical lines.

For example let’s begin with the ‘complete words’ of Shakespeare in one file, sh.txt. We can use tr to tokenize the words by changing every sequence of non-alphabetic characters to a newline (‘A-Za-z’ means alphabetic and the -c option complements to non-alphabet, so together they mean to change every non-alphabetic character into a newline. The -s (‘squeeze’) option is used to replace the result of multiple consecutive changes into a single output, so a series of non-alphabetic characters in a row would all be ‘squeezed’ into a single newline):

```
tr -sc 'A-Za-z' '
' < sh.txt
```

The output of this command will be:

```
THE
SONNETS
by
William
Shakespeare
From
fairest
creatures
We
...
```

Now that there is one word per line, we can sort the lines, and pass them to uniq -c which will collapse and count them:

```
tr -sc 'A-Za-z' '
' < sh.txt | sort | uniq -c
```
with the following output:

```
1945 A
72 AARON
19 ABBESS
25 Aaron
6 Abate
1 Abates
5 Abbess
6 Abbey
3 Abbot
...
```

Alternatively, we can collapse all the upper case to lower case:

```
tr -sc 'A-Za-z' '\n' < sh.txt | tr A-Z a-z | sort | uniq -c
```

whose output is

```
14725 a
 97 aaron
 1 abaissiez
 10 abandon
 2 abandoned
 2 abase
 1 abash
 14 abate
 3 abated
 3 abatement
...
```

Now we can sort again to find the frequent words. The `-n` option to `sort` means to sort numerically rather than alphabetically, and the `-r` option means to sort in reverse order (highest-to-lowest):

```
tr -sc 'A-Za-z' '\n' < sh.txt | tr A-Z a-z | sort | uniq -c | sort -n -r
```

The results show that the most frequent words in Shakespeare, as in any other corpus, are the short **function words** like articles, pronouns, prepositions:

```
27378 the
26084 and
22538 i
19771 to
17481 of
14725 a
13826 you
12489 my
11318 that
11112 in
...
```

Unix tools of this sort can be very handy in building quick word count statistics for any corpus in English. While in some versions of Unix these command-line tools also correctly handle Unicode characters and so can be used for many languages, in general for handling most languages outside English we use more sophisticated tokenization algorithms.
2.5  Word Tokenization

The simple UNIX tools above were fine for getting rough word statistics but more sophisticated algorithms are generally necessary for *tokenization*, the task of segmenting running text into words. There are roughly two classes of tokenization algorithms. In top-down tokenization, we define a standard and implement rules to implement that kind of tokenization. In bottom-up tokenization, we use simple statistics of letter sequences to break up words into subword tokens.

### 2.5.1  Top-down (rule-based) tokenization

While the Unix command sequence just removed all the numbers and punctuation, for most NLP applications we’ll need to keep these in our tokenization. We often want to break off punctuation as a separate token; commas are a useful piece of information for parsers, periods help indicate sentence boundaries. But we’ll often want to keep the punctuation that occurs word internally, in examples like *m.p.h.*, *Ph.D.*, *AT&T*, and *cap’n*. Special characters and numbers will need to be kept in prices ($45.55) and dates (01/02/06); we don’t want to segment that price into separate tokens of “45” and “55”. And there are URLs ([https://www.stanford.edu](https://www.stanford.edu)), Twitter hashtags (#nlproc), or email addresses (someone@cs.colorado.edu).

Number expressions introduce other complications as well; while commas normally appear at word boundaries, commas are used inside numbers in English, every three digits: **555, 500, 50**. Languages, and hence tokenization requirements, differ on this; many continental European languages like Spanish, French, and German, by contrast, use a comma to mark the decimal point, and spaces (or sometimes periods) where English puts commas, for example, **555 500, 50**.

A tokenizer can also be used to expand clitic contractions that are marked by apostrophes, for example, converting *what’re* to the two tokens *what* and *are*, and *we’re* to *we* and *are*. A clitic is a part of a word that can’t stand on its own, and can only occur when it is attached to another word. Some such contractions occur in other alphabetic languages, including articles and pronouns in French (*j’ai*, *l’homme*).

Depending on the application, tokenization algorithms may also tokenize multiword expressions like *New York* or *rock ’n’ roll* as a single token, which requires a multiword expression dictionary of some sort. Tokenization is thus intimately tied up with *named entity recognition*, the task of detecting names, dates, and organizations (Chapter 8).

One commonly used tokenization standard is known as the Penn Treebank tokenization standard, used for the parsed corpora (treebanks) released by the Linguistic Data Consortium (LDC), the source of many useful datasets. This standard separates out clitics (*doesn’t* becomes *does* plus *n’t*), keeps hyphenated words together, and separates out all punctuation (to save space we’re showing visible spaces ‘.’ between tokens, although newlines is a more common output):

**Input:** "The San Francisco-based restaurant," they said, "doesn’t charge $10".

**Output:** "The San Francisco-based restaurant.o.s they.o said.o.n’t does.o s charge.o.$ 10.o".

In practice, since tokenization needs to be run before any other language processing, it needs to be very fast. The standard method for tokenization is therefore to use deterministic algorithms based on regular expressions compiled into very efficient...
finite state automata. For example, Fig. 2.12 shows an example of a basic regular expression that can be used to tokenize English with the nltk.regexp_tokenize function of the Python-based Natural Language Toolkit (NLTK) (Bird et al. 2009; https://www.nltk.org).

>>> text = 'That U.S.A. poster-print costs $12.40...

>>> pattern = r''(?x) # set flag to allow verbose regexps
... (?:[A-Z]\.| )+ # abbreviations, e.g. U.S.A.
... | \w+(?:-\w+)* # words with optional internal hyphens
... | \$?d+(?:\./|\s)d?>%? # currency, percentages, e.g. $12.40, 82%
... | \.\.\.
... | [\[\].\(;\':\-\]
... | # these are separate tokens; includes ]

>>> nltk.regexp_tokenize(text, pattern)
['That', 'U.S.A.', 'poster-print', 'costs', '$12.40', '...']

Figure 2.12 A Python trace of regular expression tokenization in the NLTK Python-based natural language processing toolkit (Bird et al., 2009), commented for readability; the (?x) verbose flag tells Python to strip comments and whitespace. Figure from Chapter 3 of Bird et al. (2009).

Carefully designed deterministic algorithms can deal with the ambiguities that arise, such as the fact that the apostrophe needs to be tokenized differently when used as a genitive marker (as in the book’s cover), a quotative as in ‘The other class’, she said, or in clitics like they’re.

Word tokenization is more complex in languages like written Chinese, Japanese, and Thai, which do not use spaces to mark potential word-boundaries. In Chinese, for example, words are composed of characters (called hanzi in Chinese). Each character generally represents a single unit of meaning (called a morpheme) and is pronounceable as a single syllable. Words are about 2.4 characters long on average. But deciding what counts as a word in Chinese is complex. For example, consider the following sentence:

(2.4) 姚明进入总决赛 yáo mínɡ jìn rù zǒnɡ jué sài
“Yao Ming reaches the finals”

As Chen et al. (2017b) point out, this could be treated as 3 words (‘Chinese Treebank’ segmentation):

(2.5) 姚明 进入 总决赛 YaoMing reaches finals

or as 5 words (‘Peking University’ segmentation):

(2.6) 姚明 进入 总决赛 Yao Ming reaches overall finals

Finally, it is possible in Chinese simply to ignore words altogether and use characters as the basic elements, treating the sentence as a series of 7 characters:

(2.7) 姚明 进入 总决赛 Yao Ming enter enter overall decision game

In fact, for most Chinese NLP tasks it turns out to work better to take characters rather than words as input, since characters are at a reasonable semantic level for most applications, and since most word standards, by contrast, result in a huge vocabulary with large numbers of very rare words (Li et al., 2019b).
However, for Japanese and Thai the character is too small a unit, and so algorithms for word segmentation are required. These can also be useful for Chinese in the rare situations where word rather than character boundaries are required. The standard segmentation algorithms for these languages use neural sequence models trained via supervised machine learning on hand-segmented training sets; we’ll introduce sequence models in Chapter 8 and Chapter 9.

2.5.2 Byte-Pair Encoding: A Bottom-up Tokenization Algorithm

There is a third option to tokenizing text, one that is most commonly used by large language models. Instead of defining tokens as words (whether delimited by spaces or more complex algorithms), or as characters (as in Chinese), we can use our data to automatically tell us what the tokens should be. This is especially useful in dealing with unknown words, an important problem in language processing. As we will see in the next chapter, NLP algorithms often learn some facts about language from one corpus (a training corpus) and then use these facts to make decisions about a separate test corpus and its language. Thus if our training corpus contains, say the words low, new, newer, but not lower, then if the word lower appears in our test corpus, our system will not know what to do with it.

To deal with this unknown word problem, modern tokenizers automatically induce sets of tokens that include tokens smaller than words, called subwords. Subwords can be arbitrary substrings, or they can be meaning-bearing units like the morphemes -est or -er. (A morpheme is the smallest meaning-bearing unit of a language; for example the word unlikeliest has the morphemes un-, likely, and -est.) In modern tokenization schemes, most tokens are words, but some tokens are frequently occurring morphemes or other subwords like -er. Every unseen word like lower can thus be represented by some sequence of known subword units, such as low and er, or even as a sequence of individual letters if necessary.

Most tokenization schemes have two parts: a token learner, and a token segmenter. The token learner takes a raw training corpus (sometimes roughly pre-separated into words, for example by whitespace) and induces a vocabulary, a set of tokens. The token segmenter takes a raw test sentence and segments it into the tokens in the vocabulary. Two algorithms are widely used: byte-pair encoding (Sennrich et al., 2016), and unigram language modeling (Kudo, 2018). There is also a SentencePiece library that includes implementations of both of these (Kudo and Richardson, 2018a), and people often use the name SentencePiece to simply mean unigram language modeling tokenization.

In this section we introduce the simplest of the three, the byte-pair encoding or BPE algorithm (Sennrich et al., 2016); see Fig. 2.13. The BPE token learner begins with a vocabulary that is just the set of all individual characters. It then examines the training corpus, chooses the two symbols that are most frequently adjacent (say ‘A’, ‘B’), adds a new merged symbol ‘AB’ to the vocabulary, and replaces every adjacent ‘A’ ‘B’ in the corpus with the new ‘AB’. It continues to count and merge, creating new longer and longer character strings, until k merges have been done creating k novel tokens; k is thus a parameter of the algorithm. The resulting vocabulary consists of the original set of characters plus k new symbols.

The algorithm is usually run inside words (not merging across word boundaries), so the input corpus is first white-space-separated to give a set of strings, each corresponding to the characters of a word, plus a special end-of-word symbol __, and its counts. Let’s see its operation on the following tiny input corpus of 18 word tokens with counts for each word (the word low appears 5 times, the word newer 6 times,
and so on), which would have a starting vocabulary of 11 letters:

<table>
<thead>
<tr>
<th>corpus</th>
<th>vocabulary</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 low</td>
<td>_, d, e, i, l, n, o, r, s, t, w</td>
</tr>
<tr>
<td>2 lowest</td>
<td></td>
</tr>
<tr>
<td>6 newer</td>
<td></td>
</tr>
<tr>
<td>3 wider</td>
<td></td>
</tr>
<tr>
<td>2 new</td>
<td></td>
</tr>
</tbody>
</table>

The BPE algorithm first counts all pairs of adjacent symbols: the most frequent is the pair er because it occurs in newer (frequency of 6) and wider (frequency of 3) for a total of 9 occurrences. We then merge these symbols, treating er as one symbol, and count again:

<table>
<thead>
<tr>
<th>corpus</th>
<th>vocabulary</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 low</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er</td>
</tr>
<tr>
<td>2 lowest</td>
<td></td>
</tr>
<tr>
<td>6 newer</td>
<td></td>
</tr>
<tr>
<td>3 wider</td>
<td></td>
</tr>
<tr>
<td>2 new</td>
<td></td>
</tr>
</tbody>
</table>

Now the most frequent pair is er _, which we merge; our system has learned that there should be a token for word-final er, represented as er _: 

<table>
<thead>
<tr>
<th>corpus</th>
<th>vocabulary</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 low</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _</td>
</tr>
<tr>
<td>2 lowest</td>
<td></td>
</tr>
<tr>
<td>6 newer</td>
<td></td>
</tr>
<tr>
<td>3 wider</td>
<td></td>
</tr>
<tr>
<td>2 new</td>
<td></td>
</tr>
</tbody>
</table>

Next n e (total count of 8) get merged to ne:

<table>
<thead>
<tr>
<th>corpus</th>
<th>vocabulary</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 low</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne</td>
</tr>
<tr>
<td>2 lowest</td>
<td></td>
</tr>
<tr>
<td>6 newer</td>
<td></td>
</tr>
<tr>
<td>3 wider</td>
<td></td>
</tr>
<tr>
<td>2 new</td>
<td></td>
</tr>
</tbody>
</table>

If we continue, the next merges are:

<table>
<thead>
<tr>
<th>merge</th>
<th>current vocabulary</th>
</tr>
</thead>
<tbody>
<tr>
<td>(ne, w)</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne, new</td>
</tr>
<tr>
<td>(l, o)</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne, new, lo</td>
</tr>
<tr>
<td>(lo, w)</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne, new, lo, low</td>
</tr>
<tr>
<td>(new, er _)</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne, new, lo, low, newer _</td>
</tr>
<tr>
<td>(low, _)</td>
<td>_, d, e, i, l, n, o, r, s, t, w, er, er _, ne, new, lo, low, newer _, low</td>
</tr>
</tbody>
</table>

Once we’ve learned our vocabulary, the token segmenter is used to tokenize a test sentence. The token segmenter just runs on the test data the merges we have learned from the training data, greedily, in the order we learned them. (Thus the frequencies in the test data don’t play a role, just the frequencies in the training data). So first we segment each test sentence word into characters. Then we apply the first rule: replace every instance of er _ in the test corpus with er, and then the second rule: replace every instance of er _ in the test corpus with er _, and so on.

2 Note that there can be ties; we could have instead chosen to merge r _ first, since that also has a frequency of 9.
2.6 • Word Normalization, Lemmatization and Stemming

Word normalization is the task of putting words/tokens in a standard format. The simplest case of word normalization is case folding. Mapping everything to lower case means that Woodchuck and woodchuck are represented identically, which is very helpful for generalization in many tasks, such as information retrieval or speech recognition. For sentiment analysis and other text classification tasks, information extraction, and machine translation, by contrast, case can be quite helpful and case folding is generally not done. This is because maintaining the difference between, for example, US the country and us the pronoun can outweigh the advantage in generalization that case folding would have provided for other words.

Systems that use BPE or other kinds of bottom-up tokenization may do no further word normalization. In other NLP systems, we may want to do further normalizations, like choosing a single normal form for words with multiple forms like USA and US or uh–uh and uhhuh. This standardization may be valuable, despite the spelling information that is lost in the normalization process. For information retrieval or information extraction about the US, we might want to see information from documents whether they mention the US or the USA.

2.6.1 Lemmatization

For other natural language processing situations we also want two morphologically different forms of a word to behave similarly. For example in web search, someone may type the string woodchucks but a useful system might want to also return pages that mention woodchuck with no s. This is especially common in morphologically complex languages like Polish, where for example the word Warsaw has different endings when it is the subject (Warszawa), or after a preposition like “in Warsaw” (w
Warszawie), or “to Warsaw” (do Warszawy), and so on. **Lemmatization** is the task of determining that two words have the same root, despite their surface differences. The words *am, are, and is* have the shared lemma *be*; the words *dinner and dinners* both have the lemma *dinner*. Lemmatizing each of these forms to the same lemma will let us find all mentions of words in Polish like *Warsaw*. The lemmatized form of a sentence like *He is reading detective stories* would thus be *He be read detective story*.

How is lemmatization done? The most sophisticated methods for lemmatization involve complete **morphological parsing** of the word. **Morphology** is the study of the way words are built up from smaller meaning-bearing units called **morphemes**.

Two broad classes of morphemes can be distinguished: **stems**—the central morpheme of the word, supplying the main meaning—and **affixes**—adding “additional” meanings of various kinds. So, for example, the word *fox* consists of one morpheme (the morpheme *fox*) and the word *cats* consists of two: the morpheme *cat* and the morpheme *-s*. A morphological parser takes a word like *cats* and parses it into the two morphemes *cat* and *s*, or parses a Spanish word like *amaren* (‘if in the future they would love’) into the morpheme *amar* ‘to love’, and the morphological features 3PL and *future subjunctive*.

**Stemming: The Porter Stemmer**

Lemmatization algorithms can be complex. For this reason we sometimes make use of a simpler but cruder method, which mainly consists of chopping off word-final affixes. This naïve version of morphological analysis is called **stemming**. For example, the **Porter stemmer**, a widely used stemming algorithm (Porter, 1980), when applied to the following paragraph:

> This was not the map we found in Billy Bones’s chest, but an accurate copy, complete in all things—names and heights and soundings—with the single exception of the red crosses and the written notes.

produces the following stemmed output:

> Thi wa not the map we found in Billi Bone s chest but an accur copi complet in all thing name and height and sound with the singl except of the red cross and the written note

The algorithm is based on series of rewrite rules run in series: the output of each pass is fed as input to the next pass. Here are some sample rules (more details can be found at [https://tartarus.org/martin/PorterStemmer/](https://tartarus.org/martin/PorterStemmer/)):

- ATIONAL → ATE (e.g., relational → relate)
- ING → ε if the stem contains a vowel (e.g., motoring → motor)
- SSES → SS (e.g., grasses → grass)

Simple stemmers can be useful in cases where we need to collapse across different variants of the same lemma. Nonetheless, they do tend to commit errors of both over- and under-generalizing, as shown in the table below (Krovetz, 1993):

<table>
<thead>
<tr>
<th>Errors of Commission</th>
<th>Errors of Omission</th>
</tr>
</thead>
<tbody>
<tr>
<td>organization</td>
<td>European</td>
</tr>
<tr>
<td>doing</td>
<td>analyzes</td>
</tr>
<tr>
<td>numerical policy</td>
<td>noisy</td>
</tr>
<tr>
<td></td>
<td>sparsity</td>
</tr>
</tbody>
</table>
2.7 Sentence Segmentation

Sentence segmentation is another important step in text processing. The most useful cues for segmenting a text into sentences are punctuation, like periods, question marks, and exclamation points. Question marks and exclamation points are relatively unambiguous markers of sentence boundaries. Periods, on the other hand, are more ambiguous. The period character “.” is ambiguous between a sentence boundary marker and a marker of abbreviations like Mr. or Inc. The previous sentence that you just read showed an even more complex case of this ambiguity, in which the final period of Inc. marked both an abbreviation and the sentence boundary marker. For this reason, sentence tokenization and word tokenization may be addressed jointly.

In general, sentence tokenization methods work by first deciding (based on rules or machine learning) whether a period is part of the word or is a sentence-boundary marker. An abbreviation dictionary can help determine whether the period is part of a commonly used abbreviation; the dictionaries can be hand-built or machine-learned (Kiss and Strunk, 2006), as can the final sentence splitter. In the Stanford CoreNLP toolkit (Manning et al., 2014), for example sentence splitting is rule-based, a deterministic consequence of tokenization; a sentence ends when a sentence-ending punctuation (., !, or ?) is not already grouped with other characters into a token (such as for an abbreviation or number), optionally followed by additional final quotes or brackets.

2.8 Minimum Edit Distance

Much of natural language processing is concerned with measuring how similar two strings are. For example in spelling correction, the user typed some erroneous string—let’s say graffe—and we want to know what the user meant. The user probably intended a word that is similar to giraffe. Among candidate similar words, the word giraffe, which differs by only one letter from graffe, seems intuitively to be more similar than, say grail or graf, which differ in more letters. Another example comes from coreference, the task of deciding whether two strings such as the following refer to the same entity:

Stanford President Marc Tessier-Lavigne
Stanford University President Marc Tessier-Lavigne

Again, the fact that these two strings are very similar (differing by only one word) seems like useful evidence for deciding that they might be coreferent.

Edit distance gives us a way to quantify both of these intuitions about string similarity. More formally, the minimum edit distance between two strings is defined as the minimum number of editing operations (operations like insertion, deletion, substitution) needed to transform one string into another.

The gap between intention and execution, for example, is 5 (delete an i, substitute e for n, substitute x for t, insert c, substitute u for n). It’s much easier to see this by looking at the most important visualization for string distances, an alignment between the two strings, shown in Fig. 2.14. Given two sequences, an alignment is a correspondence between substrings of the two sequences. Thus, we say I aligns with the empty string, N with E, and so on. Beneath the aligned strings is another representation; a series of symbols expressing an operation list for converting the
top string into the bottom string: d for deletion, s for substitution, i for insertion.

We can also assign a particular cost or weight to each of these operations. The Levenshtein distance between two sequences is the simplest weighting factor in which each of the three operations has a cost of 1 (Levenshtein, 1966)—we assume that the substitution of a letter for itself, for example, t for t, has zero cost. The Levenshtein distance between intention and execution is 5. Levenshtein also proposed an alternative version of his metric in which each insertion or deletion has a cost of 1 and substitutions are not allowed. (This is equivalent to allowing substitution, but giving each substitution a cost of 2 since any substitution can be represented by one insertion and one deletion). Using this version, the Levenshtein distance between intention and execution is 8.

2.8.1 The Minimum Edit Distance Algorithm

How do we find the minimum edit distance? We can think of this as a search task, in which we are searching for the shortest path—a sequence of edits—from one string to another.

The space of all possible edits is enormous, so we can’t search naively. However, lots of distinct edit paths will end up in the same state (string), so rather than recomputing all those paths, we could just remember the shortest path to a state each time we saw it. We can do this by using dynamic programming. Dynamic programming is the name for a class of algorithms, first introduced by Bellman (1957), that apply a table-driven method to solve problems by combining solutions to subproblems. Some of the most commonly used algorithms in natural language processing make use of dynamic programming, such as the Viterbi algorithm (Chapter 8) and the CKY algorithm for parsing (Chapter 17).

The intuition of a dynamic programming problem is that a large problem can be solved by properly combining the solutions to various subproblems. Consider the shortest path of transformed words that represents the minimum edit distance between the strings intention and execution shown in Fig. 2.16.

Imagine some string (perhaps it is exention) that is in this optimal path (whatever it is). The intuition of dynamic programming is that if exention is in the optimal
2.8 • Minimum Edit Distance

The minimum edit distance algorithm was named by Wagner and Fischer (1974) but independently discovered by many people (see the Historical Notes section of Chapter 8).

Let’s first define the minimum edit distance between two strings. Given two strings, the source string $X$ of length $n$, and target string $Y$ of length $m$, we’ll define $D[i][j]$ as the edit distance between $X[1..i]$ and $Y[1..j]$, i.e., the first $i$ characters of $X$ and the first $j$ characters of $Y$. The edit distance between $X$ and $Y$ is thus $D[n][m]$.

We’ll use dynamic programming to compute $D[n][m]$ bottom up, combining solutions to subproblems. In the base case, with a source substring of length $i$ but an empty target string, going from $i$ characters to 0 requires $i$ deletes. With a target substring of length $j$ but an empty source going from 0 characters to $j$ characters requires $j$ inserts. Having computed $D[i][j]$ for small $i, j$ we then compute larger $D[i][j]$ based on previously computed smaller values. The value of $D[i][j]$ is computed by taking the minimum of the three possible paths through the matrix which arrive there:

$$D[i,j] = \min \begin{cases} D[i-1,j] + \text{del-cost}(source[i]) \\ D[i,j-1] + \text{ins-cost}(target[j]) \\ D[i-1, j-1] + \text{sub-cost}(source[i], target[j]) \end{cases}$$ (2.8)

If we assume the version of Levenshtein distance in which the insertions and deletions each have a cost of 1 (ins-cost(·) = del-cost(·) = 1), and substitutions have a cost of 2 (except substitution of identical letters have zero cost), the computation for $D[i][j]$ becomes:

$$D[i,j] = \min \begin{cases} D[i-1,j] + 1 \\ D[i,j-1] + 1 \\ D[i-1, j-1] + \begin{cases} 2; & \text{if } source[i] \neq target[j] \\ 0; & \text{if } source[i] = target[j] \end{cases} \end{cases}$$ (2.9)

The algorithm is summarized in Fig. 2.17; Fig. 2.18 shows the results of applying the algorithm to the distance between intention and execution with the version of Levenshtein in Eq. 2.9.

Alignment Knowing the minimum edit distance is useful for algorithms like finding potential spelling error corrections. But the edit distance algorithm is important in another way; with a small change, it can also provide the minimum cost alignment between two strings. Aligning two strings is useful throughout speech and
**function** MIN-EDIT-DISTANCE(source, target) **returns** min-distance

\[ n \leftarrow \text{LENGTH}(source) \]
\[ m \leftarrow \text{LENGTH}(target) \]

Create a distance matrix \( D[n+1,m+1] \)

# Initialization: the zeroth row and column is the distance from the empty string
\[ D[0,0] = 0 \]

for each row \( i \) from 1 to \( n \) do
\[ D[i,0] \leftarrow D[i-1,0] + \text{del-cost}(source[i]) \]

for each column \( j \) from 1 to \( m \) do
\[ D[0,j] \leftarrow D[0,j-1] + \text{ins-cost}(target[j]) \]

# Recurrence relation:
for each row \( i \) from 1 to \( n \) do
  for each column \( j \) from 1 to \( m \) do
    \[ D[i,j] \leftarrow \text{MIN}( D[i-1,j] + \text{del-cost}(source[i]), D[i,j-1] + \text{sub-cost}(source[i],target[j]), D[i-1,j-1] + \text{ins-cost}(target[j]) ) \]

# Termination
return \( D[n,m] \)

**Figure 2.17** The minimum edit distance algorithm, an example of the class of dynamic programming algorithms. The various costs can either be fixed (e.g., \( \forall x. \text{ins-cost}(x) = 1 \)) or can be specific to the letter (to model the fact that some letters are more likely to be inserted than others). We assume that there is no cost for substituting a letter for itself (i.e., \( \text{sub-cost}(x,x) = 0 \)).

<table>
<thead>
<tr>
<th>Src</th>
<th>Tar</th>
<th>#</th>
<th>e</th>
<th>x</th>
<th>e</th>
<th>c</th>
<th>u</th>
<th>t</th>
<th>i</th>
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**Figure 2.18** Computation of minimum edit distance between intention and execution with the algorithm of Fig. 2.17, using Levenshtein distance with cost of 1 for insertions or deletions, 2 for substitutions.

In speech recognition, minimum edit distance alignment is used to compute the word error rate (Chapter 16). Alignment plays a role in machine translation, in which sentences in a parallel corpus (a corpus with a text in two languages) need to be matched to each other.

To extend the edit distance algorithm to produce an alignment, we can start by visualizing an alignment as a path through the edit distance matrix. Figure 2.19 shows this path with boldfaced cells. Each boldfaced cell represents an alignment of a pair of letters in the two strings. If two boldfaced cells occur in the same row, there will be an insertion in going from the source to the target; two boldfaced cells...
in the same column indicate a deletion.

Figure 2.19 also shows the intuition of how to compute this alignment path. The computation proceeds in two steps. In the first step, we augment the minimum edit distance algorithm to store backpointers in each cell. The backpointer from a cell points to the previous cell (or cells) that we came from in entering the current cell. We’ve shown a schematic of these backpointers in Fig. 2.19. Some cells have multiple backpointers because the minimum extension could have come from multiple previous cells. In the second step, we perform a backtrace. In a backtrace, we start from the last cell (at the final row and column), and follow the pointers back through the dynamic programming matrix. Each complete path between the final cell and the initial cell is a minimum distance alignment. Exercise 2.7 asks you to modify the minimum edit distance algorithm to store the pointers and compute the backtrace to output an alignment.

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Figure 2.19 When entering a value in each cell, we mark which of the three neighboring cells we came from with up to three arrows. After the table is full we compute an alignment (minimum edit path) by using a backtrace, starting at the 8 in the lower-right corner and following the arrows back. The sequence of bold cells represents one possible minimum cost alignment between the two strings. Diagram design after Gusfield (1997).

While we worked our example with simple Levenshtein distance, the algorithm in Fig. 2.17 allows arbitrary weights on the operations. For spelling correction, for example, substitutions are more likely to happen between letters that are next to each other on the keyboard. The Viterbi algorithm is a probabilistic extension of minimum edit distance. Instead of computing the “minimum edit distance” between two strings, Viterbi computes the “maximum probability alignment” of one string with another. We’ll discuss this more in Chapter 8.

2.9 Summary

This chapter introduced a fundamental tool in language processing, the regular expression, and showed how to perform basic text normalization tasks including word segmentation and normalization, sentence segmentation, and stemming. We also introduced the important minimum edit distance algorithm for comparing strings. Here’s a summary of the main points we covered about these ideas:

- The regular expression language is a powerful tool for pattern-matching.
- Basic operations in regular expressions include concatenation of symbols, disjunction of symbols ([], |, and .), counters (*, +, and {n,m}), anchors
• Word tokenization and normalization are generally done by cascades of simple regular expression substitutions or finite automata.
• The Porter algorithm is a simple and efficient way to do stemming, stripping off affixes. It does not have high accuracy but may be useful for some tasks.
• The minimum edit distance between two strings is the minimum number of operations it takes to edit one into the other. Minimum edit distance can be computed by dynamic programming, which also results in an alignment of the two strings.

Bibliographical and Historical Notes

Kleene 1951; 1956 first defined regular expressions and the finite automaton, based on the McCulloch-Pitts neuron. Ken Thompson was one of the first to build regular expressions compilers into editors for text searching (Thompson, 1968). His editor ed included a command “g/regular expression/p”, or Global Regular Expression Print, which later became the Unix grep utility.

Text normalization algorithms have been applied since the beginning of the field. One of the earliest widely used stemmers was Lovins (1968). Stemming was also applied early to the digital humanities, by Packard (1973), who built an affix-stripping morphological parser for Ancient Greek. Currently a wide variety of code for tokenization and normalization is available, such as the Stanford Tokenizer (https://nlp.stanford.edu/software/tokenizer.shtml) or specialized tokenizers for Twitter (O’Connor et al., 2010), or for sentiment (http://sentiment christopherpotts.net/tokenizing.html). See Palmer (2012) for a survey of text preprocessing. NLTK is an essential tool that offers both useful Python libraries (https://www.nltk.org) and textbook descriptions (Bird et al., 2009) of many algorithms including text normalization and corpus interfaces.

For more on Herdan’s law and Heaps’ Law, see Herdan (1960, p. 28), Heaps (1978), Egghe (2007) and Baayen (2001); Yasseri et al. (2012) discuss the relationship with other measures of linguistic complexity. For more on edit distance, see the excellent Gusfield (1997). Our example measuring the edit distance from ‘intention’ to ‘execution’ was adapted from Kruskal (1983). There are various publicly available packages to compute edit distance, including Unix diff and the NIST sclite program (NIST, 2005).

In his autobiography Bellman (1984) explains how he originally came up with the term dynamic programming:

“...The 1950s were not good years for mathematical research. [the] Secretary of Defense ... had a pathological fear and hatred of the word, research... I decided therefore to use the word, “programming”. I wanted to get across the idea that this was dynamic, this was multi-stage... I thought, let’s ... take a word that has an absolutely precise meaning, namely dynamic... it’s impossible to use the word, dynamic, in a pejorative sense. Try thinking of some combination that will possibly give it a pejorative meaning. It’s impossible. Thus, I thought dynamic programming was a good name. It was something not even a Congressman could object to.”
Exercises

2.1 Write regular expressions for the following languages.
   1. the set of all alphabetic strings;
   2. the set of all lower case alphabetic strings ending in a b;
   3. the set of all strings from the alphabet a, b such that each a is immediately preceded by and immediately followed by a b;

2.2 Write regular expressions for the following languages. By “word”, we mean an alphabetic string separated from other words by whitespace, any relevant punctuation, line breaks, and so forth.
   1. the set of all strings with two consecutive repeated words (e.g., “Humbert Humbert” and “the the” but not “the bug” or “the big bug”);
   2. all strings that start at the beginning of the line with an integer and that end at the end of the line with a word;
   3. all strings that have both the word grotto and the word raven in them (but not, e.g., words like grottos that merely contain the word grotto);
   4. write a pattern that places the first word of an English sentence in a register. Deal with punctuation.

2.3 Implement an ELIZA-like program, using substitutions such as those described on page 13. You might want to choose a different domain than a Rogerian psychologist, although keep in mind that you would need a domain in which your program can legitimately engage in a lot of simple repetition.

2.4 Compute the edit distance (using insertion cost 1, deletion cost 1, substitution cost 1) of “leda” to “deal”. Show your work (using the edit distance grid).

2.5 Figure out whether drive is closer to brief or to divers and what the edit distance is to each. You may use any version of distance that you like.

2.6 Now implement a minimum edit distance algorithm and use your hand-computed results to check your code.

2.7 Augment the minimum edit distance algorithm to output an alignment; you will need to store pointers and add a stage to compute the backtrace.
“You are uniformly charming!” cried he, with a smile of associating and now and then I bowed and they perceived a chaise and four to wish for.

Random sentence generated from a Jane Austen trigram model

Predicting is difficult—especially about the future, as the old quip goes. But how about predicting something that seems much easier, like the next few words someone is going to say? What word, for example, is likely to follow

Please turn your homework ...

Hopefully, most of you concluded that a very likely word is in, or possibly over, but probably not refrigerator or the. In this chapter we formalize this intuition by introducing models that assign a probability to each possible next word.

Models that assign probabilities to upcoming words, or sequences of words in general, are called language models or LMs. Why would we want to predict upcoming words? It turns out that the large language models that revolutionized modern NLP are trained just by predicting words!! As we’ll see in chapters 7-10, large language models learn an enormous amount about language solely from being trained to predict upcoming words from neighboring words.

Language models can also assign a probability to an entire sentence. For example, they can predict that the following sequence has a much higher probability of appearing in a text:

all of a sudden I notice three guys standing on the sidewalk

than does this same set of words in a different order:

on guys all I of notice sidewalk three a sudden standing the

Why does it matter what the probability of a sentence is or how probable the next word is? In many NLP applications we can use the probability as a way to choose a better sentence or word over a less-appropriate one. For example we can correct grammar or spelling errors like Their are two midterms, in which There was mistyped as Their, or Everything has improve, in which improve should have been improved. The phrase There are will be much more probable than Their are, and has improved than has improve, allowing a language model to help users select the more grammatical variant. Or for a speech recognizer to realize that you said I will be back soonish and not I will be bassoon dish, it helps to know that back soonish is a much more probable sequence. Language models can also help in augmentative and alternative communication systems (Trnka et al. 2007, Kane et al. 2017). People often use such AAC devices if they are physically unable to speak or sign but can instead use eye gaze or other specific movements to select words from a menu. Word prediction can be used to suggest likely words for the menu.
In this chapter we introduce the simplest kind of language model: the n-gram language model. An n-gram is a sequence of n words: a 2-gram (which we’ll call bigram) is a two-word sequence of words like “please turn”, “turn your”, or “your homework”; and a 3-gram (a trigram) is a three-word sequence of words like “please turn your”, or “turn your homework”. But we also (in a bit of terminological ambiguity) use the word ‘n-gram’ to mean a probabilistic model that can estimate the probability of a word given the n-1 previous words, and thereby also to assign probabilities to entire sequences.

In later chapters we will introduce the much more powerful neural large language models, based on the transformer architecture of Chapter 10. But because n-grams have a remarkably simple and clear formalization, we begin our study of language modeling with them, introducing major concepts that will play a role throughout language modeling, concepts like training and test sets, perplexity, sampling, and interpolation.

3.1 N-Grams

Let’s begin with the task of computing $P(w|h)$, the probability of a word $w$ given some history $h$. Suppose the history $h$ is “its water is so transparent that” and we want to know the probability that the next word is the:

$$P(\text{the}|\text{its water is so transparent that}).$$  

(3.1)

One way to estimate this probability is from relative frequency counts: take a very large corpus, count the number of times we see “its water is so transparent that”, and count the number of times this is followed by the word “the”. This would be answering the question “Out of the times we saw the history $h$, how many times was it followed by the word $w$?”, as follows:

$$P(\text{the}|\text{its water is so transparent that}) = \frac{C(\text{its water is so transparent that the})}{C(\text{its water is so transparent that})}.$$  

(3.2)

With a large enough corpus, such as the web, we can compute these counts and estimate the probability from Eq. 3.2. You should pause now, go to the web, and compute this estimate for yourself.

While this method of estimating probabilities directly from counts works fine in many cases, it turns out that even the web isn’t big enough to give us good estimates in most cases. This is because language is creative; new sentences are created all the time, and we won’t always be able to count entire sentences. Even simple extensions of the example sentence may have counts of zero on the web (such as “Walden Pond’s water is so transparent that the”; well, used to have counts of zero).

Similarly, if we wanted to know the joint probability of an entire sequence of words like “its water is so transparent”, we could do it by asking “out of all possible sequences of five words, how many of them are “its water is so transparent”?” We would have to get the count of “its water is so transparent” and divide by the sum of the counts of all possible five word sequences. That seems rather a lot to estimate!

For this reason, we’ll need to introduce more clever ways of estimating the probability of a word $w$ given a history $h$, or the probability of an entire word sequence $W$. Let’s start with a little formalizing of notation. To represent the probability of a
particular random variable $X_i$ taking on the value “the”, or $P(X_i = \text{“the”})$, we will use the simplification $P(\text{the})$. We’ll represent a sequence of $n$ words either as $w_1 \ldots w_n$ or $w_{1:n}$. Thus the expression $w_{1:n-1}$ means the string $w_1, w_2, \ldots, w_{n-1}$, but we’ll also be using the equivalent notation $w_{<n}$, which can be read as “all the elements of $w$ from $w_1$ up to and including $w_{n-1}$. For the joint probability of each word in a sequence having a particular value $P(X_1 = w_1, X_2 = w_2, X_3 = w_3, \ldots, X_n = w_n)$ we’ll use $P(w_1, w_2, \ldots, w_n)$.

Now, how can we compute probabilities of entire sequences like $P(w_1, w_2, \ldots, w_n)$? One thing we can do is decompose this probability using the chain rule of probability:

$$P(X_1 \ldots X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1,2) \ldots P(X_n|X_1,\ldots,n-1)$$

$$= \prod_{k=1}^{n} P(X_k|X_1:k-1) \quad (3.3)$$

Applying the chain rule to words, we get

$$P(w_1 \ldots w_n) = P(w_1)P(w_2|w_1)P(w_3|w_1,2) \ldots P(w_n|w_1,\ldots,n-1)$$

$$= \prod_{k=1}^{n} P(w_k|w_1:k-1) \quad (3.4)$$

The chain rule shows the link between computing the joint probability of a sequence and computing the conditional probability of a word given previous words. Equation 3.4 suggests that we could estimate the joint probability of an entire sequence of words by multiplying together a number of conditional probabilities. But using the chain rule doesn’t really seem to help us! We don’t know any way to compute the exact probability of a word given a long sequence of preceding words, $P(w_n|w_{1:n-1})$. As we said above, we can’t just estimate by counting the number of times every word occurs following every long string, because language is creative and any particular context might have never occurred before!

The intuition of the n-gram model is that instead of computing the probability of a word given its entire history, we can approximate the history by just the last few words. The bigram model, for example, approximates the probability of a word given all the previous words $P(w_n|w_{1:n-1})$ by using only the conditional probability of the preceding word $P(w_n|w_{n-1})$. In other words, instead of computing the probability

$$P(\text{the}|\text{Walden Pond’s water is so transparent that}) \quad (3.5)$$

we approximate it with the probability

$$P(\text{the}|\text{that}) \quad (3.6)$$

When we use a bigram model to predict the conditional probability of the next word, we are thus making the following approximation:

$$P(w_n|w_{1:n-1}) \approx P(w_n|w_{n-1}) \quad (3.7)$$

The assumption that the probability of a word depends only on the previous word is called a Markov assumption. Markov models are the class of probabilistic models that assume we can predict the probability of some future unit without looking too
far into the past. We can generalize the bigram (which looks one word into the past) to the trigram (which looks two words into the past) and thus to the n-gram (which looks \( n-1 \) words into the past).

Let’s see a general equation for this n-gram approximation to the conditional probability of the next word in a sequence. We’ll use \( N \) here to mean the n-gram size, so \( N = 2 \) means bigrams and \( N = 3 \) means trigrams. Then we approximate the probability of a word given its entire context as follows:

\[
P(w_n | w_{1:n-1}) \approx P(w_n | w_{n-N+1:n-1})
\] (3.8)

Given the bigram assumption for the probability of an individual word, we can compute the probability of a complete word sequence by substituting Eq. 3.7 into Eq. 3.4:

\[
P(w_1:n) \approx \prod_{k=1}^{n} P(w_k | w_{k-1})
\] (3.9)

How do we estimate these bigram or n-gram probabilities? An intuitive way to estimate probabilities is called maximum likelihood estimation or MLE. We get the MLE estimate for the parameters of an n-gram model by getting counts from a corpus, and normalizing the counts so that they lie between 0 and 1.\(^1\)

For example, to compute a particular bigram probability of a word \( w_n \) given a previous word \( w_{n-1} \), we’ll compute the count of the bigram \( C(w_{n-1} w_n) \) and normalize by the sum of all the bigrams that share the same first word \( w_{n-1} \):

\[
P(w_n | w_{n-1}) = \frac{C(w_{n-1} w_n)}{\sum_{w} C(w_{n-1} w)}
\] (3.10)

We can simplify this equation, since the sum of all bigram counts that start with a given word \( w_{n-1} \) must be equal to the unigram count for that word \( w_{n-1} \) (the reader should take a moment to be convinced of this):

\[
P(w_n | w_{n-1}) = \frac{C(w_{n-1} w_n)}{C(w_{n-1})}
\] (3.11)

Let’s work through an example using a mini-corpus of three sentences. We’ll first need to augment each sentence with a special symbol \(<s>\) at the beginning of the sentence, to give us the bigram context of the first word. We’ll also need a special end-symbol. \(</s>\)^2

\(<s>\) I am Sam \(</s>\)
\(<s>\) Sam I am \(</s>\)
\(<s>\) I do not like green eggs and ham \(</s>\)

Here are the calculations for some of the bigram probabilities from this corpus

\[
P(I | <s>) = \frac{2}{3} = .67 \quad P(\text{Sam} | <s>) = \frac{1}{3} = .33 \quad P(\text{am} | I) = \frac{2}{3} = .67
\]

\[
P(\text{} | \text{Sam}) = \frac{1}{2} = .5 \quad P(\text{Sam} | \text{am}) = \frac{1}{2} = .5 \quad P(\text{do} | I) = \frac{1}{4} = .33
\]

\(^1\) For probabilistic models, normalizing means dividing by some total count so that the resulting probabilities fall between 0 and 1.

\(^2\) We need the end-symbol to make the bigram grammar a true probability distribution. Without an end-symbol, instead of the sentence probabilities of all sentences summing to one, the sentence probabilities for all sentences of a given length would sum to one. This model would define an infinite set of probability distributions, with one distribution per sentence length. See Exercise 3.5.
For the general case of MLE n-gram parameter estimation:

\[
P(w_n|w_{n-N+1:n-1}) = \frac{C(w_{n-N+1:n-1}w_n)}{C(w_{n-N+1:n-1})}
\]  

(3.12)

Equation 3.12 (like Eq. 3.11) estimates the n-gram probability by dividing the observed frequency of a particular sequence by the observed frequency of a prefix. This ratio is called a **relative frequency**. We said above that this use of relative frequencies as a way to estimate probabilities is an example of maximum likelihood estimation or MLE. In MLE, the resulting parameter set maximizes the likelihood of the training set \(T\) given the model \(M\) (i.e., \(P(T|M)\)). For example, suppose the word *Chinese* occurs 400 times in a corpus of a million words like the Brown corpus. What is the probability that a random word selected from some other text of, say, a million words will be the word *Chinese*? The MLE of its probability is \(\frac{400}{1000000}\) or 0.0004. Now 0.0004 is not the best possible estimate of the probability of *Chinese* occurring in all situations; it might turn out that in some other corpus or context *Chinese* is a very unlikely word. But it is the probability that makes it most likely that *Chinese* will occur 400 times in a million-word corpus. We present ways to modify the MLE estimates slightly to get better probability estimates in Section 3.6.

Let’s move on to some examples from a slightly larger corpus than our 14-word example above. We’ll use data from the now-defunct Berkeley Restaurant Project, a dialogue system from the last century that answered questions about a database of restaurants in Berkeley, California (Jurafsky et al., 1994). Here are some text-normalized sample user queries (a sample of 9332 sentences is on the website):

- can you tell me about any good cantonese restaurants close by
- mid priced thai food is what i’m looking for
- tell me about chez panisse
- can you give me a listing of the kinds of food that are available
- i’m looking for a good place to eat breakfast
- when is caffe venezia open during the day

Figure 3.1 shows the bigram counts from a piece of a bigram grammar from the Berkeley Restaurant Project. Note that the majority of the values are zero. In fact, we have chosen the sample words to cohere with each other; a matrix selected from a random set of eight words would be even more sparse.

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<tr>
<td>i</td>
<td>5</td>
<td>827</td>
<td>0</td>
<td>9</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>want</td>
<td>2</td>
<td>608</td>
<td>1</td>
<td>6</td>
<td>6</td>
<td>5</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>to</td>
<td>2</td>
<td>4</td>
<td>686</td>
<td>2</td>
<td>0</td>
<td>6</td>
<td>211</td>
<td></td>
</tr>
<tr>
<td>eat</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>16</td>
<td>2</td>
<td>42</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>chinese</td>
<td>1</td>
<td>0</td>
<td>82</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>food</td>
<td>15</td>
<td>0</td>
<td>15</td>
<td>0</td>
<td>4</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>lunch</td>
<td>2</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>spend</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
</tbody>
</table>

**Figure 3.1** Bigram counts for eight of the words (out of \(V = 1446\)) in the Berkeley Restaurant Project corpus of 9332 sentences. Zero counts are in gray.

Figure 3.2 shows the bigram probabilities after normalization (dividing each cell in Fig. 3.1 by the appropriate unigram for its row, taken from the following set of unigram probabilities):
Here are a few other useful probabilities:

\[
P(i|<s>) = 0.25 \quad P(\text{english}|\text{want}) = 0.0011
\]
\[
P(\text{food}|\text{english}) = 0.5 \quad P(</s>|\text{food}) = 0.68
\]

Now we can compute the probability of sentences like \textit{I want English food} or \textit{I want Chinese food} by simply multiplying the appropriate bigram probabilities together, as follows:

\[
P(<s> \ i \ \text{want} \ \text{english} \ \text{food} \ </s>)
\]
\[
= P(i|<s>)P(\text{want}|i)P(\text{english}|\text{want})
\]
\[
P(\text{food}|\text{english})P(</s>|\text{food})
\]
\[
= .25 \times .33 \times .0011 \times 0.5 \times 0.68
\]
\[
= .000031
\]

We leave it as Exercise 3.2 to compute the probability of \textit{I want chinese food}.

What kinds of linguistic phenomena are captured in these bigram statistics? Some of the bigram probabilities above encode some facts that we think of as strictly \textit{syntactic} in nature, like the fact that what comes after \textit{eat} is usually a noun or an adjective, or that what comes after \textit{to} is usually a verb. Others might be a fact about the personal assistant task, like the high probability of sentences beginning with the words \textit{I}. And some might even be cultural rather than linguistic, like the higher probability that people are looking for Chinese versus English food.

\textbf{Some practical issues:} Although for pedagogical purposes we have only described bigram models, in practice we might use \textbf{trigram} models, which condition on the previous two words rather than the previous word, or \textbf{4-gram} or even \textbf{5-gram} models, when there is sufficient training data. Note that for these larger n-grams, we’ll need to assume extra contexts to the left and right of the sentence end. For example, to compute trigram probabilities at the very beginning of the sentence, we use two pseudo-words for the first trigram (i.e., \(P(I|<s><s>)\)).

We always represent and compute language model probabilities in log format as \textbf{log probabilities}. Since probabilities are (by definition) less than or equal to 1, the more probabilities we multiply together, the smaller the product becomes. Multiplying enough n-grams together would result in numerical underflow. By using log probabilities instead of raw probabilities, we get numbers that are not as small.
Adding in log space is equivalent to multiplying in linear space, so we combine log probabilities by adding them. The result of doing all computation and storage in log space is that we only need to convert back into probabilities if we need to report them at the end; then we can just take the exp of the logprob:

\[ p_1 \times p_2 \times p_3 \times p_4 = \exp(\log p_1 + \log p_2 + \log p_3 + \log p_4) \]  

(3.13)

In practice throughout this book, we’ll use log to mean natural log (ln) when the base is not specified.

### 3.2 Evaluating Language Models: Training and Test Sets

The best way to evaluate the performance of a language model is to embed it in an application and measure how much the application improves. Such end-to-end evaluation is called extrinsic evaluation. Extrinsic evaluation is the only way to know if a particular improvement in the language model (or any component) is really going to help the task at hand. Thus for evaluating n-gram language models that are a component of some task like speech recognition or machine translation, we can compare the performance of two candidate language models by running the speech recognizer or machine translator twice, once with each language model, and seeing which gives the more accurate transcription.

Unfortunately, running big NLP systems end-to-end is often very expensive. Instead, it’s helpful to have a metric that can be used to quickly evaluate potential improvements in a language model. An intrinsic evaluation metric is one that measures the quality of a model independent of any application. In the next section we’ll introduce perplexity, which is the standard intrinsic metric for measuring language model performance, both for simple n-gram language models and for the more sophisticated neural large language models of Chapter 10.

In order to evaluate any machine learning model, we need to have at least three distinct data sets: the training set, the development set, and the test set.

The training set is the data we use to learn the parameters of our model; for simple n-gram language models it’s the corpus from which we get the counts that we normalize into the probabilities of the n-gram language model.

The test set is a different, held-out set of data, not overlapping with the training set, that we use to evaluate the model. We need a separate test set to give us an unbiased estimate of how well the model we trained can generalize when we apply it to some new unknown dataset. A machine learning model that perfectly captured the training data, but performed terribly on any other data, wouldn’t be much use when it comes time to apply it to any new data or problem! We thus measure the quality of an n-gram model by its performance on this unseen test set or test corpus.

How should we choose a training and test set? The test set should reflect the language we want to use the model for. If we’re going to use our language model for speech recognition of chemistry lectures, the test set should be text of chemistry lectures. If we’re going to use it as part of a system for translating hotel booking requests from Chinese to English, the test set should be text of hotel booking requests. If we want our language model to be general purpose, then the test set should be drawn from a wide variety of texts. In such cases we might collect a lot of texts from different sources, and then divide it up into a training set and a test set. It’s important to do the dividing carefully; if we’re building a general purpose model,
we don’t want the test set to consist of only text from one document, or one author, since that wouldn’t be a good measure of general performance.

Thus if we are given a corpus of text and want to compare the performance of two different n-gram models, we divide the data into training and test sets, and train the parameters of both models on the training set. We can then compare how well the two trained models fit the test set.

But what does it mean to “fit the test set”? The standard answer is simple: whichever language model assigns a higher probability to the test set—which means it more accurately predicts the test set—is a better model. Given two probabilistic models, the better model is the one that has a tighter fit to the test data or that better predicts the details of the test data, and hence will assign a higher probability to the test data.

Since our evaluation metric is based on test set probability, it’s important not to let the test sentences into the training set. Suppose we are trying to compute the probability of a particular “test” sentence. If our test sentence is part of the training corpus, we will mistakenly assign it an artificially high probability when it occurs in the test set. We call this situation training on the test set. Training on the test set introduces a bias that makes the probabilities all look too high, and causes huge inaccuracies in perplexity, the probability-based metric we introduce below.

Even if we don’t train on the test set, if we test our language model on it many times after making different changes, we might implicitly tune to its characteristics, by noticing which changes seem to make the model better. For this reason, we only want to run our model on the test set once, or a very few number of times, once we are sure our model is ready.

For this reason we normally instead have a third dataset called a development test set or, devset. We do all our testing on this dataset until the very end, and then we test on the test set once to see how good our model is.

How do we divide our data into training, development, and test sets? We want our test set to be as large as possible, since a small test set may be accidentally unrepresentative, but we also want as much training data as possible. At the minimum, we would want to pick the smallest test set that gives us enough statistical power to measure a statistically significant difference between two potential models. It’s important that the dev set be drawn from the same kind of text as the test set, since its goal is to measure how we would do on the test set.

### 3.3 Evaluating Language Models: Perplexity

In practice we don’t use raw probability as our metric for evaluating language models, but a function of probability called perplexity. Perplexity is one of the most important metrics in natural language processing, and we use it to evaluate neural language models as well.

The perplexity (sometimes abbreviated as PP or PPL) of a language model on a test set is the inverse probability of the test set (one over the probability of the test set), normalized by the number of words. For this reason it’s sometimes called the per-word perplexity. For a test set $W = w_1w_2\ldots w_N$,:
perplexity \( (W) \) = \( P(w_1w_2\ldots w_N)^{-\frac{1}{N}} \) \hspace{1cm} (3.14)

\[ = \sqrt[N]{\frac{1}{P(w_1w_2\ldots w_N)}}, \]

Or we can use the chain rule to expand the probability of \( W \):

\[ \text{perplexity} (W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1\ldots w_{i-1})}} \] (3.15)

Note that because of the inverse in Eq. 3.15, the higher the probability of the word sequence, the lower the perplexity. Thus the lower the perplexity of a model on the data, the better the model, and minimizing perplexity is equivalent to maximizing the test set probability according to the language model. Why does perplexity use the inverse probability? It turns out the inverse arises from the original definition of perplexity from cross-entropy rate in information theory; for those interested, the explanation is in the advanced section Section 3.9. Meanwhile, we just have to remember that perplexity has an inverse relationship with probability.

The details of computing the perplexity of a test set \( W \) depends on which language model we use. Here’s the perplexity of \( W \) with a unigram language model (just the geometric mean of the unigram probabilities):

\[ \text{perplexity} (W) = \sqrt[N]{\prod_{i=1}^{N} P(w_i)} \] (3.16)

The perplexity of \( W \) computed with a bigram language model is still a geometric mean, but now of the bigram probabilities:

\[ \text{perplexity} (W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}} \] (3.17)

What we generally use for word sequence in Eq. 3.15 or Eq. 3.17 is the entire sequence of words in some test set. Since this sequence will cross many sentence boundaries, if our vocabulary includes a between-sentence token \(<\text{EOS}>\) or separate begin- and end-sentence markers \(<\text{s}>\) and \(<\text{/s}>\) then we can include them in the probability computation. If we do, then we also include one token per sentence in the total count of word tokens \( N \).

We mentioned above that perplexity is a function of both the text and the language model: given a text \( W \), different language models will have different perplexities. Because of this, perplexity can be used to compare different n-gram models. Let’s look at an example, in which we trained unigram, bigram, and trigram grammars on 38 million words (including start-of-sentence tokens) from the Wall Street Journal, using a 19,979 word vocabulary. We then computed the perplexity of each

---

3. For example if we use both begin and end tokens, we would include the end-of-sentence marker \(<\text{/s}>\) but not the beginning-of-sentence marker \(<\text{s}>\) in our count of \( N \). This is because the end-sentence token is followed directly by the begin-sentence token with probability almost 1, so we don’t want the probability of that fake transition to influence our perplexity.
of these models on a test set of 1.5 million words, using Eq. 3.16 for unigrams, Eq. 3.17 for bigrams, and the corresponding equation for trigrams. The table below shows the perplexity of a 1.5 million word WSJ test set according to each of these grammars.

<table>
<thead>
<tr>
<th></th>
<th>Unigram</th>
<th>Bigram</th>
<th>Trigram</th>
</tr>
</thead>
<tbody>
<tr>
<td>Perplexity</td>
<td>962</td>
<td>170</td>
<td>109</td>
</tr>
</tbody>
</table>

As we see above, the more information the n-gram gives us about the word sequence, the higher the probability the n-gram will assign to the string. A trigram model is less surprised than a unigram model because it has a better idea of what words might come next, and so it assigns them a higher probability. And the higher the probability, the lower the perplexity (since as Eq. 3.15 showed, perplexity is related inversely to the likelihood of the test sequence according to the model). So a lower perplexity can tell us that a language model is a better predictor of the words in the test set.

Note that in computing perplexities, the n-gram model \( P \) must be constructed without any knowledge of the test set or any prior knowledge of the vocabulary of the test set. Any kind of knowledge of the test set can cause the perplexity to be artificially low. The perplexity of two language models is only comparable if they use identical vocabularies.

An (intrinsic) improvement in perplexity does not guarantee an (extrinsic) improvement in the performance of a language processing task like speech recognition or machine translation. Nonetheless, because perplexity usually correlates with task improvements, it is commonly used as a convenient evaluation metric. Still, when possible a model’s improvement in perplexity should be confirmed by an end-to-end evaluation on a real task.

**Advanced: Perplexity as Weighted Average Branching Factor**

It turns out that perplexity can also be thought of as the **weighted average branching factor** of a language. The branching factor of a language is the number of possible next words that can follow any word. If we have an artificial deterministic language of integer numbers whose vocabulary consists of the 10 digits (zero, one, two,..., nine), in which any digit can follow any other digit, then the branching factor of that language is 10.

Let’s first convince ourselves that if we compute the perplexity of this artificial digit language we indeed get 10. Let’s suppose that (in training and in test) each of the 10 digits occurs with exactly equal probability \( P = \frac{1}{10} \). Now imagine a test string of digits of length \( N \), and, again, assume that in the training set all the digits occurred with equal probability. By Eq. 3.15, the perplexity will be

\[
\text{perplexity}(W) = P(w_1w_2\ldots w_N)^{-\frac{1}{N}}
\]

\[
= \left( \frac{1}{10} \right)^{-\frac{1}{N}}
\]

\[
= \frac{1}{10}
\]

\[
= 10
\]

(3.18)

But suppose that the number zero is really frequent and occurs far more often than other numbers. Let’s say that 0 occur 91 times in the training set, and each of the other digits occurred 1 time each. Now we see the following test set: 0 0 0 0 0 3 0 0 0
0. We should expect the perplexity of this test set to be lower since most of the time the next number will be zero, which is very predictable, i.e. has a high probability. Thus, although the branching factor is still 10, the perplexity or weighted branching factor is smaller. We leave this exact calculation as exercise 3.12.

3.4 Sampling sentences from a language model

One important way to visualize what kind of knowledge a language model embodies is to sample from it. Sampling from a distribution means to choose random points according to their likelihood. Thus sampling from a language model—which represents a distribution over sentences—means to generate some sentences, choosing each sentence according to its likelihood as defined by the model. Thus we are more likely to generate sentences that the model thinks have a high probability and less likely to generate sentences that the model thinks have a low probability.

This technique of visualizing a language model by sampling was first suggested very early on by Shannon (1948) and Miller and Selfridge (1950). It’s simplest to visualize how this works for the unigram case. Imagine all the words of the English language covering the probability space between 0 and 1, each word covering an interval proportional to its frequency. Fig. 3.3 shows a visualization, using a unigram LM computed from the text of this book. We choose a random value between 0 and 1, find that point on the probability line, and print the word whose interval includes this chosen value. We continue choosing random numbers and generating words until we randomly generate the sentence-final token \(<s>\).

![Sampling Distribution Visualization](image)

Figure 3.3 A visualization of the sampling distribution for sampling sentences by repeatedly sampling unigrams. The blue bar represents the relative frequency of each word (we’ve ordered them from most frequent to least frequent, but the choice of order is arbitrary). The number line shows the cumulative probabilities. If we choose a random number between 0 and 1, it will fall in an interval corresponding to some word. The expectation for the random number to fall in the larger intervals of one of the frequent words (the, of, a) is much higher than in the smaller interval of one of the rare words (polyphonic).

We can use the same technique to generate bigrams by first generating a random bigram that starts with \(<s>\) (according to its bigram probability). Let’s say the second word of that bigram is \(w\). We next choose a random bigram starting with \(w\) (again, drawn according to its bigram probability), and so on.

3.5 Generalization and Zeros

The n-gram model, like many statistical models, is dependent on the training corpus. One implication of this is that the probabilities often encode specific facts about a
given training corpus. Another implication is that n-grams do a better and better job of modeling the training corpus as we increase the value of \( N \).

We can use the sampling method from the prior section to visualize both of these facts! To give an intuition for the increasing power of higher-order n-grams, Fig. 3.4 shows random sentences generated from unigram, bigram, trigram, and 4-gram models trained on Shakespeare’s works.

The longer the context on which we train the model, the more coherent the sentences. In the unigram sentences, there is no coherent relation between words or any sentence-final punctuation. The bigram sentences have some local word-to-word coherence (especially if we consider that punctuation counts as a word). The trigram and 4-gram sentences are beginning to look a lot like Shakespeare. Indeed, a careful investigation of the 4-gram sentences shows that they look a little too much like Shakespeare. The words *It cannot be but so* are directly from *King John*. This is because, not to put the knock on Shakespeare, his oeuvre is not very large as corpora go (\( N = 884,647, V = 29,066 \)), and our n-gram probability matrices are ridiculously sparse. There are \( V^2 = 844,000,000 \) possible bigrams alone, and the number of possible 4-grams is \( V^4 = 7 \times 10^{17} \). Thus, once the generator has chosen the first 3-gram (*It cannot be*), there are only seven possible next words for the 4th element (*but, I, that, thus, this, and the period*).

To get an idea of the dependence of a grammar on its training set, let’s look at an n-gram grammar trained on a completely different corpus: the *Wall Street Journal* (WSJ) newspaper. Shakespeare and the *Wall Street Journal* are both English, so we might expect some overlap between our n-grams for the two genres. Fig. 3.5 shows sentences generated by unigram, bigram, and trigram grammars trained on 40 million words from WSJ.

Compare these examples to the pseudo-Shakespeare in Fig. 3.4. While they both model “English-like sentences”, there is clearly no overlap in generated sentences, and little overlap even in small phrases. Statistical models are likely to be pretty useless as predictors if the training sets and the test sets are as different as Shakespeare and WSJ.

How should we deal with this problem when we build n-gram models? One step is to be sure to use a training corpus that has a similar genre to whatever task we are trying to accomplish. To build a language model for translating legal documents,
we need a training corpus of legal documents. To build a language model for a question-answering system, we need a training corpus of questions.

It is equally important to get training data in the appropriate dialect or variety, especially when processing social media posts or spoken transcripts. For example some tweets will use features of African American English (AAE)— the name for the many variations of language used in African American communities (King, 2020). Such features include words like finna—an auxiliary verb that marks immediate future tense—that don’t occur in other varieties, or spellings like den for then, in tweets like this one (Blodgett and O’Connor, 2017):

(3.19) Bored af den my phone finna die!!!

while tweets from English-based languages like Nigerian Pidgin have markedly different vocabulary and n-gram patterns from American English (Jurgens et al., 2017):

(3.20) @username R u a wizard or wat gan set: in d mornin - u tweet, afternoon - u tweet, nyt gan u dey tweet. beta get ur IT placement wiv twitter

Matching genres and dialects is still not sufficient. Our models may still be subject to the problem of sparsity. For any n-gram that occurred a sufficient number of times, we might have a good estimate of its probability. But because any corpus is limited, some perfectly acceptable English word sequences are bound to be missing from it. That is, we’ll have many cases of putative “zero probability n-grams” that should really have some non-zero probability. Consider the words that follow the bigram denied the in the WSJ Treebank3 corpus, together with their counts:

<table>
<thead>
<tr>
<th>n-gram</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>denied the allegations:</td>
<td>5</td>
</tr>
<tr>
<td>denied the speculation:</td>
<td>2</td>
</tr>
<tr>
<td>denied the rumors:</td>
<td>1</td>
</tr>
<tr>
<td>denied the report:</td>
<td>1</td>
</tr>
</tbody>
</table>

But suppose our test set has phrases like:

denied the offer

denied the loan

Our model will incorrectly estimate that the \( P(\text{offer} | \text{denied the}) \) is 0!

These zeros—things that don’t ever occur in the training set but do occur in the test set—are a problem for two reasons. First, their presence means we are underestimating the probability of all sorts of words that might occur, which will hurt the performance of any application we want to run on this data.

Second, if the probability of any word in the test set is 0, the entire probability of the test set is 0. By definition, perplexity is based on the inverse probability of the
3.6 • Smoothing

test set. Thus if some words have zero probability, we can’t compute perplexity at all, since we can’t divide by 0!

What do we do about zeros? There are two solutions, depending on the kind of zero. For words whose n-gram probability is zero because they occur in a novel test set context, like the example of denied the offer above, we’ll introduce in Section 3.6 algorithms called smoothing or discounting. Smoothing algorithms shave off a bit of probability mass from some more frequent events and give it to these unseen events. But first, let’s talk about an even more insidious form of zero: words that the model has never seen before at all (in any context): unknown words!

Unknown Words

What do we do about words we have never seen before? Perhaps the word Jurafsky simply did not occur in our training set, but pops up in the test set! We usually disallow this situation by stipulating that we already know all the words that can occur. In such a closed vocabulary system the test set can only contain words from this known lexicon, and there will be no unknown words. This is what we do for the neural language models of later chapters. For these models we use subword tokens rather than words. With subword tokenization (like the BPE algorithm of Chapter 2) any unknown word can be modeled as a sequence of smaller subwords, if necessary by a sequence of individual letters, so we never have unknown words.

If our language model is using words instead of tokens, however, we have to deal with unknown words, or out of vocabulary (OOV) words: words we haven’t seen before. The percentage of OOV words that appear in the test set is called the OOV rate. One way to create an open vocabulary system is to model potential unknown words in the test set by adding a pseudo-word called <UNK>. Again, most modern language models are closed vocabulary and don’t use an <UNK> token. But when necessary, we can train <UNK> probabilities by turning the problem back into a closed vocabulary one by choosing a fixed vocabulary in advance:

1. Choose a vocabulary (word list) that is fixed in advance.
2. Convert in the training set any word that is not in this set (any OOV word) to the unknown word token <UNK> in a text normalization step.
3. Estimate the probabilities for <UNK> from its counts just like any other regular word in the training set.

The exact choice of <UNK> has an effect on perplexity. A language model can achieve low perplexity by choosing a small vocabulary and assigning the unknown word a high probability. Thus perplexities can only be compared across language models with <UNK> if they have the exact same vocabularies (Buck et al., 2014).

3.6 Smoothing

What do we do with words that are in our vocabulary (they are not unknown words) but appear in a test set in an unseen context (for example they appear after a word they never appeared after in training)? To keep a language model from assigning zero probability to these unseen events, we’ll have to shave off a bit of probability mass from some more frequent events and give it to the events we’ve never seen. This modification is called smoothing or discounting. In this section and the following ones we’ll introduce a variety of ways to do smoothing: Laplace (add-one)
smoothing, add-k smoothing, and stupid backoff. At the end of the chapter we also summarize a more complex method, Kneser-Ney smoothing.

3.6.1 Laplace Smoothing

The simplest way to do smoothing is to add one to all the n-gram counts, before we normalize them into probabilities. All the counts that used to be zero will now have a count of 1, the counts of 1 will be 2, and so on. This algorithm is called Laplace smoothing. Laplace smoothing does not perform well enough to be used in modern n-gram models, but it usefully introduces many of the concepts that we see in other smoothing algorithms, gives a useful baseline, and is also a practical smoothing algorithm for other tasks like text classification (Chapter 4).

Let’s start with the application of Laplace smoothing to unigram probabilities. Recall that the unsmoothed maximum likelihood estimate of the unigram probability of the word \( w_i \) is its count \( c_i \) normalized by the total number of word tokens \( N \):

\[
P(w_i) = \frac{c_i}{N}
\]

Laplace smoothing merely adds one to each count (hence its alternate name add-one smoothing). Since there are \( V \) words in the vocabulary and each one was incremented, we also need to adjust the denominator to take into account the extra \( V \) observations. (What happens to our \( P \) values if we don’t increase the denominator?)

\[
P_{\text{Laplace}}(w_i) = \frac{c_i + 1}{N + V} \quad (3.21)
\]

Instead of changing both the numerator and denominator, it is convenient to describe how a smoothing algorithm affects the numerator, by defining an adjusted count \( c^* \). This adjusted count is easier to compare directly with the MLE counts and can be turned into a probability like an MLE count by normalizing by \( N \). To define this count, since we are only changing the numerator in addition to adding 1 we’ll also need to multiply by a normalization factor \( \frac{N}{N+V} \):

\[
c^*_i = (c_i + 1) \frac{N}{N + V} \quad (3.22)
\]

We can now turn \( c^*_i \) into a probability \( P^*_i \) by normalizing by \( N \).

A related way to view smoothing is as discounting (lowering) some non-zero counts in order to get the probability mass that will be assigned to the zero counts. Thus, instead of referring to the discounted counts \( c^* \), we might describe a smoothing algorithm in terms of a relative discount \( d_c \), the ratio of the discounted counts to the original counts:

\[
d_c = \frac{c^*_i}{c_i}
\]

Now that we have the intuition for the unigram case, let’s smooth our Berkeley Restaurant Project bigrams. Figure 3.6 shows the add-one smoothed counts for the bigrams in Fig. 3.1.

Figure 3.7 shows the add-one smoothed probabilities for the bigrams in Fig. 3.2. Recall that normal bigram probabilities are computed by normalizing each row of counts by the unigram count:
3.6  *  Smoothing  47

For add-one smoothed bigram counts, we need to augment the unigram count by the number of total word types in the vocabulary $V$:

$$P_Laplace(w_n | w_{n-1}) = \frac{C(w_{n-1}w_n) + 1}{\sum_w (C(w_{n-1}w) + 1)} = \frac{C(w_{n-1}w_n) + 1}{C(w_{n-1}) + V} \quad (3.24)$$

Thus, each of the unigram counts given in the previous section will need to be augmented by $V = 1446$. The result is the smoothed bigram probabilities in Fig. 3.7.

It is often convenient to reconstruct the count matrix so we can see how much a smoothing algorithm has changed the original counts. These adjusted counts can be computed by Eq. 3.25. Figure 3.8 shows the reconstructed counts.

$$c^*(w_{n-1}w_n) = \frac{[C(w_{n-1}w_n) + 1] \times C(w_{n-1})}{C(w_{n-1}) + V} \quad (3.25)$$

Note that add-one smoothing has made a very big change to the counts. Comparing Fig. 3.8 to the original counts in Fig. 3.1, we can see that $C(want to)$ changed from 608 to 238! We can see this in probability space as well: $P(to|want)$ decreases from .66 in the unsmoothed case to .26 in the smoothed case. Looking at the discount $d$ (the ratio between new and old counts) shows us how strikingly the counts for each prefix word have been reduced; the discount for the bigram want to is .39, while the discount for Chinese food is .10, a factor of 10!

The sharp change in counts and probabilities occurs because too much probability mass is moved to all the zeros.
3.6.2 Add-k smoothing

One alternative to add-one smoothing is to move a bit less of the probability mass from the seen to the unseen events. Instead of adding 1 to each count, we add a fractional count $k$ ($0.01, 0.05, 0.5$). This algorithm is therefore called add-k smoothing.

$$P_{\text{Add-k}}(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n) + k}{C(w_{n-1}) + kV}$$ (3.26)

Add-k smoothing requires that we have a method for choosing $k$; this can be done, for example, by optimizing on a devset. Although add-k is useful for some tasks (including text classification), it turns out that it still doesn’t work well for language modeling, generating counts with poor variances and often inappropriate discounts (Gale and Church, 1994).

3.6.3 Backoff and Interpolation

The discounting we have been discussing so far can help solve the problem of zero frequency n-grams. But there is an additional source of knowledge we can draw on. If we are trying to compute $P(w_n|w_{n-2}w_{n-1})$ but we have no examples of a particular trigram $w_{n-2}w_{n-1}w_n$, we can instead estimate its probability by using the bigram probability $P(w_n|w_{n-1})$. Similarly, if we don’t have counts to compute $P(w_n|w_{n-1})$, we can look to the unigram $P(w_n)$.

In other words, sometimes using less context is a good thing, helping to generalize more for contexts that the model hasn’t learned much about. There are two ways to use this n-gram “hierarchy”. In backoff, we use the trigram if the evidence is sufficient, otherwise we use the bigram, otherwise the unigram. In other words, we only “back off” to a lower-order n-gram if we have zero evidence for a higher-order n-gram. By contrast, in interpolation, we always mix the probability estimates from all the n-gram estimators, weighting and combining the trigram, bigram, and unigram counts.

In simple linear interpolation, we combine different order n-grams by linearly interpolating them. Thus, we estimate the trigram probability $P(w_n|w_{n-2}w_{n-1})$ by mixing together the unigram, bigram, and trigram probabilities, each weighted by a $\lambda$:

$$P(w_n|w_{n-2}w_{n-1}) = \hat{\lambda}_1 P(w_n) + \hat{\lambda}_2 P(w_n|w_{n-1}) + \hat{\lambda}_3 P(w_n|w_{n-2}w_{n-1})$$ (3.27)
The $\lambda$s must sum to 1, making Eq. 3.27 equivalent to a weighted average. In a slightly more sophisticated version of linear interpolation, each $\lambda$ weight is computed by conditioning on the context. This way, if we have particularly accurate counts for a particular bigram, we assume that the counts of the trigrams based on this bigram will be more trustworthy, so we can make the $\lambda$s for those trigrams higher and thus give that trigram more weight in the interpolation. Equation 3.28 shows the equation for interpolation with context-conditioned weights:

$$
\hat{P}(w_n|w_{n-2}w_{n-1}) = \lambda_1(w_{n-2}w_{n-1})P(w_n) \\
+ \lambda_2(w_{n-2}w_{n-1})P(w_n|w_{n-1}) \\
+ \lambda_3(w_{n-2}w_{n-1})P(w_n|w_{n-2}w_{n-1})
$$

(3.28)

How are these $\lambda$ values set? Both the simple interpolation and conditional interpolation $\lambda$s are learned from a held-out corpus. A held-out corpus is an additional training corpus, so-called because we hold it out from the training data, that we use to set hyperparameters like these $\lambda$ values. We do so by choosing the $\lambda$ values that maximize the likelihood of the held-out corpus. That is, we fix the n-gram probabilities and then search for the $\lambda$ values that—when plugged into Eq. 3.27—give us the highest probability of the held-out set. There are various ways to find this optimal set of $\lambda$s. One way is to use the EM algorithm, an iterative learning algorithm that converges on locally optimal $\lambda$s (Jelinek and Mercer, 1980).

In a backoff n-gram model, if the n-gram we need has zero counts, we approximate it by backing off to the (n-1)-gram. We continue backing off until we reach a history that has some counts.

In order for a backoff model to give a correct probability distribution, we have to discount the higher-order n-grams to save some probability mass for the lower order n-grams. Just as with add-one smoothing, if the higher-order n-grams aren’t discounted and we just used the undiscounted MLE probability, then as soon as we replaced an n-gram which has zero probability with a lower-order n-gram, we would be adding probability mass, and the total probability assigned to all possible strings by the language model would be greater than 1! In addition to this explicit discount factor, we’ll need a function $\alpha$ to distribute this probability mass to the lower order n-grams.

This kind of backoff with discounting is also called Katz backoff. In Katz backoff we rely on a discounted probability $P^*$ if we’ve seen this n-gram before (i.e., if we have non-zero counts). Otherwise, we recursively back off to the Katz probability for the shorter-history (n-1)-gram. The probability for a backoff n-gram $P_{BO}$ is thus computed as follows:

$$
P_{BO}(w_n|w_{n-N+1\ldots n-1}) = 
\begin{cases} 
P^*(w_n|w_{n-N+1\ldots n-1}), & \text{if } C(w_{n-N+1\ldots n}) > 0 \\
\alpha(w_{n-N+1\ldots n-1})P_{BO}(w_n|w_{n-N+2\ldots n-1}), & \text{otherwise.}
\end{cases}
$$

(3.29)

Katz backoff is often combined with a smoothing method called Good-Turing. The combined Good-Turing backoff algorithm involves quite detailed computation for estimating the Good-Turing smoothing and the $P^*$ and $\alpha$ values.
3.7 Huge Language Models and Stupid Backoff

By using text from the web or other enormous collections, it is possible to build extremely large language models. The Web 1 Trillion 5-gram corpus released by Google includes various large sets of n-grams, including 1-grams through 5-grams from all the five-word sequences that appear at least 40 times from 1,024,908,267,229 words of text from publicly accessible Web pages in English (Franz and Brants, 2006). Google has also released Google Books Ngrams corpora with n-grams drawn from their book collections, including another 800 billion tokens of n-grams from Chinese, English, French, German, Hebrew, Italian, Russian, and Spanish (Lin et al., 2012a). Smaller but more carefully curated n-gram corpora for English include the million most frequent n-grams drawn from the COCA (Corpus of Contemporary American English) 1 billion word corpus of American English (Davies, 2020). COCA is a balanced corpus, meaning that it has roughly equal numbers of words from different genres: web, newspapers, spoken conversation transcripts, fiction, and so on, drawn from the period 1990-2019, and has the context of each n-gram as well as labels for genre and provenance.

Some example 4-grams from the Google Web corpus:

<table>
<thead>
<tr>
<th>4-gram</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>serve as the incoming</td>
<td>92</td>
</tr>
<tr>
<td>serve as the incubator</td>
<td>99</td>
</tr>
<tr>
<td>serve as the independent</td>
<td>794</td>
</tr>
<tr>
<td>serve as the index</td>
<td>223</td>
</tr>
<tr>
<td>serve as the indication</td>
<td>72</td>
</tr>
<tr>
<td>serve as the indicator</td>
<td>120</td>
</tr>
<tr>
<td>serve as the indicators</td>
<td>45</td>
</tr>
</tbody>
</table>

Efficiency considerations are important when building language models that use such large sets of n-grams. Rather than store each word as a string, it is generally represented in memory as a 64-bit hash number, with the words themselves stored on disk. Probabilities are generally quantized using only 4-8 bits (instead of 8-byte floats), and n-grams are stored in reverse tries.

An n-gram language model can also be shrunk by pruning, for example only storing n-grams with counts greater than some threshold (such as the count threshold of 40 used for the Google n-gram release) or using entropy to prune less-important n-grams (Stolcke, 1998). Another option is to build approximate language models using techniques like Bloom filters (Talbot and Osborne 2007, Church et al. 2007). Finally, efficient language model toolkits like KenLM (Heafield 2011, Heafield et al. 2013) use sorted arrays, efficiently combine probabilities and backoffs in a single value, and use merge sorts to efficiently build the probability tables in a minimal number of passes through a large corpus.

Although with these toolkits it is possible to build web-scale language models using advanced smoothing algorithms like the Kneser-Ney algorithm we will see in Section 3.8, Brants et al. (2007) show that with very large language models a much simpler algorithm may be sufficient. The algorithm is called stupid backoff. Stupid backoff gives up the idea of trying to make the language model a true probability distribution. There is no discounting of the higher-order probabilities. If a higher-order n-gram has a zero count, we simply backoff to a lower order n-gram, weighed by a fixed (context-independent) weight. This algorithm does not produce a probability
distribution, so we’ll follow Brants et al. (2007) in referring to it as $S$:

$$S(w_i|w_{i-N+1:i-1}) = \begin{cases} \frac{\text{count}(w_{i-N+1:i})}{\text{count}(w_{i-N+1:i-1})} & \text{if count}(w_{i-N+1:i}) > 0 \\ \lambda S(w_i|w_{i-N+2:i-1}) & \text{otherwise} \end{cases}$$  \hspace{1cm} (3.30)

The backoff terminates in the unigram, which has score $S(w) = \frac{\text{count}(w)}{N}$. Brants et al. (2007) find that a value of 0.4 worked well for $\lambda$.

### 3.8 Advanced: Kneser-Ney Smoothing

A popular advanced n-gram smoothing method is the interpolated Kneser-Ney algorithm (Kneser and Ney 1995, Chen and Goodman 1998).

#### 3.8.1 Absolute Discounting

Kneser-Ney has its roots in a method called absolute discounting. Recall that discounting of the counts for frequent n-grams is necessary to save some probability mass for the smoothing algorithm to distribute to the unseen n-grams.

To see this, we can use a clever idea from Church and Gale (1991). Consider an n-gram that has count 4. We need to discount this count by some amount. But how much should we discount it? Church and Gale’s clever idea was to look at a held-out corpus and just see what the count is for all those bigrams that had count 4 in the training set. They computed a bigram grammar from 22 million words of AP newswire and then checked the counts of each of these bigrams in another 22 million words. On average, a bigram that occurred 4 times in the first 22 million words occurred 3.23 times in the next 22 million words. Fig. 3.9 from Church and Gale (1991) shows these counts for bigrams with $c$ from 0 to 9.

<table>
<thead>
<tr>
<th>Bigram count in training set</th>
<th>Bigram count in heldout set</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.0000270</td>
</tr>
<tr>
<td>1</td>
<td>0.448</td>
</tr>
<tr>
<td>2</td>
<td>1.25</td>
</tr>
<tr>
<td>3</td>
<td>2.24</td>
</tr>
<tr>
<td>4</td>
<td>3.23</td>
</tr>
<tr>
<td>5</td>
<td>4.21</td>
</tr>
<tr>
<td>6</td>
<td>5.23</td>
</tr>
<tr>
<td>7</td>
<td>6.21</td>
</tr>
<tr>
<td>8</td>
<td>7.21</td>
</tr>
<tr>
<td>9</td>
<td>8.26</td>
</tr>
</tbody>
</table>

**Figure 3.9** For all bigrams in 22 million words of AP newswire of count 0, 1, 2,...,9, the counts of these bigrams in a held-out corpus also of 22 million words.

Notice in Fig. 3.9 that except for the held-out counts for 0 and 1, all the other bigram counts in the held-out set could be estimated pretty well by just subtracting 0.75 from the count in the training set! **Absolute discounting** formalizes this intuition by subtracting a fixed (absolute) discount $d$ from each count. The intuition is that since we have good estimates already for the very high counts, a small discount...
\(d\) won’t affect them much. It will mainly modify the smaller counts, for which we
don’t necessarily trust the estimate anyway, and Fig. 3.9 suggests that in practice this
discount is actually a good one for bigrams with counts 2 through 9. The equation
for interpolated absolute discounting applied to bigrams:

\[
P_{\text{AbsoluteDiscounting}}(w_i|w_{i-1}) = \frac{C(w_{i-1}w_i) - d}{\sum_v C(w_{i-1}v)} + \lambda(w_{i-1})P(w_i)
\]  
(3.31)

The first term is the discounted bigram, with \(0 \leq d \leq 1\), and the second term is
the unigram with an interpolation weight \(\lambda\). By inspection of Fig. 3.9, it looks like just
setting all the \(d\) values to .75 would work very well, or perhaps keeping a separate
second discount value of 0.5 for the bigrams with counts of 1. There are principled
methods for setting \(d\); for example, Ney et al. (1994) set \(d\) as a function of \(n_1\) and
\(n_2\), the number of unigrams that have a count of 1 and a count of 2, respectively:

\[d = \frac{n_1}{n_1 + 2n_2}\]  
(3.32)

3.8.2 Kneser-Ney Discounting

Kneser-Ney discounting (Kneser and Ney, 1995) augments absolute discounting
with a more sophisticated way to handle the lower-order unigram distribution. Con-
sider the job of predicting the next word in this sentence, assuming we are interpo-
lating a bigram and a unigram model.

I can’t see without my reading ________________.

The word glasses seems much more likely to follow here than, say, the word
Kong, so we’d like our unigram model to prefer glasses. But in fact it’s Kong that is
more common, since Hong Kong is a very frequent word. A standard unigram model
will assign Kong a higher probability than glasses. We would like to capture the
intuition that although Kong is frequent, it is mainly only frequent in the phrase Hong
Kong, that is, after the word Hong. The word glasses has a much wider distribution.

In other words, instead of \(P(w)\), which answers the question “How likely is
\(w\)?”, we’d like to create a unigram model that we might call \(P_{\text{CONTINUATION}}\), which
answers the question “How likely is \(w\) to appear as a novel continuation?” How can
we estimate this probability of seeing the word \(w\) as a novel continuation, in a new
unseen context? The Kneser-Ney intuition is to base our estimate of \(P_{\text{CONTINUATION}}\)
on the number of different contexts word \(w\) has appeared in, that is, the number of
bigram types it completes. Every bigram type was a novel continuation the first time
it was seen. We hypothesize that words that have appeared in more contexts in the
past are more likely to appear in some new context as well. The number of times a
word \(w\) appears as a novel continuation can be expressed as:

\[P_{\text{CONTINUATION}}(w) \propto |\{v : C(vw) > 0\}|\]  
(3.33)

To turn this count into a probability, we normalize by the total number of word
bigram types. In summary:

\[P_{\text{CONTINUATION}}(w) = \frac{|\{v : C(vw) > 0\}|}{|\{(u',w') : C(u'w') > 0\}|}\]  
(3.34)

An equivalent formulation based on a different metaphor is to use the number of
word types seen to precede \(w\) (Eq. 3.33 repeated):

\[P_{\text{CONTINUATION}}(w) \propto |\{v : C(vw) > 0\}|\]  
(3.35)
3.8 * ADVANCED: KNESER-NEY SMOOTHING

normalized by the number of words preceding all words, as follows:

$$P_{\text{CONTINUATION}}(w) = \frac{|\{v : C(vw) > 0\}|}{\sum_{w'} |\{v : C(vw') > 0\}|}$$ \hspace{1cm} (3.36)

A frequent word (Kong) occurring in only one context (Hong) will have a low continuation probability.

The final equation for Interpolated Kneser-Ney smoothing for bigrams is then:

$$P_{\text{KN}}(w_i|w_{i-1}) = \max\left( C(w_{i-1}w_i) - d, 0 \right) + \lambda(w_{i-1}) P_{\text{CONTINUATION}}(w_i)$$ \hspace{1cm} (3.37)

The $\lambda$ is a normalizing constant that is used to distribute the probability mass we’ve discounted:

$$\lambda(w_{i-1}) = \frac{d}{\sum_{v} C(w_{i-1}v)} |\{w : C(w_{i-1}w) > 0\}|$$ \hspace{1cm} (3.38)

The first term, $\frac{d}{\sum_{v} C(w_{i-1}v)}$, is the normalized discount (the discount $d$, $0 \leq d \leq 1$, was introduced in the absolute discounting section above). The second term, $|\{w : C(w_{i-1}w) > 0\}|$, is the number of word types that can follow $w_{i-1}$ or, equivalently, the number of word types that we discounted; in other words, the number of times we applied the normalized discount.

The general recursive formulation is as follows:

$$P_{\text{KN}}(w_i|w_{i-n+1:i-1}) = \max\left( c_{\text{KN}}(w_{i-n+1:i-1}) - d, 0 \right) + \frac{\lambda(w_{i-n+1:i-1}) P_{\text{KN}}(w_i|w_{i-n+2:i-1})}{\sum_{w'} c_{\text{KN}}(w_{i-n+1:i-1}w')}$$ \hspace{1cm} (3.39)

where the definition of the count $c_{\text{KN}}$ depends on whether we are counting the highest-order n-gram being interpolated (for example trigram if we are interpolating trigram, bigram, and unigram) or one of the lower-order n-grams (bigram or unigram if we are interpolating trigram, bigram, and unigram):

$$c_{\text{KN}}(\cdot) = \begin{cases} \text{count}(\cdot) & \text{for the highest order} \\ \text{continuation count}(\cdot) & \text{for lower orders} \end{cases}$$ \hspace{1cm} (3.40)

The continuation count of a string $\cdot$ is the number of unique single word contexts for that string $\cdot$.

At the termination of the recursion, unigrams are interpolated with the uniform distribution, where the parameter $\epsilon$ is the empty string:

$$P_{\text{KN}}(w) = \max\left( c_{\text{KN}}(w) - d, 0 \right) + \frac{\lambda(\epsilon) 1}{V}$$ \hspace{1cm} (3.41)

If we want to include an unknown word $<\text{UNK}>$, it’s just included as a regular vocabulary entry with count zero, and hence its probability will be a lambda-weighted uniform distribution $\frac{\lambda(\epsilon)}{V}$.

The best performing version of Kneser-Ney smoothing is called modified Kneser-Ney smoothing, and is due to Chen and Goodman (1998). Rather than use a single fixed discount $d$, modified Kneser-Ney uses three different discounts $d_1$, $d_2$, and $d_3+$ for n-grams with counts of 1, 2 and three or more, respectively. See Chen and Goodman (1998, p. 19) or Heafield et al. (2013) for the details.
3.9 Advanced: Perplexity’s Relation to Entropy

We introduced perplexity in Section 3.3 as a way to evaluate n-gram models on a test set. A better n-gram model is one that assigns a higher probability to the test data, and perplexity is a normalized version of the probability of the test set. The perplexity measure actually arises from the information-theoretic concept of cross-entropy, which explains otherwise mysterious properties of perplexity (why the inverse probability, for example?) and its relationship to entropy. **Entropy** is a measure of information. Given a random variable $X$ ranging over whatever we are predicting (words, letters, parts of speech, the set of which we’ll call $\chi$) and with a particular probability function, call it $p(x)$, the entropy of the random variable $X$ is:

$$H(X) = -\sum_{x \in \chi} p(x) \log_2 p(x)$$  \hspace{1cm} (3.42)

The log can, in principle, be computed in any base. If we use log base 2, the resulting value of entropy will be measured in **bits**.

One intuitive way to think about entropy is as a lower bound on the number of bits it would take to encode a certain decision or piece of information in the optimal coding scheme.

Consider an example from the standard information theory textbook **Cover and Thomas (1991)**. Imagine that we want to place a bet on a horse race but it is too far to go all the way to Yonkers Racetrack, so we’d like to send a short message to the bookie to tell him which of the eight horses to bet on. One way to encode this message is just to use the binary representation of the horse’s number as the code; thus, horse 1 would be $001$, horse 2 $010$, horse 3 $011$, and so on, with horse 8 coded as $000$. If we spend the whole day betting and each horse is coded with 3 bits, on average we would be sending 3 bits per race.

Can we do better? Suppose that the spread is the actual distribution of the bets placed and that we represent it as the prior probability of each horse as follows:

<table>
<thead>
<tr>
<th>Horse</th>
<th>Probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\frac{1}{8}$</td>
</tr>
<tr>
<td>2</td>
<td>$\frac{1}{4}$</td>
</tr>
<tr>
<td>3</td>
<td>$\frac{1}{8}$</td>
</tr>
<tr>
<td>4</td>
<td>$\frac{1}{16}$</td>
</tr>
<tr>
<td>5</td>
<td>$\frac{1}{64}$</td>
</tr>
<tr>
<td>6</td>
<td>$\frac{1}{64}$</td>
</tr>
<tr>
<td>7</td>
<td>$\frac{1}{64}$</td>
</tr>
<tr>
<td>8</td>
<td>$\frac{1}{64}$</td>
</tr>
</tbody>
</table>

The entropy of the random variable $X$ that ranges over horses gives us a lower bound on the number of bits and is

$$H(X) = - \sum_{i=1}^{8} p(i) \log_2 p(i)$$

$$= - \frac{1}{2} \log_2 \frac{1}{8} - \frac{1}{4} \log_2 \frac{1}{4} - \frac{1}{8} \log_2 \frac{1}{8} - \frac{1}{16} \log_2 \frac{1}{16} - 4 \left( \frac{1}{64} \log_2 \frac{1}{64} \right)$$

$$= 2 \text{ bits}$$  \hspace{1cm} (3.43)

A code that averages 2 bits per race can be built with short encodings for more probable horses, and longer encodings for less probable horses. For example, we could encode the most likely horse with the code 0, and the remaining horses as 10, then 110, 1110, 111100, 111101, 111110, and 111111.
What if the horses are equally likely? We saw above that if we used an equal-length binary code for the horse numbers, each horse took 3 bits to code, so the average was 3. Is the entropy the same? In this case each horse would have a probability of $\frac{1}{8}$. The entropy of the choice of horses is then

$$H(X) = -\sum_{i=1}^{8} \frac{1}{8} \log_2 \frac{1}{8} = -\log_2 \frac{1}{8} = 3 \text{ bits}$$  \hspace{1cm} (3.44)

Until now we have been computing the entropy of a single variable. But most of what we will use entropy for involves sequences. For a grammar, for example, we will be computing the entropy of some sequence of words $W = \{w_1, w_2, \ldots, w_n\}$. One way to do this is to have a variable that ranges over sequences of words. For example we can compute the entropy of a random variable that ranges over all finite sequences of words of length $n$ in some language $L$ as follows:

$$H(w_1, w_2, \ldots, w_n) = -\sum_{w_1, n \in L} p(w_1, n) \log p(w_1, n)$$  \hspace{1cm} (3.45)

We could define the entropy rate (we could also think of this as the per-word entropy) as the entropy of this sequence divided by the number of words:

$$\frac{1}{n} H(w_1, w_2, \ldots, w_n) = -\frac{1}{n} \sum_{w_1, n \in L} p(w_1, n) \log p(w_1, n)$$  \hspace{1cm} (3.46)

But to measure the true entropy of a language, we need to consider sequences of infinite length. If we think of a language as a stochastic process $L$ that produces a sequence of words, and allow $W$ to represent the sequence of words $w_1, \ldots, w_n$, then $L$’s entropy rate $H(L)$ is defined as

$$H(L) = \lim_{n \to \infty} \frac{1}{n} H(w_1, w_2, \ldots, w_n)$$

$$= -\lim_{n \to \infty} \frac{1}{n} \sum_{W \in L} p(w_1, \ldots, w_n) \log p(w_1, \ldots, w_n)$$  \hspace{1cm} (3.47)

The Shannon-McMillan-Breiman theorem (Algoet and Cover 1988, Cover and Thomas 1991) states that if the language is regular in certain ways (to be exact, if it is both stationary and ergodic),

$$H(L) = \lim_{n \to \infty} -\frac{1}{n} \log p(w_1 w_2 \ldots w_n)$$  \hspace{1cm} (3.48)

That is, we can take a single sequence that is long enough instead of summing over all possible sequences. The intuition of the Shannon-McMillan-Breiman theorem is that a long-enough sequence of words will contain in it many other shorter sequences and that each of these shorter sequences will reoccur in the longer sequence according to their probabilities.

A stochastic process is said to be stationary if the probabilities it assigns to a sequence are invariant with respect to shifts in the time index. In other words, the probability distribution for words at time $t$ is the same as the probability distribution at time $t + 1$. Markov models, and hence n-grams, are stationary. For example, in a bigram, $P_i$ is dependent only on $P_{i-1}$. So if we shift our time index by $x$, $P_{i+x}$ is still dependent on $P_{i+x-1}$. But natural language is not stationary, since as we show
in Appendix D, the probability of upcoming words can be dependent on events that were arbitrarily distant and time dependent. Thus, our statistical models only give an approximation to the correct distributions and entropies of natural language.

To summarize, by making some incorrect but convenient simplifying assumptions, we can compute the entropy of some stochastic process by taking a very long sample of the output and computing its average log probability.

Now we are ready to introduce cross-entropy. The cross-entropy is useful when we don’t know the actual probability distribution \( p \) that generated some data. It allows us to use some \( m \), which is a model of \( p \) (i.e., an approximation to \( p \)). The cross-entropy of \( m \) on \( p \) is defined by

\[
H(p, m) = \lim_{n \to \infty} -\frac{1}{n} \sum_{W \in L} p(w_1, \ldots, w_n) \log m(w_1, \ldots, w_n)
\] (3.49)

That is, we draw sequences according to the probability distribution \( p \), but sum the log of their probabilities according to \( m \).

Again, following the Shannon-McMillan-Breiman theorem, for a stationary ergodic process:

\[
H(p, m) = \lim_{n \to \infty} -\frac{1}{n} \log m(w_1 w_2 \ldots w_n)
\] (3.50)

This means that, as for entropy, we can estimate the cross-entropy of a model \( m \) on some distribution \( p \) by taking a single sequence that is long enough instead of summing over all possible sequences.

What makes the cross-entropy useful is that the cross-entropy \( H(p, m) \) is an upper bound on the entropy \( H(p) \). For any model \( m \):

\[
H(p) \leq H(p, m)
\] (3.51)

This means that we can use some simplified model \( m \) to help estimate the true entropy of a sequence of symbols drawn according to probability \( p \). The more accurate \( m \) is, the closer the cross-entropy \( H(p, m) \) will be to the true entropy \( H(p) \). Thus, the difference between \( H(p, m) \) and \( H(p) \) is a measure of how accurate a model is. Between two models \( m_1 \) and \( m_2 \), the more accurate model will be the one with the lower cross-entropy. (The cross-entropy can never be lower than the true entropy, so a model cannot err by underestimating the true entropy.)

We are finally ready to see the relation between perplexity and cross-entropy as we saw it in Eq. 3.50. Cross-entropy is defined in the limit as the length of the observed word sequence goes to infinity. We will need an approximation to cross-entropy, relying on a (sufficiently long) sequence of fixed length. This approximation to the cross-entropy of a model \( M = P(w_i|w_{i-N+1:i-1}) \) on a sequence of words \( W \) is

\[
H(W) = -\frac{1}{N} \log P(w_1 w_2 \ldots w_N)
\] (3.52)

The perplexity of a model \( P \) on a sequence of words \( W \) is now formally defined as 2 raised to the power of this cross-entropy:
Perplexity($W$) = $2^{H(W)}$

= $P(w_1w_2...w_N)^{-\frac{1}{N}}$

= $\sqrt[N]{\frac{1}{P(w_1w_2...w_N)}}$

= $\sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1...w_{i-1})}}$ (3.53)

3.10 Summary

This chapter introduced language modeling and the n-gram, one of the most widely used tools in language processing.

- Language models offer a way to assign a probability to a sentence or other sequence of words, and to predict a word from preceding words.
- n-grams are Markov models that estimate words from a fixed window of previous words. n-gram probabilities can be estimated by counting in a corpus and normalizing (the maximum likelihood estimate).
- n-gram language models are evaluated extrinsically in some task, or intrinsically using perplexity.
- The perplexity of a test set according to a language model is the geometric mean of the inverse test set probability computed by the model.
- Smoothing algorithms provide a more sophisticated way to estimate the probability of n-grams. Commonly used smoothing algorithms for n-grams rely on lower-order n-gram counts through backoff or interpolation.
- Both backoff and interpolation require discounting to create a probability distribution.
- Kneser-Ney smoothing makes use of the probability of a word being a novel continuation. The interpolated Kneser-Ney smoothing algorithm mixes a discounted probability with a lower-order continuation probability.

Bibliographical and Historical Notes

The underlying mathematics of the n-gram was first proposed by Markov (1913), who used what are now called Markov chains (bigrams and trigrams) to predict whether an upcoming letter in Pushkin’s Eugene Onegin would be a vowel or a consonant. Markov classified 20,000 letters as V or C and computed the bigram and trigram probability that a given letter would be a vowel given the previous one or two letters. Shannon (1948) applied n-grams to compute approximations to English word sequences. Based on Shannon’s work, Markov models were commonly used in engineering, linguistic, and psychological work on modeling word sequences by the 1950s. In a series of extremely influential papers starting with Chomsky (1956) and including Chomsky (1957) and Miller and Chomsky (1963), Noam Chomsky argued that “finite-state Markov processes”, while a possibly useful engineering heuristic,
were incapable of being a complete cognitive model of human grammatical knowledge. These arguments led many linguists and computational linguists to ignore work in statistical modeling for decades.

The resurgence of n-gram models came from Fred Jelinek and colleagues at the IBM Thomas J. Watson Research Center, who were influenced by Shannon, and James Baker at CMU, who was influenced by the prior, classified work of Leonard Baum and colleagues on these topics at labs like IDA. Independently these two labs successfully used n-grams in their speech recognition systems at the same time (Baker 1975b, Jelinek et al. 1975, Baker 1975a, Bahl et al. 1983, Jelinek 1990).

The terms “language model” and “perplexity” were first used for this technology by the IBM group. Jelinek and his colleagues used the term language model in pretty modern way, to mean the entire set of linguistic influences on word sequence probabilities, including grammar, semantics, discourse, and even speaker characteristics, rather than just the particular n-gram model itself.

Add-one smoothing derives from Laplace’s 1812 law of succession and was first applied as an engineering solution to the zero frequency problem by Jeffreys (1948) based on an earlier Add-K suggestion by Johnson (1932). Problems with the add-one algorithm are summarized in Gale and Church (1994).

A wide variety of different language modeling and smoothing techniques were proposed in the 80s and 90s, including Good-Turing discounting—first applied to the n-gram smoothing at IBM by Katz (Nádas 1984, Church and Gale 1991)—Witten-Bell discounting (Witten and Bell, 1991), and varieties of class-based n-gram models that used information about word classes. Starting in the late 1990s, Chen and Goodman performed a number of carefully controlled experiments comparing different discounting algorithms, cache models, class-based models, and other language model parameters (Chen and Goodman 1999, Goodman 2006, inter alia). They showed the advantages of Modified Interpolated Kneser-Ney, which became the standard baseline for n-gram language modeling, especially because they showed that caches and class-based models provided only minor additional improvement.

Modern language modeling is more commonly done with neural network language models, which solve the major problems with n-grams: the number of parameters increases exponentially as the n-gram order increases, and n-grams have no way to generalize from training to test set. Neural language models instead project words into a continuous space in which words with similar contexts have similar representations. We’ll introduce feedforward language models (Bengio et al. 2006, Schwenk 2007) in Chapter 7, recurrent language models (Mikolov, 2012) in Chapter 9, and transformer-based large language models in Chapter 10.

Exercises

3.1 Write out the equation for trigram probability estimation (modifying Eq. 3.11). Now write out all the non-zero trigram probabilities for the I am Sam corpus on page 35.

3.2 Calculate the probability of the sentence i want chinese food. Give two probabilities, one using Fig. 3.2 and the ‘useful probabilities’ just below it on page 37, and another using the add-1 smoothed table in Fig. 3.7. Assume the additional add-1 smoothed probabilities $P(i | <s>) = 0.19$ and $P(<s> | \text{food}) = 0.40$. 
3.3 Which of the two probabilities you computed in the previous exercise is higher, unsmoothed or smoothed? Explain why.

3.4 We are given the following corpus, modified from the one in the chapter:
<s> I am Sam </s>
<s> Sam I am </s>
<s> I am Sam </s>
<s> I do not like green eggs and Sam </s>
Using a bigram language model with add-one smoothing, what is \( P(Sam \mid am) \)? Include <s> and </s> in your counts just like any other token.

3.5 Suppose we didn’t use the end-symbol </s>. Train an unsmoothed bigram grammar on the following training corpus without using the end-symbol </s>:
<s> a b </s>
<s> b b </s>
<s> b a </s>
<s> a a </s>
Demonstrate that your bigram model does not assign a single probability distribution across all sentence lengths by showing that the sum of the probability of the four possible 2 word sentences over the alphabet \{a,b\} is 1.0, and the sum of the probability of all possible 3 word sentences over the alphabet \{a,b\} is also 1.0.

3.6 Suppose we train a trigram language model with add-one smoothing on a given corpus. The corpus contains \( V \) word types. Express a formula for estimating \( P(w_3 \mid w_1,w_2) \), where \( w_3 \) is a word which follows the bigram \((w_1,w_2)\), in terms of various n-gram counts and \( V \). Use the notation \( c(w_1,w_2,w_3) \) to denote the number of times that trigram \((w_1,w_2,w_3)\) occurs in the corpus, and so on for bigrams and unigrams.

3.7 We are given the following corpus, modified from the one in the chapter:
<s> I am Sam </s>
<s> Sam I am </s>
<s> I am Sam </s>
<s> I do not like green eggs and Sam </s>
If we use linear interpolation smoothing between a maximum-likelihood bigram model and a maximum-likelihood unigram model with \( \lambda_1 = \frac{1}{2} \) and \( \lambda_2 = \frac{1}{2} \), what is \( P(Sam \mid am) \)? Include <s> and </s> in your counts just like any other token.

3.8 Write a program to compute unsmoothed unigrams and bigrams.

3.9 Run your n-gram program on two different small corpora of your choice (you might use email text or newsgroups). Now compare the statistics of the two corpora. What are the differences in the most common unigrams between the two? How about interesting differences in bigrams?

3.10 Add an option to your program to generate random sentences.

3.11 Add an option to your program to compute the perplexity of a test set.

3.12 You are given a training set of 100 numbers that consists of 91 zeros and 1 each of the other digits 1-9. Now we see the following test set: 0 0 0 0 0 3 0 0 0 0. What is the unigram perplexity?
Naive Bayes, Text Classification, and Sentiment

Classification lies at the heart of both human and machine intelligence. Deciding what letter, word, or image has been presented to our senses, recognizing faces or voices, sorting mail, assigning grades to homeworks; these are all examples of assigning a category to an input. The potential challenges of this task are highlighted by the fabulist Jorge Luis Borges (1964), who imagined classifying animals into:

(a) those that belong to the Emperor, (b) embalmed ones, (c) those that are trained, (d) suckling pigs, (e) mermaids, (f) fabulous ones, (g) stray dogs, (h) those that are included in this classification, (i) those that tremble as if they were mad, (j) innumerable ones, (k) those drawn with a very fine camel’s hair brush, (l) others, (m) those that have just broken a flower vase, (n) those that resemble flies from a distance.

Many language processing tasks involve classification, although luckily our classes are much easier to define than those of Borges. In this chapter we introduce the naive Bayes algorithm and apply it to text categorization, the task of assigning a label or category to an entire text or document.

We focus on one common text categorization task, sentiment analysis, the extraction of sentiment, the positive or negative orientation that a writer expresses toward some object. A review of a movie, book, or product on the web expresses the author’s sentiment toward the product, while an editorial or political text expresses sentiment toward a candidate or political action. Extracting consumer or public sentiment is thus relevant for fields from marketing to politics.

The simplest version of sentiment analysis is a binary classification task, and the words of the review provide excellent cues. Consider, for example, the following phrases extracted from positive and negative reviews of movies and restaurants. Words like great, richly, awesome, and pathetic, and awful and ridiculously are very informative cues:

+ ...zany characters and richly applied satire, and some great plot twists
− It was pathetic. The worst part about it was the boxing scenes...
+ ...awesome caramel sauce and sweet toasty almonds. I love this place!
− ...awful pizza and ridiculously overpriced...

Spam detection is another important commercial application, the binary classification task of assigning an email to one of the two classes spam or not-spam. Many lexical and other features can be used to perform this classification. For example you might quite reasonably be suspicious of an email containing phrases like “online pharmaceutical” or “WITHOUT ANY COST” or “Dear Winner”.

Another thing we might want to know about a text is the language it’s written in. Texts on social media, for example, can be in any number of languages and we’ll need to apply different processing. The task of language id is thus the first step in most language processing pipelines. Related text classification tasks like authorship attribution—determining a text’s author—are also relevant to the digital humanities, social sciences, and forensic linguistics.
Finally, one of the oldest tasks in text classification is assigning a library subject category or topic label to a text. Deciding whether a research paper concerns epidemiology or instead, perhaps, embryology, is an important component of information retrieval. Various sets of subject categories exist, such as the MeSH (Medical Subject Headings) thesaurus. In fact, as we will see, subject category classification is the task for which the naive Bayes algorithm was invented in 1961 Maron (1961).

Classification is essential for tasks below the level of the document as well. We’ve already seen period disambiguation (deciding if a period is the end of a sentence or part of a word), and word tokenization (deciding if a character should be a word boundary). Even language modeling can be viewed as classification: each word can be thought of as a class, and so predicting the next word is classifying the context-so-far into a class for each next word. A part-of-speech tagger (Chapter 8) classifies each occurrence of a word in a sentence as, e.g., a noun or a verb.

The goal of classification is to take a single observation, extract some useful features, and thereby classify the observation into one of a set of discrete classes. One method for classifying text is to use rules handwritten by humans. Handwritten rule-based classifiers can be components of state-of-the-art systems in language processing. But rules can be fragile, as situations or data change over time, and for some tasks humans aren’t necessarily good at coming up with the rules.

The most common way of doing text classification in language processing is instead via supervised machine learning, the subject of this chapter. In supervised learning, we have a data set of input observations, each associated with some correct output (a ‘supervision signal’). The goal of the algorithm is to learn how to map from a new observation to a correct output.

Formally, the task of supervised classification is to take an input \( x \) and a fixed set of output classes \( Y = \{y_1, y_2, \ldots, y_M\} \) and return a predicted class \( y \in Y \). For text classification, we’ll sometimes talk about \( c \) (for “class”) instead of \( y \) as our output variable, and \( d \) (for “document”) instead of \( x \) as our input variable. In the supervised situation we have a training set of \( N \) documents that have each been hand-labeled with a class: \( \{(d_1, c_1), \ldots, (d_N, c_N)\} \). Our goal is to learn a classifier that is capable of mapping from a new document \( d \) to its correct class \( c \in C \), where \( C \) is some set of useful document classes. A probabilistic classifier additionally will tell us the probability of the observation being in the class. This full distribution over the classes can be useful information for downstream decisions; avoiding making discrete decisions early on can be useful when combining systems.

Many kinds of machine learning algorithms are used to build classifiers. This chapter introduces naive Bayes; the following one introduces logistic regression. These exemplify two ways of doing classification. Generative classifiers like naive Bayes build a model of how a class could generate some input data. Given an observation, they return the class most likely to have generated the observation. Discriminative classifiers like logistic regression instead learn what features from the input are most useful to discriminate between the different possible classes. While discriminative systems are often more accurate and hence more commonly used, generative classifiers still have a role.

### 4.1 Naive Bayes Classifiers

In this section we introduce the multinomial naive Bayes classifier, so called because it is a Bayesian classifier that makes a simplifying (naive) assumption about
how the features interact.

The intuition of the classifier is shown in Fig. 4.1. We represent a text document as if it were a bag of words, that is, an unordered set of words with their position ignored, keeping only their frequency in the document. In the example in the figure, instead of representing the word order in all the phrases like “I love this movie” and “I would recommend it”, we simply note that the word I occurred 5 times in the entire excerpt, the word it 6 times, the words love, recommend, and movie once, and so on.

Figure 4.1 Intuition of the multinomial naive Bayes classifier applied to a movie review. The position of the words is ignored (the bag-of-words assumption) and we make use of the frequency of each word.

Naive Bayes is a probabilistic classifier, meaning that for a document \( d \), out of all classes \( c \in C \) the classifier returns the class \( \hat{c} \) which has the maximum posterior probability given the document. In Eq. 4.1 we use the hat notation “\( \hat{c} \)” to mean “our estimate of the correct class”.

\[
\hat{c} = \operatorname{argmax}_{c \in C} P(c|d)
\]  

(4.1)

This idea of Bayesian inference has been known since the work of Bayes (1763), and was first applied to text classification by Mosteller and Wallace (1964). The intuition of Bayesian classification is to use Bayes’ rule to transform Eq. 4.1 into other probabilities that have some useful properties. Bayes’ rule is presented in Eq. 4.2; it gives us a way to break down any conditional probability \( P(x|y) \) into three other probabilities:

\[
P(x|y) = \frac{P(y|x)P(x)}{P(y)}
\]  

(4.2)

We can then substitute Eq. 4.2 into Eq. 4.1 to get Eq. 4.3:

\[
\hat{c} = \operatorname{argmax}_{c \in C} P(c|d) = \operatorname{argmax}_{c \in C} \frac{P(d|c)P(c)}{P(d)}
\]  

(4.3)
We can conveniently simplify Eq. 4.3 by dropping the denominator $P(d)$. This is possible because we will be computing $\frac{P(d|c)P(c)}{P(d)}$ for each possible class. But $P(d)$ doesn’t change for each class; we are always asking about the most likely class for the same document $d$, which must have the same probability $P(d)$. Thus, we can choose the class that maximizes this simpler formula:

$$\hat{c} = \text{argmax}_{c \in C} P(c|d) = \text{argmax}_{c \in C} P(d|c)P(c)$$ (4.4)

We call Naive Bayes a generative model because we can read Eq. 4.4 as stating a kind of implicit assumption about how a document is generated: first a class is sampled from $P(c)$, and then the words are generated by sampling from $P(d|c)$. (In fact we could imagine generating artificial documents, or at least their word counts, by following this process). We’ll say more about this intuition of generative models in Chapter 5.

To return to classification: we compute the most probable class $\hat{c}$ given some document $d$ by choosing the class which has the highest product of two probabilities: the prior probability of the class $P(c)$ and the likelihood of the document $P(d|c)$:

$$\hat{c} = \text{argmax}_{c \in C} \underbrace{P(d|c)}_{\text{likelihood}} \underbrace{P(c)}_{\text{prior}}$$ (4.5)

Without loss of generalization, we can represent a document $d$ as a set of features $f_1, f_2, ..., f_n$:

$$\hat{c} = \text{argmax}_{c \in C} \prod_{f \in F} P(f|c) \prod_{c \in C} P(c)$$ (4.6)

Unfortunately, Eq. 4.6 is still too hard to compute directly: without some simplifying assumptions, estimating the probability of every possible combination of features (for example, every possible set of words and positions) would require huge numbers of parameters and impossibly large training sets. Naive Bayes classifiers therefore make two simplifying assumptions.

The first is the bag-of-words assumption discussed intuitively above: we assume position doesn’t matter, and that the word “love” has the same effect on classification whether it occurs as the 1st, 20th, or last word in the document. Thus we assume that the features $f_1, f_2, ..., f_n$ only encode word identity and not position.

The second is commonly called the naive Bayes assumption: this is the conditional independence assumption that the probabilities $P(f_i|c)$ are independent given the class $c$ and hence can be ‘naively’ multiplied as follows:

$$P(f_1, f_2, ..., f_n|c) = P(f_1|c) \cdot P(f_2|c) \cdot ... \cdot P(f_n|c)$$ (4.7)

The final equation for the class chosen by a naive Bayes classifier is thus:

$$c_{NB} = \text{argmax}_{c \in C} P(c) \prod_{f \in F} P(f|c)$$ (4.8)

To apply the naive Bayes classifier to text, we need to consider word positions, by simply walking an index through every word position in the document:

$$c_{NB} = \text{argmax}_{c \in C} P(c) \prod_{i \in \text{positions}} P(w_i|c)$$ (4.9)
Naive Bayes calculations, like calculations for language modeling, are done in log space, to avoid underflow and increase speed. Thus Eq. 4.9 is generally instead expressed as

$$c_{NB} = \arg\max_{c \in C} \log P(c) + \sum_{i \in \text{positions}} \log P(w_i | c) \quad (4.10)$$

By considering features in log space, Eq. 4.10 computes the predicted class as a linear function of input features. Classifiers that use a linear combination of the inputs to make a classification decision —like naive Bayes and also logistic regression—are called **linear classifiers**.

### 4.2 Training the Naive Bayes Classifier

How can we learn the probabilities $P(c)$ and $P(f_i | c)$? Let’s first consider the maximum likelihood estimate. We’ll simply use the frequencies in the data. For the class prior $P(c)$ we ask what percentage of the documents in our training set are in each class $c$. Let $N_c$ be the number of documents in our training data with class $c$ and $N_{\text{doc}}$ the total number of documents. Then:

$$\hat{P}(c) = \frac{N_c}{N_{\text{doc}}} \quad (4.11)$$

To learn the probability $P(f_i | c)$, we’ll assume a feature is just the existence of a word in the document’s bag of words, and so we’ll want $P(w_i | c)$, which we compute as the fraction of times the word $w_i$ appears among all words in all documents of topic $c$. We first concatenate all documents with category $c$ into one big “category c” text. Then we use the frequency of $w_i$ in this concatenated document to give a maximum likelihood estimate of the probability:

$$\hat{P}(w_i | c) = \frac{\text{count}(w_i, c)}{\sum_{w \in V} \text{count}(w, c)} \quad (4.12)$$

Here the vocabulary $V$ consists of the union of all the word types in all classes, not just the words in one class $c$.

There is a problem, however, with maximum likelihood training. Imagine we are trying to estimate the likelihood of the word “fantastic” given class positive, but suppose there are no training documents that both contain the word “fantastic” and are classified as positive. Perhaps the word “fantastic” happens to occur (sarcastically?) in the class negative. In such a case the probability for this feature will be zero:

$$\hat{P}(\text{"fantastic"} | \text{positive}) = \frac{\text{count}(\text{"fantastic"}, \text{positive})}{\sum_{w \in V} \text{count}(w, \text{positive})} = 0 \quad (4.13)$$

But since naive Bayes naively multiplies all the feature likelihoods together, zero probabilities in the likelihood term for any class will cause the probability of the class to be zero, no matter the other evidence!

The simplest solution is the add-one (Laplace) smoothing introduced in Chapter 3. While Laplace smoothing is usually replaced by more sophisticated smoothing

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1 In practice throughout this book, we’ll use log to mean natural log (ln) when the base is not specified.
algorithms in language modeling, it is commonly used in naive Bayes text categorization:

\[
P(w|c) = \frac{\text{count}(w, c) + 1}{\sum_{w \in V} (\text{count}(w, c) + 1)}
\]

Note once again that it is crucial that the vocabulary \( V \) consists of the union of all the word types in all classes, not just the words in one class \( c \) (try to convince yourself why this must be true; see the exercise at the end of the chapter).

What do we do about words that occur in our test data but are not in our vocabulary at all because they did not occur in any training document in any class? The solution for such unknown words is to ignore them—remove them from the test document and not include any probability for them at all.

Finally, some systems choose to completely ignore another class of words: stop words, very frequent words like the and a. This can be done by sorting the vocabulary by frequency in the training set, and defining the top 10–100 vocabulary entries as stop words, or alternatively by using one of the many predefined stop word lists available online. Then each instance of these stop words is simply removed from both training and test documents as if it had never occurred. In most text classification applications, however, using a stop word list doesn’t improve performance, and so it is more common to make use of the entire vocabulary and not use a stop word list.

Fig. 4.2 shows the final algorithm.

```plaintext
function Train Naive Bayes(D, C) returns log P(c) and log P(w|c)
    # Calculate P(c) terms
    N_{doc} = number of documents in D
    N_c = number of documents from D in class c
    \text{logprior}[c] \leftarrow \log \frac{N_c}{N_{doc}}
    V \leftarrow \text{vocabulary of D}
    \text{bigdoc}[c] \leftarrow \text{append}(d) \text{ for } d \in D \text{ with class } c
    \text{for each word } w \text{ in } V \text{ # Calculate } P(w|c) \text{ terms}
        \text{count}(w, c) \leftarrow \# \text{ of occurrences of } w \text{ in } \text{bigdoc}[c]
        \text{loglikelihood}[w, c] \leftarrow \log \frac{\text{count}(w, c) + 1}{\sum_{w' \in V} (\text{count}(w', c) + 1)}
    \text{return } \text{logprior}, \text{loglikelihood}, V

function Test Naive Bayes(testdoc, logprior, loglikelihood, C, V) returns best c
    for each class \( c \in C \)
        \text{sum}[c] \leftarrow \text{logprior}[c]
        \text{for each position } i \text{ in testdoc}
            word \leftarrow \text{testdoc}[i]
            \text{if } word \in V
                \text{sum}[c] \leftarrow \text{sum}[c] + \text{loglikelihood}[word, c]
    \text{return } \arg \max_c \text{ sum}[c]
```

Figure 4.2 The naive Bayes algorithm, using add-1 smoothing. To use add-\( \alpha \) smoothing instead, change the +1 to +\( \alpha \) for loglikelihood counts in training.
4.3 Worked example

Let’s walk through an example of training and testing naive Bayes with add-one smoothing. We’ll use a sentiment analysis domain with the two classes positive (+) and negative (-), and take the following miniature training and test documents simplified from actual movie reviews.

<table>
<thead>
<tr>
<th>Cat</th>
<th>Documents</th>
</tr>
</thead>
<tbody>
<tr>
<td>Training</td>
<td>- just plain boring</td>
</tr>
<tr>
<td></td>
<td>- entirely predictable and lacks energy</td>
</tr>
<tr>
<td></td>
<td>- no surprises and very few laughs</td>
</tr>
<tr>
<td></td>
<td>+ very powerful</td>
</tr>
<tr>
<td></td>
<td>+ the most fun film of the summer</td>
</tr>
<tr>
<td>Test</td>
<td>? predictable with no fun</td>
</tr>
</tbody>
</table>

The prior $P(c)$ for the two classes is computed via Eq. 4.11 as $\frac{N_c}{N_{doc}}$:

$$P(-) = \frac{3}{5} \quad P(+) = \frac{2}{5}$$

The word *with* doesn’t occur in the training set, so we drop it completely (as mentioned above, we don’t use unknown word models for naive Bayes). The likelihoods from the training set for the remaining three words “predictable”, “no”, and “fun”, are as follows, from Eq. 4.14 (computing the probabilities for the remainder of the words in the training set is left as an exercise for the reader):

$$P(\text{“predictable”}|-) = \frac{1+1}{14+20} \quad P(\text{“predictable”}|+) = \frac{0+1}{9+20}$$

$$P(\text{“no”}|-) = \frac{1+1}{14+20} \quad P(\text{“no”}|+) = \frac{0+1}{9+20}$$

$$P(\text{“fun”}|-) = \frac{0+1}{14+20} \quad P(\text{“fun”}|+) = \frac{1+1}{9+20}$$

For the test sentence $S = \text{“predictable with no fun”}$, after removing the word ‘with’, the chosen class, via Eq. 4.9, is therefore computed as follows:

$$P(-)P(S|-) = \frac{3}{5} \times \frac{2 \times 2 \times 1}{343} = 6.1 \times 10^{-5}$$

$$P(+)P(S|+) = \frac{2}{5} \times \frac{1 \times 1 \times 2}{293} = 3.2 \times 10^{-5}$$

The model thus predicts the class negative for the test sentence.

4.4 Optimizing for Sentiment Analysis

While standard naive Bayes text classification can work well for sentiment analysis, some small changes are generally employed that improve performance.

First, for sentiment classification and a number of other text classification tasks, whether a word occurs or not seems to matter more than its frequency. Thus it often improves performance to clip the word counts in each document at 1 (see the end
of the chapter for pointers to these results). This variant is called binary multinomial naive Bayes or binary naive Bayes. The variant uses the same algorithm as in Fig. 4.2 except that for each document we remove all duplicate words before concatenating them into the single big document during training and we also remove duplicate words from test documents. Fig. 4.3 shows an example in which a set of four documents (shortened and text-normalized for this example) are remapped to binary, with the modified counts shown in the table on the right. The example is worked without add-1 smoothing to make the differences clearer. Note that the results counts need not be 1; the word great has a count of 2 even for binary naive Bayes, because it appears in multiple documents.

<table>
<thead>
<tr>
<th>Four original documents:</th>
<th>NB Counts</th>
<th>Binary Counts</th>
</tr>
</thead>
<tbody>
<tr>
<td>− it was pathetic the worst part was the boxing scenes</td>
<td>+ 2</td>
<td>− 0</td>
</tr>
<tr>
<td>− no plot twists or great scenes</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
<tr>
<td>+ and satire and great plot twists</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
<tr>
<td>+ great scenes great film</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
<tr>
<td>After per-document binarization:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>− it was pathetic the worst part boxing scenes</td>
<td>+ 2</td>
<td>− 0</td>
</tr>
<tr>
<td>− no plot twists or great scenes</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
<tr>
<td>+ and satire great plot twists</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
<tr>
<td>+ great scenes film</td>
<td>+ 1</td>
<td>− 0</td>
</tr>
</tbody>
</table>

| and | 2 | 0 | 1 | 0 |
| boxing | 0 | 1 | 0 | 1 |
| film | 1 | 0 | 1 | 0 |
| great | 3 | 1 | 2 | 1 |
| it | 0 | 1 | 0 | 1 |
| no | 0 | 1 | 0 | 1 |
| or | 0 | 1 | 0 | 1 |
| part | 0 | 1 | 0 | 1 |
| pathetic | 0 | 1 | 0 | 1 |
| plot | 1 | 1 | 1 | 1 |
| satire | 1 | 0 | 1 | 0 |
| scenes | 1 | 2 | 1 | 2 |
| the | 0 | 2 | 0 | 1 |
| twists | 1 | 1 | 1 | 1 |
| was | 0 | 2 | 0 | 1 |
| worst | 0 | 1 | 0 | 1 |

Figure 4.3  An example of binarization for the binary naive Bayes algorithm.

A second important addition commonly made when doing text classification for sentiment is to deal with negation. Consider the difference between I really like this movie (positive) and I didn’t like this movie (negative). The negation expressed by didn’t completely alters the inferences we draw from the predicate like. Similarly, negation can modify a negative word to produce a positive review (don’t dismiss this film, doesn’t let us get bored).

A very simple baseline that is commonly used in sentiment analysis to deal with negation is the following: during text normalization, prepend the prefix NOT_ to every word after a token of logical negation (n’t, not, no, never) until the next punctuation mark. Thus the phrase

didn’t like this movie, but I

becomes

didn’t NOT_like NOT_this NOT_movie, but I

Newly formed ‘words’ like NOT_like, NOT_recommend will thus occur more often in negative document and act as cues for negative sentiment, while words like NOT_bored, NOT_dismiss will acquire positive associations. We will return in Chapter 20 to the use of parsing to deal more accurately with the scope relationship between these negation words and the predicates they modify, but this simple baseline works quite well in practice.
Finally, in some situations we might have insufficient labeled training data to train accurate naive Bayes classifiers using all words in the training set to estimate positive and negative sentiment. In such cases we can instead derive the positive and negative word features from **sentiment lexicons**, lists of words that are pre-annotated with positive or negative sentiment. Four popular lexicons are the **General Inquirer** (Stone et al., 1966), **LIWC** (Pennebaker et al., 2007), the opinion lexicon of Hu and Liu (2004a) and the MPQA Subjectivity Lexicon (Wilson et al., 2005).

For example the MPQA subjectivity lexicon has 6885 words each marked for whether it is strongly or weakly biased positive or negative. Some examples:

- **+**: admirable, beautiful, confident, dazzling, ecstatic, favor, glee, great
- **−**: awful, bad, bias, catastrophe, cheat, deny, envious, foul, harsh, hate

A common way to use lexicons in a naive Bayes classifier is to add a feature that is counted whenever a word from that lexicon occurs. Thus we might add a feature called ‘this word occurs in the positive lexicon’, and treat all instances of words in the lexicon as counts for that one feature, instead of counting each word separately. Similarly, we might add as a second feature ‘this word occurs in the negative lexicon’ of words in the negative lexicon. If we have lots of training data, and if the test data matches the training data, using just two features won’t work as well as using all the words. But when training data is sparse or not representative of the test set, using dense lexicon features instead of sparse individual-word features may generalize better.

We’ll return to this use of lexicons in Chapter 25, showing how these lexicons can be learned automatically, and how they can be applied to many other tasks beyond sentiment classification.

### 4.5 Naive Bayes for other text classification tasks

In the previous section we pointed out that naive Bayes doesn’t require that our classifier use all the words in the training data as features. In fact features in naive Bayes can express any property of the input text we want.

Consider the task of **spam detection**, deciding if a particular piece of email is an example of spam (unsolicited bulk email)—one of the first applications of naive Bayes to text classification (Sahami et al., 1998).

A common solution here, rather than using all the words as individual features, is to predefine likely sets of words or phrases as features, combined with features that are not purely linguistic. For example the open-source SpamAssassin tool\(^2\) predefines features like the phrase “one hundred percent guaranteed”, or the feature mentions millions of dollars, which is a regular expression that matches suspiciously large sums of money. But it also includes features like **HTML has a low ratio of text to image area**, that aren’t purely linguistic and might require some sophisticated computation, or totally non-linguistic features about, say, the path that the email took to arrive. More sample SpamAssassin features:

- Email subject line is all capital letters
- Contains phrases of urgency like “urgent reply”
- Email subject line contains “online pharmaceutical”
- HTML has unbalanced “head” tags

\(^2\) [https://spamassassin.apache.org](https://spamassassin.apache.org)
4.6 Naive Bayes as a Language Model

As we saw in the previous section, naive Bayes classifiers can use any sort of feature: dictionaries, URLs, email addresses, network features, phrases, and so on. But if, as in the previous section, we use only individual word features, and we use all of the words in the text (not a subset), then naive Bayes has an important similarity to language modeling. Specifically, a naive Bayes model can be viewed as a set of class-specific unigram language models, in which the model for each class instantiates a unigram language model.

Since the likelihood features from the naive Bayes model assign a probability to each word $P(\text{word}|c)$, the model also assigns a probability to each sentence:

$$P(s|c) = \prod_{i:\text{positions}} P(w_i|c)$$

(4.15)

Thus consider a naive Bayes model with the classes positive (+) and negative (-) and the following model parameters:

| w  | $P(w|+)$ | $P(w|-)$ |
|----|----------|----------|
| I  | 0.1      | 0.2      |
| love | 0.1     | 0.001    |
| this | 0.01    | 0.01     |
| fun | 0.05    | 0.005    |
| film | 0.1     | 0.1      |
| ... | ...     | ...      |

Each of the two columns above instantiates a language model that can assign a probability to the sentence “I love this fun film”:

$$P(\text{“I love this fun film”}|+) = 0.1 \times 0.1 \times 0.01 \times 0.05 \times 0.1 = 0.0000005$$

$$P(\text{“I love this fun film”}|-) = 0.2 \times 0.001 \times 0.01 \times 0.005 \times 0.1 = 0.00000001$$
As it happens, the positive model assigns a higher probability to the sentence: \( P(x|\text{pos}) > P(x|\text{neg}) \). Note that this is just the likelihood part of the naive Bayes model; once we multiply in the prior a full naive Bayes model might well make a different classification decision.

### 4.7 Evaluation: Precision, Recall, F-measure

To introduce the methods for evaluating text classification, let’s first consider some simple binary detection tasks. For example, in spam detection, our goal is to label every text as being in the spam category (“positive”) or not in the spam category (“negative”). For each item (email document) we therefore need to know whether our system called it spam or not. We also need to know whether the email is actually spam or not, i.e. the human-defined labels for each document that we are trying to match. We will refer to these human labels as the gold labels.

Or imagine you’re the CEO of the Delicious Pie Company and you need to know what people are saying about your pies on social media, so you build a system that detects tweets concerning Delicious Pie. Here the positive class is tweets about Delicious Pie and the negative class is all other tweets.

In both cases, we need a metric for knowing how well our spam detector (or pie-tweet-detector) is doing. To evaluate any system for detecting things, we start by building a confusion matrix like the one shown in Fig. 4.4. A confusion matrix is a table for visualizing how an algorithm performs with respect to the human gold labels, using two dimensions (system output and gold labels), and each cell labeling a set of possible outcomes. In the spam detection case, for example, true positives are documents that are indeed spam (indicated by human-created gold labels) that our system correctly said were spam. False negatives are documents that are indeed spam but our system incorrectly labeled as non-spam.

To the bottom right of the table is the equation for accuracy, which asks what percentage of all the observations (for the spam or pie examples that means all emails or tweets) our system labeled correctly. Although accuracy might seem a natural metric, we generally don’t use it for text classification tasks. That’s because accuracy doesn’t work well when the classes are unbalanced (as indeed they are with spam, which is a large majority of email, or with tweets, which are mainly not about pie).

- **true positive**
- **false positive**
- **false negative**
- **true negative**

\[
\text{precision} = \frac{tp}{tp+fp} \\
\text{accuracy} = \frac{tp+tn}{tp+fp+tn+fn} \\
\text{recall} = \frac{tp}{tp+fn}
\]

<table>
<thead>
<tr>
<th>gold standard labels</th>
<th>system output labels</th>
</tr>
</thead>
<tbody>
<tr>
<td>gold positive</td>
<td>system positive</td>
</tr>
<tr>
<td>gold negative</td>
<td>system negative</td>
</tr>
<tr>
<td>true positive</td>
<td>false positive</td>
</tr>
<tr>
<td>false negative</td>
<td>true negative</td>
</tr>
</tbody>
</table>

Figure 4.4 A confusion matrix for visualizing how well a binary classification system performs against gold standard labels.

To make this more explicit, imagine that we looked at a million tweets, and let’s say that only 100 of them are discussing their love (or hatred) for our pie,
while the other 999,900 are tweets about something completely unrelated. Imagine a simple classifier that stupidly classified every tweet as “not about pie”. This classifier would have 999,900 true negatives and only 100 false negatives for an accuracy of 999,900/1,000,000 or 99.99%! What an amazing accuracy level! Surely we should be happy with this classifier? But of course this fabulous ‘no pie’ classifier would be completely useless, since it wouldn’t find a single one of the customer comments we are looking for. In other words, accuracy is not a good metric when the goal is to discover something that is rare, or at least not completely balanced in frequency, which is a very common situation in the world.

That’s why instead of accuracy we generally turn to two other metrics shown in Fig. 4.4: precision and recall. Precision measures the percentage of the items that the system detected (i.e., the system labeled as positive) that are in fact positive (i.e., are positive according to the human gold labels). Precision is defined as

\[
\text{Precision} = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}
\]

Recall measures the percentage of items actually present in the input that were correctly identified by the system. Recall is defined as

\[
\text{Recall} = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}
\]

Precision and recall will help solve the problem with the useless “nothing is pie” classifier. This classifier, despite having a fabulous accuracy of 99.99%, has a terrible recall of 0 (since there are no true positives, and 100 false negatives, the recall is 0/100). You should convince yourself that the precision at finding relevant tweets is equally problematic. Thus precision and recall, unlike accuracy, emphasize true positives: finding the things that we are supposed to be looking for.

There are many ways to define a single metric that incorporates aspects of both precision and recall. The simplest of these combinations is the F-measure (van Rijsbergen, 1975), defined as:

\[
F_\beta = \frac{(\beta^2 + 1)PR}{\beta^2P + R}
\]

The \( \beta \) parameter differentially weights the importance of recall and precision, based perhaps on the needs of an application. Values of \( \beta > 1 \) favor recall, while values of \( \beta < 1 \) favor precision. When \( \beta = 1 \), precision and recall are equally balanced; this is the most frequently used metric, and is called \( F_{\beta=1} \) or just \( F_1 \):

\[
F_1 = \frac{2PR}{P + R}
\]

F-measure comes from a weighted harmonic mean of precision and recall. The harmonic mean of a set of numbers is the reciprocal of the arithmetic mean of reciprocals:

\[
\text{HarmonicMean}(a_1, a_2, a_3, a_4, \ldots, a_n) = \frac{n}{\frac{1}{a_1} + \frac{1}{a_2} + \frac{1}{a_3} + \ldots + \frac{1}{a_n}}
\]

and hence F-measure is

\[
F = \frac{1}{\alpha \frac{1}{P} + (1-\alpha) \frac{1}{R}} \quad \text{or} \quad \left(\text{with } \beta^2 = \frac{1-\alpha}{\alpha}\right) \quad F = \frac{(\beta^2 + 1)PR}{\beta^2P + R}
\]
Harmonic mean is used because the harmonic mean of two values is closer to the minimum of the two values than the arithmetic mean is. Thus it weighs the lower of the two numbers more heavily, which is more conservative in this situation.

### 4.7.1 Evaluating with more than two classes

Up to now we have been describing text classification tasks with only two classes. But lots of classification tasks in language processing have more than two classes. For sentiment analysis we generally have 3 classes (positive, negative, neutral) and even more classes are common for tasks like part-of-speech tagging, word sense disambiguation, semantic role labeling, emotion detection, and so on. Luckily the naive Bayes algorithm is already a multi-class classification algorithm.

![Confusion matrix for a three-class categorization task](image)

**Figure 4.5** Confusion matrix for a three-class categorization task, showing for each pair of classes \((c_1, c_2)\), how many documents from \(c_1\) were (in)correctly assigned to \(c_2\).

But we’ll need to slightly modify our definitions of precision and recall. Consider the sample confusion matrix for a hypothetical 3-way one-of email categorization decision (urgent, normal, spam) shown in Fig. 4.5. The matrix shows, for example, that the system mistakenly labeled one spam document as urgent, and we have shown how to compute a distinct precision and recall value for each class. In order to derive a single metric that tells us how well the system is doing, we can combine these values in two ways. In macroaveraging, we compute the performance for each class, and then average over classes. In microaveraging, we collect the decisions for all classes into a single confusion matrix, and then compute precision and recall from that table. Fig. 4.6 shows the confusion matrix for each class separately, and shows the computation of microaveraged and macroaveraged precision.

As the figure shows, a microaverage is dominated by the more frequent class (in this case spam), since the counts are pooled. The macroaverage better reflects the statistics of the smaller classes, and so is more appropriate when performance on all the classes is equally important.

### 4.8 Test sets and Cross-validation

The training and testing procedure for text classification follows what we saw with language modeling (Section 3.2): we use the training set to train the model, then use the development test set (also called a devset) to perhaps tune some parameters,
4.9 Statistical Significance Testing

In building systems we often need to compare the performance of two systems. How can we know if the new system we just built is better than our old one? Or better than some other system described in the literature? This is the domain of statistical hypothesis testing, and in this section we introduce tests for statistical significance for NLP classifiers, drawing especially on the work of Dror et al. (2020) and Berg-Kirkpatrick et al. (2012).

Suppose we’re comparing the performance of classifiers $A$ and $B$ on a metric $M$ and in general decide what the best model is. Once we come up with what we think is the best model, we run it on the (hitherto unseen) test set to report its performance.

While the use of a devset avoids overfitting the test set, having a fixed training set, devset, and test set creates another problem: in order to save lots of data for training, the test set (or devset) might not be large enough to be representative. Wouldn’t it be better if we could somehow use all our data for training and still use all our data for test? We can do this by cross-validation.

In cross-validation, we choose a number $k$, and partition our data into $k$ disjoint subsets called folds. Now we choose one of those $k$ folds as a test set, train our classifier on the remaining $k - 1$ folds, and then compute the error rate on the test set. Then we repeat with another fold as the test set, again training on the other $k - 1$ folds. We do this sampling process $k$ times and average the test set error rate from these $k$ runs to get an average error rate. If we choose $k = 10$, we would train 10 different models (each on 90% of our data), test the model 10 times, and average these 10 values. This is called 10-fold cross-validation.

The only problem with cross-validation is that because all the data is used for testing, we need the whole corpus to be blind; we can’t examine any of the data to suggest possible features and in general see what’s going on, because we’d be peeking at the test set, and such cheating would cause us to overestimate the performance of our system. However, looking at the corpus to understand what’s going on is important in designing NLP systems! What to do? For this reason, it is common to create a fixed training set and test set, then do 10-fold cross-validation inside the training set, but compute error rate the normal way in the test set, as shown in Fig. 4.7.

### Figure 4.6
Separate confusion matrices for the 3 classes from the previous figure, showing the pooled confusion matrix and the microaveraged and macroaveraged precision.
such as F1, or accuracy. Perhaps we want to know if our logistic regression sentiment classifier \( A \) (Chapter 5) gets a higher F1 score than our naive Bayes classifier \( B \) on a particular test set \( x \). Let’s call \( M(A,x) \) the score that system \( A \) gets on test set \( x \), and \( \delta(x) \) the performance difference between \( A \) and \( B \) on \( x \):

\[
\delta(x) = M(A,x) - M(B,x)
\]  

We would like to know if \( \delta(x) > 0 \), meaning that our logistic regression classifier has a higher F1 than our naive Bayes classifier on \( x \). \( \delta(x) \) is called the **effect size**; a bigger \( \delta \) means that \( A \) seems to be way better than \( B \); a small \( \delta \) means \( A \) seems to be only a little better.

Why don’t we just check if \( \delta(x) \) is positive? Suppose we do, and we find that the F1 score of \( A \) is higher than \( B \)’s by .04. Can we be certain that \( A \) is better? We cannot! That’s because \( A \) might just be accidentally better than \( B \) on this particular \( x \). We need something more: we want to know if \( A \)’s superiority over \( B \) is likely to hold again if we checked another test set \( x’ \), or under some other set of circumstances.

In the paradigm of statistical hypothesis testing, we test this by formalizing two hypotheses.

\[
H_0 : \delta(x) \leq 0 \\
H_1 : \delta(x) > 0
\]  

The hypothesis \( H_0 \), called the **null hypothesis**, supposes that \( \delta(x) \) is actually negative or zero, meaning that \( A \) is not better than \( B \). We would like to know if we can confidently rule out this hypothesis, and instead support \( H_1 \), that \( A \) is better.

We do this by creating a random variable \( X \) ranging over all test sets. Now we ask how likely is it, if the null hypothesis \( H_0 \) was correct, that among these test sets we would encounter the value of \( \delta(x) \) that we found, if we repeated the experiment a great many times. We formalize this likelihood as the **p-value**: the probability, assuming the null hypothesis \( H_0 \) is true, of seeing the \( \delta(x) \) that we saw or one even greater

\[
P(\delta(X) \geq \delta(x)|H_0 \text{ is true})
\]  

So in our example, this p-value is the probability that we would see \( \delta(x) \) assuming \( A \) is not better than \( B \). If \( \delta(x) \) is huge (let’s say \( A \) has a very respectable F1 of .9 and \( B \) has a terrible F1 of only .2 on \( x \)), we might be surprised, since that would be
extremely unlikely to occur if \( H_0 \) were in fact true, and so the p-value would be low (unlikely to have such a large \( \delta \) if \( A \) is in fact not better than \( B \)). But if \( \delta(x) \) is very small, it might be less surprising to us even if \( H_0 \) were true and \( A \) is not really better than \( B \), and so the p-value would be higher.

A very small p-value means that the difference we observed is very unlikely under the null hypothesis, and we can reject the null hypothesis. What counts as very small? It is common to use values like .05 or .01 as the thresholds. A value of .01 means that if the p-value (the probability of observing the \( \delta \) we saw assuming \( H_0 \) is true) is less than .01, we reject the null hypothesis and assume that \( A \) is indeed better than \( B \). We say that a result (e.g., “\( A \) is better than \( B \)” is statistically significant if the \( \delta \) we saw has a probability that is below the threshold and we therefore reject this null hypothesis.

How do we compute this probability we need for the p-value? In NLP we generally don’t use simple parametric tests like t-tests or ANOVAs that you might be familiar with. Parametric tests make assumptions about the distributions of the test statistic (such as normality) that don’t generally hold in our cases. So in NLP we usually use non-parametric tests based on sampling: we artificially create many versions of the experimental setup. For example, if we had lots of different test sets \( x' \) we could just measure all the \( \delta(x') \) for all the \( x' \). That gives us a distribution. Now we set a threshold (like .01) and if we see in this distribution that 99% or more of those deltas are smaller than the delta we observed, i.e., that p-value(\( x \))—the probability of seeing a \( \delta(x) \) as big as the one we saw—is less than .01, then we can reject the null hypothesis and agree that \( \delta(x) \) was a sufficiently surprising difference and \( A \) is really a better algorithm than \( B \).

There are two common non-parametric tests used in NLP: approximate randomization (Noreen, 1989) and the bootstrap test. We will describe bootstrap below, showing the paired version of the test, which again is most common in NLP. Paired tests are those in which we compare two sets of observations that are aligned: each observation in one set can be paired with an observation in another. This happens naturally when we are comparing the performance of two systems on the same test set; we can pair the performance of system \( A \) on an individual observation \( x_i \) with the performance of system \( B \) on the same \( x_i \).

### 4.9.1 The Paired Bootstrap Test

The bootstrap test (Efron and Tibshirani, 1993) can apply to any metric; from precision, recall, or F1 to the BLEU metric used in machine translation. The word bootstrapping refers to repeatedly drawing large numbers of samples with replacement (called bootstrap samples) from an original set. The intuition of the bootstrap test is that we can create many virtual test sets from an observed test set by repeatedly sampling from it. The method only makes the assumption that the sample is representative of the population.

Consider a tiny text classification example with a test set \( x \) of 10 documents. The first row of Fig. 4.8 shows the results of two classifiers (\( A \) and \( B \)) on this test set, with each document labeled by one of the four possibilities: (\( A \) and \( B \) both right, both wrong, \( A \) right and \( B \) wrong, \( A \) wrong and \( B \) right); a slash through a letter (\( B \)) means that that classifier got the answer wrong. On the first document both \( A \) and \( B \) get the correct class (\( AB \)), while on the second document \( A \) got it right but \( B \) got it wrong (\( AB \)). If we assume for simplicity that our metric is accuracy, \( A \) has an accuracy of .70 and \( B \) of .50, so \( \delta(x) \) is .20.

Now we create a large number \( b \) (perhaps \( 10^5 \)) of virtual test sets \( x^{(i)} \), each of size
\( n = 10 \). Fig. 4.8 shows a couple of examples. To create each virtual test set \( x^{(i)} \), we repeatedly (\( n = 10 \) times) select a cell from row \( x \) with replacement. For example, to create the first cell of the first virtual test set \( x^{(1)} \), if we happened to randomly select the second cell of the \( x \) row; we would copy the value \( AB \) into our new cell, and move on to create the second cell of \( x^{(1)} \), each time sampling (randomly choosing) from the original \( x \) with replacement.

<table>
<thead>
<tr>
<th>( x )</th>
<th>( x^{(1)} )</th>
<th>( x^{(2)} )</th>
<th>( x^{(b)} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( AB )</td>
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<td>( AB )</td>
<td>( AB )</td>
<td>( AB )</td>
<td>( AB )</td>
</tr>
</tbody>
</table>

**Figure 4.8** The paired bootstrap test: Examples of \( b \) pseudo test sets \( x^{(i)} \) being created from an initial true test set \( x \). Each pseudo test set is created by sampling \( n = 10 \) times with replacement; thus an individual sample is a single cell, a document with its gold label and the correct or incorrect performance of classifiers A and B. Of course real test sets don’t have only 10 examples, and \( b \) needs to be large as well.

Now that we have the \( b \) test sets, providing a sampling distribution, we can do statistics on how often A has an accidental advantage. There are various ways to compute this advantage: here we follow the version laid out in Berg-Kirkpatrick et al. (2012). Assuming \( H_0 \) (\( A \) isn’t better than \( B \)), we would expect that \( \delta(X) \), estimated over many test sets, would be zero; a much higher value would be surprising, since \( H_0 \) specifically assumes \( A \) isn’t better than \( B \). To measure exactly how surprising our observed \( \delta(x) \) is, we would in other circumstances compute the p-value by counting over many test sets how often \( \delta(x^{(i)}) \) exceeds the expected zero value by \( \delta(x) \) or more:

\[
p\text{-value}(x) = \frac{1}{b} \sum_{i=1}^{b} \mathbb{1}(\delta(x^{(i)}) - \delta(x) \geq 0)
\]

(We use the notation \( \mathbb{1}(x) \) to mean “1 if \( x \) is true, and 0 otherwise”.) However, although it’s generally true that the expected value of \( \delta(X) \) over many test sets, (again assuming \( A \) isn’t better than \( B \)) is 0, this isn’t true for the bootstrapped test sets we created. That’s because we didn’t draw these samples from a distribution with 0 mean; we happened to create them from the original test set \( x \), which happens to be biased (by \( .20 \)) in favor of \( A \). So to measure how surprising is our observed \( \delta(x) \), we actually compute the p-value by counting over many test sets how often \( \delta(x^{(i)}) \) exceeds the expected value of \( \delta(x) \) by \( \delta(x) \) or more:

\[
p\text{-value}(x) = \frac{1}{b} \sum_{i=1}^{b} \mathbb{1}(\delta(x^{(i)}) - \delta(x) \geq \delta(x)) = \frac{1}{b} \sum_{i=1}^{b} \mathbb{1}(\delta(x^{(i)}) \geq 2\delta(x)) \] (4.22)

So if for example we have 10,000 test sets \( x^{(i)} \) and a threshold of .01, and in only 47 of the test sets do we find that \( A \) is accidentally better \( \delta(x^{(i)}) \geq 2\delta(x) \), the resulting p-value of .0047 is smaller than .01, indicating that the delta we found, \( \delta(x) \) is indeed
sufficiently surprising and unlikely to have happened by accident, and we can reject the null hypothesis and conclude $A$ is better than $B$.

```
function Bootstrap(test set $x$, num of samples $b$) returns $p$-value($x$)

Calculate $\delta(x)$  # how much better does algorithm A do than B on $x$
$s = 0$
for $i = 1$ to $b$
    for $j = 1$ to $n$
        # Draw a bootstrap sample $x^{(i)}$ of size $n$
        Select a member of $x$ at random and add it to $x^{(i)}$
        Calculate $\delta(x^{(i)})$  # how much better does algorithm A do than B on $x^{(i)}$
        $s \leftarrow s + 1$ if $\delta(x^{(i)}) \geq 2\delta(x)$

$p$-value($x$) $\approx \frac{s}{b}$  # on what % of the b samples did algorithm A beat expectations?
return $p$-value($x$)  # if very few did, our observed $\delta$ is probably not accidental
```

Figure 4.9  A version of the paired bootstrap algorithm after Berg-Kirkpatrick et al. (2012).

The full algorithm for the bootstrap is shown in Fig. 4.9. It is given a test set $x$, a number of samples $b$, and counts the percentage of the $b$ bootstrap test sets in which $\delta(x^{(i)}) > 2\delta(x)$. This percentage then acts as a one-sided empirical $p$-value.

4.10 Avoiding Harms in Classification

It is important to avoid harms that may result from classifiers, harms that exist both for naive Bayes classifiers and for the other classification algorithms we introduce in later chapters.

One class of harms is **representational harms** (Crawford 2017, Blodgett et al. 2020), harms caused by a system that demeans a social group, for example by perpetuating negative stereotypes about them. For example Kiritchenko and Moham-mad (2018) examined the performance of 200 sentiment analysis systems on pairs of sentences that were identical except for containing either a common African American first name (like Shaniqua) or a common European American first name (like Stephanie), chosen from the Caliskan et al. (2017) study discussed in Chapter 6. They found that most systems assigned lower sentiment and more negative emotion to sentences with African American names, reflecting and perpetuating stereotypes that associate African Americans with negative emotions (Popp et al., 2003).

In other tasks classifiers may lead to both representational harms and other harms, such as censorship. For example the important text classification task of **toxicity detection** is the task of detecting hate speech, abuse, harassment, or other kinds of toxic language. While the goal of such classifiers is to help reduce societal harm, toxicity classifiers can themselves cause harms. For example, researchers have shown that some widely used toxicity classifiers incorrectly flag as being toxic sentences that are non-toxic but simply mention minority identities like women (Park et al., 2018), blind people (Hutchinson et al., 2020) or gay people (Dixon et al., 2018; Dias Oliva et al., 2021), or simply use linguistic features characteristic of varieties like African-American Vernacular English (Sap et al. 2019, Davidson et al. 2019). Such false positive errors, if employed by toxicity detection systems without human oversight, could lead to the censoring of discourse by or about these groups.

These model problems can be caused by biases or other problems in the training
data; in general, machine learning systems replicate and even amplify the biases in their training data. But these problems can also be caused by the labels (for example due to biases in the human labelers), by the resources used (like lexicons, or model components like pretrained embeddings), or even by model architecture (like what the model is trained to optimize). While the mitigation of these biases (for example by carefully considering the training data sources) is an important area of research, we currently don’t have general solutions. For this reason it’s important, when introducing any NLP model, to study these kinds of factors and make them clear. One way to do this is by releasing a model card (Mitchell et al., 2019) for each version of a model. A model card documents a machine learning model with information like:

- training algorithms and parameters
- training data sources, motivation, and preprocessing
- evaluation data sources, motivation, and preprocessing
- intended use and users
- model performance across different demographic or other groups and environmental situations

4.11 Summary

This chapter introduced the naive Bayes model for classification and applied it to the text categorization task of sentiment analysis.

- Many language processing tasks can be viewed as tasks of classification.
- Text categorization, in which an entire text is assigned a class from a finite set, includes such tasks as sentiment analysis, spam detection, language identification, and authorship attribution.
- Sentiment analysis classifies a text as reflecting the positive or negative orientation (sentiment) that a writer expresses toward some object.
- Naive Bayes is a generative model that makes the bag-of-words assumption (position doesn’t matter) and the conditional independence assumption (words are conditionally independent of each other given the class).
- Naive Bayes with binarized features seems to work better for many text classification tasks.
- Classifiers are evaluated based on precision and recall.
- Classifiers are trained using distinct training, dev, and test sets, including the use of cross-validation in the training set.
- Statistical significance tests should be used to determine whether we can be confident that one version of a classifier is better than another.
- Designers of classifiers should carefully consider harms that may be caused by the model, including its training data and other components, and report model characteristics in a model card.

Bibliographical and Historical Notes

Multinomial naive Bayes text classification was proposed by Maron (1961) at the RAND Corporation for the task of assigning subject categories to journal abstracts.
His model introduced most of the features of the modern form presented here, approximating the classification task with one-of categorization, and implementing add-δ smoothing and information-based feature selection.

The conditional independence assumptions of naive Bayes and the idea of Bayesian analysis of text seems to have arisen multiple times. The same year as Maron’s paper, Minsky (1961) proposed a naive Bayes classifier for vision and other artificial intelligence problems, and Bayesian techniques were also applied to the text classification task of authorship attribution by Mosteller and Wallace (1963). It had long been known that Alexander Hamilton, John Jay, and James Madison wrote the anonymously-published *Federalist* papers in 1787–1788 to persuade New York to ratify the United States Constitution. Yet although some of the 85 essays were clearly attributable to one author or another, the authorship of 12 were in dispute between Hamilton and Madison. Mosteller and Wallace (1963) trained a Bayesian probabilistic model of the writing of Hamilton and another model on the writings of Madison, then computed the maximum-likelihood author for each of the disputed essays. Naive Bayes was first applied to spam detection in Heckerman et al. (1998). Metsis et al. (2006), Pang et al. (2002), and Wang and Manning (2012) show that using boolean attributes with multinomial naive Bayes works better than full counts. Binary multinomial naive Bayes is sometimes confused with another variant of naive Bayes that also uses a binary representation of whether a term occurs in a document: **Multivariate Bernoulli naive Bayes**. The Bernoulli variant instead estimates $P(w|c)$ as the fraction of documents that contain a term, and includes a probability for whether a term is not in a document. McCallum and Nigam (1998) and Wang and Manning (2012) show that the multivariate Bernoulli variant of naive Bayes doesn’t work as well as the multinomial algorithm for sentiment or other text tasks.

There are a variety of sources covering the many kinds of text classification tasks. For sentiment analysis see Pang and Lee (2008), and Liu and Zhang (2012). Stamatatos (2009) surveys authorship attribute algorithms. On language identification see Jauhiainen et al. (2019); Jaech et al. (2016) is an important early neural system. The task of newswire indexing was often used as a test case for text classification algorithms, based on the Reuters-21578 collection of newswire articles. See Manning et al. (2008) and Aggarwal and Zhai (2012) on text classification; classification in general is covered in machine learning textbooks (Hastie et al. 2001, Witten and Frank 2005, Bishop 2006, Murphy 2012).

Non-parametric methods for computing statistical significance were used first in NLP in the MUC competition (Chinchor et al., 1993), and even earlier in speech recognition (Gillick and Cox 1989, Bisani and Ney 2004). Our description of the bootstrap draws on the description in Berg-Kirkpatrick et al. (2012). Recent work has focused on issues including multiple test sets and multiple metrics (Søgaard et al. 2014, Dror et al. 2017).

Feature selection is a method of removing features that are unlikely to generalize well. Features are generally ranked by how informative they are about the classification decision. A very common metric, **information gain**, tells us how many bits of information the presence of the word gives us for guessing the class. Other feature selection metrics include $\chi^2$, pointwise mutual information, and GINI index; see Yang and Pedersen (1997) for a comparison and Guyon and Elisseeff (2003) for an introduction to feature selection.
Exercises

4.1 Assume the following likelihoods for each word being part of a positive or negative movie review, and equal prior probabilities for each class.

<table>
<thead>
<tr>
<th>Word</th>
<th>pos</th>
<th>neg</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>0.09</td>
<td>0.16</td>
</tr>
<tr>
<td>always</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>like</td>
<td>0.29</td>
<td>0.06</td>
</tr>
<tr>
<td>foreign</td>
<td>0.04</td>
<td>0.15</td>
</tr>
<tr>
<td>films</td>
<td>0.08</td>
<td>0.11</td>
</tr>
</tbody>
</table>

What class will Naive bayes assign to the sentence “I always like foreign films.”?

4.2 Given the following short movie reviews, each labeled with a genre, either comedy or action:

1. fun, couple, love, love  comedy
2. fast, furious, shoot  action
3. couple, fly, fast, fun, fun  comedy
4. furious, shoot, shoot, fun  action
5. fly, fast, shoot, love  action

and a new document D:

fast, couple, shoot, fly

compute the most likely class for D. Assume a naive Bayes classifier and use add-1 smoothing for the likelihoods.

4.3 Train two models, multinomial naive Bayes and binarized naive Bayes, both with add-1 smoothing, on the following document counts for key sentiment words, with positive or negative class assigned as noted.

<table>
<thead>
<tr>
<th>doc</th>
<th>“good”</th>
<th>“poor”</th>
<th>“great”</th>
<th>(class)</th>
</tr>
</thead>
<tbody>
<tr>
<td>d1.</td>
<td>3</td>
<td>0</td>
<td>3</td>
<td>pos</td>
</tr>
<tr>
<td>d2.</td>
<td>0</td>
<td>1</td>
<td>2</td>
<td>pos</td>
</tr>
<tr>
<td>d3.</td>
<td>1</td>
<td>3</td>
<td>0</td>
<td>neg</td>
</tr>
<tr>
<td>d4.</td>
<td>1</td>
<td>5</td>
<td>2</td>
<td>neg</td>
</tr>
<tr>
<td>d5.</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>neg</td>
</tr>
</tbody>
</table>

Use both naive Bayes models to assign a class (pos or neg) to this sentence:

A good, good plot and great characters, but poor acting.

Recall from page 65 that with naive Bayes text classification, we simply ignore (throw out) any word that never occurred in the training document. (We don’t throw out words that appear in some classes but not others; that’s what add-one smoothing is for.) Do the two models agree or disagree?
“And how do you know that these fine begonias are not of equal importance?”
Hercule Poirot, in Agatha Christie’s The Mysterious Affair at Styles

Detective stories are as littered with clues as texts are with words. Yet for the poor reader it can be challenging to know how to weigh the author’s clues in order to make the crucial classification task: deciding whodunnit.

In this chapter we introduce an algorithm that is admirably suited for discovering the link between features or cues and some particular outcome: **logistic regression**. Indeed, logistic regression is one of the most important analytic tools in the social and natural sciences. In natural language processing, logistic regression is the baseline supervised machine learning algorithm for classification, and also has a very close relationship with neural networks. As we will see in Chapter 7, a neural network can be viewed as a series of logistic regression classifiers stacked on top of each other. Thus the classification and machine learning techniques introduced here will play an important role throughout the book.

Logistic regression can be used to classify an observation into one of two classes (like ‘positive sentiment’ and ‘negative sentiment’), or into one of many classes. Because the mathematics for the two-class case is simpler, we’ll describe this special case of logistic regression first in the next few sections, and then briefly summarize the use of **multinomial logistic regression** for more than two classes in Section 5.3.

We’ll introduce the mathematics of logistic regression in the next few sections. But let’s begin with some high-level issues.

**Generative and Discriminative Classifiers:** The most important difference between naive Bayes and logistic regression is that logistic regression is a **discriminative** classifier while naive Bayes is a **generative** classifier.

These are two very different frameworks for how to build a machine learning model. Consider a visual metaphor: imagine we’re trying to distinguish dog images from cat images. A generative model would have the goal of understanding what dogs look like and what cats look like. You might literally ask such a model to ‘generate’, i.e., draw, a dog. Given a test image, the system then asks whether it’s the cat model or the dog model that better fits (is less surprised by) the image, and chooses that as its label.

A discriminative model, by contrast, is only trying to learn to distinguish the classes (perhaps without learning much about them). So maybe all the dogs in the training data are wearing collars and the cats aren’t. If that one feature neatly separates the classes, the model is satisfied. If you ask such a model what it knows about cats all it can say is that they don’t wear collars.
More formally, recall that the naive Bayes assigns a class \( c \) to a document \( d \) not by directly computing \( P(c|d) \) but by computing a likelihood and a prior

\[
\hat{c} = \arg\max_{c \in C} \frac{P(d|c)}{\hat{P}(c)}
\]

A generative model like naive Bayes makes use of this likelihood term, which expresses how to generate the features of a document if we knew it was of class \( c \).

By contrast a discriminative model in this text categorization scenario attempts to directly compute \( P(c|d) \). Perhaps it will learn to assign a high weight to document features that directly improve its ability to discriminate between possible classes, even if it couldn’t generate an example of one of the classes.

Components of a probabilistic machine learning classifier: Like naive Bayes, logistic regression is a probabilistic classifier that makes use of supervised machine learning. Machine learning classifiers require a training corpus of \( m \) input/output pairs \((x^{(i)}, y^{(i)})\). (We’ll use superscripts in parentheses to refer to individual instances in the training set—for sentiment classification each instance might be an individual document to be classified.) A machine learning system for classification then has four components:

1. A feature representation of the input. For each input observation \( x^{(i)} \), this will be a vector of features \([x_1, x_2, ..., x_n]\). We will generally refer to feature \( i \) for input \( x^{(i)} \) as \( x_i^{(i)} \), sometimes simplified as \( x_i \), but we will also see the notation \( f_i \), \( f_i(x) \), or, for multiclass classification, \( f_i(c, x) \).
2. A classification function that computes \( \hat{y} \), the estimated class, via \( p(y|x) \). In the next section we will introduce the sigmoid and softmax tools for classification.
3. An objective function for learning, usually involving minimizing error on training examples. We will introduce the cross-entropy loss function.
4. An algorithm for optimizing the objective function. We introduce the stochastic gradient descent algorithm.

Logistic regression has two phases:

training: We train the system (specifically the weights \( w \) and \( b \)) using stochastic gradient descent and the cross-entropy loss.

test: Given a test example \( x \) we compute \( p(y|x) \) and return the higher probability label \( y = 1 \) or \( y = 0 \).

5.1 The sigmoid function

The goal of binary logistic regression is to train a classifier that can make a binary decision about the class of a new input observation. Here we introduce the sigmoid classifier that will help us make this decision.

Consider a single input observation \( x \), which we will represent by a vector of features \([x_1, x_2, ..., x_n]\) (we’ll show sample features in the next subsection). The classifier output \( y \) can be 1 (meaning the observation is a member of the class) or 0 (the observation is not a member of the class). We want to know the probability \( P(y = 1|x) \) that this observation is a member of the class. So perhaps the decision is “positive
sentiment” versus “negative sentiment”, the features represent counts of words in a document, \( P(y = 1 | x) \) is the probability that the document has positive sentiment, and \( P(y = 0 | x) \) is the probability that the document has negative sentiment.

Logistic regression solves this task by learning, from a training set, a vector of **weights** and a **bias term**. Each weight \( w_i \) is a real number, and is associated with one of the input features \( x_i \). The weight \( w_i \) represents how important that input feature is to the classification decision, and can be positive (providing evidence that the instance being classified belongs in the positive class) or negative (providing evidence that the instance being classified belongs in the negative class). Thus we might expect in a sentiment task the word *awesome* to have a high positive weight, and *abysmal* to have a very negative weight. The **bias term**, also called the **intercept**, is another real number that’s added to the weighted inputs.

To make a decision on a test instance—after we’ve learned the weights in training—the classifier first multiplies each \( x_i \) by its weight \( w_i \), sums up the weighted features, and adds the bias term \( b \). The resulting single number \( z \) expresses the weighted sum of the evidence for the class.

\[
z = \left( \sum_{i=1}^{n} w_i x_i \right) + b \tag{5.2}
\]

In the rest of the book we’ll represent such sums using the **dot product** notation from linear algebra. The dot product of two vectors \( a \) and \( b \), written as \( a \cdot b \), is the sum of the products of the corresponding elements of each vector. (Notice that we represent vectors using the boldface notation \( \mathbf{b} \)). Thus the following is an equivalent formation to Eq. 5.2:

\[
z = \mathbf{w} \cdot \mathbf{x} + b \tag{5.3}
\]

But note that nothing in Eq. 5.3 forces \( z \) to be a legal probability, that is, to lie between 0 and 1. In fact, since weights are real-valued, the output might even be negative; \( z \) ranges from \(-\infty \) to \( \infty \).

To create a probability, we’ll pass \( z \) through the **sigmoid function**, \( \sigma(z) \). The sigmoid function (named because it looks like an \( s \)) is also called the **logistic function**, and gives logistic regression its name. The sigmoid has the following equation, shown graphically in Fig. 5.1:

\[
\sigma(z) = \frac{1}{1 + e^{-z}} \tag{5.4}
\]

(For the rest of the book, we’ll use the notation \( \exp(x) \) to mean \( e^x \).) The sigmoid has a number of advantages; it takes a real-valued number and maps it into the range **sigmoid function** **logistic function**
(0, 1), which is just what we want for a probability. Because it is nearly linear around 0 but flattens toward the ends, it tends to squash outlier values toward 0 or 1. And it’s differentiable, which as we’ll see in Section 5.10 will be handy for learning.

We’re almost there. If we apply the sigmoid to the sum of the weighted features, we get a number between 0 and 1. To make it a probability, we just need to make sure that the two cases, \( p(y = 1) \) and \( p(y = 0) \), sum to 1. We can do this as follows:

\[
P(y = 1) = \sigma(w \cdot x + b) = \frac{1}{1 + \exp(-(w \cdot x + b))}
\]

\[
P(y = 0) = 1 - \sigma(w \cdot x + b) = \frac{1 - 1}{1 + \exp(-(w \cdot x + b))} = \frac{\exp(-(w \cdot x + b))}{1 + \exp(-(w \cdot x + b))}
\]

The sigmoid function has the property

\[
1 - \sigma(x) = \sigma(-x)
\]

so we could also have expressed \( P(y = 0) \) as \( \sigma(-(w \cdot x + b)) \).

Finally, one terminological point. The input to the sigmoid function, the score \( z = w \cdot x + b \) from (5.3), is often called the logit. This is because the logit function is the inverse of the sigmoid. The logit function is the log of the odds ratio \( \frac{p}{1-p} \):

\[
\text{logit}(p) = \sigma^{-1}(p) = \ln \frac{p}{1-p}
\]

Using the term logit for \( z \) is a way of reminding us that by using the sigmoid to turn \( z \) (which ranges from \(-\infty\) to \(\infty\)) into a probability, we are implicitly interpreting \( z \) as not just any real-valued number, but as specifically a log odds.

## 5.2 Classification with Logistic Regression

The sigmoid function from the prior section thus gives us a way to take an instance \( x \) and compute the probability \( P(y = 1|x) \).

How do we make a decision about which class to apply to a test instance \( x \)? For a given \( x \), we say yes if the probability \( P(y = 1|x) \) is more than .5, and no otherwise. We call .5 the decision boundary:

\[
\text{decision}(x) = \begin{cases} 
1 & \text{if } P(y = 1|x) > 0.5 \\
0 & \text{otherwise}
\end{cases}
\]

Let’s have some examples of applying logistic regression as a classifier for language tasks.

### 5.2.1 Sentiment Classification

Suppose we are doing binary sentiment classification on movie review text, and we would like to know whether to assign the sentiment class + or − to a review
document \( \text{doc} \). We’ll represent each input observation by the 6 features \( x_1 \ldots x_6 \) of the input shown in the following table; Fig. 5.2 shows the features in a sample mini test document.

<table>
<thead>
<tr>
<th>Var</th>
<th>Definition</th>
<th>Value in Fig. 5.2</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x_1 )</td>
<td>count(positive lexicon words ( \in \text{doc} ))</td>
<td>3</td>
</tr>
<tr>
<td>( x_2 )</td>
<td>count(negative lexicon words ( \in \text{doc} ))</td>
<td>2</td>
</tr>
</tbody>
</table>
| \( x_3 \) | \( \begin{cases} 
1 & \text{if "no" \( \in \text{doc} \) } \\
0 & \text{otherwise}
\end{cases} \) | 1 |
| \( x_4 \) | count(1st and 2nd pronouns \( \in \text{doc} \)) | 3 |
| \( x_5 \) | \( \begin{cases} 
1 & \text{if "!" \( \in \text{doc} \) } \\
0 & \text{otherwise}
\end{cases} \) | 0 |
| \( x_6 \) | ln(word count of \( \text{doc} \)) | \( \ln(66) = 4.19 \) |

Let’s assume for the moment that we’ve already learned a real-valued weight for

\[ p(+|x) = P(y = 1|x) = \sigma(w \cdot x + b) \]

\[ = \sigma([2.5, -5.0, -1.2, 0.5, 2.0, 0.7] \cdot [3, 2, 1, 3, 0, 4.19] + 0.1) \]

\[ = \sigma(0.833) \]

\[ = 0.70 \]

\[ p(-|x) = P(y = 0|x) = 1 - \sigma(w \cdot x + b) \]

\[ = 0.30 \]

5.2.2 Other classification tasks and features

Logistic regression is commonly applied to all sorts of NLP tasks, and any property of the input can be a feature. Consider the task of \textit{period disambiguation}: deciding
if a period is the end of a sentence or part of a word, by classifying each period into one of two classes EOS (end-of-sentence) and not-EOS. We might use features like \( x_1 \) below expressing that the current word is lower case (perhaps with a positive weight), or that the current word is in our abbreviations dictionary (“Prof.”) (perhaps with a negative weight). A feature can also express a quite complex combination of properties. For example a period following an upper case word is likely to be an EOS, but if the word itself is St. and the previous word is capitalized, then the period is likely part of a shortening of the word street.

\[
x_1 = \begin{cases} 
1 & \text{if } "\text{Case}(w_i) = \text{Lower}" \\
0 & \text{otherwise}
\end{cases}
\]

\[
x_2 = \begin{cases} 
1 & \text{if } "w_i \in \text{AcronymDict}" \\
0 & \text{otherwise}
\end{cases}
\]

\[
x_3 = \begin{cases} 
1 & \text{if } "w_i = \text{St. } \& \text{Case}(w_{i-1}) = \text{Cap}" \\
0 & \text{otherwise}
\end{cases}
\]

**Designing features:** Features are generally designed by examining the training set with an eye to linguistic intuitions and the linguistic literature on the domain. A careful error analysis on the training set or devset of an early version of a system often provides insights into features.

For some tasks it is especially helpful to build complex features that are combinations of more primitive features. We saw such a feature for period disambiguation above, where a period on the word St. was less likely to be the end of the sentence if the previous word was capitalized. For logistic regression and na"ive Bayes these combination features or **feature interactions** have to be designed by hand.

For many tasks (especially when feature values can reference specific words) we’ll need large numbers of features. Often these are created automatically via **feature templates**, abstract specifications of features. For example a bigram template for period disambiguation might create a feature for every pair of words that occurs before a period in the training set. Thus the feature space is sparse, since we only have to create a feature if that n-gram exists in that position in the training set. The feature is generally created as a hash from the string descriptions. A user description of a feature as, “bigram(American breakfast)” is hashed into a unique integer \( i \) that becomes the feature number \( f_i \).

In order to avoid the extensive human effort of feature design, recent research in NLP has focused on **representation learning**: ways to learn features automatically in an unsupervised way from the input. We’ll introduce methods for representation learning in Chapter 6 and Chapter 7.

**Scaling input features:** When different input features have extremely different ranges of values, it’s common to rescale them so they have comparable ranges. We **standardize** input values by centering them to result in a zero mean and a standard deviation of one (this transformation is sometimes called the **z-score**). That is, if \( \mu_i \) is the mean of the values of feature \( x_i \) across the \( m \) observations in the input dataset, and \( \sigma_i \) is the standard deviation of the values of features \( x_i \) across the input dataset, we can replace each feature \( x_i \) by a new feature \( x'_i \) computed as follows:

\[
\mu_i = \frac{1}{m} \sum_{j=1}^{m} x_{i(j)} \quad \sigma_i = \sqrt{\frac{1}{m} \sum_{j=1}^{m} (x_{i(j)} - \mu_i)^2}
\]

\[
x'_i = \frac{x_i - \mu_i}{\sigma_i}
\] (5.9)
Alternatively, we can normalize the input features values to lie between 0 and 1:

\[ x'_i = \frac{x_i - \min(x_i)}{\max(x_i) - \min(x_i)} \]  

Having input data with comparable range is useful when comparing values across features. Data scaling is especially important in large neural networks, since it helps speed up gradient descent.

### 5.2.3 Processing many examples at once

We’ve shown the equations for logistic regression for a single example. But in practice we’ll of course want to process an entire test set with many examples. Let’s suppose we have a test set consisting of \( m \) test examples each of which we’d like to classify. We’ll continue to use the notation from page 82, in which a superscript value in parentheses refers to the example index in some set of data (either for training or for test). So in this case each test example \( x^{(i)} \) has a feature vector \( x^{(i)} \), \( 1 \leq i \leq m \). (As usual, we’ll represent vectors and matrices in bold.)

One way to compute each output value \( \hat{y}^{(i)} \) is just to have a for-loop, and compute each test example one at a time:

\[
\text{foreach } \ x^{(i)} \text{ in input } [x^{(1)}, x^{(2)}, \ldots, x^{(m)}] \\
\hat{y}^{(i)} = \sigma(w \cdot x^{(i)} + b) \tag{5.11}
\]

For the first 3 test examples, then, we would be separately computing the predicted \( \hat{y}^{(i)} \) as follows:

\[
\begin{align*}
P(y^{(1)} = 1|x^{(1)}) &= \sigma(w \cdot x^{(1)} + b) \\
P(y^{(2)} = 1|x^{(2)}) &= \sigma(w \cdot x^{(2)} + b) \\
P(y^{(3)} = 1|x^{(3)}) &= \sigma(w \cdot x^{(3)} + b)
\end{align*}
\]

But it turns out that we can slightly modify our original equation Eq. 5.5 to do this much more efficiently. We’ll use matrix arithmetic to assign a class to all the examples with one matrix operation!

First, we’ll pack all the input feature vectors for each input \( x \) into a single input matrix \( X \), where each row \( i \) is a row vector consisting of the feature vector for input example \( x^{(i)} \) (i.e., the vector \( x^{(i)} \)). Assuming each example has \( f \) features and weights, \( X \) will therefore be a matrix of shape \([m \times f]\), as follows:

\[
X = \begin{bmatrix}
x^{(1)}_1 & x^{(1)}_2 & \ldots & x^{(1)}_f \\
x^{(2)}_1 & x^{(2)}_2 & \ldots & x^{(2)}_f \\
x^{(3)}_1 & x^{(3)}_2 & \ldots & x^{(3)}_f \\
\vdots & \vdots & \ddots & \vdots 
\end{bmatrix} \tag{5.12}
\]

Now if we introduce \( b \) as a vector of length \( m \) which consists of the scalar bias term \( b \) repeated \( m \) times, \( b = [b, b, \ldots, b] \), and \( \hat{y} = [\hat{y}^{(1)}, \hat{y}^{(2)}, \ldots, \hat{y}^{(m)}] \) as the vector of outputs (one scalar \( \hat{y}^{(i)} \) for each input \( x^{(i)} \) and its feature vector \( x^{(i)} \)), and represent the weight vector \( w \) as a column vector, we can compute all the outputs with a single matrix multiplication and one addition:

\[
y = Xw + b \tag{5.13}
\]
You should convince yourself that Eq. 5.13 computes the same thing as our for-loop in Eq. 5.11. For example \( \hat{y}^{(1)} \), the first entry of the output vector \( y \), will correctly be:

\[
\hat{y}^{(1)} = [x_1^{(1)}, x_2^{(1)}, \ldots, x_f^{(1)}] \cdot [w_1, w_2, \ldots, w_f] + b \tag{5.14}
\]

Note that we had to reorder \( X \) and \( w \) from the order they appeared in in Eq. 5.5 to make the multiplications come out properly. Here is Eq. 5.13 again with the shapes shown:

\[
y = X \cdot w + b \hspace{1cm} (m \times 1) \hspace{1cm} (m \times f) \hspace{1cm} (f \times 1) \hspace{1cm} (m \times 1) \tag{5.15}
\]

Modern compilers and compute hardware can compute this matrix operation very efficiently, making the computation much faster, which becomes important when training or testing on very large datasets.

### 5.2.4 Choosing a classifier

Logistic regression has a number of advantages over naive Bayes. Naive Bayes has overly strong conditional independence assumptions. Consider two features which are strongly correlated; in fact, imagine that we just add the same feature \( f_1 \) twice. Naive Bayes will treat both copies of \( f_1 \) as if they were separate, multiplying them both in, overestimating the evidence. By contrast, logistic regression is much more robust to correlated features; if two features \( f_1 \) and \( f_2 \) are perfectly correlated, regression will simply assign part of the weight to \( w_1 \) and part to \( w_2 \). Thus when there are many correlated features, logistic regression will assign a more accurate probability than naive Bayes. So logistic regression generally works better on larger documents or datasets and is a common default.

Despite the less accurate probabilities, naive Bayes still often makes the correct classification decision. Furthermore, naive Bayes can work extremely well (sometimes even better than logistic regression) on very small datasets (Ng and Jordan, 2002) or short documents (Wang and Manning, 2012). Furthermore, naive Bayes is easy to implement and very fast to train (there’s no optimization step). So it’s still a reasonable approach to use in some situations.

### 5.3 Multinomial logistic regression

Sometimes we need more than two classes. Perhaps we might want to do 3-way sentiment classification (positive, negative, or neutral). Or we could be assigning some of the labels we will introduce in Chapter 8, like the part of speech of a word (choosing from 10, 30, or even 50 different parts of speech), or the named entity type of a phrase (choosing from tags like person, location, organization).

In such cases we use **multinomial logistic regression**, also called **softmax regression** (in older NLP literature you will sometimes see the name **maxent classifier**). In multinomial logistic regression we want to label each observation with a class \( k \) from a set of \( K \) classes, under the stipulation that only one of these classes is the correct one (sometimes called **hard classification**; an observation can not be in multiple classes). Let’s use the following representation: the output \( y \) for each input \( x \) will be a vector of length \( K \). If class \( c \) is the correct class, we’ll set \( y_c = 1 \), and set all the other elements of \( y \) to be 0, i.e., \( y_c = 1 \) and \( y_j = 0 \) \( \forall j \neq c \). A vector like
this $y$, with one value=1 and the rest 0, is called a one-hot vector. The job of the classifier is to produce an estimate vector $\hat{y}$. For each class $k$, the value $\hat{y}_k$ will be the classifier’s estimate of the probability $p(y_k = 1|x)$.

### 5.3.1 Softmax

The multinomial logistic classifier uses a generalization of the sigmoid, called the softmax function, to compute $p(y_k = 1|x)$. The softmax function takes a vector $z = [z_1, z_2, ..., z_K]$ of $K$ arbitrary values and maps them to a probability distribution, with each value in the range $[0,1]$, and all the values summing to 1. Like the sigmoid, it is an exponential function.

For a vector $z$ of dimensionality $K$, the softmax is defined as:

$$\text{softmax}(z) = \left[ \frac{\exp(z_1)}{\sum_{i=1}^{K} \exp(z_i)}, \frac{\exp(z_2)}{\sum_{i=1}^{K} \exp(z_i)}, ..., \frac{\exp(z_K)}{\sum_{i=1}^{K} \exp(z_i)} \right]$$

(5.17)

The softmax of an input vector $z = [z_1, z_2, ..., z_K]$ is thus a vector itself:

$$\text{softmax}(z)$$

The denominator $\sum_{i=1}^{K} \exp(z_i)$ is used to normalize all the values into probabilities. Thus for example given a vector:

$$z = [0.6, 1.1, -1.5, 1.2, 3.2, -1.1]$$

the resulting (rounded) softmax$(z)$ is

$$[0.055, 0.090, 0.006, 0.099, 0.74, 0.010]$$

Like the sigmoid, the softmax has the property of squashing values toward 0 or 1. Thus if one of the inputs is larger than the others, it will tend to push its probability toward 1, and suppress the probabilities of the smaller inputs.

Finally, note that, just as for the sigmoid, we refer to $z$, the vector of scores that is the input to the softmax, as logits (see (5.7)).

### 5.3.2 Applying softmax in logistic regression

When we apply softmax for logistic regression, the input will (just as for the sigmoid) be the dot product between a weight vector $w$ and an input vector $x$ (plus a bias). But now we’ll need separate weight vectors $w_k$ and bias $b_k$ for each of the $K$ classes. The probability of each of our output classes $\hat{y}_k$ can thus be computed as:

$$p(y_k = 1|x) = \frac{\exp(w_k \cdot x + b_k)}{\sum_{j=1}^{K} \exp(w_j \cdot x + b_j)}$$

(5.18)

The form of Eq. 5.18 makes it seem that we would compute each output separately. Instead, it’s more common to set up the equation for more efficient computation by modern vector processing hardware. We’ll do this by representing the set of $K$ weight vectors as a weight matrix $W$ and a bias vector $b$. Each row $k$ of
corresponds to the vector of weights \( w_k \). \( W \) thus has shape \([K \times f]\), for \( K \) the number of output classes and \( f \) the number of input features. The bias vector \( b \) has one value for each of the \( K \) output classes. If we represent the weights in this way, we can compute \( \hat{y} \), the vector of output probabilities for each of the \( K \) classes, by a single elegant equation:

\[
\hat{y} = \text{softmax}(Wx + b)
\] (5.19)

If you work out the matrix arithmetic, you can see that the estimated score of the first output class \( \hat{y}_1 \) (before we take the softmax) will correctly turn out to be \( w_1 \cdot x + b_1 \).

Fig. 5.3 shows an intuition of the role of the weight vector versus weight matrix in the computation of the output class probabilities for binary versus multinomial logistic regression.

**Figure 5.3** Binary versus multinomial logistic regression. Binary logistic regression uses a single weight vector \( w \), and has a scalar output \( \hat{y} \). In multinomial logistic regression we have \( K \) separate weight vectors corresponding to the \( K \) classes, all packed into a single weight matrix \( W \), and a vector output \( \hat{y} \).
5.3.3 Features in Multinomial Logistic Regression

Features in multinomial logistic regression act like features in binary logistic regression, with the difference mentioned above that we’ll need separate weight vectors and biases for each of the $K$ classes. Recall our binary exclamation point feature $x_5$ from page 85:

$$x_5 = \begin{cases} 1 & \text{if "!" \in doc} \\ 0 & \text{otherwise} \end{cases}$$

In binary classification a positive weight $w_5$ on a feature influences the classifier toward $y = 1$ (positive sentiment) and a negative weight influences it toward $y = 0$ (negative sentiment) with the absolute value indicating how important the feature is. For multinomial logistic regression, by contrast, with separate weights for each class, a feature can be evidence for or against each individual class.

In 3-way multiclass sentiment classification, for example, we must assign each document one of the 3 classes $+$, $-$, or 0 (neutral). Now a feature related to exclamation marks might have a negative weight for 0 documents, and a positive weight for $+$ or $-$ documents:

<table>
<thead>
<tr>
<th>Feature $f_5(x)$</th>
<th>Definition</th>
<th>$w_{5,+}$</th>
<th>$w_{5,-}$</th>
<th>$w_{5,0}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_5(x)$</td>
<td>$\begin{cases} 1 &amp; \text{if &quot;!&quot; \in doc} \ 0 &amp; \text{otherwise} \end{cases}$</td>
<td>3.5</td>
<td>3.1</td>
<td>-5.3</td>
</tr>
</tbody>
</table>

Because these feature weights are dependent both on the input text and the output class, we sometimes make this dependence explicit and represent the features themselves as $f(x,y)$: a function of both the input and the class. Using such a notation $f_5(x)$ above could be represented as three features $f_5(x,+)$, $f_5(x,-)$, and $f_5(x,0)$, each of which has a single weight. We’ll use this kind of notation in our description of the CRF in Chapter 8.

5.4 Learning in Logistic Regression

How are the parameters of the model, the weights $\mathbf{w}$ and bias $b$, learned? Logistic regression is an instance of supervised classification in which we know the correct label $y$ (either 0 or 1) for each observation $x$. What the system produces via Eq. 5.5 is $\hat{y}$, the system’s estimate of the true $y$. We want to learn parameters (meaning $\mathbf{w}$ and $b$) that make $\hat{y}$ for each training observation as close as possible to the true $y$.

This requires two components that we foreshadowed in the introduction to the chapter. The first is a metric for how close the current label ($\hat{y}$) is to the true gold label $y$. Rather than measure similarity, we usually talk about the opposite of this: the 

\textit{distance} \textit{between the system output and the gold output, and we call this distance the \textbf{loss} function or the \textbf{cost function}}. In the next section we’ll introduce the loss function that is commonly used for logistic regression and also for neural networks, the \textit{cross-entropy loss}.

The second thing we need is an optimization algorithm for iteratively updating the weights so as to minimize this loss function. The standard algorithm for this is \textit{gradient descent}; we’ll introduce the \textit{stochastic gradient descent} algorithm in the following section.
We’ll describe these algorithms for the simpler case of binary logistic regression in the next two sections, and then turn to multinomial logistic regression in Section 5.8.

5.5 The cross-entropy loss function

We need a loss function that expresses, for an observation \( x \), how close the classifier output (\( \hat{y} = \sigma(w \cdot x + b) \)) is to the correct output (\( y \), which is 0 or 1). We’ll call this:

\[
L(\hat{y}, y) = \text{How much } \hat{y} \text{ differs from the true } y
\]  
(5.20)

We do this via a loss function that prefers the correct class labels of the training examples to be more likely. This is called conditional maximum likelihood estimation: we choose the parameters \( w, b \) that maximize the log probability of the true \( y \) labels in the training data given the observations \( x \). The resulting loss function is the negative log likelihood loss, generally called the cross-entropy loss.

Let’s derive this loss function, applied to a single observation \( x \). We’d like to learn weights that maximize the probability of the correct label \( p(y|x) \). Since there are only two discrete outcomes (1 or 0), this is a Bernoulli distribution, and we can express the probability \( p(y|x) \) that our classifier produces for one observation as the following (keeping in mind that if \( y = 1 \), Eq. 5.21 simplifies to \( \hat{y} \); if \( y = 0 \), Eq. 5.21 simplifies to \( 1 - \hat{y} \)):

\[
p(y|x) = \hat{y}^y(1 - \hat{y})^{1-y}
\]  
(5.21)

Now we take the log of both sides. This will turn out to be handy mathematically, and doesn’t hurt us; whatever values maximize a probability will also maximize the log of the probability:

\[
\log p(y|x) = \log [\hat{y}^y(1 - \hat{y})^{1-y}]
\]

\[
= y \log \hat{y} + (1 - y) \log (1 - \hat{y})
\]  
(5.22)

Eq. 5.22 describes a log likelihood that should be maximized. In order to turn this into a loss function (something that we need to minimize), we’ll just flip the sign on Eq. 5.22. The result is the cross-entropy loss \( L_{CE} \):

\[
L_{CE}(\hat{y}, y) = -\log p(y|x) = -[y \log \hat{y} + (1 - y) \log (1 - \hat{y})]
\]  
(5.23)

Finally, we can plug in the definition of \( \hat{y} = \sigma(w \cdot x + b) \):

\[
L_{CE}(\hat{y}, y) = -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))]
\]  
(5.24)

Let’s see if this loss function does the right thing for our example from Fig. 5.2. We want the loss to be smaller if the model’s estimate is close to correct, and bigger if the model is confused. So first let’s suppose the correct gold label for the sentiment example in Fig. 5.2 is positive, i.e., \( y = 1 \). In this case our model is doing well, since from Eq. 5.8 it indeed gave the example a higher probability of being positive (.70) than negative (.30). If we plug \( \sigma(w \cdot x + b) = .70 \) and \( y = 1 \) into Eq. 5.24, the right side of the equation drops out, leading to the following loss (we’ll use log to mean
natural log when the base is not specified):

\[ L_{CE}(\hat{y}, y) = -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \]

By contrast, let’s pretend instead that the example in Fig. 5.2 was actually negative, i.e., \( y = 0 \) (perhaps the reviewer went on to say “But bottom line, the movie is terrible! I beg you not to see it!”). In this case our model is confused and we’d want the loss to be higher. Now if we plug \( y = 0 \) and \( 1 - \sigma(w \cdot x + b) = .31 \) from Eq. 5.8 into Eq. 5.24, the left side of the equation drops out:

\[ L_{CE}(\hat{y}, y) = -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \]

Sure enough, the loss for the first classifier (.36) is less than the loss for the second classifier (1.2).

Why does minimizing this negative log probability do what we want? A perfect classifier would assign probability 1 to the correct outcome \((y = 1 \text{ or } y = 0)\) and probability 0 to the incorrect outcome. That means if \( y \) equals 1, the higher \( \hat{y} \) is (the closer it is to 1), the better the classifier; the lower \( \hat{y} \) is (the closer it is to 0), the worse the classifier. If \( y \) equals 0, instead, the higher \( 1 - \hat{y} \) is (closer to 1), the better the classifier. The negative log of \( \hat{y} \) (if the true \( y \) equals 1) or \( 1 - \hat{y} \) (if the true \( y \) equals 0) is a convenient loss metric since it goes from 0 (negative log of 1, no loss) to infinity (negative log of 0, infinite loss). This loss function also ensures that as the probability of the correct answer is maximized, the probability of the incorrect answer is minimized; since the two sum to one, any increase in the probability of the correct answer is coming at the expense of the incorrect answer. It’s called the cross-entropy loss, because Eq. 5.22 is also the formula for the cross-entropy between the true probability distribution \( y \) and our estimated distribution \( \hat{y} \).

Now we know what we want to minimize; in the next section, we’ll see how to find the minimum.

### 5.6 Gradient Descent

Our goal with gradient descent is to find the optimal weights: minimize the loss function we’ve defined for the model. In Eq. 5.25 below, we’ll explicitly represent the fact that the loss function \( L \) is parameterized by the weights, which we’ll refer to in machine learning in general as \( \theta \) (in the case of logistic regression \( \theta = w, b \)). So the goal is to find the set of weights which minimizes the loss function, averaged over all examples:

\[
\hat{\theta} = \text{argmin}_{\theta} \frac{1}{m} \sum_{i=1}^{m} L_{CE}(f(x^{(i)}; \theta), y^{(i)})
\]  

(5.25)

How shall we find the minimum of this (or any) loss function? Gradient descent is a method that finds a minimum of a function by figuring out in which direction (in the
space of the parameters \( \theta \) the function’s slope is rising the most steeply, and moving in the opposite direction. The intuition is that if you are hiking in a canyon and trying to descend most quickly down to the river at the bottom, you might look around yourself 360 degrees, find the direction where the ground is sloping the steepest, and walk downhill in that direction.

For logistic regression, this loss function is conveniently convex. A convex function has at most one minimum; there are no local minima to get stuck in, so gradient descent starting from any point is guaranteed to find the minimum. (By contrast, the loss for multi-layer neural networks is non-convex, and gradient descent may get stuck in local minima for neural network training and never find the global optimum.)

Although the algorithm (and the concept of gradient) are designed for direction vectors, let’s first consider a visualization of the case where the parameter of our system is just a single scalar \( w \), shown in Fig. 5.4.

Given a random initialization of \( w \) at some value \( w^1 \), and assuming the loss function \( L \) happened to have the shape in Fig. 5.4, we need the algorithm to tell us whether at the next iteration we should move left (making \( w^2 \) smaller than \( w^1 \)) or right (making \( w^2 \) bigger than \( w^1 \)) to reach the minimum. The gradient descent algorithm answers this question by finding the gradient of the loss function at the current point and moving in the opposite direction. The gradient of a function of many variables is a vector pointing in the direction of the greatest increase in a function. The gradient is a multi-variable generalization of the slope, so for a function of one variable like the one in Fig. 5.4, we can informally think of the gradient as the slope. The dotted line in Fig. 5.4 shows the slope of this hypothetical loss function at point \( w = w^1 \). You can see that the slope of this dotted line is negative. Thus to find the minimum, gradient descent tells us to go in the opposite direction: moving \( w \) in a positive direction.

The magnitude of the amount to move in gradient descent is the value of the slope \( \frac{d}{dw} L(f(x,w), y) \) weighted by a learning rate \( \eta \). A higher (faster) learning rate means that we should move \( w \) more on each step. The change we make in our parameter is the learning rate times the gradient (or the slope, in our single-variable
example):

\[ w^{t+1} = w^t - \eta \frac{d}{dw} L(f(x;w), y) \]  

(5.26)

Now let’s extend the intuition from a function of one scalar variable \( w \) to many variables, because we don’t just want to move left or right, we want to know where in the \( N \)-dimensional space (of the \( N \) parameters that make up \( \theta \)) we should move. The gradient is just such a vector; it expresses the directional components of the sharpest slope along each of those \( N \) dimensions. If we’re just imagining two weight dimensions (say for one weight \( w \) and one bias \( b \)), the gradient might be a vector with two orthogonal components, each of which tells us how much the ground slopes in the \( w \) dimension and in the \( b \) dimension. Fig. 5.5 shows a visualization of the value of a 2-dimensional gradient vector taken at the red point.

In an actual logistic regression, the parameter vector \( w \) is much longer than 1 or 2, since the input feature vector \( x \) can be quite long, and we need a weight \( w_i \) for each \( x_i \). For each dimension/variable \( w_i \) in \( w \) (plus the bias \( b \)), the gradient will have a component that tells us the slope with respect to that variable. In each dimension \( w_i \), we express the slope as a partial derivative \( \frac{\partial}{\partial w_i} \) of the loss function. Essentially we’re asking: “How much would a small change in that variable \( w_i \) influence the total loss function \( L \)?”

Formally, then, the gradient of a multi-variable function \( f \) is a vector in which each component expresses the partial derivative of \( f \) with respect to one of the variables. We’ll use the inverted Greek delta symbol \( \nabla \) to refer to the gradient, and represent \( \hat{y} \) as \( f(x;\theta) \) to make the dependence on \( \theta \) more obvious:

\[
\nabla L(f(x;\theta), y) = \begin{bmatrix}
\frac{\partial}{\partial w_1} L(f(x;\theta), y) \\
\frac{\partial}{\partial w_2} L(f(x;\theta), y) \\
\vdots \\
\frac{\partial}{\partial w_n} L(f(x;\theta), y) \\
\frac{\partial}{\partial b} L(f(x;\theta), y)
\end{bmatrix}
\]  

(5.27)

The final equation for updating \( \theta \) based on the gradient is thus

\[ \theta^{t+1} = \theta^t - \eta \nabla L(f(x;\theta), y) \]  

(5.28)

Figure 5.5 | Visualization of the gradient vector at the red point in two dimensions \( w \) and \( b \), showing a red arrow in the \( x \)-\( y \) plane pointing in the direction we will go to look for the minimum: the opposite direction of the gradient (recall that the gradient points in the direction of increase not decrease).
5.6.1 The Gradient for Logistic Regression

In order to update \( \theta \), we need a definition for the gradient \( \nabla L(f(x; \theta), y) \). Recall that for logistic regression, the cross-entropy loss function is:

\[
L_{CE}(\hat{y}, y) = -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))]
\] (5.29)

It turns out that the derivative of this function for one observation vector \( x \) is Eq. 5.30 (the interested reader can see Section 5.10 for the derivation of this equation):

\[
\frac{\partial L_{CE}(\hat{y}, y)}{\partial w_j} = [\sigma(w \cdot x + b) - y]x_j = (\hat{y} - y)x_j
\] (5.30)

You’ll also sometimes see this equation in the equivalent form:

\[
\frac{\partial L_{CE}(\hat{y}, y)}{\partial w_j} = -(y - \hat{y})x_j
\] (5.31)

Note in these equations that the gradient with respect to a single weight \( w_j \) represents a very intuitive value: the difference between the true \( y \) and our estimated \( \hat{y} = \sigma(w \cdot x + b) \) for that observation, multiplied by the corresponding input value \( x_j \).

5.6.2 The Stochastic Gradient Descent Algorithm

Stochastic gradient descent is an online algorithm that minimizes the loss function by computing its gradient after each training example, and nudging \( \theta \) in the right direction (the opposite direction of the gradient). (An “online algorithm” is one that processes its input example by example, rather than waiting until it sees the entire input.) Fig. 5.6 shows the algorithm.

The learning rate \( \eta \) is a hyperparameter that must be adjusted. If it’s too high, the learner will take steps that are too large, overshooting the minimum of the loss function. If it’s too low, the learner will take steps that are too small, and take too long to get to the minimum. It is common to start with a higher learning rate and then slowly decrease it, so that it is a function of the iteration \( k \) of training; the notation \( \eta_k \) can be used to mean the value of the learning rate at iteration \( k \).

We’ll discuss hyperparameters in more detail in Chapter 7, but in short, they are a special kind of parameter for any machine learning model. Unlike regular parameters of a model (weights like \( w \) and \( b \)), which are learned by the algorithm from the training set, hyperparameters are special parameters chosen by the algorithm designer that affect how the algorithm works.

5.6.3 Working through an example

Let’s walk through a single step of the gradient descent algorithm. We’ll use a simplified version of the example in Fig. 5.2 as it sees a single observation \( x \), whose correct value is \( y = 1 \) (this is a positive review), and with a feature vector \( x = [x_1, x_2] \) consisting of these two features:

\[
x_1 = 3 \quad \text{(count of positive lexicon words)}
\]

\[
x_2 = 2 \quad \text{(count of negative lexicon words)}
\]
Let's assume the initial weights and bias in $\theta^0$ are all set to 0, and the initial learning rate $\eta$ is 0.1:

\[
\begin{align*}
  w_1 &= w_2 = b = 0 \\
  \eta &= 0.1
\end{align*}
\]

The single update step requires that we compute the gradient, multiplied by the learning rate

\[
\theta^{t+1} = \theta^t - \eta \nabla_\theta L(f(x^{(i)}; \theta), y^{(i)})
\]

In our mini example there are three parameters, so the gradient vector has 3 dimensions, for $w_1, w_2,$ and $b$. We can compute the first gradient as follows:

\[
\nabla_{w,b} L = \begin{bmatrix}
\frac{\partial L(f(x), y)}{\partial w_1} \\
\frac{\partial L(f(x), y)}{\partial w_2} \\
\frac{\partial L(f(x), y)}{\partial b}
\end{bmatrix} = \begin{bmatrix}
(s(w \cdot x + b) - y)x_1 \\
(s(w \cdot x + b) - y)x_2 \\
(s(w \cdot x + b) - y)
\end{bmatrix} = \begin{bmatrix}
(s(0) - 1)x_1 \\
(s(0) - 1)x_2 \\
(s(0) - 1)
\end{bmatrix} = \begin{bmatrix}
-0.5x_1 \\
-0.5x_2 \\
-0.5
\end{bmatrix} = \begin{bmatrix}
-1.5 \\
-1.0 \\
-0.5
\end{bmatrix}
\]

Now that we have a gradient, we compute the new parameter vector $\theta^1$ by moving $\theta^0$ in the opposite direction from the gradient:

\[
\theta^1 = \begin{bmatrix}
w_1 \\
w_2 \\
b
\end{bmatrix} - \eta \begin{bmatrix}
-1.5 \\
-1.0 \\
-0.5
\end{bmatrix} = \begin{bmatrix}
.15 \\
.1 \\
.05
\end{bmatrix}
\]

So after one step of gradient descent, the weights have shifted to be: $w_1 = .15$, $w_2 = .1$, and $b = .05$.

Note that this observation $x$ happened to be a positive example. We would expect that after seeing more negative examples with high counts of negative words, that the weight $w_2$ would shift to have a negative value.
5.6.4 Mini-batch training

Stochastic gradient descent is called stochastic because it chooses a single random example at a time, moving the weights so as to improve performance on that single example. That can result in very choppy movements, so it’s common to compute the gradient over batches of training instances rather than a single instance.

For example in **batch training** we compute the gradient over the entire dataset. By seeing so many examples, batch training offers a superb estimate of which direction to move the weights, at the cost of spending a lot of time processing every single example in the training set to compute this perfect direction.

A compromise is **mini-batch** training: we train on a group of \( m \) examples (perhaps 512, or 1024) that is less than the whole dataset. (If \( m \) is the size of the dataset, then we are doing **batch** gradient descent; if \( m = 1 \), we are back to doing stochastic gradient descent.) Mini-batch training also has the advantage of computational efficiency. The mini-batches can easily be vectorized, choosing the size of the mini-batch based on the computational resources. This allows us to process all the examples in one mini-batch in parallel and then accumulate the loss, something that’s not possible with individual or batch training.

We just need to define mini-batch versions of the cross-entropy loss function we defined in Section 5.5 and the gradient in Section 5.6.1. Let’s extend the cross-entropy loss for one example from Eq. 5.23 to mini-batches of size \( m \). We’ll continue to use the notation that \( x^{(i)} \) and \( y^{(i)} \) mean the \( i \)th training features and training label, respectively. We make the assumption that the training examples are independent:

\[
\log p(\text{training labels}) = \log \prod_{i=1}^{m} p(y^{(i)}|x^{(i)}) \\
= \sum_{i=1}^{m} \log p(y^{(i)}|x^{(i)}) \\
= -\sum_{i=1}^{m} L_{\text{CE}}(\hat{y}^{(i)}, y^{(i)}) \tag{5.32}
\]

Now the cost function for the mini-batch of \( m \) examples is the average loss for each example:

\[
Cost(\hat{y}, y) = \frac{1}{m} \sum_{i=1}^{m} L_{\text{CE}}(\hat{y}^{(i)}, y^{(i)}) \\
= -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \sigma(w \cdot x^{(i)} + b) + (1 - y^{(i)}) \log \left( 1 - \sigma(w \cdot x^{(i)} + b) \right) \tag{5.33}
\]

The mini-batch gradient is the average of the individual gradients from Eq. 5.30:

\[
\frac{\partial Cost(\hat{y}, y)}{\partial w_j} = \frac{1}{m} \sum_{i=1}^{m} \left[ \sigma(w \cdot x^{(i)} + b) - y^{(i)} \right] x_j^{(i)} \tag{5.34}
\]

Instead of using the sum notation, we can more efficiently compute the gradient in its matrix form, following the vectorization we saw on page 87, where we have a matrix \( X \) of size \([m \times f]\) representing the \( m \) inputs in the batch, and a vector \( y \) of size \([m \times 1]\) representing the correct outputs:
5.7 Regularization

\[ \frac{\partial \text{Cost}(\hat{y}, y)}{\partial \mathbf{w}} = \frac{1}{m} (\hat{y} - y)^\top \mathbf{X} = \frac{1}{m} (\sigma(\mathbf{Xw} + \mathbf{b}) - y)^\top \mathbf{X} \] (5.35)

There is a problem with learning weights that make the model perfectly match the training data. If a feature is perfectly predictive of the outcome because it happens to only occur in one class, it will be assigned a very high weight. The weights for features will attempt to perfectly fit details of the training set, in fact too perfectly, modeling noisy factors that just accidentally correlate with the class. This problem is called overfitting. A good model should be able to generalize well from the training data to the unseen test set, but a model that overfits will have poor generalization.

To avoid overfitting, a new regularization term \( R(\theta) \) is added to the objective function in Eq. 5.25, resulting in the following objective for a batch of \( m \) examples (slightly rewritten from Eq. 5.25 to be maximizing log probability rather than minimizing loss, and removing the \( \frac{1}{m} \) term which doesn’t affect the argmax):

\[
\hat{\theta} = \arg\max_\theta \sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) - \alpha R(\theta) \quad (5.36)
\]

The new regularization term \( R(\theta) \) is used to penalize large weights. Thus a setting of the weights that matches the training data perfectly— but uses many weights with high values to do so—will be penalized more than a setting that matches the data a little less well, but does so using smaller weights. There are two common ways to compute this regularization term \( R(\theta) \). \textbf{L2 regularization} is a quadratic function of the weight values, named because it uses the (square of the) L2 norm of the weight values. The L2 norm, \( ||\theta||_2 \), is the same as the Euclidean distance of the vector \( \theta \) from the origin. If \( \theta \) consists of \( n \) weights, then:

\[
R(\theta) = ||\theta||_2^2 = \sum_{j=1}^{n} \theta_j^2 \quad (5.37)
\]

The L2 regularized objective function becomes:

\[
\hat{\theta} = \arg\max_\theta \left[ \sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) \right] - \alpha \sum_{j=1}^{n} \theta_j^2 \quad (5.38)
\]

\textbf{L1 regularization} is a linear function of the weight values, named after the L1 norm \( ||W||_1 \), the sum of the absolute values of the weights, or Manhattan distance (the...
Manhattan distance is the distance you’d have to walk between two points in a city with a street grid like New York):

\[
R(\theta) = ||\theta||_1 = \sum_{i=1}^{n} |\theta_i| \tag{5.39}
\]

The L1 regularized objective function becomes:

\[
\hat{\theta} = \operatorname*{argmax}_{\theta} \left[ \sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) - \alpha \sum_{j=1}^{n} |\theta_j| \right] \tag{5.40}
\]

These kinds of regularization come from statistics, where L1 regularization is called lasso regression (Tibshirani, 1996) and L2 regularization is called ridge regression, and both are commonly used in language processing. L2 regularization is easier to optimize because of its simple derivative (the derivative of \(\theta^2\) is just 2\(\theta\)), while L1 regularization is more complex (the derivative of \(|\theta|\) is non-continuous at zero). But while L2 prefers weight vectors with many small weights, L1 prefers sparse solutions with some larger weights but many more weights set to zero. Thus L1 regularization leads to much sparser weight vectors, that is, far fewer features.

Both L1 and L2 regularization have Bayesian interpretations as constraints on the prior of how weights should look. L1 regularization can be viewed as a Laplace prior on the weights. L2 regularization corresponds to assuming that weights are distributed according to a Gaussian distribution with mean \(\mu = 0\). In a Gaussian or normal distribution, the further away a value is from the mean, the lower its probability (scaled by the variance \(\sigma\)). By using a Gaussian prior on the weights, we are saying that weights prefer to have the value 0. A Gaussian for a weight \(\theta_j\) is

\[
\frac{1}{\sqrt{2\pi\sigma_j^2}} \exp \left( -\frac{(\theta_j - \mu_j)^2}{2\sigma_j^2} \right) \tag{5.41}
\]

If we multiply each weight by a Gaussian prior on the weight, we are thus maximizing the following constraint:

\[
\hat{\theta} = \operatorname*{argmax}_{\theta} \prod_{i=1}^{m} P(y^{(i)}|x^{(i)}) \times \prod_{j=1}^{n} \frac{1}{\sqrt{2\pi\sigma_j^2}} \exp \left( -\frac{(\theta_j - \mu_j)^2}{2\sigma_j^2} \right) \tag{5.42}
\]

which in log space, with \(\mu = 0\), and assuming \(2\sigma^2 = 1\), corresponds to

\[
\hat{\theta} = \operatorname*{argmax}_{\theta} \sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) - \alpha \sum_{j=1}^{n} \theta_j^2 \tag{5.43}
\]

which is in the same form as Eq. 5.38.

### 5.8 Learning in Multinomial Logistic Regression

The loss function for multinomial logistic regression generalizes the loss function for binary logistic regression from 2 to \(K\) classes. Recall that the cross-entropy loss for binary logistic regression (repeated from Eq. 5.23) is:

\[
L_{CE}(\hat{y}, y) = -\log p(y|x) = -[y \log \hat{y} + (1 - y) \log (1 - \hat{y})] \tag{5.44}
\]
The loss function for multinomial logistic regression generalizes the two terms in Eq. 5.44 (one that is non-zero when \( y = 1 \) and one that is non-zero when \( y = 0 \)) to \( K \) terms. As we mentioned above, for multinomial regression we’ll represent both \( y \) and \( \hat{y} \) as vectors. The true label \( y \) is a vector with \( K \) elements, each corresponding to a class, with \( y_c = 1 \) if the correct class is \( c \), with all other elements of \( y \) being 0. And our classifier will produce an estimate vector with \( K \) elements \( \hat{y} \), each element \( \hat{y}_k \) of which represents the estimated probability \( p(y_k = 1 | x) \).

The loss function for a single example \( x \), generalizing from binary logistic regression, is the sum of the logs of the \( K \) output classes, each weighted by their probability \( y_k \) (Eq. 5.45). This turns out to be just the negative log probability of the correct class \( c \) (Eq. 5.46):

\[
L_{CE}(\hat{y}, y) = - \sum_{k=1}^{K} y_k \log \hat{y}_k \\
= - \log \hat{y}_c, \quad \text{(where } c \text{ is the correct class)}
\]

\[
= - \log \hat{p}(y_c = 1 | x) \quad \text{(where } c \text{ is the correct class)}
\]

\[
= - \log \frac{\exp(\mathbf{w}_c \cdot \mathbf{x} + b_c)}{\sum_{j=1}^{K} \exp(\mathbf{w}_j \cdot \mathbf{x} + b_j)} \quad \text{(} c \text{ is the correct class)}
\]

How did we get from Eq. 5.45 to Eq. 5.46? Because only one class (let’s call it \( c \)) is the correct one, the vector \( y \) takes the value 1 only for this value of \( k \), i.e., has \( y_c = 1 \) and \( y_j = 0 \) \( \forall j \neq c \). That means the terms in the sum in Eq. 5.45 will all be 0 except for the term corresponding to the true class \( c \). Hence the cross-entropy loss is simply the log of the output probability corresponding to the correct class, and we therefore also call Eq. 5.46 the negative log likelihood loss.

Of course for gradient descent we don’t need the loss, we need its gradient. The gradient for a single example turns out to be very similar to the gradient for binary logistic regression, \((\hat{y} - y)x\), that we saw in Eq. 5.30. Let’s consider one piece of the gradient, the derivative for a single weight. For each class \( k \), the weight of the \( i \)th element of input \( x \) is \( w_{k,i} \). What is the partial derivative of the loss with respect to \( w_{k,i} \)? This derivative turns out to be just the difference between the true value for the class \( k \) (which is either 1 or 0) and the probability the classifier outputs for class \( k \), weighted by the value of the input \( x_i \) corresponding to the \( i \)th element of the weight vector for class \( k \):

\[
\frac{\partial L_{CE}}{\partial w_{k,i}} = -(y_k - \hat{y}_k)x_i
\]

\[
= -(y_k - p(y_k = 1 | x))x_i
\]

\[
= - \left( y_k - \frac{\exp(\mathbf{w}_k \cdot \mathbf{x} + b_k)}{\sum_{j=1}^{K} \exp(\mathbf{w}_j \cdot \mathbf{x} + b_j)} \right) x_i
\]

We’ll return to this case of the gradient for softmax regression when we introduce neural networks in Chapter 7, and at that time we’ll also discuss the derivation of this gradient in equations Eq. 7.33–Eq. 7.41.
5.9 Interpreting models

Often we want to know more than just the correct classification of an observation. We want to know why the classifier made the decision it did. That is, we want our decision to be interpretable. Interpretability can be hard to define strictly, but the core idea is that as humans we should know why our algorithms reach the conclusions they do. Because the features to logistic regression are often human-designed, one way to understand a classifier’s decision is to understand the role each feature plays in the decision. Logistic regression can be combined with statistical tests (the likelihood ratio test, or the Wald test); investigating whether a particular feature is significant by one of these tests, or inspecting its magnitude (how large is the weight $w$ associated with the feature?) can help us interpret why the classifier made the decision it makes. This is enormously important for building transparent models.

Furthermore, in addition to its use as a classifier, logistic regression in NLP and many other fields is widely used as an analytic tool for testing hypotheses about the effect of various explanatory variables (features). In text classification, perhaps we want to know if logically negative words (no, not, never) are more likely to be associated with negative sentiment, or if negative reviews of movies are more likely to discuss the cinematography. However, in doing so it’s necessary to control for potential confounds: other factors that might influence sentiment (the movie genre, the year it was made, perhaps the length of the review in words). Or we might be studying the relationship between NLP-extracted linguistic features and non-linguistic outcomes (hospital readmissions, political outcomes, or product sales), but need to control for confounds (the age of the patient, the county of voting, the brand of the product). In such cases, logistic regression allows us to test whether some feature is associated with some outcome above and beyond the effect of other features.

5.10 Advanced: Deriving the Gradient Equation

In this section we give the derivation of the gradient of the cross-entropy loss function $L_{CE}$ for logistic regression. Let’s start with some quick calculus refreshers. First, the derivative of $\ln(x)$:

$$\frac{d}{dx} \ln(x) = \frac{1}{x} \quad (5.49)$$

Second, the (very elegant) derivative of the sigmoid:

$$\frac{d\sigma(z)}{dz} = \sigma(z)(1 - \sigma(z)) \quad (5.50)$$

Finally, the chain rule of derivatives. Suppose we are computing the derivative of a composite function $f(x) = u(v(x))$. The derivative of $f(x)$ is the derivative of $u(x)$ with respect to $v(x)$ times the derivative of $v(x)$ with respect to $x$:

$$\frac{df}{dx} = \frac{du}{dv} \cdot \frac{dv}{dx} \quad (5.51)$$

First, we want to know the derivative of the loss function with respect to a single weight $w_j$ (we’ll need to compute it for each weight, and for the bias):
\[
\frac{\partial L_{CE}}{\partial w_j} = \frac{\partial}{\partial w_j} \left[ y \log(\sigma(w \cdot x + b)) + (1 - y) \log(1 - \sigma(w \cdot x + b)) \right]
\]
\[
= - \left[ \frac{\partial}{\partial w_j} y \log(\sigma(w \cdot x + b)) + \frac{\partial}{\partial w_j} (1 - y) \log(1 - \sigma(w \cdot x + b)) \right]
\] (5.52)

Next, using the chain rule, and relying on the derivative of log:
\[
\frac{\partial L_{CE}}{\partial w_j} = - \frac{y}{\sigma(w \cdot x + b)} \frac{\partial}{\partial w_j} \sigma(w \cdot x + b) - \frac{1 - y}{1 - \sigma(w \cdot x + b)} \frac{\partial}{\partial w_j} (1 - \sigma(w \cdot x + b))
\] (5.53)

Rearranging terms:
\[
\frac{\partial L_{CE}}{\partial w_j} = - \left[ \frac{y}{\sigma(w \cdot x + b)} - \frac{1 - y}{1 - \sigma(w \cdot x + b)} \right] \frac{\partial}{\partial w_j} \sigma(w \cdot x + b)
\] (5.54)

And now plugging in the derivative of the sigmoid, and using the chain rule one more time, we end up with Eq. 5.55:
\[
\frac{\partial L_{CE}}{\partial w_j} = - \left[ \frac{y - \sigma(w \cdot x + b)}{\sigma(w \cdot x + b)[1 - \sigma(w \cdot x + b)]} \right] \sigma(w \cdot x + b)[1 - \sigma(w \cdot x + b)] \frac{\partial (w \cdot x + b)}{\partial w_j}
\]
\[
= - \left[ \frac{y - \sigma(w \cdot x + b)}{\sigma(w \cdot x + b)[1 - \sigma(w \cdot x + b)]} \right] \sigma(w \cdot x + b)[1 - \sigma(w \cdot x + b)] x_j
\]
\[
= -[y - \sigma(w \cdot x + b)] x_j
\]
\[
= \left[ \sigma(w \cdot x + b) - y \right] x_j
\] (5.55)

5.11 Summary

This chapter introduced the **logistic regression** model of classification.

- Logistic regression is a supervised machine learning classifier that extracts real-valued features from the input, multiplies each by a weight, sums them, and passes the sum through a **sigmoid** function to generate a probability. A threshold is used to make a decision.
- Logistic regression can be used with two classes (e.g., positive and negative sentiment) or with multiple classes (**multinomial logistic regression**, for example for n-ary text classification, part-of-speech labeling, etc.).
- Multinomial logistic regression uses the **softmax** function to compute probabilities.
- The weights (vector \( w \) and bias \( b \)) are learned from a labeled training set via a loss function, such as the **cross-entropy loss**, that must be minimized.
- Minimizing this loss function is a **convex optimization** problem, and iterative algorithms like **gradient descent** are used to find the optimal weights.
- **Regularization** is used to avoid overfitting.
- Logistic regression is also one of the most useful analytic tools, because of its ability to transparently study the importance of individual features.
Bibliographical and Historical Notes

Logistic regression was developed in the field of statistics, where it was used for the analysis of binary data by the 1960s, and was particularly common in medicine (Cox, 1969). Starting in the late 1970s it became widely used in linguistics as one of the formal foundations of the study of linguistic variation (Sankoff and Labov, 1979).

Nonetheless, logistic regression didn’t become common in natural language processing until the 1990s, when it seems to have appeared simultaneously from two directions. The first source was the neighboring fields of information retrieval and speech processing, both of which had made use of regression, and both of which lent many other statistical techniques to NLP. Indeed a very early use of logistic regression for document routing was one of the first NLP applications to use (LSI) embeddings as word representations (Schütze et al., 1995).

At the same time in the early 1990s logistic regression was developed and applied to NLP at IBM Research under the name maximum entropy modeling or maxent (Berger et al., 1996), seemingly independent of the statistical literature. Under that name it was applied to language modeling (Rosenfeld, 1996), part-of-speech tagging (Ratnaparkhi, 1996), parsing (Ratnaparkhi, 1997), coreference resolution (Kehler, 1997b), and text classification (Nigam et al., 1999).

More on classification can be found in machine learning textbooks (Hastie et al. 2001, Witten and Frank 2005, Bishop 2006, Murphy 2012).

Exercises
CHAPTER 6

Vector Semantics and Embeddings

Nets are for fish;
Once you get the fish, you can forget the net.
Words are for meaning;
Once you get the meaning, you can forget the words
庄子(Zhuangzi), Chapter 26

The asphalt that Los Angeles is famous for occurs mainly on its freeways. But in the middle of the city is another patch of asphalt, the La Brea tar pits, and this asphalt preserves millions of fossil bones from the last of the Ice Ages of the Pleistocene Epoch. One of these fossils is the Smilodon, or saber-toothed tiger, instantly recognizable by its long canines. Five million years ago or so, a completely different saber-tooth tiger called Thylacosmilus lived in Argentina and other parts of South America. Thylacosmilus was a marsupial whereas Smilodon was a placental mammal, but Thylacosmilus had the same long upper canines and, like Smilodon, had a protective bone flange on the lower jaw. The similarity of these two mammals is one of many examples of parallel or convergent evolution, in which particular contexts or environments lead to the evolution of very similar structures in different species (Gould, 1980).

The role of context is also important in the similarity of a less biological kind of organism: the word. Words that occur in similar contexts tend to have similar meanings. This link between similarity in how words are distributed and similarity in what they mean is called the **distributional hypothesis**. The hypothesis was first formulated in the 1950s by linguists like Joos (1950), Harris (1954), and Firth (1957), who noticed that words which are synonyms (like *oculist* and *eye-doctor*) tended to occur in the same environment (e.g., near words like *eye* or *examined*) with the amount of meaning difference between two words “corresponding roughly to the amount of difference in their environments” (Harris, 1954, 157).

In this chapter we introduce **vector semantics**, which instantiates this linguistic hypothesis by learning representations of the meaning of words, called **embeddings**, directly from their distributions in texts. These representations are used in every natural language processing application that makes use of meaning, and the **static embeddings** we introduce here underlie the more powerful dynamic or **contextualized embeddings** like BERT that we will see in Chapter 11.

These word representations are also the first example in this book of **representation learning**, automatically learning useful representations of the input text. Finding such **self-supervised** ways to learn representations of the input, instead of creating representations by hand via **feature engineering**, is an important focus of NLP research (Bengio et al., 2013).
6.1 Lexical Semantics

Let’s begin by introducing some basic principles of word meaning. How should we represent the meaning of a word? In the n-gram models of Chapter 3, and in classical NLP applications, our only representation of a word is as a string of letters, or an index in a vocabulary list. This representation is not that different from a tradition in philosophy, perhaps you’ve seen it in introductory logic classes, in which the meaning of words is represented by just spelling the word with small capital letters; representing the meaning of “dog” as DOG, and “cat” as CAT, or by using an apostrophe (DOG’).

Representing the meaning of a word by capitalizing it is a pretty unsatisfactory model. You might have seen a version of a joke due originally to semanticist Barbara Partee (Carlson, 1977):

Q: What’s the meaning of life?
A: LIFE’

Surely we can do better than this! After all, we’ll want a model of word meaning to do all sorts of things for us. It should tell us that some words have similar meanings (cat is similar to dog), others are antonyms (cold is the opposite of hot), some have positive connotations (happy) while others have negative connotations (sad). It should represent the fact that the meanings of buy, sell, and pay offer differing perspectives on the same underlying purchasing event. (If I buy something from you, you’ve probably sold it to me, and I likely paid you.) More generally, a model of word meaning should allow us to draw inferences to address meaning-related tasks like question-answering or dialogue.

In this section we summarize some of these desiderata, drawing on results in the linguistic study of word meaning, which is called lexical semantics; we’ll return to lexical semantics and expand on this list in Chapter 23 and Chapter 24.

**Lemmas and Senses** Let’s start by looking at how one word (we’ll choose mouse) might be defined in a dictionary (simplified from the online dictionary WordNet):

mouse (N)
1. any of numerous small rodents...
2. a hand-operated device that controls a cursor...

Here the form mouse is the lemma, also called the citation form. The form mouse would also be the lemma for the word mice; dictionaries don’t have separate definitions for inflected forms like mice. Similarly sing is the lemma for sing, sang, sung. In many languages the infinitive form is used as the lemma for the verb, so Spanish dormir “to sleep” is the lemma for duermes “you sleep”. The specific forms sung or carpets or sing or duermes are called wordforms.

As the example above shows, each lemma can have multiple meanings; the lemma mouse can refer to the rodent or the cursor control device. We call each of these aspects of the meaning of mouse a word sense. The fact that lemmas can be polysemous (have multiple senses) can make interpretation difficult (is someone who types “mouse info” into a search engine looking for a pet or a tool?). Chapter 11 and Chapter 23 will discuss the problem of polysemy, and introduce word sense disambiguation, the task of determining which sense of a word is being used in a particular context.

**Synonymy** One important component of word meaning is the relationship between word senses. For example when one word has a sense whose meaning is
identical to a sense of another word, or nearly identical, we say the two senses of those two words are synonyms. Synonyms include such pairs as
couch/sofa vomit/throw up filbert/hazelnut car/automobile

A more formal definition of synonymy (between words rather than senses) is that two words are synonymous if they are substitutable for one another in any sentence without changing the truth conditions of the sentence, the situations in which the sentence would be true.

While substitutions between some pairs of words like car/automobile or water/H₂O are truth preserving, the words are still not identical in meaning. Indeed, probably no two words are absolutely identical in meaning. One of the fundamental tenets of semantics, called the principle of contrast (Girard 1718, Bréal 1897, Clark 1987), states that a difference in linguistic form is always associated with some difference in meaning. For example, the word H₂O is used in scientific contexts and would be inappropriate in a hiking guide—water would be more appropriate—and this genre difference is part of the meaning of the word. In practice, the word synonym is therefore used to describe a relationship of approximate or rough synonymy.

Word Similarity While words don’t have many synonyms, most words do have lots of similar words. Cat is not a synonym of dog, but cats and dogs are certainly similar words. In moving from synonymy to similarity, it will be useful to shift from talking about relations between word senses (like synonymy) to relations between words (like similarity). Dealing with words avoids having to commit to a particular representation of word senses, which will turn out to simplify our task.

The notion of word similarity is very useful in larger semantic tasks. Knowing how similar two words are can help in computing how similar the meaning of two phrases or sentences are, a very important component of tasks like question answering, paraphrasing, and summarization. One way of getting values for word similarity is to ask humans to judge how similar one word is to another. A number of datasets have resulted from such experiments. For example the SimLex-999 dataset (Hill et al., 2015) gives values on a scale from 0 to 10, like the examples below, which range from near-synonyms (vanish, disappear) to pairs that scarcely seem to have anything in common (hole, agreement):

<table>
<thead>
<tr>
<th></th>
<th></th>
<th>9.8</th>
</tr>
</thead>
<tbody>
<tr>
<td>vanish</td>
<td>disappear</td>
<td></td>
</tr>
<tr>
<td>belief</td>
<td>impression</td>
<td>5.95</td>
</tr>
<tr>
<td>muscle</td>
<td>bone</td>
<td>3.65</td>
</tr>
<tr>
<td>modest</td>
<td>flexible</td>
<td>0.98</td>
</tr>
<tr>
<td>hole</td>
<td>agreement</td>
<td>0.3</td>
</tr>
</tbody>
</table>

Word Relatedness The meaning of two words can be related in ways other than similarity. One such class of connections is called word relatedness (Budanitsky and Hirst, 2006), also traditionally called word association in psychology.

Consider the meanings of the words coffee and cup. Coffee is not similar to cup; they share practically no features (coffee is a plant or a beverage, while a cup is a manufactured object with a particular shape). But coffee and cup are clearly related; they are associated by co-participating in an everyday event (the event of drinking coffee out of a cup). Similarly scalpel and surgeon are not similar but are related eventively (a surgeon tends to make use of a scalpel).

One common kind of relatedness between words is if they belong to the same semantic field. A semantic field is a set of words which cover a particular semantic domain and bear structured relations with each other. For example, words might be
related by being in the semantic field of hospitals (surgeon, scalpel, nurse, anesthetic, hospital), restaurants (waiter, menu, plate, food, chef), or houses (door, roof, kitchen, family, bed). Semantic fields are also related to topic models, like Latent Dirichlet Allocation, LDA, which apply unsupervised learning on large sets of texts to induce sets of associated words from text. Semantic fields and topic models are very useful tools for discovering topical structure in documents.

In Chapter 23 we’ll introduce more relations between senses like hypernymy or IS-A, antonymy (opposites) and meronymy (part-whole relations).

Semantic Frames and Roles  
Closely related to semantic fields is the idea of a semantic frame. A semantic frame is a set of words that denote perspectives or participants in a particular type of event. A commercial transaction, for example, is a kind of event in which one entity trades money to another entity in return for some good or service, after which the good changes hands or perhaps the service is performed. This event can be encoded lexically by using verbs like buy (the event from the perspective of the buyer), sell (from the perspective of the seller), pay (focusing on the monetary aspect), or nouns like buyer. Frames have semantic roles (like buyer, seller, goods, money), and words in a sentence can take on these roles.

Knowing that buy and sell have this relation makes it possible for a system to know that a sentence like Sam bought the book from Ling could be paraphrased as Ling sold the book to Sam, and that Sam has the role of the buyer in the frame and Ling the seller. Being able to recognize such paraphrases is important for question answering, and can help in shifting perspective for machine translation.

Connotation  
Finally, words have affective meanings or connotations. The word connotation has different meanings in different fields, but here we use it to mean the aspects of a word’s meaning that are related to a writer or reader’s emotions, sentiment, opinions, or evaluations. For example some words have positive connotations (wonderful) while others have negative connotations (dreary). Even words whose meanings are similar in other ways can vary in connotation; consider the difference in connotations between fake, knockoff, forgery, on the one hand, and copy, replica, reproduction on the other, or innocent (positive connotation) and naive (negative connotation). Some words describe positive evaluation (great, love) and others negative evaluation (terrible, hate). Positive or negative evaluation language is called sentiment, as we saw in Chapter 4, and word sentiment plays a role in important tasks like sentiment analysis, stance detection, and applications of NLP to the language of politics and consumer reviews.

Early work on affective meaning (Osgood et al., 1957) found that words varied along three important dimensions of affective meaning:

- **valence:** the pleasantness of the stimulus
- **arousal:** the intensity of emotion provoked by the stimulus
- **dominance:** the degree of control exerted by the stimulus

Thus words like happy or satisfied are high on valence, while unhappy or annoyed are low on valence. Excited is high on arousal, while calm is low on arousal. Controlling is high on dominance, while awed or influenced are low on dominance. Each word is thus represented by three numbers, corresponding to its value on each of the three dimensions:
Osgood et al. (1957) noticed that in using these 3 numbers to represent the meaning of a word, the model was representing each word as a point in a three-dimensional space, a vector whose three dimensions corresponded to the word’s rating on the three scales. This revolutionary idea that word meaning could be represented as a point in space (e.g., that part of the meaning of heartbreak can be represented as the point [2.45, 5.65, 3.58]) was the first expression of the vector semantics models that we introduce next.

### 6.2 Vector Semantics

**Vector semantics** is the standard way to represent word meaning in NLP, helping us model many of the aspects of word meaning we saw in the previous section. The roots of the model lie in the 1950s when two big ideas converged: Osgood’s 1957 idea mentioned above to use a point in three-dimensional space to represent the connotation of a word, and the proposal by linguists like Joos (1950), Harris (1954), and Firth (1957) to define the meaning of a word by its *distribution* in language use, meaning its neighboring words or grammatical environments. Their idea was that two words that occur in very similar distributions (whose neighboring words are similar) have similar meanings.

For example, suppose you didn’t know the meaning of the word *ongchoi* (a recent borrowing from Cantonese) but you see it in the following contexts:

(6.1) Ongchoi is delicious sauteed with garlic.
(6.2) Ongchoi is superb over rice.
(6.3) ...ongchoi leaves with salty sauces...

And suppose that you had seen many of these context words in other contexts:

(6.4) ...spinach sauteed with garlic over rice...
(6.5) ...chard stems and leaves are delicious...
(6.6) ...collard greens and other salty leafy greens

The fact that ongchoi occurs with words like *rice* and *garlic* and *delicious* and *salty*, as do words like *spinach*, *chard*, and *collard greens* might suggest that ongchoi is a leafy green similar to these other leafy greens.\(^1\) We can do the same thing computationally by just counting words in the context of ongchoi.

The idea of vector semantics is to represent a word as a point in a multidimensional semantic space that is derived (in ways we’ll see) from the distributions of word neighbors. Vectors for representing words are called **embeddings** (although the term is sometimes more strictly applied only to dense vectors like word2vec (Section 6.8), rather than sparse tf-idf or PPMI vectors (Section 6.3-Section 6.6)). The word “embedding” derives from its mathematical sense as a mapping from one space or structure to another, although the meaning has shifted; see the end of the chapter.

\(^1\) It’s in fact *Ipomoea aquatica*, a relative of morning glory sometimes called *water spinach* in English.
Fig. 6.1 shows a visualization of embeddings learned for sentiment analysis, showing the location of selected words projected down from 60-dimensional space into a two-dimensional space. Notice the distinct regions containing positive words, negative words, and neutral function words.

The fine-grained model of word similarity of vector semantics offers enormous power to NLP applications. NLP applications like the sentiment classifiers of Chapter 4 or Chapter 5 depend on the same words appearing in the training and test sets. But by representing words as embeddings, classifiers can assign sentiment as long as it sees some words with similar meanings. And as we’ll see, vector semantic models can be learned automatically from text without supervision.

In this chapter we’ll introduce the two most commonly used models. In the tf-idf model, an important baseline, the meaning of a word is defined by a simple function of the counts of nearby words. We will see that this method results in very long vectors that are sparse, i.e., mostly zeros (since most words simply never occur in the context of others). We’ll introduce the word2vec model family for constructing short, dense vectors that have useful semantic properties. We’ll also introduce the cosine, the standard way to use embeddings to compute semantic similarity, between two words, two sentences, or two documents, an important tool in practical applications like question answering, summarization, or automatic essay grading.

6.3 Words and Vectors

“The most important attributes of a vector in 3-space are {Location, Location, Location}”

Randall Munroe, https://xkcd.com/2358/

Vector or distributional models of meaning are generally based on a co-occurrence matrix, a way of representing how often words co-occur. We’ll look at two popular matrices: the term-document matrix and the term-term matrix.

6.3.1 Vectors and documents

In a term-document matrix, each row represents a word in the vocabulary and each column represents a document from some collection of documents. Fig. 6.2 shows a small selection from a term-document matrix showing the occurrence of four words in four plays by Shakespeare. Each cell in this matrix represents the number of times
a particular word (defined by the row) occurs in a particular document (defined by the column). Thus *fool* appeared 58 times in *Twelfth Night*.

<table>
<thead>
<tr>
<th></th>
<th>As You Like It</th>
<th>Twelfth Night</th>
<th>Julius Caesar</th>
<th>Henry V</th>
</tr>
</thead>
<tbody>
<tr>
<td>battle</td>
<td>1</td>
<td>0</td>
<td>7</td>
<td>13</td>
</tr>
<tr>
<td>good</td>
<td>114</td>
<td>80</td>
<td>62</td>
<td>89</td>
</tr>
<tr>
<td>fool</td>
<td>36</td>
<td>58</td>
<td>1</td>
<td>4</td>
</tr>
<tr>
<td>wit</td>
<td>20</td>
<td>15</td>
<td>2</td>
<td>3</td>
</tr>
</tbody>
</table>

*Figure 6.2* The term-document matrix for four words in four Shakespeare plays. Each cell contains the number of times the (row) word occurs in the (column) document.

The term-document matrix of Fig. 6.2 was first defined as part of the vector space model of information retrieval (Salton, 1971). In this model, a document is represented as a count vector, a column in Fig. 6.3.

To review some basic linear algebra, a vector is, at heart, just a list or array of numbers. So *As You Like It* is represented as the list \([1, 114, 36, 20]\) (the first column vector in Fig. 6.3) and *Julius Caesar* is represented as the list \([7, 62, 1, 2]\) (the third column vector). A vector space is a collection of vectors, characterized by their dimension. In the example in Fig. 6.3, the document vectors are of dimension 4, just so they fit on the page; in real term-document matrices, the vectors representing each document would have dimensionality \(|V|\), the vocabulary size.

The ordering of the numbers in a vector space indicates different dimensions on which documents vary. Thus the first dimension for both these vectors corresponds to the number of times the word *battle* occurs, and we can compare each dimension, noting for example that the vectors for *As You Like It* and *Twelfth Night* have similar values (1 and 0, respectively) for the first dimension.

We can think of the vector for a document as a point in \(|V|\)-dimensional space; thus the documents in Fig. 6.3 are points in 4-dimensional space. Since 4-dimensional spaces are hard to visualize, Fig. 6.4 shows a visualization in two dimensions; we’ve arbitrarily chosen the dimensions corresponding to the words *battle* and *fool*.

Term-document matrices were originally defined as a means of finding similar documents for the task of document information retrieval. Two documents that are similar will tend to have similar words, and if two documents have similar words their column vectors will tend to be similar. The vectors for the comedies *As You Like It* \([1, 114, 36, 20]\) and *Twelfth Night* \([0, 80, 58, 15]\) look a lot more like each other (more fools and wit than battles) than they look like *Julius Caesar* \([7, 62, 1, 2]\) or *Henry V* \([13, 89, 4, 3]\). This is clear with the raw numbers; in the first dimension (battle) the comedies have low numbers and the others have high numbers, and we can see it visually in Fig. 6.4; we’ll see very shortly how to quantify this intuition more formally.

A real term-document matrix, of course, wouldn’t just have 4 rows and columns, let alone 2. More generally, the term-document matrix has \(|V|\) rows (one for each word type in the vocabulary) and \(D\) columns (one for each document in the collec-
### 6.3 Words as vectors: document dimensions

We’ve seen that documents can be represented as vectors in a vector space. But vector semantics can also be used to represent the meaning of words. We do this by associating each word with a word vector—a row vector rather than a column vector, hence with different dimensions, as shown in Fig. 6.5. The four dimensions of the vector for *fool*, [36,58,1,4], correspond to the four Shakespeare plays. Word counts in the same four dimensions are used to form the vectors for the other 3 words: *wit*, [20,15,2,3]; *battle*, [1,0,7,13]; and *good* [114,80,62,89].

![Figure 6.5](image_url)  
**Figure 6.5** The term-document matrix for four words in four Shakespeare plays. The red boxes show that each word is represented as a row vector of length four.

For documents, we saw that similar documents had similar vectors, because similar documents tend to have similar words. This same principle applies to words: similar words have similar vectors because they tend to occur in similar documents. The term-document matrix thus lets us represent the meaning of a word by the documents it tends to occur in.
6.3.3 Words as vectors: word dimensions

An alternative to using the term-document matrix to represent words as vectors of document counts, is to use the term-term matrix, also called the word-word matrix or the term-context matrix, in which the columns are labeled by words rather than documents. This matrix is thus of dimensionality \(|V| \times |V|\) and each cell records the number of times the row (target) word and the column (context) word co-occur in some context in some training corpus. The context could be the document, in which case the cell represents the number of times the two words appear in the same document. It is most common, however, to use smaller contexts, generally a window around the word, for example of 4 words to the left and 4 words to the right, in which case the cell represents the number of times (in some training corpus) the column word occurs in such a \(\pm 4\) word window around the row word. Here are four examples of words in their windows:

- is traditionally followed by cherry pie, a traditional dessert
- often mixed, such as strawberry rhubarb pie. Apple pie computer peripherals and personal digital assistants. These devices usually a computer. This includes information available on the internet

If we then take every occurrence of each word (say strawberry) and count the context words around it, we get a word-word co-occurrence matrix. Fig. 6.6 shows a simplified subset of the word-word co-occurrence matrix for these four words computed from the Wikipedia corpus (Davies, 2015).

| aardvark | ... | computer | data | result | pie | sugar | ...
|---------|-----|----------|------|--------|-----|-------|-----
| cherry  | 0   | ...      | 2    | 8      | 9   | 442   | 25  |
| strawberry | 0 | ... | 0    | 0      | 1   | 60    | 19  |
| digital | 0   | ...      | 1670 | 1683   | 85  | 5     | 4   |
| information | 0 | ... | 3325 | 3982   | 378 | 5     | 13  |

Figure 6.6 Co-occurrence vectors for four words in the Wikipedia corpus, showing six of the dimensions (hand-picked for pedagogical purposes). The vector for digital is outlined in red. Note that a real vector would have vastly more dimensions and thus be much sparser.

Note in Fig. 6.6 that the two words cherry and strawberry are more similar to each other (both pie and sugar tend to occur in their window) than they are to other words like digital; conversely, digital and information are more similar to each other than, say, to strawberry. Fig. 6.7 shows a spatial visualization.

Note that \(|V|\), the dimensionality of the vector, is generally the size of the vocabulary, often between 10,000 and 50,000 words (using the most frequent words
in the training corpus; keeping words after about the most frequent 50,000 or so is generally not helpful). Since most of these numbers are zero these are sparse vector representations; there are efficient algorithms for storing and computing with sparse matrices.

Now that we have some intuitions, let’s move on to examine the details of computing word similarity. Afterwards we’ll discuss methods for weighting cells.

### 6.4 Cosine for measuring similarity

To measure similarity between two target words \( v \) and \( w \), we need a metric that takes two vectors (of the same dimensionality, either both with words as dimensions, hence of length \( |V| \), or both with documents as dimensions, of length \( |D| \)) and gives a measure of their similarity. By far the most common similarity metric is the cosine of the angle between the two vectors.

The cosine—like most measures for vector similarity used in NLP—is based on the dot product operator from linear algebra, also called the inner product:

\[
\text{dot product}(v, w) = v \cdot w = \sum_{i=1}^{N} v_i w_i = v_1 w_1 + v_2 w_2 + \ldots + v_N w_N \quad (6.7)
\]

The dot product acts as a similarity metric because it will tend to be high just when the two vectors have large values in the same dimensions. Alternatively, vectors that have zeros in different dimensions—orthogonal vectors—will have a dot product of 0, representing their strong dissimilarity.

This raw dot product, however, has a problem as a similarity metric: it favors long vectors. The vector length is defined as

\[
|v| = \sqrt{\sum_{i=1}^{N} v_i^2} \quad (6.8)
\]

The dot product is higher if a vector is longer, with higher values in each dimension. More frequent words have longer vectors, since they tend to co-occur with more words and have higher co-occurrence values with each of them. The raw dot product thus will be higher for frequent words. But this is a problem; we’d like a similarity metric that tells us how similar two words are regardless of their frequency.

We modify the dot product to normalize for the vector length by dividing the dot product by the lengths of each of the two vectors. This normalized dot product turns out to be the same as the cosine of the angle between the two vectors, following from the definition of the dot product between two vectors \( a \) and \( b \):

\[
\frac{a \cdot b}{|a||b|} = \cos \theta \quad (6.9)
\]

The cosine similarity metric between two vectors \( v \) and \( w \) thus can be computed as:
6.5 TF-IDF: Weighing terms in the vector

The co-occurrence matrices above represent each cell by frequencies, either of words with documents (Fig. 6.5), or words with other words (Fig. 6.6). But raw frequency

\[
\text{cosine}(v, w) = \frac{v \cdot w}{|v| |w|} = \frac{\sum_{i=1}^{N} v_i w_i}{\sqrt{\sum_{i=1}^{N} v_i^2} \sqrt{\sum_{i=1}^{N} w_i^2}}
\]

For some applications we pre-normalize each vector, by dividing it by its length, creating a unit vector of length 1. Thus we could compute a unit vector from \( a \) by dividing it by \( |a| \). For unit vectors, the dot product is the same as the cosine.

The cosine value ranges from 1 for vectors pointing in the same direction, through 0 for orthogonal vectors, to -1 for vectors pointing in opposite directions. But since raw frequency values are non-negative, the cosine for these vectors ranges from 0–1.

Let’s see how the cosine computes which of the words cherry or digital is closer in meaning to information, just using raw counts from the following shortened table:

<table>
<thead>
<tr>
<th></th>
<th>pie</th>
<th>data</th>
<th>computer</th>
</tr>
</thead>
<tbody>
<tr>
<td>cherry</td>
<td>442</td>
<td>8</td>
<td>2</td>
</tr>
<tr>
<td>digital</td>
<td>5</td>
<td>1683</td>
<td>1670</td>
</tr>
<tr>
<td>information</td>
<td>5</td>
<td>3982</td>
<td>3325</td>
</tr>
</tbody>
</table>

\[
\cos(\text{cherry, information}) = \frac{442 \times 5 + 8 \times 3982 + 2 \times 3325}{\sqrt{442^2 + 8^2 + 2^2} \sqrt{3982^2 + 3325^2}} = .018
\]

\[
\cos(\text{digital, information}) = \frac{5 \times 5 + 1683 \times 3982 + 1670 \times 3325}{\sqrt{5^2 + 1683^2 + 1670^2} \sqrt{3982^2 + 3325^2}} = .996
\]

The model decides that information is way closer to digital than it is to cherry, a result that seems sensible. Fig. 6.8 shows a visualization.

---

**Figure 6.8** A (rough) graphical demonstration of cosine similarity, showing vectors for three words (cherry, digital, and information) in the two dimensional space defined by counts of the words computer and pie nearby. The figure doesn’t show the cosine, but it highlights the angles; note that the angle between digital and information is smaller than the angle between cherry and information. When two vectors are more similar, the cosine is larger but the angle is smaller; the cosine has its maximum (1) when the angle between two vectors is smallest (0°); the cosine of all other angles is less than 1.

6.5 TF-IDF: Weighing terms in the vector

The co-occurrence matrices above represent each cell by frequencies, either of words with documents (Fig. 6.5), or words with other words (Fig. 6.6). But raw frequency
is not the best measure of association between words. Raw frequency is very skewed and not very discriminative. If we want to know what kinds of contexts are shared by cherry and strawberry but not by digital and information, we’re not going to get good discrimination from words like the, it, or they, which occur frequently with all sorts of words and aren’t informative about any particular word. We saw this also in Fig. 6.3 for the Shakespeare corpus; the dimension for the word good is not very discriminative between plays; good is simply a frequent word and has roughly equivalent high frequencies in each of the plays.

It’s a bit of a paradox. Words that occur nearby frequently (maybe pie nearby cherry) are more important than words that only appear once or twice. Yet words that are too frequent—ubiquitous, like the or good—are unimportant. How can we balance these two conflicting constraints?

There are two common solutions to this problem: in this section we’ll describe the tf-idf weighting, usually used when the dimensions are documents. In the next we introduce the PPMI algorithm (usually used when the dimensions are words).

The tf-idf weighting (the ‘-’ here is a hyphen, not a minus sign) is the product of two terms, each term capturing one of these two intuitions:

The first is the term frequency (Luhn, 1957): the frequency of the word \( t \) in the document \( d \). We can just use the raw count as the term frequency:

\[
\text{tf}_{t,d} = \text{count}(t,d) \quad (6.11)
\]

More commonly we squash the raw frequency a bit, by using the \( \log_{10} \) of the frequency instead. The intuition is that a word appearing 100 times in a document doesn’t make that word 100 times more likely to be relevant to the meaning of the document. We also need to do something special with counts of 0, since we can’t take the log of 0.\(^2\)

\[
\text{tf}_{t,d} = \begin{cases} 
1 + \log_{10} \text{count}(t,d) & \text{if } \text{count}(t,d) > 0 \\
0 & \text{otherwise} 
\end{cases} \quad (6.12)
\]

If we use log weighting, terms which occur 0 times in a document would have \( \text{tf} = 0 \), 1 times in a document \( \text{tf} = 1 + \log_{10}(1) = 1 + 0 = 1 \), 10 times in a document \( \text{tf} = 1 + \log_{10}(10) = 2 \), 100 times \( \text{tf} = 1 + \log_{10}(100) = 3 \), 1000 times \( \text{tf} = 4 \), and so on.

The second factor in tf-idf is used to give a higher weight to words that occur only in a few documents. Terms that are limited to a few documents are useful for discriminating those documents from the rest of the collection; terms that occur frequently across the entire collection aren’t as helpful. The document frequency \( df \), of a term \( t \) is the number of documents it occurs in. Document frequency is not the same as the collection frequency of a term, which is the total number of times the word appears in the whole collection in any document. Consider in the collection of Shakespeare’s 37 plays the two words Romeo and action. The words have identical collection frequencies (they both occur 113 times in all the plays) but very different document frequencies, since Romeo only occurs in a single play. If our goal is to find documents about the romantic tribulations of Romeo, the word Romeo should be highly weighted, but not action:

<table>
<thead>
<tr>
<th>Collection Frequency</th>
<th>Document Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Romeo</td>
<td>113</td>
</tr>
<tr>
<td>action</td>
<td>113</td>
</tr>
</tbody>
</table>

\(^2\) We can also use this alternative formulation, which we have used in earlier editions: \( \text{tf}_{t,d} = \log_{10}(\text{count}(t,d) + 1) \)
6.5 • TF-IDF: Weighing Terms in the Vector

We emphasize discriminative words like *Romeo* via the **inverse document frequency** or **idf** term weight (Sparck Jones, 1972). The idf is defined using the fraction $N/df_t$, where $N$ is the total number of documents in the collection, and $df_t$ is the number of documents in which term $t$ occurs. The fewer documents in which a term occurs, the higher this weight. The lowest weight of 1 is assigned to terms that occur in all the documents. It’s usually clear what counts as a document: in Shakespeare we would use a play; when processing a collection of encyclopedia articles like Wikipedia, the document is a Wikipedia page; in processing newspaper articles, the document is a single article. Occasionally your corpus might not have appropriate document divisions and you might need to break up the corpus into documents yourself for the purposes of computing idf.

Because of the large number of documents in many collections, this measure too is usually squashed with a log function. The resulting definition for inverse document frequency (idf) is thus

$$
\text{idf}_t = \log_{10} \left( \frac{N}{df_t} \right)
$$

(6.13)

Here are some idf values for some words in the Shakespeare corpus, ranging from extremely informative words which occur in only one play like *Romeo*, to those that occur in a few like *salad* or *Falstaff*, to those which are very common like *fool* or so common as to be completely non-discriminative since they occur in all 37 plays like *good* or *sweet.*

<table>
<thead>
<tr>
<th>Word</th>
<th>df</th>
<th>idf</th>
</tr>
</thead>
<tbody>
<tr>
<td>Romeo</td>
<td>1</td>
<td>1.57</td>
</tr>
<tr>
<td>salad</td>
<td>2</td>
<td>1.27</td>
</tr>
<tr>
<td>Falstaff</td>
<td>4</td>
<td>0.967</td>
</tr>
<tr>
<td>forest</td>
<td>12</td>
<td>0.489</td>
</tr>
<tr>
<td>battle</td>
<td>21</td>
<td>0.246</td>
</tr>
<tr>
<td>wit</td>
<td>34</td>
<td>0.037</td>
</tr>
<tr>
<td>fool</td>
<td>36</td>
<td>0.012</td>
</tr>
<tr>
<td>good</td>
<td>37</td>
<td>0</td>
</tr>
<tr>
<td>sweet</td>
<td>37</td>
<td>0</td>
</tr>
</tbody>
</table>

The **tf-idf** weighted value $w_{t,d}$ for word $t$ in document $d$ thus combines term frequency $tf_{t,d}$ (defined either by Eq. 6.11 or by Eq. 6.12) with idf from Eq. 6.13:

$$
w_{t,d} = tf_{t,d} \times \text{idf}_t
$$

(6.14)

Fig. 6.9 applies tf-idf weighting to the Shakespeare term-document matrix in Fig. 6.2, using the tf equation Eq. 6.12. Note that the tf-idf values for the dimension corresponding to the word *good* have now all become 0; since this word appears in every document, the tf-idf weighting leads it to be ignored. Similarly, the word *fool*, which appears in 36 out of the 37 plays, has a much lower weight.

The tf-idf weighting is the way for weighting co-occurrence matrices in information retrieval, but also plays a role in many other aspects of natural language processing. It’s also a great baseline, the simple thing to try first. We’ll look at other weightings like PPMI (Positive Pointwise Mutual Information) in Section 6.6.

---

*Sweet* was one of Shakespeare’s favorite adjectives, a fact probably related to the increased use of sugar in European recipes around the turn of the 16th century (Jurafsky, 2014, p. 175).
6.6 Pointwise Mutual Information (PMI)

An alternative weighting function to tf-idf, PPMI (positive pointwise mutual information), is used for term-term-matrices, when the vector dimensions correspond to words rather than documents. PPMI draws on the intuition that the best way to weigh the association between two words is to ask how much more the two words co-occur in our corpus than we would have a priori expected them to appear by chance.

Pointwise mutual information (Fano, 1961)\(^4\) is one of the most important concepts in NLP. It is a measure of how often two events \(x\) and \(y\) occur, compared with what we would expect if they were independent:

\[
I(x, y) = \log_2 \frac{P(x, y)}{P(x)P(y)} \tag{6.16}
\]

The pointwise mutual information between a target word \(w\) and a context word \(c\) (Church and Hanks 1989, Church and Hanks 1990) is then defined as:

\[
\text{PMI}(w, c) = \log_2 \frac{P(w, c)}{P(w)P(c)} \tag{6.17}
\]

The numerator tells us how often we observed the two words together (assuming we compute probability by using the MLE). The denominator tells us how often we would expect the two words to co-occur assuming they each occurred independently: recall that the probability of two independent events both occurring is just the product of the probabilities of the two events. Thus, the ratio gives us an estimate of how much more the two words co-occur than we expect by chance. PMI is a useful tool whenever we need to find words that are strongly associated.

PMI values range from negative to positive infinity. But negative PMI values (which imply things are co-occurring less often than we would expect by chance) tend to be unreliable unless our corpora are enormous. To distinguish whether two words whose individual probability is each \(10^{-6}\) occur together less often than chance, we would need to be certain that the probability of the two occurring together is significantly less than \(10^{-12}\), and this kind of granularity would require an enormous corpus. Furthermore it’s not clear whether it’s even possible to evaluate such scores of ‘unrelatedness’ with human judgments. For this reason it is more

---

\(^4\) PMI is based on the **mutual information** between two random variables \(X\) and \(Y\), defined as:

\[
I(X, Y) = \sum_x \sum_y P(x, y)\log_2 \frac{P(x, y)}{P(x)P(y)} \tag{6.15}
\]

In a confusion of terminology, Fano used the phrase **mutual information** to refer to what we now call pointwise mutual information and the phrase **expectation of the mutual information** for what we now call mutual information.
common to use Positive PMI (called PPMI) which replaces all negative PMI values with zero (Church and Hanks 1989, Dagan et al. 1993, Niwa and Nitta 1994):

$$\text{PPMI}(w, c) = \max\left(\log_2 \frac{P(w, c)}{P(w)P(c)}, 0\right)$$  \hspace{1cm} (6.18)

More formally, let’s assume we have a co-occurrence matrix $F$ with $W$ rows (words) and $C$ columns (contexts), where $f_{ij}$ gives the number of times word $w_i$ occurs with context $c_j$. This can be turned into a PPMI matrix where $\text{PPMI}_{ij}$ gives the PMI value of word $w_i$ with context $c_j$ (which we can also express as $\text{PPMI}(w_i, c_j)$ or $\text{PPMI}(w = i, c = j)$) as follows:

$$P_{ij} = \frac{f_{ij}}{\sum_{i=1}^{W} \sum_{j=1}^{C} f_{ij}}, \quad P_{i*} = \frac{\sum_{j=1}^{C} f_{ij}}{\sum_{i=1}^{W} \sum_{j=1}^{C} f_{ij}}, \quad P_{*j} = \frac{\sum_{i=1}^{W} f_{ij}}{\sum_{i=1}^{W} \sum_{j=1}^{C} f_{ij}}$$  \hspace{1cm} (6.19)

$$\text{PPMI}_{ij} = \max\left(\log_2 \frac{P_{ij}}{P_{i*}P_{*j}}, 0\right)$$  \hspace{1cm} (6.20)

Let’s see some PPMI calculations. We’ll use Fig. 6.10, which repeats Fig. 6.6 plus all the count marginals, and let’s pretend for ease of calculation that these are the only words/contexts that matter.

<table>
<thead>
<tr>
<th></th>
<th>computer</th>
<th>data</th>
<th>result</th>
<th>pie</th>
<th>sugar</th>
<th>count(w)</th>
</tr>
</thead>
<tbody>
<tr>
<td>cherry</td>
<td>2</td>
<td>8</td>
<td>9</td>
<td>442</td>
<td>25</td>
<td>486</td>
</tr>
<tr>
<td>strawberry</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>60</td>
<td>19</td>
<td>80</td>
</tr>
<tr>
<td>digital</td>
<td>1670</td>
<td>1683</td>
<td>85</td>
<td>5</td>
<td>4</td>
<td>3447</td>
</tr>
<tr>
<td>information</td>
<td>3325</td>
<td>3982</td>
<td>378</td>
<td>5</td>
<td>13</td>
<td>7703</td>
</tr>
<tr>
<td>count(context)</td>
<td>4997</td>
<td>5673</td>
<td>473</td>
<td>512</td>
<td>61</td>
<td>11716</td>
</tr>
</tbody>
</table>

**Figure 6.10** Co-occurrence counts for four words in 5 contexts in the Wikipedia corpus, together with the marginals, pretending for the purpose of this calculation that no other words/contexts matter.

Thus for example we could compute $\text{PPMI}(\text{information}, \text{data})$, assuming we pretended that Fig. 6.6 encompassed all the relevant word contexts/dimensions, as follows:

$$P(w=\text{information}, c=\text{data}) = \frac{3982}{11716} = .3399$$

$$P(w=\text{information}) = \frac{7703}{11716} = .6575$$

$$P(c=\text{data}) = \frac{5673}{11716} = .4842$$

$$\text{PPMI}(\text{information}, \text{data}) = \log_2(.3399/(.6575 \times .4842)) = .0944$$

Fig. 6.11 shows the joint probabilities computed from the counts in Fig. 6.10, and Fig. 6.12 shows the PPMI values. Not surprisingly, *cherry* and *strawberry* are highly associated with both *pie* and *sugar*, and *data* is mildly associated with *information*.

PMI has the problem of being biased toward infrequent events; very rare words tend to have very high PMI values. One way to reduce this bias toward low frequency

---

5 Positive PMI also cleanly solves the problem of what to do with zero counts, using 0 to replace the $-\infty$ from $\log(0)$.
events is to slightly change the computation for $P(c)$, using a different function $P_\alpha(c)$ that raises the probability of the context word to the power of $\alpha$:

$$PPMI_\alpha(w,c) = \max(\log_2 \frac{P(w,c)}{P(w)P_\alpha(c)}, 0)$$

(6.21)

$$P_\alpha(c) = \frac{\text{count}(c)^\alpha}{\sum_c \text{count}(c)^\alpha}$$

(6.22)

Levy et al. (2015) found that a setting of $\alpha = 0.75$ improved performance of embeddings on a wide range of tasks (drawing on a similar weighting used for skip-grams described below in Eq. 6.32). This works because raising the count to $\alpha = 0.75$ increases the probability assigned to rare contexts, and hence lowers their PMI ($P_\alpha(c) > P(c)$ when $c$ is rare).

Another possible solution is Laplace smoothing: Before computing PMI, a small constant $k$ (values of 0.1-3 are common) is added to each of the counts, shrinking (discounting) all the non-zero values. The larger the $k$, the more the non-zero counts are discounted.

### 6.7 Applications of the tf-idf or PPMI vector models

In summary, the vector semantics model we’ve described so far represents a target word as a vector with dimensions corresponding either to the documents in a large collection (the term-document matrix) or to the counts of words in some neighboring window (the term-term matrix). The values in each dimension are counts, weighted by tf-idf (for term-document matrices) or PPMI (for term-term matrices), and the vectors are sparse (since most values are zero).

The model computes the similarity between two words $x$ and $y$ by taking the cosine of their tf-idf or PPMI vectors; high cosine, high similarity. This entire model
6.8 Word2vec

is sometimes referred to as the tf-idf model or the PPMI model, after the weighting function.

The tf-idf model of meaning is often used for document functions like deciding if two documents are similar. We represent a document by taking the vectors of all the words in the document, and computing the centroid of all those vectors. The centroid is the multidimensional version of the mean; the centroid of a set of vectors is a single vector that has the minimum sum of squared distances to each of the vectors in the set. Given \( k \) word vectors \( w_1, w_2, \ldots, w_k \), the centroid document vector \( d \) is:

\[
d = \frac{w_1 + w_2 + \ldots + w_k}{k}
\]  

(6.23)

Given two documents, we can then compute their document vectors \( d_1 \) and \( d_2 \), and estimate the similarity between the two documents by \( \cos(d_1, d_2) \). Document similarity is also useful for all sorts of applications; information retrieval, plagiarism detection, news recommender systems, and even for digital humanities tasks like comparing different versions of a text to see which are similar to each other.

Either the PPMI model or the tf-idf model can be used to compute word similarity, for tasks like finding word paraphrases, tracking changes in word meaning, or automatically discovering meanings of words in different corpora. For example, we can find the 10 most similar words to any target word \( w \) by computing the cosines between \( w \) and each of the \( V - 1 \) other words, sorting, and looking at the top 10.

6.8 Word2vec

In the previous sections we saw how to represent a word as a sparse, long vector with dimensions corresponding to words in the vocabulary or documents in a collection. We now introduce a more powerful word representation: embeddings, short dense vectors. Unlike the vectors we’ve seen so far, embeddings are short, with number of dimensions \( d \) ranging from 50-1000, rather than the much larger vocabulary size \( |V| \) or number of documents \( D \) we’ve seen. These \( d \) dimensions don’t have a clear interpretation. And the vectors are dense: instead of vector entries being sparse, mostly-zero counts or functions of counts, the values will be real-valued numbers that can be negative.

It turns out that dense vectors work better in every NLP task than sparse vectors. While we don’t completely understand all the reasons for this, we have some intuitions. Representing words as 300-dimensional dense vectors requires our classifiers to learn far fewer weights than if we represented words as 50,000-dimensional vectors, and the smaller parameter space possibly helps with generalization and avoiding overfitting. Dense vectors may also do a better job of capturing synonymy. For example, in a sparse vector representation, dimensions for synonyms like car and automobile dimension are distinct and unrelated; sparse vectors may thus fail to capture the similarity between a word with car as a neighbor and a word with automobile as a neighbor.

In this section we introduce one method for computing embeddings: skip-gram with negative sampling, sometimes called SGNS. The skip-gram algorithm is one of two algorithms in a software package called word2vec, and so sometimes the algorithm is loosely referred to as word2vec (Mikolov et al. 2013a, Mikolov et al. 2013b). The word2vec methods are fast, efficient to train, and easily available on-
line with code and pretrained embeddings. Word2vec embeddings are static embeddings, meaning that the method learns one fixed embedding for each word in the vocabulary. In Chapter 11 we’ll introduce methods for learning dynamic contextual embeddings like the popular family of BERT representations, in which the vector for each word is different in different contexts.

The intuition of word2vec is that instead of counting how often each word \( w \) occurs near, say, apricot, we’ll instead train a classifier on a binary prediction task: “Is word \( w \) likely to show up near apricot?” We don’t actually care about this prediction task; instead we’ll take the learned classifier weights as the word embeddings.

The revolutionary intuition here is that we can just use running text as implicitly supervised training data for such a classifier; a word \( c \) that occurs near the target word apricot acts as gold ‘correct answer’ to the question “Is word \( c \) likely to show up near apricot?” This method, often called self-supervision, avoids the need for any sort of hand-labeled supervision signal. This idea was first proposed in the task of neural language modeling, when Bengio et al. (2003) and Collobert et al. (2011) showed that a neural language model (a neural network that learned to predict the next word from prior words) could just use the next word in running text as its supervision signal, and could be used to learn an embedding representation for each word as part of doing this prediction task.

We’ll see how to do neural networks in the next chapter, but word2vec is a much simpler model than the neural network language model, in two ways. First, word2vec simplifies the task (making it binary classification instead of word prediction). Second, word2vec simplifies the architecture (training a logistic regression classifier instead of a multi-layer neural network with hidden layers that demand more sophisticated training algorithms). The intuition of skip-gram is:

1. Treat the target word and a neighboring context word as positive examples.
2. Randomly sample other words in the lexicon to get negative samples.
3. Use logistic regression to train a classifier to distinguish those two cases.
4. Use the learned weights as the embeddings.

### 6.8.1 The classifier

Let’s start by thinking about the classification task, and then turn to how to train. Imagine a sentence like the following, with a target word apricot, and assume we’re using a window of \( \pm 2 \) context words:

... lemon, a [tablespoon of apricot jam, a] pinch ...

\[ c_1 \quad c_2 \quad w \quad c_3 \quad c_4 \]

Our goal is to train a classifier such that, given a tuple \((w, c)\) of a target word \( w \) paired with a candidate context word \( c \) (for example (apricot, jam), or perhaps (apricot, aardvark)) it will return the probability that \( c \) is a real context word (true for jam, false for aardvark):

\[
P(+|w, c)
\]

(6.24)

The probability that word \( c \) is not a real context word for \( w \) is just 1 minus Eq. 6.24:

\[
P(-|w, c) = 1 - P(+|w, c)
\]

(6.25)

How does the classifier compute the probability \( P \)? The intuition of the skip-gram model is to base this probability on embedding similarity: a word is likely to
occur near the target if its embedding vector is similar to the target embedding. To compute similarity between these dense embeddings, we rely on the intuition that two vectors are similar if they have a high dot product (after all, cosine is just a normalized dot product). In other words:

\[ \text{Similarity}(w, c) \approx c \cdot w \]  

(6.26)

The dot product \( c \cdot w \) is not a probability, it’s just a number ranging from \(-\infty\) to \(\infty\) (since the elements in word2vec embeddings can be negative, the dot product can be negative). To turn the dot product into a probability, we’ll use the logistic or sigmoid function \( \sigma(x) \), the fundamental core of logistic regression:

\[ \sigma(x) = \frac{1}{1 + \exp(-x)} \]  

(6.27)

We model the probability that word \( c \) is a real context word for target word \( w \) as:

\[ P(+|w, c) = \sigma(c \cdot w) = \frac{1}{1 + \exp(-c \cdot w)} \]  

(6.28)

The sigmoid function returns a number between 0 and 1, but to make it a probability we’ll also need the total probability of the two possible events (\( c \) is a context word, and \( c \) isn’t a context word) to sum to 1. We thus estimate the probability that word \( c \) is not a real context word for \( w \) as:

\[ P(-|w, c) = 1 - P(+|w, c) \]
\[ = \sigma(-c \cdot w) = \frac{1}{1 + \exp(c \cdot w)} \]  

(6.29)

Equation 6.28 gives us the probability for one word, but there are many context words in the window. Skip-gram makes the simplifying assumption that all context words are independent, allowing us to just multiply their probabilities:

\[ P(+|w, c_1:L) = \prod_{i=1}^{L} \sigma(c_i \cdot w) \]  

(6.30)

\[ \log P(+|w, c_1:L) = \sum_{i=1}^{L} \log \sigma(c_i \cdot w) \]  

(6.31)

In summary, skip-gram trains a probabilistic classifier that, given a test target word \( w \) and its context window of \( L \) words \( c_{1:L} \), assigns a probability based on how similar this context window is to the target word. The probability is based on applying the logistic (sigmoid) function to the dot product of the embeddings of the target word with each context word. To compute this probability, we just need embeddings for each target word and context word in the vocabulary.

Fig. 6.13 shows the intuition of the parameters we’ll need. Skip-gram actually stores two embeddings for each word, one for the word as a target, and one for the word considered as context. Thus the parameters we need to learn are two matrices \( \mathbf{W} \) and \( \mathbf{C} \), each containing an embedding for every one of the \(|V|\) words in the vocabulary \( V \). Let’s now turn to learning these embeddings (which is the real goal of training this classifier in the first place).

---

6 In principle the target matrix and the context matrix could use different vocabularies, but we’ll simplify by assuming one shared vocabulary \( V \).
6.8.2 Learning skip-gram embeddings

The learning algorithm for skip-gram embeddings takes as input a corpus of text, and a chosen vocabulary size N. It begins by assigning a random embedding vector for each of the N vocabulary words, and then proceeds to iteratively shift the embedding of each word \( w \) to be more like the embeddings of words that occur nearby in texts, and less like the embeddings of words that don’t occur nearby. Let’s start by considering a single piece of training data:

\[
\text{... lemon, a [tablespoon of apricot jam, a] pinch ...}
\]

This example has a target word \( w \) (apricot), and 4 context words in the \( L = \pm 2 \) window, resulting in 4 positive training instances (on the left below):

<table>
<thead>
<tr>
<th>positive examples +</th>
<th>negative examples -</th>
</tr>
</thead>
<tbody>
<tr>
<td>( w )</td>
<td>( c_{pos} )</td>
</tr>
<tr>
<td>apricot</td>
<td>tablespoon</td>
</tr>
<tr>
<td>apricot</td>
<td>of</td>
</tr>
<tr>
<td>apricot</td>
<td>jam</td>
</tr>
<tr>
<td>apricot</td>
<td>a</td>
</tr>
</tbody>
</table>

For training a binary classifier we also need negative examples. In fact skip-gram with negative sampling (SGNS) uses more negative examples than positive examples (with the ratio between them set by a parameter \( k \)). So for each of these \( (w, c_{pos}) \) training instances we’ll create \( k \) negative samples, each consisting of the target \( w \) plus a ‘noise word’ \( c_{neg} \). A noise word is a random word from the lexicon, constrained not to be the target word \( w \). The right above shows the setting where \( k = 2 \), so we’ll have 2 negative examples in the negative training set — for each positive example \( w, c_{pos} \).

The noise words are chosen according to their weighted unigram frequency \( p_\alpha(w) \), where \( \alpha \) is a weight. If we were sampling according to unweighted frequency \( p(w) \), it would mean that with unigram probability \( p(“the”) \) we would choose the word \( the \) as a noise word, with unigram probability \( p(“aardvark”) \) we would choose \( aardvark \), and so on. But in practice it is common to set \( \alpha = .75 \), i.e. use the
weighting $p^\frac{1}{2}(w)$:

$$P_\alpha(w) = \frac{\text{count}(w)^\alpha}{\sum_{w'} \text{count}(w')^\alpha} \quad (6.32)$$

Setting $\alpha = .75$ gives better performance because it gives rare noise words slightly higher probability: for rare words, $P_\alpha(w) > P(w)$. To illustrate this intuition, it might help to work out the probabilities for an example with two events, $P(a) = .99$ and $P(b) = .01$:

$$P_\alpha(a) = \frac{.99^{.75}}{.99^{.75} + .01^{.75}} = .97$$
$$P_\alpha(b) = \frac{.01^{.75}}{.99^{.75} + .01^{.75}} = .03 \quad (6.33)$$

Given the set of positive and negative training instances, and an initial set of embeddings, the goal of the learning algorithm is to adjust those embeddings to

- Maximize the similarity of the target word, context word pairs $(w, c_{\text{pos}})$ drawn from the positive examples
- Minimize the similarity of the $(w, c_{\text{neg}})$ pairs from the negative examples.

If we consider one word/context pair $(w, c_{\text{pos}})$ with its $k$ noise words $c_{\text{neg}1} \ldots c_{\text{neg}k}$, we can express these two goals as the following loss function $L$ to be minimized (hence the $-$); here the first term expresses that we want the classifier to assign the real context word $c_{\text{pos}}$ a high probability of being a neighbor, and the second term expresses that we want to assign each of the noise words $c_{\text{neg}}$ a high probability of being a non-neighbor, all multiplied because we assume independence:

$$L_{CE} = -\log \left[ P(+|w, c_{\text{pos}}) \prod_{i=1}^{k} P(-|w, c_{\text{neg}i}) \right]$$

$$= -\left[ \log P(+|w, c_{\text{pos}}) + \sum_{i=1}^{k} \log P(-|w, c_{\text{neg}i}) \right]$$

$$= -\left[ \log P(+|w, c_{\text{pos}}) + \sum_{i=1}^{k} \log (1 - P(+|w, c_{\text{neg}i})) \right]$$

$$= -\left[ \log \sigma(c_{\text{pos}} \cdot w) + \sum_{i=1}^{k} \log \sigma(-c_{\text{neg}i} \cdot w) \right] \quad (6.34)$$

That is, we want to maximize the dot product of the word with the actual context words, and minimize the dot products of the word with the $k$ negative sampled non-neighbor words.

We minimize this loss function using stochastic gradient descent. Fig. 6.14 shows the intuition of one step of learning.

To get the gradient, we need to take the derivative of Eq. 6.34 with respect to the different embeddings. It turns out the derivatives are the following (we leave the
proof as an exercise at the end of the chapter):

\[
\frac{\partial L_{CE}}{\partial c_{pos}} = \left[ \sigma(c_{pos} \cdot w) - 1 \right] w \quad (6.35)
\]

\[
\frac{\partial L_{CE}}{\partial c_{neg}} = \left[ \sigma(c_{neg} \cdot w) \right] w \quad (6.36)
\]

\[
\frac{\partial L_{CE}}{\partial w} = \left[ \sigma(c_{pos} \cdot w) - 1 \right] c_{pos} + \sum_{i=1}^{k} \left[ \sigma(c_{neg_i} \cdot w) \right] c_{neg_i} \quad (6.37)
\]

The update equations going from time step \( t \) to \( t + 1 \) in stochastic gradient descent are thus:

\[
c_{pos}^{t+1} = c_{pos}^t - \eta \left[ \sigma(c_{pos}^t \cdot w') - 1 \right] w' \quad (6.38)
\]

\[
c_{neg}^{t+1} = c_{neg}^t - \eta \left[ \sigma(c_{neg}^t \cdot w') \right] w' \quad (6.39)
\]

\[
w^{t+1} = w' - \eta \left[ \sigma(c_{pos}^t \cdot w') - 1 \right] c_{pos}^t + \sum_{i=1}^{k} \left[ \sigma(c_{neg_i}^t \cdot w') \right] c_{neg_i}^t \quad (6.40)
\]

Just as in logistic regression, then, the learning algorithm starts with randomly initialized \( W \) and \( C \) matrices, and then walks through the training corpus using gradient descent to move \( W \) and \( C \) so as to minimize the loss in Eq. 6.34 by making the updates in (Eq. 6.38)-(Eq. 6.40).

Recall that the skip-gram model learns two separate embeddings for each word \( i \): the target embedding \( w_i \) and the context embedding \( c_i \), stored in two matrices, the target matrix \( W \) and the context matrix \( C \). It’s common to just add them together, representing word \( i \) with the vector \( w_i + c_i \). Alternatively we can throw away the \( C \) matrix and just represent each word \( i \) by the vector \( w_i \).

As with the simple count-based methods like tf-idf, the context window size \( L \) affects the performance of skip-gram embeddings, and experiments often tune the parameter \( L \) on a devset.
6.8.3 Other kinds of static embeddings

There are many kinds of static embeddings. An extension of word2vec, **fasttext** (Bojanowski et al., 2017), addresses a problem with word2vec as we have presented it so far: it has no good way to deal with **unknown words**—words that appear in a test corpus but were unseen in the training corpus. A related problem is word sparsity, such as in languages with rich morphology, where some of the many forms for each noun and verb may only occur rarely. Fasttext deals with these problems by using subword models, representing each word as itself plus a bag of constituent n-grams, with special boundary symbols `<` and `>` added to each word. For example, with \( n = 3 \) the word *where* would be represented by the sequence `<where>` plus the character n-grams:

\[
<\text{wh}, \text{whe}, \text{her}, \text{ere}, \text{re}>
\]

Then a skipgram embedding is learned for each constituent n-gram, and the word *where* is represented by the sum of all of the embeddings of its constituent n-grams. Unknown words can then be presented only by the sum of the constituent n-grams. A fasttext open-source library, including pretrained embeddings for 157 languages, is available at [https://fasttext.cc](https://fasttext.cc).

Another very widely used static embedding model is GloVe (Pennington et al., 2014), short for Global Vectors, because the model is based on capturing global corpus statistics. GloVe is based on ratios of probabilities from the word-word co-occurrence matrix, combining the intuitions of count-based models like PPMI while also capturing the linear structures used by methods like word2vec.

It turns out that dense embeddings like word2vec actually have an elegant mathematical relationship with sparse embeddings like PPMI, in which word2vec can be seen as implicitly optimizing a shifted version of a PPMI matrix (Levy and Goldberg, 2014c).

6.9 Visualizing Embeddings

“I see well in many dimensions as long as the dimensions are around two.”

The late economist Martin Shubik

Visualizing embeddings is an important goal in helping understand, apply, and improve these models of word meaning. But how can we visualize a (for example) 100-dimensional vector?

The simplest way to visualize the meaning of a word \( w \) embedded in a space is to list the most similar words to \( w \) by sorting the vectors for all words in the vocabulary by their cosine with the vector for \( w \). For example, the 7 closest words to *frog* using a particular embeddings computed with the GloVe algorithm are: *frogs, toad, litoria, leptodactylii, rana, lizard*, and *eleutherodactylus* (Pennington et al., 2014).

Yet another visualization method is to use a clustering algorithm to show a hierarchical representation of which words are similar to others in the embedding space. The uncaptioned figure on the left uses hierarchical clustering of some embedding vectors for nouns as a visualization...
Probably the most common visualization method, however, is to project the 100 dimensions of a word down into 2 dimensions. Fig. 6.1 showed one such visualization, as does Fig. 6.16, using a projection method called t-SNE (van der Maaten and Hinton, 2008).

6.10 Semantic properties of embeddings

In this section we briefly summarize some of the semantic properties of embeddings that have been studied.

**Different types of similarity or association:** One parameter of vector semantic models that is relevant to both sparse tf-idf vectors and dense word2vec vectors is the size of the context window used to collect counts. This is generally between 1 and 10 words on each side of the target word (for a total context of 2-20 words).

The choice depends on the goals of the representation. Shorter context windows tend to lead to representations that are a bit more syntactic, since the information is coming from immediately nearby words. When the vectors are computed from short context windows, the most similar words to a target word \( w \) tend to be semantically similar words with the same parts of speech. When vectors are computed from long context windows, the highest cosine words to a target word \( w \) tend to be words that are topically related but not similar.

For example Levy and Goldberg (2014a) showed that using skip-gram with a window of ±2, the most similar words to the word *Hogwarts* (from the *Harry Potter* series) were names of other fictional schools: *Sunnydale* (from *Buffy the Vampire Slayer*) or *Evernight* (from a vampire series). With a window of ±5, the most similar words to *Hogwarts* were other words topically related to the *Harry Potter* series: *Dumbledore*, *Malfoy*, and *half-blood*.

It’s also often useful to distinguish two kinds of similarity or association between words (Schütze and Pedersen, 1993). Two words have **first-order co-occurrence** (sometimes called **syntagmatic association**) if they are typically nearby each other. Thus *wrote* is a first-order associate of *book* or *poem*. Two words have **second-order co-occurrence** (sometimes called **paradigmatic association**) if they have similar neighbors. Thus *wrote* is a second-order associate of words like *said* or *remarked*.

**Analogy/Relational Similarity:** Another semantic property of embeddings is their ability to capture relational meanings. In an important early vector space model of cognition, Rumelhart and Abrahamson (1973) proposed the **parallelogram model** for solving simple analogy problems of the form \( a \) is to \( b \) as \( a^* \) is to \( \_\_\_\_\_ \). In such problems, a system is given a problem like *apple:tree::grape:*?, i.e., *apple is to tree as grape is to ?*. In the parallelogram model, illustrated in Fig. 6.15, the vector from the word *apple* to the word *tree* (= tree – apple) is added to the vector for *grape* (grape); the nearest word to that point is returned.

In early work with sparse embeddings, scholars showed that sparse vector models of meaning could solve such analogy problems (Turney and Littman, 2005), but the parallelogram method received more modern attention because of its success with word2vec or GloVe vectors (Mikolov et al. 2013c, Levy and Goldberg 2014b, Pennington et al. 2014). For example, the result of the expression king –
man + woman is a vector close to queen. Similarly, Paris − France + Italy results in a vector that is close to Rome. The embedding model thus seems to be extracting representations of relations like MALE-FEMALE, or CAPITAL-CITY-OF, or even COMPARATIVE/SUPERLATIVE, as shown in Fig. 6.16 from GloVe.

For a \( \mathbf{a} : \mathbf{b} :: \mathbf{a}^* : \mathbf{b}^* \) problem, meaning the algorithm is given vectors \( \mathbf{a}, \mathbf{b}, \) and \( \mathbf{a}^* \) and must find \( \mathbf{b}^* \), the parallelogram method is thus:

\[
\mathbf{b}^* = \operatorname{argmin}_x \text{distance}(x, \mathbf{b} - \mathbf{a} + \mathbf{a}^*)
\]

(6.41)

with some distance function, such as Euclidean distance.

There are some caveats. For example, the closest value returned by the parallelogram algorithm in word2vec or GloVe embedding spaces is usually not in fact \( \mathbf{b}^* \) but one of the 3 input words or their morphological variants (i.e., cherry:red :: potato:x returns potato or potatoes instead of brown), so these must be explicitly excluded. Furthermore, while embedding spaces perform well if the task involves frequent words, small distances, and certain relations (like relating countries with their capitals or verbs/nouns with their inflected forms), the parallelogram method with embeddings doesn’t work as well for other relations (Linzen 2016, Gladkova et al. 2016, Schluter 2018, Ethayarajh et al. 2019a), and indeed Peterson et al. (2020) argue that the parallelogram method is in general too simple to model the human cognitive process of forming analogies of this kind.
6.10.1 Embeddings and Historical Semantics

Embeddings can also be a useful tool for studying how meaning changes over time, by computing multiple embedding spaces, each from texts written in a particular time period. For example Fig. 6.17 shows a visualization of changes in meaning in English words over the last two centuries, computed by building separate embedding spaces for each decade from historical corpora like Google n-grams (Lin et al., 2012b) and the Corpus of Historical American English (Davies, 2012).

![Figure 6.17](image_url) A t-SNE visualization of the semantic change of 3 words in English using word2vec vectors. The modern sense of each word, and the grey context words, are computed from the most recent (modern) time-point embedding space. Earlier points are computed from earlier historical embedding spaces. The visualizations show the changes in the word gay from meanings related to “cheerful” or “frolicsome” to referring to homosexuality, the development of the modern “transmission” sense of broadcast from its original sense of sowing seeds, and the pejoration of the word awful as it shifted from meaning “full of awe” to meaning “terrible or appalling” (Hamilton et al., 2016b).

6.11 Bias and Embeddings

In addition to their ability to learn word meaning from text, embeddings, alas, also reproduce the implicit biases and stereotypes that were latent in the text. As the prior section just showed, embeddings can roughly model relational similarity: ‘queen’ as the closest word to ‘king’ - ‘man’ + ‘woman’ implies the analogy man:woman::king:queen. But these same embedding analogies also exhibit gender stereotypes. For example Bolukbasi et al. (2016) find that the closest occupation to ‘computer programmer’ - ‘man’ + ‘woman’ in word2vec embeddings trained on news text is ‘homemaker’, and that the embeddings similarly suggest the analogy ‘father’ is to ‘doctor’ as ‘mother’ is to ‘nurse’. This could result in what Crawford (2017) and Blodgett et al. (2020) call an allocational harm, when a system allocates resources (jobs or credit) unfairly to different groups. For example algorithms that use embeddings as part of a search for hiring potential programmers or doctors might thus incorrectly downweight documents with women’s names.

It turns out that embeddings don’t just reflect the statistics of their input, but also amplify bias; gendered terms become more gendered in embedding space than they were in the input text statistics (Zhao et al. 2017, Ethayarajh et al. 2019b, Jia et al. 2020), and biases are more exaggerated than in actual labor employment statistics (Garg et al., 2018).

Embeddings also encode the implicit associations that are a property of human reasoning. The Implicit Association Test (Greenwald et al., 1998) measures pep-
people’s associations between concepts (like ‘flowers’ or ‘insects’) and attributes (like ‘pleasantness’ and ‘unpleasantness’) by measuring differences in the latency with which they label words in the various categories. Using such methods, people in the United States have been shown to associate African-American names with unpleasant words (more than European-American names), male names more with mathematics and female names with the arts, and old people’s names with unpleasant words (Greenwald et al. 1998, Nosek et al. 2002a, Nosek et al. 2002b). Caliskan et al. (2017) replicated all these findings of implicit associations using GloVe vectors and cosine similarity instead of human latencies. For example African-American names like ‘Leroy’ and ‘Shaniqua’ had a higher GloVe cosine with unpleasant words while European-American names (‘Brad’, ‘Greg’, ‘Courtney’) had a higher cosine with pleasant words. These problems with embeddings are an example of a representational harm (Crawford 2017, Blodgett et al. 2020), which is a harm caused by a system demeaning or even ignoring some social groups. Any embedding-aware algorithm that made use of word sentiment could thus exacerbate bias against African Americans.

Recent research focuses on ways to try to remove these kinds of biases, for example by developing a transformation of the embedding space that removes gender stereotypes but preserves definitional gender (Bolukbasi et al. 2016, Zhao et al. 2017) or changing the training procedure (Zhao et al., 2018b). However, although these sorts of debiasing may reduce bias in embeddings, they do not eliminate it (Gonen and Goldberg, 2019), and this remains an open problem.

Historical embeddings are also being used to measure biases in the past. Garg et al. (2018) used embeddings from historical texts to measure the association between embeddings for occupations and embeddings for names of various ethnicities or genders (for example the relative cosine similarity of women’s names versus men’s to occupation words like ‘librarian’ or ‘carpenter’) across the 20th century. They found that the cosines correlate with the empirical historical percentages of women or ethnic groups in those occupations. Historical embeddings also replicated old surveys of ethnic stereotypes; the tendency of experimental participants in 1933 to associate adjectives like ‘industrious’ or ‘superstitious’ with, e.g., Chinese ethnicity, correlates with the cosine between Chinese last names and those adjectives using embeddings trained on 1930s text. They also were able to document historical gender biases, such as the fact that embeddings for adjectives related to competence (‘smart’, ‘wise’, ‘thoughtful’, ‘resourceful’) had a higher cosine with male than female words, and showed that this bias has been slowly decreasing since 1960. We return in later chapters to this question about the role of bias in natural language processing.

6.12 Evaluating Vector Models

The most important evaluation metric for vector models is extrinsic evaluation on tasks, i.e., using vectors in an NLP task and seeing whether this improves performance over some other model.

---

7 Roughly speaking, if humans associate ‘flowers’ with ‘pleasantness’ and ‘insects’ with ‘unpleasantness’, when they are instructed to push a green button for ‘flowers’ (daisy, iris, lilac) and ‘pleasant words’ (love, laughter, pleasure) and a red button for ‘insects’ (flea, spider, mosquito) and ‘unpleasant words’ (abuse, hatred, ugly) they are faster than in an incongruous condition where they push a red button for ‘flowers’ and ‘unpleasant words’ and a green button for ‘insects’ and ‘pleasant words’.
Nonetheless it is useful to have intrinsic evaluations. The most common metric is to test their performance on similarity, computing the correlation between an algorithm’s word similarity scores and word similarity ratings assigned by humans. **WordSim-353** (Finkelstein et al., 2002) is a commonly used set of ratings from 0 to 10 for 353 noun pairs; for example (plane, car) had an average score of 5.77. **SimLex-999** (Hill et al., 2015) is a more difficult dataset that quantifies similarity (cup, mug) rather than relatedness (cup, coffee), and including both concrete and abstract adjective, noun and verb pairs. The **TOEFL dataset** is a set of 80 questions, each consisting of a target word with 4 additional word choices; the task is to choose which is the correct synonym, as in the example: *Levied is closest in meaning to: imposed, believed, requested, correlated* (Landauer and Dumais, 1997). All of these datasets present words without context.

Slightly more realistic are intrinsic similarity tasks that include context. The Stanford Contextual Word Similarity (SCWS) dataset (Huang et al., 2012) and the Word-in-Context (WiC) dataset (Pilehvar and Camacho-Collados, 2019) offer richer evaluation scenarios. SCWS gives human judgments on 2,003 pairs of words in their sentential context, while WiC gives target words in two sentential contexts that are either in the same or different senses; see Chapter 23. The **semantic textual similarity** task (Agirre et al. 2012, Agirre et al. 2015) evaluates the performance of sentence-level similarity algorithms, consisting of a set of pairs of sentences, each pair with human-labeled similarity scores.

Another task used for evaluation is the analogy task, discussed on page 128, where the system has to solve problems of the form *a is to b as a* is to *b**, given *a*, *b*, and *a* and having to find *b* (Turney and Littman, 2005). A number of sets of tuples have been created for this task, (Mikolov et al. 2013a, Mikolov et al. 2013c, Gladkova et al. 2016), covering morphology (*city:*cities::*child:*children*), lexicographic relations (*leg:*table::*spout:*teapot*) and encyclopedia relations (*Beijing:*China::*Dublin:*Ireland*), some drawing from the SemEval-2012 Task 2 dataset of 79 different relations (Jurgens et al., 2012).

All embedding algorithms suffer from inherent variability. For example because of randomness in the initialization and the random negative sampling, algorithms like word2vec may produce different results even from the same dataset, and individual documents in a collection may strongly impact the resulting embeddings (Tian et al. 2016, Hellrich and Hahn 2016, Antoniak and Mimno 2018). When embeddings are used to study word associations in particular corpora, therefore, it is best practice to train multiple embeddings with bootstrap sampling over documents and average the results (Antoniak and Mimno, 2018).

### 6.13 Summary

- In vector semantics, a word is modeled as a vector—a point in high-dimensional space, also called an **embedding**. In this chapter we focus on **static embeddings**, where each word is mapped to a fixed embedding.

- Vector semantic models fall into two classes: **sparse** and **dense**. In sparse models each dimension corresponds to a word in the vocabulary $V$ and cells are functions of **co-occurrence counts**. The **term-document** matrix has a row for each word (**term**) in the vocabulary and a column for each document. The **word-context** or **term-term** matrix has a row for each (target) word in
the vocabulary and a column for each context term in the vocabulary. Two sparse weightings are common: the \texttt{tf-idf} weighting which weights each cell by its \textit{term frequency} and \textit{inverse document frequency}, and PPMI (point-wise positive mutual information), which is most common for word-context matrices.

- Dense vector models have dimensionality 50–1000. \texttt{Word2vec} algorithms like \texttt{skip-gram} are a popular way to compute dense embeddings. \texttt{Skip-gram} trains a logistic regression classifier to compute the probability that two words are ‘likely to occur nearby in text’. This probability is computed from the dot product between the embeddings for the two words.

- \texttt{Skip-gram} uses stochastic gradient descent to train the classifier, by learning embeddings that have a high dot product with embeddings of words that occur nearby and a low dot product with noise words.

- Other important embedding algorithms include \texttt{GloVe}, a method based on ratios of word co-occurrence probabilities.

- Whether using sparse or dense vectors, word and document similarities are computed by some function of the \textit{dot product} between vectors. The cosine of two vectors—a normalized dot product—is the most popular such metric.

Bibliographical and Historical Notes

The idea of vector semantics arose out of research in the 1950s in three distinct fields: linguistics, psychology, and computer science, each of which contributed a fundamental aspect of the model.

The idea that meaning is related to the distribution of words in context was widespread in linguistic theory of the 1950s, among distributionalists like Zellig Harris, Martin Joos, and J. R. Firth, and semioticians like Thomas Sebeok. As Joos (1950) put it,

the linguist’s “meaning” of a morpheme... is by definition the set of conditional probabilities of its occurrence in context with all other morphemes.

The idea that the meaning of a word might be modeled as a point in a multidimensional semantic space came from psychologists like Charles E. Osgood, who had been studying how people responded to the meaning of words by assigning values along scales like \textit{happy/sad} or \textit{hard/soft}. Osgood et al. (1957) proposed that the meaning of a word in general could be modeled as a point in a multidimensional Euclidean space, and that the similarity of meaning between two words could be modeled as the distance between these points in the space.

A final intellectual source in the 1950s and early 1960s was the field then called \textbf{mechanical indexing}, now known as \textbf{information retrieval}. In what became known as the \textbf{vector space model} for information retrieval (Salton 1971, Sparck Jones 1986), researchers demonstrated new ways to define the meaning of words in terms of vectors (Switzer, 1965), and refined methods for word similarity based on measures of statistical association between words like mutual information (Giuliano, 1965) and idf (Sparck Jones, 1972), and showed that the meaning of documents could be represented in the same vector spaces used for words. Around the same time, (Cordier, 1965) showed that factor analysis of word association probabilities could be used to form dense vector representations of words.
Some of the philosophical underpinning of the distributional way of thinking came from the late writings of the philosopher Wittgenstein, who was skeptical of the possibility of building a completely formal theory of meaning definitions for each word, suggesting instead that “the meaning of a word is its use in the language” (Wittgenstein, 1953, PI 43). That is, instead of using some logical language to define each word, or drawing on denotations or truth values, Wittgenstein’s idea is that we should define a word by how it is used by people in speaking and understanding in their day-to-day interactions, thus prefiguring the movement toward embodied and experiential models in linguistics and NLP (Glenberg and Robertson 2000, Lake and Murphy 2021, Bisk et al. 2020, Bender and Koller 2020).

More distantly related is the idea of defining words by a vector of discrete features, which has roots at least as far back as Descartes and Leibniz (Wierzbicka 1992, Wierzbicka 1996). By the middle of the 20th century, beginning with the work of Hjelmslev (Hjelmslev, 1969) (originally 1943) and fleshed out in early models of generative grammar (Katz and Fodor, 1963), the idea arose of representing meaning with semantic features, symbols that represent some sort of primitive meaning. For example, words like hen, rooster, or chick, have something in common (they all describe chickens) and something different (their age and sex), representable as:

- **hen** +female, +chicken, +adult
- **rooster** -female, +chicken, +adult
- **chick** +chicken, -adult

The dimensions used by vector models of meaning to define words, however, are only abstractly related to this idea of a small fixed number of hand-built dimensions. Nonetheless, there has been some attempt to show that certain dimensions of embedding models do contribute some specific compositional aspect of meaning like these early semantic features.

The use of dense vectors to model word meaning, and indeed the term embedding, grew out of the latent semantic indexing (LSI) model (Deerwester et al., 1988) recast as LSA (latent semantic analysis) (Deerwester et al., 1990). In LSA—singular value decomposition (SVD)—is applied to a term-document matrix (each cell weighted by log frequency and normalized by entropy), and then the first 300 dimensions are used as the LSA embedding. Singular Value Decomposition (SVD) is a method for finding the most important dimensions of a data set, those dimensions along which the data varies the most. LSA was then quickly widely applied: as a cognitive model Landauer and Dumais (1997), and for tasks like spell checking (Jones and Martin, 1997), language modeling (Bellegarda 1997, Coccaro and Jurafsky 1998, Bellegarda 2000) morphology induction (Schone and Jurafsky 2000, Schone and Jurafsky 2001b), multiword expressions (MWEs) (Schone and Jurafsky, 2001a), and essay grading (Rehder et al., 1998). Related models were simultaneously developed and applied to word sense disambiguation by Schütze (1992b). LSA also led to the earliest use of embeddings to represent words in a probabilistic classifier, in the logistic regression document router of Schütze et al. (1995).

The idea of SVD on the term-term matrix (rather than the term-document matrix) as a model of meaning for NLP was proposed soon after LSA by Schütze (1992b). Schütze applied the low-rank (97-dimensional) embeddings produced by SVD to the task of word sense disambiguation, analyzed the resulting semantic space, and also suggested possible techniques like dropping high-order dimensions. See Schütze (1997).

A number of alternative matrix models followed on from the early SVD work, including Probabilistic Latent Semantic Indexing (PLSI) (Hofmann, 1999), Latent
Dirichlet Allocation (LDA) (Blei et al., 2003), and Non-negative Matrix Factorization (NMF) (Lee and Seung, 1999).

The LSA community seems to have first used the word “embedding” in Landauer et al. (1997), in a variant of its mathematical meaning as a mapping from one space or mathematical structure to another. In LSA, the word embedding seems to have described the mapping from the space of sparse count vectors to the latent space of SVD dense vectors. Although the word thus originally meant the mapping from one space to another, it has metonymically shifted to mean the resulting dense vector in the latent space, and it is in this sense that we currently use the word.

By the next decade, Bengio et al. (2003) and Bengio et al. (2006) showed that neural language models could also be used to develop embeddings as part of the task of word prediction. Collobert and Weston (2007), Collobert and Weston (2008), and Collobert et al. (2011) then demonstrated that embeddings could be used to represent word meanings for a number of NLP tasks. Turian et al. (2010) compared the value of different kinds of embeddings for different NLP tasks. Mikolov et al. (2011) showed that recurrent neural nets could be used as language models. The idea of simplifying the hidden layer of these neural net language models to create the skip-gram (and also CBOW) algorithms was proposed by Mikolov et al. (2013a). The negative sampling training algorithm was proposed in Mikolov et al. (2013b). There are numerous surveys of static embeddings and their parameterizations (Bullinaria and Levy 2007, Bullinaria and Levy 2012, Lapesa and Evert 2014, Kiela and Clark 2014, Levy et al. 2015).

See Manning et al. (2008) for a deeper understanding of the role of vectors in information retrieval, including how to compare queries with documents, more details on tf-idf, and issues of scaling to very large datasets. See Kim (2019) for a clear and comprehensive tutorial on word2vec. Cruse (2004) is a useful introductory linguistic text on lexical semantics.

Exercises
Neural networks are a fundamental computational tool for language processing, and a very old one. They are called neural because their origins lie in the McCulloch-Pitts neuron (McCulloch and Pitts, 1943), a simplified model of the biological neuron as a kind of computing element that could be described in terms of propositional logic. But the modern use in language processing no longer draws on these early biological inspirations.

Instead, a modern neural network is a network of small computing units, each of which takes a vector of input values and produces a single output value. In this chapter we introduce the neural net applied to classification. The architecture we introduce is called a feedforward network because the computation proceeds iteratively from one layer of units to the next. The use of modern neural nets is often called deep learning, because modern networks are often deep (have many layers).

Neural networks share much of the same mathematics as logistic regression. But neural networks are a more powerful classifier than logistic regression, and indeed a minimal neural network (technically one with a single ‘hidden layer’) can be shown to learn any function.

Neural net classifiers are different from logistic regression in another way. With logistic regression, we applied the regression classifier to many different tasks by developing many rich kinds of feature templates based on domain knowledge. When working with neural networks, it is more common to avoid most uses of rich hand-derived features, instead building neural networks that take raw words as inputs and learn to induce features as part of the process of learning to classify. We saw examples of this kind of representation learning for embeddings in Chapter 6. Nets that are very deep are particularly good at representation learning. For that reason deep neural nets are the right tool for tasks that offer sufficient data to learn features automatically.

In this chapter we’ll introduce feedforward networks as classifiers, and also apply them to the simple task of language modeling: assigning probabilities to word sequences and predicting upcoming words. In subsequent chapters we’ll introduce many other aspects of neural models, such as recurrent neural networks (Chapter 9), the Transformer (Chapter 10), and masked language modeling (Chapter 11).
7.1 Units

The building block of a neural network is a single computational unit. A unit takes
a set of real valued numbers as input, performs some computation on them, and
produces an output.

At its heart, a neural unit is taking a weighted sum of its inputs, with one addi-
tional term in the sum called a bias term. Given a set of inputs \(x_1 \ldots x_n\), a unit has
a set of corresponding weights \(w_1 \ldots w_n\) and a bias \(b\), so the weighted sum \(z\) can be
represented as:

\[
z = b + \sum_i w_i x_i
\]  
(7.1)

Often it’s more convenient to express this weighted sum using vector notation; recall
from linear algebra that a vector is, at heart, just a list or array of numbers. Thus
we’ll talk about \(z\) in terms of a weight vector \(w\), a scalar bias \(b\), and an input vector
\(x\), and we’ll replace the sum with the convenient dot product:

\[
z = w \cdot x + b
\]  
(7.2)

As defined in Eq. 7.2, \(z\) is just a real valued number.

Finally, instead of using \(z\), a linear function of \(x\), as the output, neural units
apply a non-linear function \(f\) to \(z\). We will refer to the output of this function as
the activation value for the unit, \(a\). Since we are just modeling a single unit, the
activation for the node is in fact the final output of the network, which we’ll generally
call \(y\). So the value \(y\) is defined as:

\[
y = a = f(z)
\]

We’ll discuss three popular non-linear functions \(f()\) below (the sigmoid, the tanh,
and the rectified linear unit or ReLU) but it’s pedagogically convenient to start with
the sigmoid function since we saw it in Chapter 5:

\[
y = \sigma(z) = \frac{1}{1 + e^{-z}}
\]  
(7.3)

The sigmoid (shown in Fig. 7.1) has a number of advantages; it maps the output
into the range \((0, 1)\), which is useful in squashing outliers toward 0 or 1. And it’s
differentiable, which as we saw in Section 5.10 will be handy for learning.

Substituting Eq. 7.2 into Eq. 7.3 gives us the output of a neural unit:

\[
y = \sigma(w \cdot x + b) = \frac{1}{1 + \exp(-(w \cdot x + b))}
\]  
(7.4)
Fig. 7.2 shows a final schematic of a basic neural unit. In this example the unit takes 3 input values \( x_1, x_2, \) and \( x_3, \) and computes a weighted sum, multiplying each value by a weight \((w_1, w_2, \) and \( w_3,\) respectively), adds them to a bias term \( b, \) and then passes the resulting sum through a sigmoid function to result in a number between 0 and 1.

Let’s walk through an example just to get an intuition. Let’s suppose we have a unit with the following weight vector and bias:

\[
\mathbf{w} = [0.2, 0.3, 0.9] \\
\mathbf{b} = 0.5
\]

What would this unit do with the following input vector:

\[
\mathbf{x} = [0.5, 0.6, 0.1]
\]

The resulting output \( y \) would be:

\[
y = \sigma(\mathbf{w} \cdot \mathbf{x} + \mathbf{b}) = \frac{1}{1 + e^{-(\mathbf{w} \cdot \mathbf{x} + \mathbf{b})}} = \frac{1}{1 + e^{-(0.2 \cdot 0.5 + 0.3 \cdot 0.6 + 0.9 \cdot 0.1 + 0.5)}} = \frac{1}{1 + e^{0.87}} = .70
\]

In practice, the sigmoid is not commonly used as an activation function. A function that is very similar but almost always better is the \( \tanh \) function shown in Fig. 7.3a; \( \tanh \) is a variant of the sigmoid that ranges from -1 to +1:

\[
y = \tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}} \tag{7.5}
\]

The simplest activation function, and perhaps the most commonly used, is the rectified linear unit, also called the \( \text{ReLU} \), shown in Fig. 7.3b. It’s just the same as \( z \) when \( z \) is positive, and 0 otherwise:

\[
y = \text{ReLU}(z) = \max(z, 0) \tag{7.6}
\]

These activation functions have different properties that make them useful for different language applications or network architectures. For example, the \( \tanh \) function has the nice properties of being smoothly differentiable and mapping outlier values toward the mean. The rectifier function, on the other hand, has nice properties that
result from it being very close to linear. In the sigmoid or tanh functions, very high values of \( z \) result in values of \( y \) that are saturated, i.e., extremely close to 1, and have derivatives very close to 0. Zero derivatives cause problems for learning, because as we’ll see in Section 7.5, we’ll train networks by propagating an error signal backwards, multiplying gradients (partial derivatives) from each layer of the network; gradients that are almost 0 cause the error signal to get smaller and smaller until it is too small to be used for training, a problem called the vanishing gradient problem. Rectifiers don’t have this problem, since the derivative of ReLU for high values of \( z \) is 1 rather than very close to 0.

7.2 The XOR problem

Early in the history of neural networks it was realized that the power of neural networks, as with the real neurons that inspired them, comes from combining these units into larger networks.

One of the most clever demonstrations of the need for multi-layer networks was the proof by Minsky and Papert (1969) that a single neural unit cannot compute some very simple functions of its input. Consider the task of computing elementary logical functions of two inputs, like AND, OR, and XOR. As a reminder, here are the truth tables for those functions:

<table>
<thead>
<tr>
<th>AND</th>
<th>OR</th>
<th>XOR</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x_1 )</td>
<td>( x_2 )</td>
<td>( y )</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

This example was first shown for the perceptron, which is a very simple neural unit that has a binary output and does not have a non-linear activation function. The output \( y \) of a perceptron is 0 or 1, and is computed as follows (using the same weight \( w \), input \( x \), and bias \( b \) as in Eq. 7.2):

\[
y = \begin{cases} 
0, & \text{if } w \cdot x + b \leq 0 \\
1, & \text{if } w \cdot x + b > 0 
\end{cases}
\]  

(7.7)
It's very easy to build a perceptron that can compute the logical AND and OR functions of its binary inputs; Fig. 7.4 shows the necessary weights.

It turns out, however, that it’s not possible to build a perceptron to compute logical XOR! (It’s worth spending a moment to give it a try!)

The intuition behind this important result relies on understanding that a perceptron is a linear classifier. For a two-dimensional input $x_1$ and $x_2$, the perceptron equation, $w_1 x_1 + w_2 x_2 + b = 0$ is the equation of a line. (We can see this by putting it in the standard linear format: $x_2 = (-w_1/w_2)x_1 + (-b/w_2)$.) This line acts as a decision boundary in two-dimensional space in which the output 0 is assigned to all inputs lying on one side of the line, and the output 1 to all input points lying on the other side of the line. If we had more than 2 inputs, the decision boundary becomes a hyperplane instead of a line, but the idea is the same, separating the space into two categories.

Fig. 7.5 shows the possible logical inputs (00, 01, 10, and 11) and the line drawn by one possible set of parameters for an AND and an OR classifier. Notice that there is simply no way to draw a line that separates the positive cases of XOR (01 and 10) from the negative cases (00 and 11). We say that XOR is not a linearly separable function. Of course we could draw a boundary with a curve, or some other function, but not a single line.

7.2.1 The solution: neural networks

While the XOR function cannot be calculated by a single perceptron, it can be calculated by a layered network of perceptron units. Rather than see this with networks of simple perceptrons, however, let’s see how to compute XOR using two layers of ReLU-based units following Goodfellow et al. (2016). Fig. 7.6 shows a figure with the input being processed by two layers of neural units. The middle layer (called $h$) has two units, and the output layer (called $y$) has one unit. A set of weights and biases are shown that allows the network to correctly compute the XOR function.

Let’s walk through what happens with the input $x = [0, 0]$. If we multiply each input value by the appropriate weight, sum, and then add the bias $b$, we get the vector $[0, -1]$, and we then apply the rectified linear transformation to give the output of the $h$ layer as $[0, 0]$. Now we once again multiply by the weights, sum, and add the bias (0 in this case) resulting in the value 0. The reader should work through the computation of the remaining 3 possible input pairs to see that the resulting $y$ values are 1 for the inputs $[0, 1]$ and $[1, 0]$ and 0 for $[0, 0]$ and $[1, 1]$. 
7.2 • THE XOR PROBLEM

The functions AND, OR, and XOR, represented with input $x_1$ on the x-axis and input $x_2$ on the y-axis. Filled circles represent perceptron outputs of 1, and white circles perceptron outputs of 0. There is no way to draw a line that correctly separates the two categories for XOR. Figure styled after Russell and Norvig (2002).

It’s also instructive to look at the intermediate results, the outputs of the two hidden nodes $h_1$ and $h_2$. We showed in the previous paragraph that the h vector for the inputs $x = [0, 0]$ was $[0, 0]$. Fig. 7.7b shows the values of the h layer for all 4 inputs. Notice that hidden representations of the two input points $x = [0, 1]$ and $x = [1, 0]$ (the two cases with XOR output = 1) are merged to the single point $h = [1, 0]$. The merger makes it easy to linearly separate the positive and negative cases of XOR. In other words, we can view the hidden layer of the network as forming a representation of the input.

In this example we just stipulated the weights in Fig. 7.6. But for real examples the weights for neural networks are learned automatically using the error backpropagation algorithm to be introduced in Section 7.5. That means the hidden layers will learn to form useful representations. This intuition, that neural networks can automatically learn useful representations of the input, is one of their key advantages, and one that we will return to again and again in later chapters.
Let’s now walk through a slightly more formal presentation of the simplest kind of neural network, the feedforward network. A feedforward network is a multilayer network in which the units are connected with no cycles; the outputs from units in each layer are passed to units in the next higher layer, and no outputs are passed back to lower layers. (In Chapter 9 we’ll introduce networks with cycles, called recurrent neural networks.)

For historical reasons multilayer networks, especially feedforward networks, are sometimes called multi-layer perceptrons (or MLPs); this is a technical misnomer, since the units in modern multilayer networks aren’t perceptrons (perceptrons are purely linear, but modern networks are made up of units with non-linearities like sigmoids), but at some point the name stuck.

Simple feedforward networks have three kinds of nodes: input units, hidden units, and output units.

Fig. 7.8 shows a picture. The input layer \( x \) is a vector of simple scalar values just as we saw in Fig. 7.2.

The core of the neural network is the hidden layer \( h \) formed of hidden units \( h_i \), each of which is a neural unit as described in Section 7.1, taking a weighted sum of its inputs and then applying a non-linearity. In the standard architecture, each layer is fully-connected, meaning that each unit in each layer takes as input the outputs from all the units in the previous layer, and there is a link between every pair of units from two adjacent layers. Thus each hidden unit sums over all the input units.

Recall that a single hidden unit has as parameters a weight vector and a bias. We represent the parameters for the entire hidden layer by combining the weight vector and bias for each unit \( i \) into a single weight matrix \( \mathbf{W} \) and a single bias vector \( b \) for the whole layer (see Fig. 7.8). Each element \( \mathbf{W}_{ji} \) of the weight matrix \( \mathbf{W} \) represents the weight of the connection from the \( i \)th input unit \( x_i \) to the \( j \)th hidden unit \( h_j \).

The advantage of using a single matrix \( \mathbf{W} \) for the weights of the entire layer is that now the hidden layer computation for a feedforward network can be done very efficiently with simple matrix operations. In fact, the computation only has three
steps: multiplying the weight matrix by the input vector $x$, adding the bias vector $b$, and applying the activation function $g$ (such as the sigmoid, tanh, or ReLU activation function defined above).

The output of the hidden layer, the vector $h$, is thus the following (for this example we’ll use the sigmoid function $\sigma$ as our activation function):

$$h = \sigma(Wx + b) \quad (7.8)$$

Notice that we’re applying the $\sigma$ function here to a vector, while in Eq. 7.3 it was applied to a scalar. We’re thus allowing $\sigma(\cdot)$, and indeed any activation function $g(\cdot)$, to apply to a vector element-wise, so $g[z_1, z_2, z_3] = [g(z_1), g(z_2), g(z_3)]$.

Let’s introduce some constants to represent the dimensionalities of these vectors and matrices. We’ll refer to the input layer as layer 0 of the network, and have $n_0$ represent the number of inputs, so $x$ is a vector of real numbers of dimension $n_0$, or more formally $x \in \mathbb{R}^{n_0}$, a column vector of dimensionality $[n_0, 1]$. Let’s call the hidden layer layer 1 and the output layer layer 2. The hidden layer has dimensionality $n_1$, so $h \in \mathbb{R}^{n_1}$ and also $b \in \mathbb{R}^{n_1}$ (since each hidden unit can take a different bias value). And the weight matrix $W$ has dimensionality $W \in \mathbb{R}^{n_1 \times n_0}$, i.e. $[n_1, n_0]$.

Take a moment to convince yourself that the matrix multiplication in Eq. 7.8 will compute the value of each $h_j$ as $\sigma \left( \sum_{i=1}^{n_0} W_{ji} x_i + b_j \right)$.

As we saw in Section 7.2, the resulting value $h$ (for hidden but also for hypothesis) forms a representation of the input. The role of the output layer is to take this new representation $h$ and compute a final output. This output could be a real-valued number, but in many cases the goal of the network is to make some sort of classification decision, and so we will focus on the case of classification.

If we are doing a binary task like sentiment classification, we might have a single output node, and its scalar value $y$ is the probability of positive versus negative sentiment. If we are doing multinomial classification, such as assigning a part-of-speech tag, we might have one output node for each potential part-of-speech, whose output value is the probability of that part-of-speech, and the values of all the output nodes must sum to one. The output layer is thus a vector $y$ that gives a probability distribution across the output nodes.

Let’s see how this happens. Like the hidden layer, the output layer has a weight matrix (let’s call it $U$), but some models don’t include a bias vector $b$ in the output.
layer, so we’ll simplify by eliminating the bias vector in this example. The weight matrix is multiplied by its input vector ($h$) to produce the intermediate output $z$:

$$z = Uh$$

There are $n_2$ output nodes, so $z \in \mathbb{R}^{n_2}$, weight matrix $U$ has dimensionality $U \in \mathbb{R}^{n_2 \times n_1}$, and element $U_{ij}$ is the weight from unit $j$ in the hidden layer to unit $i$ in the output layer.

However, $z$ can’t be the output of the classifier, since it’s a vector of real-valued numbers, while what we need for classification is a vector of probabilities. There is a convenient function for normalizing a vector of real values, by which we mean converting it to a vector that encodes a probability distribution (all the numbers lie between 0 and 1 and sum to 1): the softmax function that we saw on page 89 of Chapter 5. More generally for any vector $z$ of dimensionality $d$, the softmax is defined as:

$$\text{softmax}(z_i) = \frac{\exp(z_i)}{\sum_{j=1}^{d} \exp(z_j)} \quad 1 \leq i \leq d \quad (7.9)$$

Thus for example given a vector

$$z = [0.6, 1.1, -1.5, 1.2, 3.2, -1.1], \quad (7.10)$$

the softmax function will normalize it to a probability distribution (shown rounded):

$$\text{softmax}(z) = [0.055, 0.090, 0.0067, 0.10, 0.74, 0.010] \quad (7.11)$$

You may recall that we used softmax to create a probability distribution from a vector of real-valued numbers (computed from summing weights times features) in the multinomial version of logistic regression in Chapter 5.

That means we can think of a neural network classifier with one hidden layer as building a vector $h$ which is a hidden layer representation of the input, and then running standard multinomial logistic regression on the features that the network develops in $h$. By contrast, in Chapter 5 the features were mainly designed by hand via feature templates. So a neural network is like multinomial logistic regression, but (a) with many layers, since a deep neural network is like layer after layer of logistic regression classifiers; (b) with those intermediate layers having many possible activation functions (tanh, ReLU, sigmoid) instead of just sigmoid (although we’ll continue to use $\sigma$ for convenience to mean any activation function); (c) rather than forming the features by feature templates, the prior layers of the network induce the feature representations themselves.

Here are the final equations for a feedforward network with a single hidden layer, which takes an input vector $x$, outputs a probability distribution $y$, and is parameterized by weight matrices $W$ and $U$ and a bias vector $b$:

$$h = \sigma(Wx + b)$$
$$z = Uh$$
$$y = \text{softmax}(z) \quad (7.12)$$

And just to remember the shapes of all our variables, $x \in \mathbb{R}^{n_0}$, $h \in \mathbb{R}^{n_1}$, $b \in \mathbb{R}^{n_1}$, $W \in \mathbb{R}^{n_1 \times n_0}$, $U \in \mathbb{R}^{n_2 \times n_1}$, and the output vector $y \in \mathbb{R}^{n_2}$. We’ll call this network a 2-layer network (we traditionally don’t count the input layer when numbering layers, but do count the output layer). So by this terminology logistic regression is a 1-layer network.
7.3 • Feedforward Neural Networks

7.3.1 More details on feedforward networks

Let’s now set up some notation to make it easier to talk about deeper networks of depth more than 2. We’ll use superscripts in square brackets to mean layer numbers, starting at 0 for the input layer. So $W^{[1]}$ will mean the weight matrix for the (first) hidden layer, and $b^{[1]}$ will mean the bias vector for the (first) hidden layer. $n_j$ will mean the number of units at layer $j$. We’ll use $g(\cdot)$ to stand for the activation function, which will tend to be ReLU or tanh for intermediate layers and softmax for output layers. We’ll use $a^{[i]}$ to mean the output from layer $i$, and $z^{[i]}$ to mean the combination of weights and biases $W^{[i]}a^{[i-1]} + b^{[i]}$. The 0th layer is for inputs, so we’ll refer to the inputs $x$ more generally as $a^{[0]}$.

Thus we can re-represent our 2-layer net from Eq. 7.12 as follows:

$$
\begin{align*}
    z^{[1]} &= W^{[1]} a^{[0]} + b^{[1]} \\
    a^{[1]} &= g^{[1]}(z^{[1]}) \\
    z^{[2]} &= W^{[2]} a^{[1]} + b^{[2]} \\
    a^{[2]} &= g^{[2]}(z^{[2]}) \\
    \hat{y} &= a^{[2]}
\end{align*}
$$

(7.13)

Note that with this notation, the equations for the computation done at each layer are the same. The algorithm for computing the forward step in an $n$-layer feedforward network, given the input vector $a^{[0]}$ is thus simply:

for $i$ in 1,...,n

$z^{[i]} = W^{[i]} a^{[i-1]} + b^{[i]}$

$a^{[i]} = g^{[i]}(z^{[i]})$

$\hat{y} = a^{[n]}$

The activation functions $g(\cdot)$ are generally different at the final layer. Thus $g^{[2]}$ might be softmax for multinomial classification or sigmoid for binary classification, while ReLU or tanh might be the activation function $g(\cdot)$ at the internal layers.

It’s often useful to have a name for the final set of activations right before the final softmax. So however many layers we have, we’ll generally call the unnormalized values in the final vector $z^{[n]}$, the vector of scores right before the final softmax, the logits (see (5.7).

The need for non-linear activation functions

One of the reasons we use non-linear activation functions for each layer in a neural network is that if we did not, the resulting network is exactly equivalent to a single-layer network. Let’s see why this is true. Imagine the first two layers of such a network of purely linear layers:

$$
\begin{align*}
    z^{[1]} &= W^{[1]} x + b^{[1]} \\
    z^{[2]} &= W^{[2]} z^{[1]} + b^{[2]}
\end{align*}
$$

We can rewrite the function that the network is computing as:

$$
\begin{align*}
    z^{[2]} &= W^{[2]} z^{[1]} + b^{[2]} \\
    &= W^{[2]} (W^{[1]} x + b^{[1]}) + b^{[2]} \\
    &= W^{[2]} W^{[1]} x + W^{[2]} b^{[1]} + b^{[2]} \\
    &= W^{\prime} x + b^{\prime}
\end{align*}
$$

(7.14)

This generalizes to any number of layers. So without non-linear activation functions, a multilayer network is just a notational variant of a single layer network with a
different set of weights, and we lose all the representational power of multilayer networks.

**Replacing the bias unit**  In describing networks, we will often use a slightly simplified notation that represents exactly the same function without referring to an explicit bias node \( b \). Instead, we add a dummy node \( a_0 \) to each layer whose value will always be 1. Thus layer 0, the input layer, will have a dummy node \( a_0^{(0)} = 1 \), layer 1 will have \( a_0^{(1)} = 1 \), and so on. This dummy node still has an associated weight, and that weight represents the bias value \( b \). For example instead of an equation like

\[
h = \sigma(Wx + b)
\]  

(7.15)

we’ll use:

\[
h = \sigma(Wx)
\]  

(7.16)

But now instead of our vector \( x \) having \( n_0 \) values: \( x = x_1, \ldots, x_{n_0} \), it will have \( n_0 + 1 \) values, with a new 0th dummy value \( x_0 = 1 \): \( x = x_0, \ldots, x_{n_0} \). And instead of computing each \( h_j \) as follows:

\[
h_j = \sigma \left( \sum_{i=1}^{n_0} W_{ji} x_i + b_j \right)
\]  

(7.17)

we’ll instead use:

\[
h_j = \sigma \left( \sum_{i=0}^{n_0} W_{ji} x_i \right)
\]  

(7.18)

where the value \( W_{j0} \) replaces what had been \( b_j \). Fig. 7.9 shows a visualization.

![Figure 7.9](image.png)

We’ll continue showing the bias as \( b \) when we go over the learning algorithm in Section 7.5, but then we’ll switch to this simplified notation without explicit bias terms for the rest of the book.
7.4 Feedforward networks for NLP: Classification

Let’s see how to apply feedforward networks to NLP tasks! In this section we’ll look at classification tasks like sentiment analysis; in the next section we’ll introduce neural language modeling.

Let’s begin with a simple 2-layer sentiment classifier. You might imagine taking our logistic regression classifier from Chapter 5, which corresponds to a 1-layer network, and just adding a hidden layer. The input element $x_i$ could be scalar features like those in Fig. 5.2, e.g., $x_1 =$ count(words ∈ doc), $x_2 =$ count(positive lexicon words ∈ doc), $x_3 = 1$ if “no” ∈ doc, and so on. And the output layer $\hat{y}$ could have two nodes (one each for positive and negative), or 3 nodes (positive, negative, neutral), in which case $\hat{y}_1$ would be the estimated probability of positive sentiment, $\hat{y}_2$ the probability of negative and $\hat{y}_3$ the probability of neutral. The resulting equations would be just what we saw above for a 2-layer network (as always, we’ll continue to use the $\sigma$ to stand for any non-linearity, whether sigmoid, ReLU or other).

$$x = [x_1, x_2, \ldots, x_N] \quad \text{(each } x_i \text{ is a hand-designed feature)}$$
$$h = \sigma(Wx + b)$$
$$z = Uh$$
$$\hat{y} = \text{softmax}(z) \quad (7.19)$$

Fig. 7.10 shows a sketch of this architecture. As we mentioned earlier, adding this hidden layer to our logistic regression classifier allows the network to represent the non-linear interactions between features. This alone might give us a better sentiment classifier.

![Feedforward network sentiment analysis using traditional hand-built features](image)

Most applications of neural networks for NLP do something different, however. Instead of using hand-built human-engineered features as the input to our classifier, we draw on deep learning’s ability to learn features from the data by representing words as embeddings, like the word2vec or GloVe embeddings we saw in Chapter 6. There are various ways to represent an input for classification. One simple baseline is to apply some sort of pooling function to the embeddings of all the words in the
input. For example, for a text with \( n \) input words/tokens \( w_1, \ldots, w_n \), we can turn the \( n \) embeddings \( e(w_1), \ldots, e(w_n) \) (each of dimensionality \( d \)) into a single embedding also of dimensionality \( d \) by just summing the embeddings, or by taking their mean (summing and then dividing by \( n \)):

\[
x_{\text{mean}} = \frac{1}{n} \sum_{i=1}^{n} e(w_i)
\]  

(7.20)

There are many other options, like taking the element-wise max. The element-wise max of a set of \( n \) vectors is a new vector whose \( k \)-th element is the max of the \( k \)-th elements of all the \( n \) vectors. Here are the equations for this classifier assuming mean pooling; the architecture is sketched in Fig. 7.11:

\[
x = \text{mean}(e(w_1), e(w_2), \ldots, e(w_n))
\]

\[
h = \sigma(Wx + b)
\]

\[
z =Uh
\]

\[
y = \text{softmax}(z)
\]  

(7.21)

\[\text{Figure 7.11} \quad \text{Feedforward network sentiment analysis using a pooled embedding of the input words.}\]

While Eq. 7.21 shows how to classify a single example \( x \), in practice we want to efficiently classify an entire test set of \( m \) examples. We do this by vectoring the process, just as we saw with logistic regression; instead of using for-loops to go through each example, we’ll use matrix multiplication to do the entire computation of an entire test set at once. First, we pack all the input feature vectors for each input \( x \) into a single input matrix \( X \), with each row \( i \) a row vector consisting of the pooled embedding for input example \( x(i) \) (i.e., the vector \( x(i) \)). If the dimensionality of our pooled input embedding is \( d \), \( X \) will be a matrix of shape \( [m \times d] \).

We will then need to slightly modify Eq. 7.21. \( X \) is of shape \( [m \times d] \) and \( W \) is of shape \( [d_h \times d] \), so we’ll have to reorder how we multiply \( X \) and \( W \) and transpose \( W \) so they correctly multiply to yield a matrix \( H \) of shape \( [m \times d_h] \). The bias vector \( b \) from Eq. 7.21 of shape \( [1 \times d_h] \) will now have to be replicated into a matrix of shape \( [m \times d_h] \). We’ll need to similarly reorder the next step and transpose \( U \). Finally, our output matrix \( \hat{Y} \) will be of shape \( [m \times 3] \) (or more generally \( [m \times d_o] \), where \( d_o \) is
the number of output classes), with each row $i$ of our output matrix $\hat{Y}$ consisting of the output vector $\hat{y}^{(i)}$. Here are the final equations for computing the output class distribution for an entire test set:

$$
H = \sigma(XW^T + b)
$$
$$
Z = HU^T
$$
$$
\hat{Y} = \text{softmax}(Z)
$$

(7.22)

The idea of using word2vec or GloVe embeddings as our input representation—and more generally the idea of relying on another algorithm to have already learned an embedding representation for our input words—is called **pretraining**. Using pretrained embedding representations, whether simple static word embeddings like word2vec or the much more powerful contextual embeddings we’ll introduce in Chapter 11, is one of the central ideas of deep learning. (It’s also possible, however, to train the word embeddings as part of an NLP task; we’ll talk about how to do this in Section 7.7 in the context of the neural language modeling task.)

## 7.5 Training Neural Nets

A feedforward neural net is an instance of supervised machine learning in which we know the correct output $y$ for each observation $x$. What the system produces, via Eq. 7.13, is $\hat{y}$, the system’s estimate of the true $y$. The goal of the training procedure is to learn parameters $W^{[i]}$ and $b^{[i]}$ for each layer $i$ that make $\hat{y}$ for each training observation as close as possible to the true $y$.

In general, we do all this by drawing on the methods we introduced in Chapter 5 for logistic regression, so the reader should be comfortable with that chapter before proceeding.

First, we’ll need a **loss function** that models the distance between the system output and the gold output, and it’s common to use the loss function used for logistic regression, the **cross-entropy loss**.

Second, to find the parameters that minimize this loss function, we’ll use the **gradient descent** optimization algorithm introduced in Chapter 5.

Third, gradient descent requires knowing the **gradient** of the loss function, the vector that contains the partial derivative of the loss function with respect to each of the parameters. In logistic regression, for each observation we could directly compute the derivative of the loss function with respect to an individual $w$ or $b$. But for neural networks, with millions of parameters in many layers, it’s much harder to see how to compute the partial derivative of some weight in layer 1 when the loss is attached to some much later layer. How do we partial out the loss over all those intermediate layers? The answer is the algorithm called **error backpropagation** or **backward differentiation**.

### 7.5.1 Loss function

The **cross-entropy loss** that is used in neural networks is the same one we saw for logistic regression. If the neural network is being used as a binary classifier, with the sigmoid at the final layer, the loss function is the same logistic regression loss we saw in Eq. 5.23:

$$
L_{CE}(\hat{y}, y) = -\log p(y|x) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]
$$

(7.23)
If we are using the network to classify into 3 or more classes, the loss function is exactly the same as the loss for multinomial regression that we saw in Chapter 5 on page 101. Let’s briefly summarize the explanation here for convenience. First, when we have more than 2 classes we’ll need to represent both $y$ and $\hat{y}$ as vectors. Let’s assume we’re doing hard classification, where only one class is the correct one. The true label $y$ is then a vector with $K$ elements, each corresponding to a class, with $y_c = 1$ if the correct class is $c$, with all other elements of $y$ being 0. Recall that a vector like this, with one value equal to 1 and the rest 0, is called a one-hot vector. And our classifier will produce an estimate vector with $K$ elements $\hat{y}$, each element $\hat{y}_k$ of which represents the estimated probability $p(y_k = 1|x)$.

The loss function for a single example $x$ is the negative sum of the logs of the $K$ output classes, each weighted by their probability $y_k$:

$$L_{CE}(\hat{y}, y) = -\sum_{k=1}^{K} y_k \log \hat{y}_k \tag{7.24}$$

We can simplify this equation further; let’s first rewrite the equation using the function $\mathbb{1}\{}\{\}$ which evaluates to 1 if the condition in the brackets is true and to 0 otherwise. This makes it more obvious that the terms in the sum in Eq. 7.24 will be 0 except for the term corresponding to the true class for which $y_k = 1$:

$$L_{CE}(\hat{y}, y) = -\sum_{k=1}^{K} \mathbb{1}\{y_k = 1\} \log \hat{y}_k$$

In other words, the cross-entropy loss is simply the negative log of the output probability corresponding to the correct class, and we therefore also call this the negative log likelihood loss:

$$L_{CE}(\hat{y}, y) = -\log \hat{y}_c \quad \text{(where } c \text{ is the correct class)} \tag{7.25}$$

Plugging in the softmax formula from Eq. 7.9, and with $K$ the number of classes:

$$L_{CE}(\hat{y}, y) = -\log \frac{\exp(z_c)}{\sum_{j=1}^{K} \exp(z_j)} \quad \text{(where } c \text{ is the correct class)} \tag{7.26}$$

### 7.5.2 Computing the Gradient

How do we compute the gradient of this loss function? Computing the gradient requires the partial derivative of the loss function with respect to each parameter. For a network with one weight layer and sigmoid output (which is what logistic regression is), we could simply use the derivative of the loss that we used for logistic regression in Eq. 7.27 (and derived in Section 5.10):

$$\frac{\partial L_{CE}(\hat{y}, y)}{\partial w_j} = (\hat{y} - y) x_j$$

$$= (\sigma(w \cdot x + b) - y) x_j \tag{7.27}$$

Or for a network with one weight layer and softmax output (=multinomial logistic regression), we could use the derivative of the softmax loss from Eq. 5.48, shown
for a particular weight $w_k$ and input $x_i$

$$\frac{\partial L_{CE}(\hat{y}, y)}{\partial w_{k,i}} = -(y_k - \hat{y}_k)x_i$$

$$= -(y_k - p(y_k = 1|x))x_i$$

$$= -\left(y_k - \frac{\exp(w_k \cdot x + b_k)}{\sum_{j=1}^{K} \exp(w_j \cdot x + b_j)}\right)x_i \quad (7.28)$$

But these derivatives only give correct updates for one weight layer: the last one!

For deep networks, computing the gradients for each weight is much more complex, since we are computing the derivative with respect to weight parameters that appear all the way back in the very early layers of the network, even though the loss is computed only at the very end of the network.

The solution to computing this gradient is an algorithm called **error backpropagation** or backprop (Rumelhart et al., 1986). While backprop was invented specially for neural networks, it turns out to be the same as a more general procedure called **backward differentiation**, which depends on the notion of **computation graphs**. Let’s see how that works in the next subsection.

### 7.5.3 Computation Graphs

A computation graph is a representation of the process of computing a mathematical expression, in which the computation is broken down into separate operations, each of which is modeled as a node in a graph.

Consider computing the function $L(a, b, c) = c(a + 2b)$. If we make each of the component addition and multiplication operations explicit, and add names ($d$ and $e$) for the intermediate outputs, the resulting series of computations is:

$$d = 2 \cdot b$$

$$e = a + d$$

$$L = c \cdot e$$

We can now represent this as a graph, with nodes for each operation, and directed edges showing the outputs from each operation as the inputs to the next, as in Fig. 7.12. The simplest use of computation graphs is to compute the value of the function with some given inputs. In the figure, we’ve assumed the inputs $a = 3$, $b = 1$, $c = -2$, and we’ve shown the result of the **forward pass** to compute the result $L(3, 1, -2) = -10$. In the forward pass of a computation graph, we apply each operation left to right, passing the outputs of each computation as the input to the next node.

### 7.5.4 Backward differentiation on computation graphs

The importance of the computation graph comes from the **backward pass**, which is used to compute the derivatives that we’ll need for the weight update. In this example our goal is to compute the derivative of the output function $L$ with respect to each of the input variables, i.e., $\frac{\partial L}{\partial a}$, $\frac{\partial L}{\partial b}$, and $\frac{\partial L}{\partial c}$. The derivative $\frac{\partial L}{\partial c}$ tells us how much a small change in $a$ affects $L$.

Backwards differentiation makes use of the **chain rule** in calculus, so let’s remind ourselves of that. Suppose we are computing the derivative of a composite
function \( f(x) = u(v(x)) \). The derivative of \( f(x) \) is the derivative of \( u(x) \) with respect to \( v(x) \) times the derivative of \( v(x) \) with respect to \( x \):

\[
\frac{df}{dx} = \frac{du}{dv} \cdot \frac{dv}{dx}
\]  

The chain rule extends to more than two functions. If computing the derivative of a composite function \( f(x) = u(v(w(x))) \), the derivative of \( f(x) \) is:

\[
\frac{df}{dx} = \frac{du}{dv} \cdot \frac{dv}{dw} \cdot \frac{dw}{dx}
\]  

The intuition of backward differentiation is to pass gradients back from the final node to all the nodes in the graph. Fig. 7.13 shows part of the backward computation at one node \( e \). Each node takes an upstream gradient that is passed in from its parent node to the right, and for each of its inputs computes a local gradient (the gradient of its output with respect to its input), and uses the chain rule to multiply these two to compute a downstream gradient to be passed on to the next earlier node.

Let’s now compute the 3 derivatives we need. Since in the computation graph \( L = ce \), we can directly compute the derivative \( \frac{\partial L}{\partial c} \):

\[
\frac{\partial L}{\partial c} = e
\]  

For the other two, we’ll need to use the chain rule:

\[
\begin{align*}
\frac{\partial L}{\partial a} &= \frac{\partial L}{\partial e} \cdot \frac{\partial e}{\partial a} \\
\frac{\partial L}{\partial b} &= \frac{\partial L}{\partial e} \cdot \frac{\partial e}{\partial d} \cdot \frac{\partial d}{\partial b}
\end{align*}
\]  

Figure 7.12 Computation graph for the function \( L(a, b, c) = c(a + 2b) \), with values for input nodes \( a = 3, b = 1, c = -2 \), showing the forward pass computation of \( L \).
Eq. 7.32 and Eq. 7.31 thus require five intermediate derivatives: \( \frac{\partial L}{\partial e} \), \( \frac{\partial L}{\partial c} \), \( \frac{\partial e}{\partial a} \), \( \frac{\partial e}{\partial d} \), and \( \frac{\partial d}{\partial b} \), which are as follows (making use of the fact that the derivative of a sum is the sum of the derivatives):

\[
L = ce : \quad \frac{\partial L}{\partial e} = c, \quad \frac{\partial L}{\partial c} = e
\]

\[
e = a + d : \quad \frac{\partial e}{\partial a} = 1, \quad \frac{\partial e}{\partial d} = 1
\]

\[
d = 2b : \quad \frac{\partial d}{\partial b} = 2
\]

In the backward pass, we compute each of these partials along each edge of the graph from right to left, using the chain rule just as we did above. Thus we begin by computing the downstream gradients from node \( L \), which are \( \frac{\partial L}{\partial e} \) and \( \frac{\partial L}{\partial c} \). For node \( e \), we then multiply this upstream gradient \( \frac{\partial L}{\partial e} \) by the local gradient (the gradient of the output with respect to the input), \( \frac{\partial e}{\partial d} \) to get the output we send back to node \( d \): \( \frac{\partial L}{\partial d} \).

And so on, until we have annotated the graph all the way to all the input variables. The forward pass conveniently already will have computed the values of the forward intermediate variables we need (like \( d \) and \( e \)) to compute these derivatives. Fig. 7.14 shows the backward pass.

**Backward differentiation for a neural network**

Of course computation graphs for real neural networks are much more complex. Fig. 7.15 shows a sample computation graph for a 2-layer neural network with \( n_0 = 2 \), \( n_1 = 2 \), and \( n_2 = 1 \), assuming binary classification and hence using a sigmoid output unit for simplicity. The function that the computation graph is computing is:

\[
z^{[1]} = W^{[1]}x + b^{[1]}
\]

\[
a^{[1]} = \text{ReLU}(z^{[1]})
\]

\[
z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}
\]

\[
a^{[2]} = \sigma(z^{[2]})
\]

\[
\hat{y} = a^{[2]}
\]

(7.33)
For the backward pass we’ll also need to compute the loss $L$. The loss function for binary sigmoid output from Eq. 7.23 is

$$L_{CE}(\hat{y}, y) = -[y \log(\hat{y}) + (1 - y) \log(1 - \hat{y})]$$

(7.34)

Our output $\hat{y} = a[2]$, so we can rephrase this as

$$L_{CE}(a[2], y) = -[y \log(a[2]) + (1 - y) \log(1 - a[2])]$$

(7.35)

![Sample computation graph for a simple 2-layer neural net (= 1 hidden layer) with two input units and 2 hidden units. We’ve adjusted the notation a bit to avoid long equations in the nodes by just mentioning the function that is being computed, and the resulting variable name. Thus the * to the right of node $w[1]_{11}$ means that $w[1]_{11}$ is to be multiplied by $x_1$, and the node $z[1] = +$ means that the value of $z[1]$ is computed by summing the three nodes that feed into it (the two products, and the bias term $b[1]$).](https://example.com/computation-graph.png)

Figure 7.15 Sample computation graph for a simple 2-layer neural net (= 1 hidden layer) with two input units and 2 hidden units. We’ve adjusted the notation a bit to avoid long equations in the nodes by just mentioning the function that is being computed, and the resulting variable name. Thus the * to the right of node $w[1]_{11}$ means that $w[1]_{11}$ is to be multiplied by $x_1$, and the node $z[1] = +$ means that the value of $z[1]$ is computed by summing the three nodes that feed into it (the two products, and the bias term $b[1]$).

The weights that need updating (those for which we need to know the partial derivative of the loss function) are shown in teal. In order to do the backward pass, we’ll need to know the derivatives of all the functions in the graph. We already saw in Section 5.10 the derivative of the sigmoid $\sigma$:

$$\frac{d\sigma(z)}{dz} = \sigma(z)(1 - \sigma(z))$$

(7.36)

We’ll also need the derivatives of each of the other activation functions. The derivative of tanh is:

$$\frac{dtanh(z)}{dz} = 1 - tanh^2(z)$$

(7.37)

The derivative of the ReLU is

$$\frac{dReLU(z)}{dz} = \begin{cases} 0 & \text{for } z < 0 \\ 1 & \text{for } z \geq 0 \end{cases}$$

(7.38)

We’ll give the start of the computation, computing the derivative of the loss function $L$ with respect to $z$, or $\frac{\partial L}{\partial z}$ (and leaving the rest of the computation as an exercise for the reader). By the chain rule:

$$\frac{\partial L}{\partial z} = \frac{\partial L}{\partial a[2]} \frac{\partial a[2]}{\partial z}$$

(7.39)
So let’s first compute \( \frac{\partial L}{\partial a^2} \), taking the derivative of Eq. 7.35, repeated here:

\[
L_{CE}(a^2, y) = -[y \log a^2 + (1 - y) \log(1 - a^2)]
\]

\[
\frac{\partial L}{\partial a^2} = - \left( \left( y \frac{\partial \log(a^2)}{\partial a^2} \right) + (1 - y) \frac{\partial \log(1 - a^2)}{\partial a^2} \right)
\]

\[
= - \left( y \frac{1}{a^2} + (1 - y) \frac{1}{1 - a^2} (-1) \right)
\]

\[
= - \left( \frac{y}{a^2} + \frac{y - 1}{1 - a^2} \right)
\]

(7.40)

Next, by the derivative of the sigmoid:

\[
\frac{\partial a^2}{\partial z} = a^2 (1 - a^2)
\]

Finally, we can use the chain rule:

\[
\frac{\partial L}{\partial z} = \frac{\partial L}{\partial a^2} \frac{\partial a^2}{\partial z}
\]

\[
= - \left( \frac{y}{a^2} + \frac{y - 1}{1 - a^2} \right) a^2 (1 - a^2)
\]

\[
= a^2 - y
\]

(7.41)

Continuing the backward computation of the gradients (next by passing the gradients over \( b_1^2 \) and the two product nodes, and so on, back to all the teal nodes), is left as an exercise for the reader.

### 7.5.5 More details on learning

Optimization in neural networks is a non-convex optimization problem, more complex than for logistic regression, and for that and other reasons there are many best practices for successful learning.

For logistic regression we can initialize gradient descent with all the weights and biases having the value 0. In neural networks, by contrast, we need to initialize the weights with small random numbers. It’s also helpful to normalize the input values to have 0 mean and unit variance.

Various forms of regularization are used to prevent overfitting. One of the most important is **dropout**: randomly dropping some units and their connections from the network during training (Hinton et al. 2012, Srivastava et al. 2014). Tuning of **hyperparameters** is also important. The parameters of a neural network are the weights \( W \) and biases \( b \); those are learned by gradient descent. The hyperparameters are things that are chosen by the algorithm designer; optimal values are tuned on a devset rather than by gradient descent learning on the training set. Hyperparameters include the learning rate \( \eta \), the mini-batch size, the model architecture (the number of layers, the number of hidden nodes per layer, the choice of activation functions), how to regularize, and so on. Gradient descent itself also has many architectural variants such as Adam (Kingma and Ba, 2015).

Finally, most modern neural networks are built using computation graph formalisms that make it easy and natural to do gradient computation and parallelization.
on vector-based GPUs (Graphic Processing Units). PyTorch (Paszke et al., 2017) and TensorFlow (Abadi et al., 2015) are two of the most popular. The interested reader should consult a neural network textbook for further details; some suggestions are at the end of the chapter.

7.6 Feedforward Neural Language Modeling

As our second application of feedforward networks, let’s consider language modeling: predicting upcoming words from prior words. Neural language modeling—based on the transformer architecture that we will see in Chapter 10—is the algorithm the underlies all of modern NLP. In this section and the next we’ll introduce a simpler version of neural language models for feedforward networks, an algorithm first introduced by Bengio et al. (2003). The feedforward language model introduces many of the important concepts of neural language modeling, concepts we’ll return to as we describe more powerful models in Chapter 9 and Chapter 10.

Neural language models have many advantages over the n-gram language models of Chapter 3. Compared to n-gram models, neural language models can handle much longer histories, can generalize better over contexts of similar words, and are more accurate at word-prediction. On the other hand, neural net language models are much more complex, are slower and need more energy to train, and are less interpretable than n-gram models, so for some smaller tasks an n-gram language model is still the right tool.

A feedforward neural language model (LM) is a feedforward network that takes as input at time \( t \) a representation of some number of previous words \( (w_{t-1}, w_{t-2}, \text{etc.}) \) and outputs a probability distribution over possible next words. Thus—like the n-gram LM—the feedforward neural LM approximates the probability of a word given the entire prior context \( P(w_t|w_1:t-1) \) by approximating based on the \( N-1 \) previous words:

\[
P(w_t|w_1, \ldots, w_{t-1}) \approx P(w_t|w_{t-N+1}, \ldots, w_{t-1})
\]  

(7.42)

In the following examples we’ll use a 4-gram example, so we’ll show a neural net to estimate the probability \( P(w_t = i|w_{t-3}, w_{t-2}, w_{t-1}) \).

Neural language models represent words in this prior context by their embeddings, rather than just by their word identity as used in n-gram language models. Using embeddings allows neural language models to generalize better to unseen data. For example, suppose we’ve seen this sentence in training:

I have to make sure that the cat gets fed.

but have never seen the words “gets fed” after the word “dog”. Our test set has the prefix “I forgot to make sure that the dog gets”. What’s the next word? An n-gram language model will predict “fed” after “that the cat gets”, but not after “that the dog gets”. But a neural LM, knowing that “cat” and “dog” have similar embeddings, will be able to generalize from the “cat” context to assign a high enough probability to “fed” even after seeing “dog”.

### 7.6.1 Forward inference in the neural language model

Let’s walk through forward inference or decoding for neural language models. Forward inference is the task, given an input, of running a forward pass on the
network to produce a probability distribution over possible outputs, in this case next words.

We first represent each of the $N$ previous words as a one-hot vector of length $|V|$, i.e., with one dimension for each word in the vocabulary. A one-hot vector is a vector that has one element equal to 1—in the dimension corresponding to that word’s index in the vocabulary—while all the other elements are set to zero. Thus in a one-hot representation for the word “toothpaste”, supposing it is $V_5$, i.e., index 5 in the vocabulary, $x_5 = 1$, and $x_i = 0$ for $i \neq 5$, as shown here:

$$[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ \ldots \ 0 \ 0 \ 0]$$

The feedforward neural language model (sketched in Fig. 7.17) has a moving window that can see $N$ words into the past. We’ll let $N$ equal 3, so the 3 words $w_{t-3}$, $w_{t-2}$, and $w_{t-1}$ are each represented as a one-hot vector. We then multiply these one-hot vectors by the embedding matrix $E$. The embedding weight matrix $E$ has a column for each word, each a column vector of $d$ dimensions, and hence has dimensionality $d \times |V|$. Multiplying by a one-hot vector that has only one non-zero element $x_i = 1$ simply selects out the relevant column vector for word $i$, resulting in the embedding for word $i$, as shown in Fig. 7.16.

![Figure 7.16](image)

The 3 resulting embedding vectors are concatenated to produce $e$, the embedding layer. This is followed by a hidden layer and an output layer whose softmax produces a probability distribution over words. For example $y_{42}$, the value of output node 42, is the probability of the next word $w_t$ being $V_{42}$, the vocabulary word with index 42 (which is the word ‘fish’ in our example).

Here’s the algorithm in detail for our mini example:

1. **Select three embeddings from $E$**: Given the three previous words, we look up their indices, create 3 one-hot vectors, and then multiply each by the embedding matrix $E$. Consider $w_{t-3}$. The one-hot vector for ‘for’ (index 35) is multiplied by the embedding matrix $E$, to give the first part of the first hidden layer, the embedding layer. Since each column of the input matrix $E$ is an embedding for a word, and the input is a one-hot column vector $x_i$ for word $V_i$, the embedding layer for input $w$ will be $Ex_i = e_i$, the embedding for word $i$. We now concatenate the three embeddings for the three context words to produce the embedding layer $e$.

2. **Multiply by $W$**: We multiply by $W$ (and add $b$) and pass through the ReLU (or other) activation function to get the hidden layer $h$.

3. **Multiply by $U$**: $h$ is now multiplied by $U$

4. **Apply softmax**: After the softmax, each node $i$ in the output layer estimates the probability $P(w_t = i|w_{t-1}, w_{t-2}, w_{t-3})$
Figure 7.17  Forward inference in a feedforward neural language model. At each timestep \( t \) the network computes a \( d \)-dimensional embedding for each context word (by multiplying a one-hot vector by the embedding matrix \( E \)), and concatenates the 3 resulting embeddings to get the embedding layer \( e \). The embedding vector \( e \) is multiplied by a weight matrix \( W \) and then an activation function is applied element-wise to produce the hidden layer \( h \), which is then multiplied by another weight matrix \( U \). Finally, a softmax output layer predicts at each node \( i \) the probability that the next word \( w_t \) will be vocabulary word \( V_i \).

In summary, the equations for a neural language model with a window size of 3, given one-hot input vectors for each input context word, are:

\[
\begin{align*}
    e &= [Ex_{t-3}; Ex_{t-2}; Ex_{t-1}] \\
    h &= \sigma(We + b) \\
    z &= Uh \\
    \hat{y} &= \text{softmax}(z)
\end{align*}
\]

(7.43)

Note that we formed the embedding layer \( e \) by concatenating the 3 embeddings for the three context vectors; we’ll often use semicolons to mean concatenation of vectors.

7.7 Training the neural language model

The high-level intuition of training neural language models, whether the simple feedforward language models we describe here or the more powerful transformer language models of Chapter 10, is the idea of self-training or self-supervision that we saw in Chapter 6 for learning word representations. In self-training for language modeling, we take a corpus of text as training material and at each time step \( t \) ask the model to predict the next word. At first it will do poorly at this task, but since...
in each case we know the correct answer (it’s the next word in the corpus!) we can easily train it to be better at predicting the correct next word. We call such a model self-supervised because we don’t have to add any special gold labels to the data; the natural sequence of words is its own supervision! We simply train the model to minimize the error in predicting the true next word in the training sequence.

In practice, training the model means setting the parameters $\theta = E, W, U, b$. For some tasks, it’s ok to freeze the embedding layer $E$ with initial word2vec values. Freezing means we use word2vec or some other pretraining algorithm to compute the initial embedding matrix $E$, and then hold it constant while we only modify $W, U, b$, i.e., we don’t update $E$ during language model training. However, often we’d like to learn the embeddings simultaneously with training the network. This is useful when the task the network is designed for (like sentiment classification, translation, or parsing) places strong constraints on what makes a good representation for words.

Let’s see how to train the entire model including $E$, i.e. to set all the parameters $\theta = E, W, U, b$. We’ll do this via gradient descent (Fig. 5.6), using error backpropagation on the computation graph to compute the gradient. Training thus not only sets the weights $W$ and $U$ of the network, but also as we’re predicting upcoming words, we’re learning the embeddings $E$ for each word that best predict upcoming words.

Fig. 7.18 shows the set up for a window size of $N=3$ context words. The input $x$ consists of 3 one-hot vectors, fully connected to the embedding layer via 3 instantiations of the embedding matrix $E$. We don’t want to learn separate weight matrices for mapping each of the 3 previous words to the projection layer. We want one single embedding dictionary $E$ that’s shared among these three. That’s because over time, many different words will appear as $w_{t-2}$ or $w_{t-1}$, and we’d like to just represent...
each word with one vector, whichever context position it appears in. Recall that the embedding weight matrix $E$ has a column for each word, each a column vector of $d$ dimensions, and hence has dimensionality $d \times |V|$.

Generally training proceeds by taking as input a very long text, concatenating all the sentences, starting with random weights, and then iteratively moving through the text predicting each word $w_t$. At each word $w_t$, we use the cross-entropy (negative log likelihood) loss. Recall that the general form for this (repeated from Eq. 7.25) is:

$$L_{CE}(\hat{y}, y) = -\log \hat{y}_i,$$  \hspace{1cm} (where $i$ is the correct class) \hspace{1cm} (7.44)

For language modeling, the classes are the words in the vocabulary, so $\hat{y}_i$ here means the probability that the model assigns to the correct next word $w_t$:

$$L_{CE} = -\log p(w_t|w_{t-1}, \ldots, w_{t-n+1})$$  \hspace{1cm} (7.45)

The parameter update for stochastic gradient descent for this loss from step $s$ to $s+1$ is then:

$$\theta^{s+1} = \theta^s - \eta \frac{\partial}{\partial \theta} \left[-\log p(w_t|w_{t-1}, \ldots, w_{t-n+1})\right]$$  \hspace{1cm} (7.46)

This gradient can be computed in any standard neural network framework which will then backpropagate through $\theta = E, W, U, b$.

Training the parameters to minimize loss will result both in an algorithm for language modeling (a word predictor) but also a new set of embeddings $E$ that can be used as word representations for other tasks.

7.8 Summary

- Neural networks are built out of neural units, originally inspired by biological neurons but now simply an abstract computational device.
- Each neural unit multiplies input values by a weight vector, adds a bias, and then applies a non-linear activation function like sigmoid, tanh, or rectified linear unit.
- In a fully-connected, feedforward network, each unit in layer $i$ is connected to each unit in layer $i+1$, and there are no cycles.
- The power of neural networks comes from the ability of early layers to learn representations that can be utilized by later layers in the network.
- Neural networks are trained by optimization algorithms like gradient descent.
- Error backpropagation, backward differentiation on a computation graph, is used to compute the gradients of the loss function for a network.
- Neural language models use a neural network as a probabilistic classifier, to compute the probability of the next word given the previous $n$ words.
- Neural language models can use pretrained embeddings, or can learn embeddings from scratch in the process of language modeling.
Bibliographical and Historical Notes

The origins of neural networks lie in the 1940s McCulloch-Pitts neuron (McCulloch and Pitts, 1943), a simplified model of the biological neuron as a kind of computing element that could be described in terms of propositional logic. By the late 1950s and early 1960s, a number of labs (including Frank Rosenblatt at Cornell and Bernard Widrow at Stanford) developed research into neural networks; this phase saw the development of the perceptron (Rosenblatt, 1958), and the transformation of the threshold into a bias, a notation we still use (Widrow and Hoff, 1960).

The field of neural networks declined after it was shown that a single perceptron unit was unable to model functions as simple as XOR (Minsky and Papert, 1969). While some small amount of work continued during the next two decades, a major revival for the field didn’t come until the 1980s, when practical tools for building deeper networks like error backpropagation became widespread (Rumelhart et al., 1986). During the 1980s a wide variety of neural network and related architectures were developed, particularly for applications in psychology and cognitive science (Rumelhart and McClelland 1986b, McClelland and Elman 1986, Rumelhart and McClelland 1986a, Elman 1990), for which the term connectionist or parallel distributed processing was often used (Feldman and Ballard 1982, Smolensky 1988). Many of the principles and techniques developed in this period are foundational to modern work, including the ideas of distributed representations (Hinton, 1986), recurrent networks (Elman, 1990), and the use of tensors for compositionality (Smolensky, 1990).

By the 1990s larger neural networks began to be applied to many practical language processing tasks as well, like handwriting recognition (LeCun et al. 1989) and speech recognition (Morgan and Bourlard 1990). By the early 2000s, improvements in computer hardware and advances in optimization and training techniques made it possible to train even larger and deeper networks, leading to the modern term deep learning (Hinton et al. 2006, Bengio et al. 2007). We cover more related history in Chapter 9 and Chapter 16.

There are a number of excellent books on the subject. Goldberg (2017) has superb coverage of neural networks for natural language processing. For neural networks in general see Goodfellow et al. (2016) and Nielsen (2015).
CHAPTER 8 • SEQUENCE LABELING FOR PARTS OF SPEECH AND NAMED ENTITIES

Sequence Labeling for Parts of Speech and Named Entities

To each word a warbling note
A Midsummer Night’s Dream, VI

Dionysius Thrax of Alexandria (c. 100 B.C.), or perhaps someone else (it was a long time ago), wrote a grammatical sketch of Greek (a “technē”) that summarized the linguistic knowledge of his day. This work is the source of an astonishing proportion of modern linguistic vocabulary, including the words syntax, diphthong, clitic, and analogy. Also included are a description of eight parts of speech: noun, verb, pronoun, preposition, adverb, conjunction, participle, and article. Although earlier scholars (including Aristotle as well as the Stoics) had their own lists of parts of speech, it was Thrax’s set of eight that became the basis for descriptions of European languages for the next 2000 years. (All the way to the Schoolhouse Rock educational television shows of our childhood, which had songs about 8 parts of speech, like the late great Bob Dorough’s Conjunction Junction.) The durability of parts of speech through two millennia speaks to their centrality in models of human language.

Proper names are another important and anciently studied linguistic category. While parts of speech are generally assigned to individual words or morphemes, a proper name is often an entire multiword phrase, like the name “Marie Curie”, the location “New York City”, or the organization “Stanford University”. We’ll use the term named entity for, roughly speaking, anything that can be referred to with a proper name: a person, a location, an organization, although as we’ll see the term is commonly extended to include things that aren’t entities per se.

Parts of speech (also known as POS) and named entities are useful clues to sentence structure and meaning. Knowing whether a word is a noun or a verb tells us about likely neighboring words (nouns in English are preceded by determiners and adjectives, verbs by nouns) and syntactic structure (verbs have dependency links to nouns), making part-of-speech tagging a key aspect of parsing. Knowing if a named entity like Washington is a name of a person, a place, or a university is important to many natural language processing tasks like question answering, stance detection, or information extraction.

In this chapter we’ll introduce the task of part-of-speech tagging, taking a sequence of words and assigning each word a part of speech like NOUN or VERB, and the task of named entity recognition (NER), assigning words or phrases tags like PERSON, LOCATION, or ORGANIZATION.

Such tasks in which we assign, to each word \( x_i \) in an input word sequence, a label \( y_i \), so that the output sequence \( Y \) has the same length as the input sequence \( X \) are called sequence labeling tasks. We’ll introduce classic sequence labeling algorithms, one generative—the Hidden Markov Model (HMM)—and one discriminative—the Conditional Random Field (CRF). In following chapters we’ll introduce modern sequence labelers based on RNNs and Transformers.
8.1 (Mostly) English Word Classes

Until now we have been using part-of-speech terms like \textit{noun} and \textit{verb} rather freely. In this section we give more complete definitions. While word classes do have semantic tendencies—adjectives, for example, often describe \textit{properties} and nouns \textit{people}—parts of speech are defined instead based on their grammatical relationship with neighboring words or the morphological properties about their affixes.

<table>
<thead>
<tr>
<th>Tag</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADJ</td>
<td>Adjective: noun modifiers describing properties</td>
<td>red, young, awesome</td>
</tr>
<tr>
<td>ADV</td>
<td>Adverb: verb modifiers of time, place, manner</td>
<td>very, slowly, home, yesterday</td>
</tr>
<tr>
<td>NOUN</td>
<td>words for persons, places, things, etc.</td>
<td>algorithm, cat, mango, beauty</td>
</tr>
<tr>
<td>VERB</td>
<td>words for actions and processes</td>
<td>draw, provide, go</td>
</tr>
<tr>
<td>PROP</td>
<td>Proper noun: name of a person, organization, place, etc.</td>
<td>Regina, IBM, Colorado</td>
</tr>
<tr>
<td>INTJ</td>
<td>Interjection: exclamation, greeting, yes/no response, etc.</td>
<td>oh, um, yes, helo</td>
</tr>
<tr>
<td>ADP</td>
<td>Adposition (Preposition/Postposition): marks a noun’s spacial, temporal, or other relation</td>
<td>in, on, by, under</td>
</tr>
<tr>
<td>AUX</td>
<td>Auxiliary: helping verb marking tense, aspect, mood, etc.,</td>
<td>can, may, should, are</td>
</tr>
<tr>
<td>CCONJ</td>
<td>Coordinating Conjunction: joins two phrases/clauses</td>
<td>and, or, but</td>
</tr>
<tr>
<td>DET</td>
<td>Determiner: marks noun phrase properties</td>
<td>a, an, the, this</td>
</tr>
<tr>
<td>NUM</td>
<td>Numerals</td>
<td>one, two, 2026, 11:00, hundred</td>
</tr>
<tr>
<td>PART</td>
<td>Particle: a function word that must be associated with another word</td>
<td>'s, not, (infinitive) to</td>
</tr>
<tr>
<td>PRON</td>
<td>Pronoun: a shorthand for referring to an entity or event</td>
<td>she, who, I, others</td>
</tr>
<tr>
<td>SCONJ</td>
<td>Subordinating Conjunction: joins a main clause with a subordinate clause such as a sentential complement</td>
<td>whether, because</td>
</tr>
<tr>
<td>PUNCT</td>
<td>Punctuation</td>
<td>, , ()</td>
</tr>
<tr>
<td>SYM</td>
<td>Symbols like $ or emoji</td>
<td>$, %</td>
</tr>
<tr>
<td>X</td>
<td>Other</td>
<td>asdf, qwfg</td>
</tr>
</tbody>
</table>

**Figure 8.1** The 17 parts of speech in the Universal Dependencies tagset (de Marneffe et al., 2021). Features can be added to make finer-grained distinctions (with properties like number, case, definiteness, and so on).

Parts of speech fall into two broad categories: \textit{closed class} and \textit{open class}. Closed classes are those with relatively fixed membership, such as prepositions—new prepositions are rarely coined. By contrast, nouns and verbs are open classes—new nouns and verbs like \textit{iPhone} or \textit{to fax} are continually being created or borrowed. Closed class words are generally \textit{function words} like \textit{of}, \textit{it}, \textit{and}, or \textit{you}, which tend to be very short, occur frequently, and often have structuring uses in grammar.

Four major open classes occur in the languages of the world: \textit{nouns} (including proper nouns), \textit{verbs}, \textit{adjectives}, and \textit{adverbs}, as well as the smaller open class of \textit{interjections}. English has all five, although not every language does.

**Nouns** are words for people, places, or things, but include others as well. \textit{Common nouns} include concrete terms like \textit{cat} and \textit{mango}, abstractions like \textit{algorithm} and \textit{beauty}, and verb-like terms like \textit{pacing} as in \textit{His pacing to and fro became quite annoying}. Nouns in English can occur with determiners (\textit{a goat}, \textit{this bandwidth}) take possessives (\textit{IBM’s annual revenue}), and may occur in the plural (\textit{goats}, \textit{abaci}). Many languages, including English, divide common nouns into \textit{count nouns} and \textit{mass nouns}. Count nouns can occur in the singular and plural (\textit{goat/goats}, \textit{relationship/relationships}) and can be counted (\textit{one goat}, \textit{two goats}). Mass nouns are used when something is conceptualized as a homogeneous group. So \textit{snow}, \textit{salt}, and \textit{communism} are not counted (i.e., \textit{*two snows} or \textit{*two communisms}). **Proper nouns**, like \textit{Regina}, \textit{Colorado}, and \textit{IBM}, are names of specific persons or entities.
Verbs refer to actions and processes, including main verbs like *draw*, *provide*, and *go*. English verbs have inflections (non-third-person-singular (*eat*), third-person-singular (*eats*), progressive (*eating*), past participle (*eaten*)). While many scholars believe that all human languages have the categories of noun and verb, others have argued that some languages, such as Riau Indonesian and Tongan, don’t even make this distinction (Broschart 1997; Evans 2000; Gil 2000).

Adjectives often describe properties or qualities of nouns, like color (*white*, *black*), age (*old*, *young*), and value (*good*, *bad*), but there are languages without adjectives. In Korean, for example, the words corresponding to English adjectives act as a subclass of verbs, so what is in English an adjective “beautiful” acts in Korean like a verb meaning “to be beautiful”.

Adverbs are a hodge-podge. All the italicized words in this example are adverbs:

> Actually, I ran home extremely quickly yesterday

Adverbs generally modify something (often verbs, hence the name “adverb”, but also other adverbs and entire verb phrases). *Directional adverbs* or *locative adverbs* (*home*, *here*, *downhill*) specify the direction or location of some action; *degree adverbs* (*extremely*, *very*, *somewhat*) specify the extent of some action, process, or property; *manner adverbs* (*slowly*, *slinkily*, *delicately*) describe the manner of some action or process; and *temporal adverbs* describe the time that some action or event took place (*yesterday*, *Monday*).

Interjections (*oh*, *hey*, *alas*, *uh*, *um*) are a smaller open class that also includes greetings (*hello*, *goodbye*) and question responses (*yes*, *no*, *uh-huh*).

English adpositions occur before nouns, hence are called *prepositions*. They can indicate spatial or temporal relations, whether literal (*on it, before then, by the house*) or metaphorical (*on time, with gusto, beside herself*), and relations like marking the agent in *Hamlet was written by Shakespeare*.

A *particle* resembles a preposition or an adverb and is used in combination with a verb. Particles often have extended meanings that aren’t quite the same as the prepositions they resemble, as in the particle *over* in *she turned the paper over*. A verb and a particle acting as a single unit is called a *phrasal verb*. The meaning of phrasal verbs is often *non-compositional*—not predictable from the individual meanings of the verb and the particle. Thus, *turn down* means ‘reject’, *rule out* ‘eliminate’, and *go on* ‘continue’.

Determiners like *this* and *that* (*this chapter*, *that page*) can mark the start of an English noun phrase. *Articles* like *a*, *an*, and *the*, are a type of determiner that mark discourse properties of the noun and are quite frequent; *the* is the most common word in written English, with *a* and *an* right behind.

Conjunctions join two phrases, clauses, or sentences. Coordinating conjunctions like *and*, *or*, and *but* join two elements of equal status. Subordinating conjunctions are used when one of the elements has some embedded status. For example, the subordinating conjunction *that* in “I thought that you might like some milk” links the main clause *I thought* with the subordinate clause *you might like some milk*. This clause is called subordinate because this entire clause is the “content” of the main verb *thought*. Subordinating conjunctions like *that* which link a verb to its argument in this way are also called *complementizers*.

Pronouns act as a shorthand for referring to an entity or event. Personal pronouns refer to persons or entities (*you*, *she*, *I*, *it*, *me*, etc.). Possessive pronouns are forms of personal pronouns that indicate either actual possession or more often just an abstract relation between the person and some object (*my*, *your*, *his*, *her*, *its*, *one’s*, *our*, *their*). *Wh-pronouns* (*what*, *who*, *whom*, *whoever*) are used in certain question...
forms, or act as complementizers (Frida, who married Diego...).

Auxiliary verbs mark semantic features of a main verb such as its tense, whether it is completed (aspect), whether it is negated (polarity), and whether an action is necessary, possible, suggested, or desired (mood). English auxiliaries include the copula verb be, the two verbs do and have, forms, as well as modal verbs used to mark the mood associated with the event depicted by the main verb: can indicates ability or possibility, may permission or possibility, must necessity.

An English-specific tagset, the 45-tag Penn Treebank tagset (Marcus et al., 1993), shown in Fig. 8.2, has been used to label many syntactically annotated corpora like the Penn Treebank corpora, so is worth knowing about.

<table>
<thead>
<tr>
<th>Tag</th>
<th>Description</th>
<th>Example</th>
<th>Tag</th>
<th>Description</th>
<th>Example</th>
<th>Tag</th>
<th>Description</th>
<th>Example</th>
<th>Tag</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>CC</td>
<td>coord. conj.</td>
<td>and, but, or</td>
<td>CD</td>
<td>cardinal number</td>
<td>one, two</td>
<td>DT</td>
<td>determiner</td>
<td>a, the</td>
<td>EX</td>
<td>existential ‘there’</td>
<td>there</td>
</tr>
<tr>
<td>CD</td>
<td>cardinal number</td>
<td>NNP</td>
<td>DT</td>
<td>determiner</td>
<td>NNS</td>
<td>EX</td>
<td>cardinal number</td>
<td>one, two</td>
<td>FW</td>
<td>foreign word</td>
<td>mecaulpa</td>
</tr>
<tr>
<td>DT</td>
<td>determiner</td>
<td>all, both</td>
<td>FW</td>
<td>foreign word</td>
<td>POS</td>
<td>IN</td>
<td>preposition/synonym</td>
<td>of, in, by</td>
<td>IN</td>
<td>preposition/synonym</td>
<td>I, you, he</td>
</tr>
<tr>
<td>EX</td>
<td>existential ‘there’</td>
<td>PDT</td>
<td>IN</td>
<td>personal pronoun</td>
<td>PRP</td>
<td>JJ</td>
<td>adjective</td>
<td>yellow</td>
<td>JJ</td>
<td>adjective</td>
<td>PRPS</td>
</tr>
<tr>
<td>FW</td>
<td>foreign word</td>
<td>POS</td>
<td>IN</td>
<td>personal pronoun</td>
<td>PRP</td>
<td>JJR</td>
<td>comparative adj</td>
<td>bigger</td>
<td>JJR</td>
<td>comparative adj</td>
<td>RBP</td>
</tr>
<tr>
<td>IN</td>
<td>preposition/synonym</td>
<td>all, both</td>
<td>JJS</td>
<td>superlative adj</td>
<td>RBS</td>
<td>LS</td>
<td>list item marker</td>
<td>1, 2, One</td>
<td>LS</td>
<td>list item marker</td>
<td>RBS</td>
</tr>
<tr>
<td>NN</td>
<td>sing or mass noun</td>
<td>llamas</td>
<td>MD</td>
<td>modal</td>
<td>RP</td>
<td>MD</td>
<td>modal</td>
<td>can, should</td>
<td>MD</td>
<td>modal</td>
<td>RP</td>
</tr>
<tr>
<td>NN</td>
<td>sing or mass noun</td>
<td>llamas</td>
<td>NN</td>
<td>noun</td>
<td>SYM</td>
<td>NN</td>
<td>noun</td>
<td>llama</td>
<td>NN</td>
<td>noun</td>
<td>SYM</td>
</tr>
<tr>
<td>TO</td>
<td>infinitive to</td>
<td>to</td>
<td>VB</td>
<td>verb base</td>
<td>eat</td>
<td>VB</td>
<td>verb base</td>
<td>eat</td>
<td>VB</td>
<td>verb base</td>
<td>eat</td>
</tr>
<tr>
<td>UH</td>
<td>interjection</td>
<td>ah, oops</td>
<td>VBD</td>
<td>verb past tense</td>
<td>ate</td>
<td>VBG</td>
<td>verb gerund</td>
<td>eating</td>
<td>VBN</td>
<td>verb past participle</td>
<td>eaten</td>
</tr>
<tr>
<td>VBZ</td>
<td>verb 3sg pres</td>
<td>3sg pres</td>
<td>WP</td>
<td>wh-pronoun</td>
<td>whose</td>
<td>WP$</td>
<td>wh-possess.</td>
<td>whose</td>
<td>WP</td>
<td>wh-pronoun</td>
<td>what</td>
</tr>
<tr>
<td>WP$</td>
<td>wh-possess.</td>
<td>whose</td>
<td>POS</td>
<td>possessive ending</td>
<td>'s</td>
<td>POS</td>
<td>possessive ending</td>
<td>'s</td>
<td>POS</td>
<td>possessive ending</td>
<td>'s</td>
</tr>
<tr>
<td>WDT</td>
<td>wh-determin.</td>
<td>which, that</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
</tr>
<tr>
<td>WRB</td>
<td>wh-adverb</td>
<td>how, where</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
<td>SYM</td>
<td>symbol</td>
<td>+, %, &amp;</td>
</tr>
</tbody>
</table>

Below we show some examples with each word tagged according to both the UD and Penn tags. Notice that the Penn tagset distinguishes tense and participles on verbs, and has a special tag for the existential there construction in English. Note that since London Journal of Medicine is a proper noun, both tagsets mark its component nouns as PROPN/NNP, including journal and medicine, which might otherwise be labeled as common nouns (NOUN/NN).

(8.1) There/PRO/EX are/VERB/VBP 70/NUM/CD children/NOUN/NNS there/ADV/IN /PUNC/.

(8.2) Preliminary/ADJ/IN findings/NOUN/NNS were/AUX/VBD reported/VERB/VBN in/ADP/IN today/NOUN/NN ‘s/PART/POS London/PROPN/NNP Journal/PROPN/IN off/ADP/IN Medicine/PROPN/NNP

8.2 Part-of-Speech Tagging

**Part-of-speech tagging** is the process of assigning a part-of-speech to each word in a text. The input is a sequence $x_1, x_2, ..., x_n$ of (tokenized) words and a tagset, and the output is a sequence $y_1, y_2, ..., y_n$ of tags, each output $y_i$ corresponding exactly to one input $x_i$, as shown in the intuition in Fig. 8.3.

Tagging is a disambiguation task; words are ambiguous — have more than one possible part-of-speech—and the goal is to find the correct tag for the situation. For example, book can be a verb (book that flight) or a noun (hand me that book). That can be a determiner (Does that flight serve dinner) or a complementizer (I
thought that your flight was earlier). The goal of POS-tagging is to resolve these ambiguities, choosing the proper tag for the context.

The accuracy of part-of-speech tagging algorithms (the percentage of test set tags that match human gold labels) is extremely high. One study found accuracies over 97% across 15 languages from the Universal Dependency (UD) treebank (Wu and Dredze, 2019). Accuracies on various English treebanks are also 97% (no matter the algorithm; HMMs, CRFs, BERT perform similarly). This 97% number is also about the human performance on this task, at least for English (Manning, 2011).

<table>
<thead>
<tr>
<th>Types:</th>
<th>WSJ</th>
<th>Brown</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unambiguous (1 tag)</td>
<td>44,432 (86%)</td>
<td>45,799 (85%)</td>
</tr>
<tr>
<td>Ambiguous (2+ tags)</td>
<td>7,025 (14%)</td>
<td>8,050 (15%)</td>
</tr>
<tr>
<td>Tokens:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Unambiguous (1 tag)</td>
<td>577,421 (45%)</td>
<td>384,349 (33%)</td>
</tr>
<tr>
<td>Ambiguous (2+ tags)</td>
<td>711,780 (55%)</td>
<td>786,646 (67%)</td>
</tr>
</tbody>
</table>

We’ll introduce algorithms for the task in the next few sections, but first let’s explore the task. Exactly how hard is it? Fig. 8.4 shows that most word types (85-86%) are unambiguous (Janet is always NNP, hesitantly is always RB). But the ambiguous words, though accounting for only 14-15% of the vocabulary, are very common, and 55-67% of word tokens in running text are ambiguous. Particularly ambiguous common words include that, back, down, put and set; here are some examples of the 6 different parts of speech for the word back:

- earnings growth took a back/JJ seat
- a small building in the back/NN
- a clear majority of senators back/VBP the bill
- Dave began to back/VB toward the door
- enable the country to buy back/RP debt
- I was twenty-one back/RB then

Nonetheless, many words are easy to disambiguate, because their different tags aren’t equally likely. For example, a can be a determiner or the letter a, but the determiner sense is much more likely.

This idea suggests a useful baseline: given an ambiguous word, choose the tag which is most frequent in the training corpus. This is a key concept:

**Most Frequent Class Baseline:** Always compare a classifier against a baseline at least as good as the most frequent class baseline (assigning each token to the class it occurred in most often in the training set).
The most-frequent-tag baseline has an accuracy of about 92%. The baseline thus differs from the state-of-the-art and human ceiling (97%) by only 5%.

8.3 Named Entities and Named Entity Tagging

Part of speech tagging can tell us that words like Janet, Stanford University, and Colorado are all proper nouns; being a proper noun is a grammatical property of these words. But viewed from a semantic perspective, these proper nouns refer to different kinds of entities: Janet is a person, Stanford University is an organization, and Colorado is a location.

A named entity is, roughly speaking, anything that can be referred to with a proper name: a person, a location, an organization. The task of named entity recognition (NER) is to find spans of text that constitute proper names and tag the type of the entity. Four entity tags are most common: PER (person), LOC (location), ORG (organization), or GPE (geo-political entity). However, the term named entity is commonly extended to include things that aren’t entities per se, including dates, times, and other kinds of temporal expressions, and even numerical expressions like prices. Here’s an example of the output of an NER tagger:

Citing high fuel prices, [ORG United Airlines] said [TIME Friday] it has increased fares by [MONEY $6] per round trip on flights to some cities also served by lower-cost carriers. [ORG American Airlines], a unit of [ORG AMR Corp.], immediately matched the move, spokesman [PER Tim Wagner] said. [ORG United], a unit of [ORG UAL Corp.], said the increase took effect [TIME Thursday] and applies to most routes where it competes against discount carriers, such as [LOC Chicago] to [LOC Dallas] and [LOC Denver] to [LOC San Francisco].

The text contains 13 mentions of named entities including 5 organizations, 4 locations, 2 times, 1 person, and 1 mention of money. Figure 8.5 shows typical generic named entity types. Many applications will also need to use specific entity types like proteins, genes, commercial products, or works of art.

<table>
<thead>
<tr>
<th>Type</th>
<th>Tag</th>
<th>Sample Categories</th>
<th>Example sentences</th>
</tr>
</thead>
<tbody>
<tr>
<td>People</td>
<td>PER</td>
<td>people, characters</td>
<td>Turing is a giant of computer science.</td>
</tr>
<tr>
<td>Organization</td>
<td>ORG</td>
<td>companies, sports teams</td>
<td>The IPCC warned about the cyclone.</td>
</tr>
<tr>
<td>Location</td>
<td>LOC</td>
<td>regions, mountains, seas</td>
<td>Mt. Sanitas is in Sunshine Canyon.</td>
</tr>
<tr>
<td>Geo-Political Entity</td>
<td>GPE</td>
<td>countries, states</td>
<td>Palo Alto is raising the fees for parking.</td>
</tr>
</tbody>
</table>

Figure 8.5 A list of generic named entity types with the kinds of entities they refer to.

Named entity tagging is a useful first step in lots of natural language processing tasks. In sentiment analysis we might want to know a consumer’s sentiment toward a particular entity. Entities are a useful first stage in question answering, or for linking text to information in structured knowledge sources like Wikipedia. And named entity tagging is also central to tasks involving building semantic representations, like extracting events and the relationship between participants.

Unlike part-of-speech tagging, where there is no segmentation problem since each word gets one tag, the task of named entity recognition is to find and label spans of text, and is difficult partly because of the ambiguity of segmentation; we

1 In English, on the WSJ corpus, tested on sections 22-24.
need to decide what’s an entity and what isn’t, and where the boundaries are. Indeed, most words in a text will not be named entities. Another difficulty is caused by type ambiguity. The mention JFK can refer to a person, the airport in New York, or any number of schools, bridges, and streets around the United States. Some examples of this kind of cross-type confusion are given in Figure 8.6.

<table>
<thead>
<tr>
<th>Words</th>
<th>IO Label</th>
<th>BIO Label</th>
<th>BIOES Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>[PER Washington]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Blair arrived in [LOC Washington] for what may well be his last state visit. In June, [GPE Washington] passed a primary seatbelt law.</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 8.6 Examples of type ambiguities in the use of the name Washington.

The standard approach to sequence labeling for a span-recognition problem like NER is BIO tagging (Ramshaw and Marcus, 1995). This is a method that allows us to treat NER like a word-by-word sequence labeling task, via tags that capture both the boundary and the named entity type. Consider the following sentence:


Figure 8.7 shows the same excerpt represented with BIO tagging, as well as variants called IO tagging and BIOES tagging. In BIO tagging we label any token that begins a span of interest with the label B, tokens that occur inside a span are tagged with an I, and any tokens outside of any span of interest are labeled O. While there is only one O tag, we’ll have distinct B and I tags for each named entity class. The number of tags is thus 2n + 1 tags, where n is the number of entity types. BIO tagging can represent exactly the same information as the bracketed notation, but has the advantage that we can represent the task in the same simple sequence modeling way as part-of-speech tagging: assigning a single label $y_i$ to each input word $x_i$:

<table>
<thead>
<tr>
<th>Words</th>
<th>IO Label</th>
<th>BIO Label</th>
<th>BIOES Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jane</td>
<td>I-PER</td>
<td>B-PER</td>
<td>B-PER</td>
</tr>
<tr>
<td>Villanueva</td>
<td>I-PER</td>
<td>I-PER</td>
<td>E-PER</td>
</tr>
<tr>
<td>of</td>
<td>O</td>
<td>O</td>
<td>O</td>
</tr>
<tr>
<td>United</td>
<td>I-ORG</td>
<td>B-ORG</td>
<td>B-ORG</td>
</tr>
<tr>
<td>Airlines</td>
<td>I-ORG</td>
<td>I-ORG</td>
<td>I-ORG</td>
</tr>
<tr>
<td>Holding</td>
<td>I-ORG</td>
<td>I-ORG</td>
<td>E-ORG</td>
</tr>
<tr>
<td>discussed</td>
<td>O</td>
<td>O</td>
<td>O</td>
</tr>
<tr>
<td>the</td>
<td>O</td>
<td>O</td>
<td>O</td>
</tr>
<tr>
<td>Chicago</td>
<td>I-LOC</td>
<td>B-LOC</td>
<td>S-LOC</td>
</tr>
<tr>
<td>route</td>
<td>O</td>
<td>O</td>
<td>O</td>
</tr>
</tbody>
</table>

Figure 8.7 NER as a sequence model, showing IO, BIO, and BIOES taggings.

We’ve also shown two variant tagging schemes: IO tagging, which loses some information by eliminating the B tag, and BIOES tagging, which adds an end tag E for the end of a span, and a span tag S for a span consisting of only one word. A sequence labeler (HMM, CRF, RNN, Transformer, etc.) is trained to label each token in a text with tags that indicate the presence (or absence) of particular kinds of named entities.
8.4 HMM Part-of-Speech Tagging

In this section we introduce our first sequence labeling algorithm, the Hidden Markov Model, and show how to apply it to part-of-speech tagging. Recall that a sequence labeler is a model whose job is to assign a label to each unit in a sequence, thus mapping a sequence of observations to a sequence of labels of the same length. The HMM is a classic model that introduces many of the key concepts of sequence modeling that we will see again in more modern models.

An HMM is a probabilistic sequence model: given a sequence of units (words, letters, morphemes, sentences, whatever), it computes a probability distribution over possible sequences of labels and chooses the best label sequence.

8.4.1 Markov Chains

The HMM is based on augmenting the Markov chain. A Markov chain is a model that tells us something about the probabilities of sequences of random variables, states, each of which can take on values from some set. These sets can be words, or tags, or symbols representing anything, for example the weather. A Markov chain makes a very strong assumption that if we want to predict the future in the sequence, all that matters is the current state. All the states before the current state have no impact on the future except via the current state. It’s as if to predict tomorrow’s weather you could examine today’s weather but you weren’t allowed to look at yesterday’s weather.

![Markov chain diagram](image)

Figure 8.8 A Markov chain for weather (a) and one for words (b), showing states and transitions. A start distribution \( \pi \) is required; setting \( \pi = [0.1, 0.7, 0.2] \) for (a) would mean a probability 0.7 of starting in state 2 (cold), probability 0.1 of starting in state 1 (hot), etc.

More formally, consider a sequence of state variables \( q_1, q_2, \ldots, q_t \). A Markov model embodies the Markov assumption on the probabilities of this sequence: that when predicting the future, the past doesn’t matter, only the present.

Markov Assumption: \( P(q_t = a | q_1 \ldots q_{t-1}) = P(q_t = a | q_{t-1}) \) (8.3)

Figure 8.8a shows a Markov chain for assigning a probability to a sequence of weather events, for which the vocabulary consists of HOT, COLD, and WARM. The states are represented as nodes in the graph, and the transitions, with their probabilities, as edges. The transitions are probabilities: the values of arcs leaving a given state must sum to 1. Figure 8.8b shows a Markov chain for assigning a probability to a sequence of words \( w_1 \ldots w_t \). This Markov chain should be familiar; in fact, it represents a bigram language model, with each edge expressing the probability \( p(w_t | w_{t-1}) \).

Given the two models in Fig. 8.8, we can assign a probability to any sequence from our vocabulary.
Formally, a Markov chain is specified by the following components:

- \( Q = q_1 q_2 \ldots q_N \) a set of \( N \) states
- \( A = a_{11} a_{12} \ldots a_{N1} \ldots a_{NN} \) a transition probability matrix \( A \), each \( a_{ij} \) representing the probability of moving from state \( i \) to state \( j \), s.t. \( \sum_{j=1}^{N} a_{ij} = 1 \ \forall i \)
- \( \pi = \pi_1, \pi_2, \ldots, \pi_N \) an initial probability distribution over states. \( \pi_i \) is the probability that the Markov chain will start in state \( i \). Some states \( j \) may have \( \pi_j = 0 \), meaning that they cannot be initial states. Also, \( \sum_{i=1}^{N} \pi_i = 1 \)

Before you go on, use the sample probabilities in Fig. 8.8a (with \( \pi = [0.1, 0.7, 0.2] \)) to compute the probability of each of the following sequences:

- (8.4) hot hot hot hot
- (8.5) cold hot cold hot

What does the difference in these probabilities tell you about a real-world weather fact encoded in Fig. 8.8a?

### 8.4.2 The Hidden Markov Model

A Markov chain is useful when we need to compute a probability for a sequence of observable events. In many cases, however, the events we are interested in are hidden: we don’t observe them directly. For example we don’t normally observe part-of-speech tags in a text. Rather, we see words, and must infer the tags from the word sequence. We call the tags hidden because they are not observed.

A hidden Markov model (HMM) allows us to talk about both observed events (like words that we see in the input) and hidden events (like part-of-speech tags) that we think of as causal factors in our probabilistic model. An HMM is specified by the following components:

- \( Q = q_1 q_2 \ldots q_N \) a set of \( N \) states
- \( A = a_{111} a_{112} \ldots a_{1N1} \ldots a_{NN1} \ldots a_{NNN} \) a transition probability matrix \( A \), each \( a_{ij} \) representing the probability of moving from state \( i \) to state \( j \), s.t. \( \sum_{j=1}^{N} a_{ij} = 1 \ \forall i \)
- \( B = b_i(o_t) \) a sequence of observation likelihoods, also called emission probabilities, each expressing the probability of an observation \( o_t \) (drawn from a vocabulary \( V = v_1, v_2, \ldots, v_V \)) being generated from a state \( q_i \)
- \( \pi = \pi_1, \pi_2, \ldots, \pi_N \) an initial probability distribution over states. \( \pi_i \) is the probability that the Markov chain will start in state \( i \). Some states \( j \) may have \( \pi_j = 0 \), meaning that they cannot be initial states. Also, \( \sum_{i=1}^{N} \pi_i = 1 \)

The HMM is given as input \( O = o_1 o_2 \ldots o_T \): a sequence of \( T \) observations, each one drawn from the vocabulary \( V \).

A first-order hidden Markov model instantiates two simplifying assumptions. First, as with a first-order Markov chain, the probability of a particular state depends only on the previous state:

\[
\text{Markov Assumption: } P(q_i|q_1, \ldots, q_{i-1}) = P(q_i|q_{i-1}) \quad (8.6)
\]

Second, the probability of an output observation \( o_t \) depends only on the state that produced the observation \( q_t \) and not on any other states or any other observations:

\[
\text{Output Independence: } P(o_t|q_1, \ldots, q_{i-1}, q_t, o_1, \ldots, o_i, \ldots, o_T) = P(o_t|q_t) \quad (8.7)
\]
8.4.3 The components of an HMM tagger

Let’s start by looking at the pieces of an HMM tagger, and then we’ll see how to use it to tag. An HMM has two components, the $A$ and $B$ probabilities.

The $A$ matrix contains the tag transition probabilities $P(t_i|t_{i-1})$ which represent the probability of a tag occurring given the previous tag. For example, modal verbs like will are very likely to be followed by a verb in the base form, a VB, like race, so we expect this probability to be high. We compute the maximum likelihood estimate of this transition probability by counting, out of the times we see the first tag in a labeled corpus, how often the first tag is followed by the second:

$$P(t_i|t_{i-1}) = \frac{C(t_{i-1}, t_i)}{C(t_{i-1})} \quad (8.8)$$

In the WSJ corpus, for example, MD occurs 13124 times of which it is followed by VB 10471, for an MLE estimate of

$$P(VB|MD) = \frac{C(MD, VB)}{C(MD)} = \frac{10471}{13124} = .80 \quad (8.9)$$

Let’s walk through an example, seeing how these probabilities are estimated and used in a sample tagging task, before we return to the algorithm for decoding.

In HMM tagging, the probabilities are estimated by counting on a tagged training corpus. For this example we’ll use the tagged WSJ corpus.

The $B$ emission probabilities, $P(w_i|t_i)$, represent the probability, given a tag (say MD), that it will be associated with a given word (say will). The MLE of the emission probability is

$$P(w_i|t_i) = \frac{C(t_i, w_i)}{C(t_i)} \quad (8.10)$$

Of the 13124 occurrences of MD in the WSJ corpus, it is associated with will 4046 times:

$$P(will|MD) = \frac{C(MD, will)}{C(MD)} = \frac{4046}{13124} = .31 \quad (8.11)$$

We saw this kind of Bayesian modeling in Chapter 4; recall that this likelihood term is not asking “which is the most likely tag for the word will?” That would be the posterior $P(MD|will)$. Instead, $P(will|MD)$ answers the slightly counterintuitive question “If we were going to generate a MD, how likely is it that this modal would be will?”

The $A$ transition probabilities, and $B$ observation likelihoods of the HMM are illustrated in Fig. 8.9 for three states in an HMM part-of-speech tagger; the full tagger would have one state for each tag.

8.4.4 HMM tagging as decoding

For any model, such as an HMM, that contains hidden variables, the task of determining the hidden variables sequence corresponding to the sequence of observations is called decoding. More formally,

**Decoding**: Given as input an HMM $\lambda = (A, B)$ and a sequence of observations $O = o_1, o_2, \ldots, o_T$, find the most probable sequence of states $Q = q_1 q_2 q_3 \ldots q_T$. 
Figure 8.9 An illustration of the two parts of an HMM representation: the A transition probabilities used to compute the prior probability, and the B observation likelihoods that are associated with each state, one likelihood for each possible observation word.

For part-of-speech tagging, the goal of HMM decoding is to choose the tag sequence $t_1 \ldots t_n$ that is most probable given the observation sequence of $n$ words $w_1 \ldots w_n$:

$$\hat{t}_{1:n} = \arg\max_{t_1 \ldots t_n} P(t_1 \ldots t_n | w_1 \ldots w_n)$$

(8.12)

The way we’ll do this in the HMM is to use Bayes’ rule to instead compute:

$$\hat{t}_{1:n} = \arg\max_{t_1 \ldots t_n} \frac{P(w_1 \ldots w_n | t_1 \ldots t_n)P(t_1 \ldots t_n)}{P(w_1 \ldots w_n)}$$

(8.13)

Furthermore, we simplify Eq. 8.13 by dropping the denominator $P(w_1^n)$:

$$\hat{t}_{1:n} = \arg\max_{t_1 \ldots t_n} P(w_1 \ldots w_n | t_1 \ldots t_n)P(t_1 \ldots t_n)$$

(8.14)

HMM taggers make two further simplifying assumptions. The first is that the probability of a word appearing depends only on its own tag and is independent of neighboring words and tags:

$$P(w_1 \ldots w_n | t_1 \ldots t_n) \approx \prod_{i=1}^{n} P(w_i | t_i)$$

(8.15)

The second assumption, the bigram assumption, is that the probability of a tag is dependent only on the previous tag, rather than the entire tag sequence:

$$P(t_1 \ldots t_n) \approx \prod_{i=1}^{n} P(t_i | t_{i-1})$$

(8.16)

Plugging the simplifying assumptions from Eq. 8.15 and Eq. 8.16 into Eq. 8.14 results in the following equation for the most probable tag sequence from a bigram tagger:

$$\hat{t}_{1:n} = \arg\max_{t_1 \ldots t_n} P(t_1 \ldots t_n | w_1 \ldots w_n) \approx \arg\max_{t_1 \ldots t_n} \prod_{i=1}^{n} P(w_i | t_i) P(t_i | t_{i-1})$$

(8.17)

The two parts of Eq. 8.17 correspond neatly to the B emission probability and A transition probability that we just defined above!
### 8.4.5 The Viterbi Algorithm

The decoding algorithm for HMMs is the **Viterbi algorithm** shown in Fig. 8.10. As an instance of **dynamic programming**, Viterbi resembles the dynamic programming **minimum edit distance** algorithm of Chapter 2.

**Viterbi algorithm**

Function `VITERBI(observations of len T, state-graph of len N) returns best-path, path-prob`

1. Create a path probability matrix `viterbi[N,T]`.
2. For each state `s` from 1 to `N` do:
   - Initialize `viterbi[s,1] ← π_s * b_s(o_1)` and `backpointer[s,1] ← 0`.
3. For each time step `t` from 2 to `T` do:
   - For each state `s` from 1 to `N` do:
     - `viterbi[s,t] ← max_{s'} viterbi[s',t-1] * a_{s',s} * b_s(o_t)`
     - `backpointer[s,t] ← argmax_{s'} viterbi[s',t-1] * a_{s',s} * b_s(o_t)`
4. Termination step:
   - `bestpathprob ← max_{s} viterbi[s,T]`
   - `bestpathpointer ← argmax_{s} viterbi[s,T]`
5. Best path:
   - `bestpath ← the path starting at state bestpathpointer, that follows backpointer[] to states back in time`

**Figure 8.10** Viterbi algorithm for finding the optimal sequence of tags. Given an observation sequence and an HMM `λ = (A,B)`, the algorithm returns the state path through the HMM that assigns maximum likelihood to the observation sequence.

The Viterbi algorithm first sets up a probability matrix or **lattice**, with one column for each observation `o_t` and one row for each state in the state graph. Each column thus has a cell for each state `q_i` in the single combined automaton. Figure 8.11 shows an intuition of this lattice for the sentence *Janet will back the bill*.

Each cell of the lattice, `v_t(j)`, represents the probability that the HMM is in state `j` after seeing the first `t` observations and passing through the most probable state sequence `q_1,...,q_{t-1}`, given the HMM `λ`. The value of each cell `v_t(j)` is computed by recursively taking the most probable path that could lead us to this cell. Formally, each cell expresses the probability

\[
v_t(j) = \max_{q_1,...,q_{t-1}} P(q_1...q_{t-1}, o_1, o_2 ... o_t, q_t = j | \lambda) \tag{8.18}
\]

We represent the most probable path by taking the maximum over all possible previous state sequences `max_{q_1,...,q_{t-1}}`. Like other dynamic programming algorithms, Viterbi fills each cell recursively. Given that we had already computed the probability of being in every state at time `t - 1`, we compute the Viterbi probability by taking the most probable of the extensions of the paths that lead to the current cell. For a given state `q_j` at time `t`, the value `v_t(j)` is computed as

\[
v_t(j) = \max_{i=1}^{N} v_{t-1}(i) a_{ij} b_j(o_t) \tag{8.19}
\]

The three factors that are multiplied in Eq. 8.19 for extending the previous paths to compute the Viterbi probability at time `t` are
8.4.6 Working through an example

Let’s tag the sentence Janet will back the bill; the goal is the correct series of tags (see also Fig. 8.11):

\[(8.20) \text{Janet/NNP will/MD back/VB the/DT bill/NN} \]

Let the HMM be defined by the two tables in Fig. 8.12 and Fig. 8.13. Figure 8.12 lists the \(a_{ij}\) probabilities for transitioning between the hidden states (part-of-speech tags). Figure 8.13 expresses the \(b_j(o_i)\) probabilities, the observation likelihoods of words given tags. This table is (slightly simplified) from counts in the WSJ corpus. So the word Janet only appears as an NNP, back has 4 possible parts of speech, and
8.4 • HMM Part-of-Speech Tagging 175

<table>
<thead>
<tr>
<th></th>
<th>Janet</th>
<th>will</th>
<th>back</th>
<th>the</th>
<th>bill</th>
</tr>
</thead>
<tbody>
<tr>
<td>NNP</td>
<td>0.000032</td>
<td>0</td>
<td>0</td>
<td>0.000048</td>
<td>0</td>
</tr>
<tr>
<td>MD</td>
<td>0</td>
<td>0.308431</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>VB</td>
<td>0</td>
<td>0.000028</td>
<td>0.000672</td>
<td>0</td>
<td>0.000028</td>
</tr>
<tr>
<td>JJ</td>
<td>0</td>
<td>0</td>
<td>0.000340</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>NN</td>
<td>0</td>
<td>0.000200</td>
<td>0.000223</td>
<td>0</td>
<td>0.002337</td>
</tr>
<tr>
<td>RB</td>
<td>0</td>
<td>0</td>
<td>0.010446</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>DT</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.506099</td>
<td>0</td>
</tr>
</tbody>
</table>

Figure 8.13 Observation likelihoods $B$ computed from the WSJ corpus without smoothing, simplified slightly.

the word *the* can appear as a determiner or as an NNP (in titles like “Somewhere Over the Rainbow” all words are tagged as NNP).

Figure 8.14 shows a fleshed-out version of the sketch we saw in Fig. 8.11, the Viterbi lattice for computing the best hidden state sequence for the observation sequence *Janet will back the bill*.

There are $N = 5$ state columns. We begin in column 1 (for the word *Janet*) by setting the Viterbi value in each cell to the product of the $\pi$ transition probability (the start probability for that state $i$, which we get from the $<$s$>$ entry of Fig. 8.12),
and the observation likelihood of the word Janet given the tag for that cell. Most of the cells in the column are zero since the word Janet cannot be any of those tags. The reader should find this in Fig. 8.14.

Next, each cell in the will column gets updated. For each state, we compute the value \( viterbi[s, t] \) by taking the maximum over the extensions of all the paths from the previous column that lead to the current cell according to Eq. 8.19. We have shown the values for the MD, VB, and NN cells. Each cell gets the max of the 7 values from the previous column, multiplied by the appropriate transition probability; as it happens in this case, most of them are zero from the previous column. The remaining value is multiplied by the relevant observation probability, and the (trivial) max is taken. In this case the final value, 2.772e-8, comes from the NNP state at the previous column. The reader should fill in the rest of the lattice in Fig. 8.14 and backtrace to see whether or not the Viterbi algorithm returns the gold state sequence NNP MD VB DT NN.

8.5 Conditional Random Fields (CRFs)

While the HMM is a useful and powerful model, it turns out that HMMs need a number of augmentations to achieve high accuracy. For example, in POS tagging as in other tasks, we often run into unknown words: proper names and acronyms are created very often, and even new common nouns and verbs enter the language at a surprising rate. It would be great to have ways to add arbitrary features to help with this, perhaps based on capitalization or morphology (words starting with capital letters are likely to be proper nouns, words ending with -ed tend to be past tense (VBD or VBN), etc.) Or knowing the previous or following words might be a useful feature (if the previous word is the, the current tag is unlikely to be a verb).

Although we could try to hack the HMM to find ways to incorporate some of these, in general it’s hard for generative models like HMMs to add arbitrary features directly into the model in a clean way. We’ve already seen a model for combining arbitrary features in a principled way: log-linear models like the logistic regression model of Chapter 5! But logistic regression isn’t a sequence model; it assigns a class to a single observation.

Luckily, there is a discriminative sequence model based on log-linear models: the conditional random field (CRF). We’ll describe here the linear chain CRF, the version of the CRF most commonly used for language processing, and the one whose conditioning closely matches the HMM.

Assuming we have a sequence of input words \( X = x_1...x_n \) and want to compute a sequence of output tags \( Y = y_1...y_n \). In an HMM to compute the best tag sequence that maximizes \( P(Y|X) \) we rely on Bayes’ rule and the likelihood \( P(X|Y) \):

\[
\hat{Y} = \arg\max_Y p(Y|X) \\
= \arg\max_Y p(X|Y) p(Y) \\
= \arg\max_Y \prod_i p(x_i|y_i) \prod_i p(y_i|y_{i-1})
\]  

(8.21)

In a CRF, by contrast, we compute the posterior \( p(Y|X) \) directly, training the CRF
8.5 * CONDITIONAL RANDOM FIELDS (CRFs) 177

to discriminate among the possible tag sequences:

$$\hat{Y} = \arg\max_{Y \in \mathcal{Y}} P(Y|X)$$  \tag{8.22}

However, the CRF does not compute a probability for each tag at each time step. Instead, at each time step the CRF computes log-linear functions over a set of relevant features, and these local features are aggregated and normalized to produce a global probability for the whole sequence.

Let’s introduce the CRF more formally, again using $X$ and $Y$ as the input and output sequences. A CRF is a log-linear model that assigns a probability to an entire output (tag) sequence $Y$, out of all possible sequences $\mathcal{Y}$, given the entire input (word) sequence $X$. We can think of a CRF as like a giant sequential version of the multinomial logistic regression algorithm we saw for text categorization. Recall that we introduced the feature function $f$ in regular multinomial logistic regression for text categorization as a function of a tuple: the input text $x$ and a single class $y$ (page 91). In a CRF, we’re dealing with a sequence, so the function $F$ maps an entire input sequence $X$ and an entire output sequence $Y$ to a feature vector. Let’s assume we have $K$ features, with a weight $w_k$ for each feature $F_k$:

$$p(Y|X) = \frac{\exp \left( \sum_{k=1}^{K} w_k F_k(X, Y) \right)}{\sum_{Y' \in \mathcal{Y}} \exp \left( \sum_{k=1}^{K} w_k F_k(X, Y') \right)}$$  \tag{8.23}

It’s common to also describe the same equation by pulling out the denominator into a function $Z(X)$:

$$p(Y|X) = \frac{1}{Z(X)} \exp \left( \sum_{k=1}^{K} w_k F_k(X, Y) \right)$$  \tag{8.24}

$$Z(X) = \sum_{Y' \in \mathcal{Y}} \exp \left( \sum_{k=1}^{K} w_k F_k(X, Y') \right)$$  \tag{8.25}

We’ll call these $K$ functions $F_k(X, Y)$ **global features**, since each one is a property of the entire input sequence $X$ and output sequence $Y$. We compute them by decomposing into a sum of **local** features for each position $i$ in $Y$:

$$F_k(X, Y) = \sum_{i=1}^{n} f_k(y_{i-1}, y_i, X, i)$$  \tag{8.26}

Each of these local features $f_k$ in a linear-chain CRF is allowed to make use of the current output token $y_i$, the previous output token $y_{i-1}$, the entire input string $X$ (or any subpart of it), and the current position $i$. This constraint to only depend on the current and previous output tokens $y_i$ and $y_{i-1}$ are what characterizes a **linear chain CRF**. As we will see, this limitation makes it possible to use versions of the efficient Viterbi and Forward-Backwards algorithms from the HMM. A general CRF, by contrast, allows a feature to make use of any output token, and are thus necessary for tasks in which the decision depend on distant output tokens, like $y_{i-4}$. General CRFs require more complex inference, and are less commonly used for language processing.
8.5.1 Features in a CRF POS Tagger

Let’s look at some of these features in detail, since the reason to use a discriminative sequence model is that it’s easier to incorporate a lot of features.\(^2\)

Again, in a linear-chain CRF, each local feature \(f_k\) at position \(i\) can depend on any information from: \((y_{i-1}, y_i, X, i)\). So some legal features representing common situations might be the following:

\[
\begin{align*}
\mathbb{1}\{x_i = \text{the}, y_i = \text{DET}\} \\
\mathbb{1}\{y_i = \text{PROPN}, x_{i+1} = \text{Street}, y_{i-1} = \text{NUM}\} \\
\mathbb{1}\{y_i = \text{VERB}, y_{i-1} = \text{AUX}\}
\end{align*}
\]

For simplicity, we’ll assume all CRF features take on the value 1 or 0. Above, we explicitly use the notation \(\mathbb{1}\{x\}\) to mean “1 if \(x\) is true, and 0 otherwise”. From now on, we’ll leave off the \(\mathbb{1}\) when we define features, but you can assume each feature has it there implicitly.

Although the idea of what features to use is done by the system designer by hand, the specific features are automatically populated by using feature templates as we briefly mentioned in Chapter 5. Here are some templates that only use information from \((y_{i-1}, y_i, X, i)\):

\[
\langle y_i, x_i \rangle, \langle y_i, y_{i-1} \rangle, \langle y_i, x_{i-1}, x_{i+2} \rangle
\]

These templates automatically populate the set of features from every instance in the training and test set. Thus for our example Janet/NNP will/MD back/VB the/DT bill/NN, when \(x_i\) is the word back, the following features would be generated and have the value 1 (we’ve assigned them arbitrary feature numbers):

\[
\begin{align*}
f_{3743}: y_i = \text{VB} \text{ and } x_i = \text{back} \\
f_{156}: y_i = \text{VB} \text{ and } y_{i-1} = \text{MD} \\
f_{99732}: y_i = \text{VB} \text{ and } x_{i-1} = \text{will} \text{ and } x_{i+2} = \text{bill}
\end{align*}
\]

It’s also important to have features that help with unknown words. One of the most important is word shape features, which represent the abstract letter pattern of the word by mapping lower-case letters to ‘x’, upper-case to ‘X’, numbers to ‘d’, and retaining punctuation. Thus for example I.M.F. would map to X.X.X. and DC10-30 would map to XXdd-dd. A second class of shorter word shape features is also used. In these features consecutive character types are removed, so words in all caps map to X, words with initial-caps map to Xx, DC10-30 would be mapped to Xd-d but I.M.F would still map to X.X.X. Prefix and suffix features are also useful. In summary, here are some sample feature templates that help with unknown words:

\[
\begin{align*}
x_i \text{ contains a particular prefix (perhaps from all prefixes of length } \leq 2) \\
x_i \text{ contains a particular suffix (perhaps from all suffixes of length } \leq 2) \\
x_i \text{’s word shape} \\
x_i \text{’s short word shape}
\end{align*}
\]

For example the word well-dressed might generate the following non-zero valued feature values:

\(^2\) Because in HMMs all computation is based on the two probabilities \(P(\text{tag}|\text{tag})\) and \(P(\text{word}|\text{tag})\), if we want to include some source of knowledge into the tagging process, we must find a way to encode the knowledge into one of these two probabilities. Each time we add a feature we have to do a lot of complicated conditioning which gets harder and harder as we have more and more such features.
The known-word templates are computed for every word seen in the training set; the unknown word features can also be computed for all words in training, or only on training words whose frequency is below some threshold. The result of the known-word templates and word-signature features is a very large set of features. Generally a feature cutoff is used in which features are thrown out if they have count < 5 in the training set.

Remember that in a CRF we don’t learn weights for each of these local features $f_k$. Instead, we first sum the values of each local feature (for example feature $f_{3743}$) over the entire sentence, to create each global feature (for example $F_{3743}$). It is those global features that will then be multiplied by weight $w_{3743}$. Thus for training and inference there is always a fixed set of $K$ features with $K$ weights, even though the length of each sentence is different.

### 8.5.2 Features for CRF Named Entity Recognizers

A CRF for NER makes use of very similar features to a POS tagger, as shown in Figure 8.15.

One feature that is especially useful for locations is a gazetteer, a list of place names, often providing millions of entries for locations with detailed geographical and political information.\(^3\) This can be implemented as a binary feature indicating a phrase appears in the list. Other related resources like name-lists, for example from the United States Census Bureau\(^4\), can be used, as can other entity dictionaries like lists of corporations or products, although they may not be as helpful as a gazetteer (Mikheev et al., 1999).

The sample named entity token *L’Occitane* would generate the following non-zero valued feature values (assuming that *L’Occitane* is neither in the gazetteer nor the census).

\(^3\) [www.geonames.org](http://www.geonames.org)

\(^4\) [www.census.gov](http://www.census.gov)
prefix($x_i$) = L
suffix($x_i$) = tane
prefix($x_i$) = L'
suffix($x_i$) = ane
prefix($x_i$) = L'0
suffix($x_i$) = ne
prefix($x_i$) = L'O
suffix($x_i$) = ne
prefix($x_i$) = L'Oc
suffix($x_i$) = e
word-shape($x_i$) = X'Xxxxxxxx
short-word-shape($x_i$) = X'Xx

Figure 8.16 illustrates the result of adding part-of-speech tags and some shape information to our earlier example.

<table>
<thead>
<tr>
<th>Words</th>
<th>POS</th>
<th>Short shape</th>
<th>Gazetteer</th>
<th>BIO Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jane</td>
<td>NNP</td>
<td>Xx</td>
<td>0</td>
<td>B-PER</td>
</tr>
<tr>
<td>Villanueva</td>
<td>NNP</td>
<td>Xx</td>
<td>1</td>
<td>I-PER</td>
</tr>
<tr>
<td>of</td>
<td>IN</td>
<td>x</td>
<td>0</td>
<td>O</td>
</tr>
<tr>
<td>United</td>
<td>NNP</td>
<td>Xx</td>
<td>0</td>
<td>B-ORG</td>
</tr>
<tr>
<td>Airlines</td>
<td>NNP</td>
<td>Xx</td>
<td>0</td>
<td>I-ORG</td>
</tr>
<tr>
<td>Holding</td>
<td>NNP</td>
<td>Xx</td>
<td>0</td>
<td>I-ORG</td>
</tr>
<tr>
<td>discussed</td>
<td>VBD</td>
<td>x</td>
<td>0</td>
<td>O</td>
</tr>
<tr>
<td>the</td>
<td>DT</td>
<td>x</td>
<td>0</td>
<td>O</td>
</tr>
<tr>
<td>Chicago</td>
<td>NNP</td>
<td>Xx</td>
<td>1</td>
<td>B-LOC</td>
</tr>
<tr>
<td>route</td>
<td>NN</td>
<td>x</td>
<td>0</td>
<td>O</td>
</tr>
</tbody>
</table>

8.5.3 Inference and Training for CRFs

How do we find the best tag sequence $\hat{Y}$ for a given input $X$? We start with Eq. 8.22:

$$
\hat{Y} = \arg\max_{Y \in \mathcal{Y}} P(Y|X)
$$

$$
= \arg\max_{Y \in \mathcal{Y}} \frac{1}{Z(X)} \exp \left( \sum_{k=1}^{K} w_k F_k(X, Y) \right) \tag{8.27}
$$

$$
= \arg\max_{Y \in \mathcal{Y}} \exp \left( \sum_{k=1}^{K} w_k \sum_{i=1}^{n} f_k(y_{i-1}, y_i, X, i) \right) \tag{8.28}
$$

$$
= \arg\max_{Y \in \mathcal{Y}} \sum_{k=1}^{K} w_k \sum_{i=1}^{n} f_k(y_{i-1}, y_i, X, i) \tag{8.29}
$$

$$
= \arg\max_{Y \in \mathcal{Y}} \sum_{i=1}^{n} \sum_{k=1}^{K} w_k f_k(y_{i-1}, y_i, X, i) \tag{8.30}
$$

We can ignore the exp function and the denominator $Z(X)$, as we do above, because exp doesn’t change the argmax, and the denominator $Z(X)$ is constant for a given observation sequence $X$.

How should we decode to find this optimal tag sequence $\hat{y}$? Just as with HMMs, we’ll turn to the Viterbi algorithm, which works because, like the HMM, the linear-chain CRF depends at each timestep on only one previous output token $y_{i-1}$.

Concretely, this involves filling an $N \times T$ array with the appropriate values, maintaining backpointers as we proceed. As with HMM Viterbi, when the table is filled, we simply follow pointers back from the maximum value in the final column to retrieve the desired set of labels.
The requisite changes from HMM Viterbi have to do only with how we fill each cell. Recall from Eq. 8.19 that the recursive step of the Viterbi equation computes the Viterbi value of time $t$ for state $j$ as

$$v_t(j) = \max_{i=1}^{N} v_{t-1}(i) a_{ij} b_j(o_t); \quad 1 \leq j \leq N, 1 < t \leq T$$

which is the HMM implementation of

$$v_t(j) = \max_{i=1}^{N} v_{t-1}(i) P(s_j | s_i) P(o_t | s_j); \quad 1 \leq j \leq N, 1 < t \leq T$$

The CRF requires only a slight change to this latter formula, replacing the $a$ and $b$ prior and likelihood probabilities with the CRF features:

$$v_t(j) = \max_{i=1}^{N} v_{t-1}(i) \sum_{k=1}^{K} w_k f_k(y_{t-1}, y_t, X, t); \quad 1 \leq j \leq N, 1 < t \leq T$$

Learning in CRFs relies on the same supervised learning algorithms we presented for logistic regression. Given a sequence of observations, feature functions, and corresponding outputs, we use stochastic gradient descent to train the weights to maximize the log-likelihood of the training corpus. The local nature of linear-chain CRFs means that the forward-backward algorithm introduced for HMMs in Appendix A can be extended to a CRF version that will efficiently compute the necessary derivatives. As with logistic regression, L1 or L2 regularization is important.

8.6 Evaluation of Named Entity Recognition

Part-of-speech taggers are evaluated by the standard metric of accuracy. Named entity recognizers are evaluated by recall, precision, and F$_1$ measure. Recall that recall is the ratio of the number of correctly labeled responses to the total that should have been labeled; precision is the ratio of the number of correctly labeled responses to the total labeled; and F-measure is the harmonic mean of the two.

To know if the difference between the F$_1$ scores of two NER systems is a significant difference, we use the paired bootstrap test, or the similar randomization test (Section 4.9).

For named entity tagging, the entity rather than the word is the unit of response. Thus in the example in Fig. 8.16, the two entities Jane Villanueva and United Airlines Holding and the non-entity discussed would each count as a single response.

The fact that named entity tagging has a segmentation component which is not present in tasks like text categorization or part-of-speech tagging causes some problems with evaluation. For example, a system that labeled Jane but not Jane Villanueva as a person would cause two errors, a false positive for O and a false negative for I-PER. In addition, using entities as the unit of response but words as the unit of training means that there is a mismatch between the training and test conditions.

8.7 Further Details

In this section we summarize a few remaining details of the data and models for part-of-speech tagging and NER, beginning with data. Since the algorithms we have
presented are supervised, having labeled data is essential for training and testing. A wide variety of datasets exist for part-of-speech tagging and/or NER. The Universal Dependencies (UD) dataset (de Marneffe et al., 2021) has POS tagged corpora in over a hundred languages, as do the Penn Treebanks in English, Chinese, and Arabic. OntoNotes has corpora labeled for named entities in English, Chinese, and Arabic (Hovy et al., 2006). Named entity tagged corpora are also available in particular domains, such as for biomedical (Bada et al., 2012) and literary text (Bamman et al., 2019).

### 8.7.1 Rule-based Methods

While machine learned (neural or CRF) sequence models are the norm in academic research, commercial approaches to NER are often based on pragmatic combinations of lists and rules, with some smaller amount of supervised machine learning (Chiticariu et al., 2013). For example in the IBM System T architecture, a user specifies declarative constraints for tagging tasks in a formal query language that includes regular expressions, dictionaries, semantic constraints, and other operators, which the system compiles into an efficient extractor (Chiticariu et al., 2018).

One common approach is to make repeated rule-based passes over a text, starting with rules with very high precision but low recall, and, in subsequent stages, using machine learning methods that take the output of the first pass into account (an approach first worked out for coreference (Lee et al., 2017a)):

1. First, use high-precision rules to tag unambiguous entity mentions.
2. Then, search for substring matches of the previously detected names.
3. Use application-specific name lists to find likely domain-specific mentions.
4. Finally, apply supervised sequence labeling techniques that use tags from previous stages as additional features.

Rule-based methods were also the earliest methods for part-of-speech tagging. Rule-based taggers like the English Constraint Grammar system (Karlsson et al. 1995, Voutilainen 1999) use a two-stage formalism invented in the 1950s and 1960s: (1) a morphological analyzer with tens of thousands of word stem entries returns all parts of speech for a word, then (2) a large set of thousands of constraints are applied to the input sentence to rule out parts of speech inconsistent with the context.

### 8.7.2 POS Tagging for Morphologically Rich Languages

Augmentations to tagging algorithms become necessary when dealing with languages with rich morphology like Czech, Hungarian and Turkish.

These productive word-formation processes result in a large vocabulary for these languages: a 250,000 word token corpus of Hungarian has more than twice as many word types as a similarly sized corpus of English (Oravecz and Dienes, 2002), while a 10 million word token corpus of Turkish contains four times as many word types as a similarly sized English corpus (Hakkani-Tür et al., 2002). Large vocabularies mean many unknown words, and these unknown words cause significant performance degradations in a wide variety of languages (including Czech, Slovene, Estonian, and Romanian) (Hajič, 2000).

Highly inflectional languages also have much more information than English coded in word morphology, like case (nominative, accusative, genitive) or gender (masculine, feminine). Because this information is important for tasks like parsing and coreference resolution, part-of-speech taggers for morphologically rich lan-
guages need to label words with case and gender information. Tagsets for morphologically rich languages are therefore sequences of morphological tags rather than a single primitive tag. Here’s a Turkish example, in which the word *izin* has three possible morphological/part-of-speech tags and meanings (Hakkani-Tür et al., 2002):

1. *Yerdeki* izin temizlenmesi gerek. 
   *The trace* on the floor should be cleaned.

2. *Üzerinde* parmak izin kalmış. 
   *Your* fingerprint *is left on* (it).

3. *İçeri* girmek için izin alınmak gerekiyor. 
   *You need* permission *to enter.*

Using a morphological parse sequence like Noun+A3sg+Pnon+Gen as the part-of-speech tag greatly increases the number of parts of speech, and so tagsets can be 4 to 10 times larger than the 50–100 tags we have seen for English. With such large tagsets, each word needs to be morphologically analyzed to generate the list of possible morphological tag sequences (part-of-speech tags) for the word. The role of the tagger is then to disambiguate among these tags. This method also helps with unknown words since morphological parsers can accept unknown stems and still segment the affixes properly.

### 8.8 Summary

This chapter introduced **parts of speech** and **named entities**, and the tasks of **part-of-speech tagging** and **named entity recognition**:

- Languages generally have a small set of **closed class** words that are highly frequent, ambiguous, and act as **function words**, and **open-class** words like **nouns, verbs, adjectives**. Various part-of-speech **tagsets** exist, of between 40 and 200 tags.

- **Part-of-speech tagging** is the process of assigning a part-of-speech label to each of a sequence of words.

- **Named entities** are words for proper nouns referring mainly to people, places, and organizations, but extended to many other types that aren’t strictly entities or even proper nouns.

- Two common approaches to **sequence modeling** are a **generative** approach, **HMM** tagging, and a **discriminative** approach, **CRF** tagging. We will see a neural approach in following chapters.

- The probabilities in HMM taggers are estimated by maximum likelihood estimation on tag-labeled training corpora. The Viterbi algorithm is used for **decoding**, finding the most likely tag sequence.

- **Conditional Random Fields** or **CRF taggers** train a log-linear model that can choose the best tag sequence given an observation sequence, based on features that condition on the output tag, the prior output tag, the entire input sequence, and the current timestep. They use the Viterbi algorithm for inference, to choose the best sequence of tags, and a version of the Forward-Backward algorithm (see Appendix A) for training.
Bibliographical and Historical Notes

What is probably the earliest part-of-speech tagger was part of the parser in Zellig Harris’s Transformations and Discourse Analysis Project (TDAP), implemented between June 1958 and July 1959 at the University of Pennsylvania (Harris, 1962), although earlier systems had used part-of-speech dictionaries. TDAP used 14 handwritten rules for part-of-speech disambiguation; the use of part-of-speech tag sequences and the relative frequency of tags for a word prefigures modern algorithms. The parser was implemented essentially as a cascade of finite-state transducers; see Joshi and Hopely (1999) and Karttunen (1999) for a reimplementation.

The Computational Grammar Coder (CGC) of Klein and Simmons (1963) had three components: a lexicon, a morphological analyzer, and a context disambiguator. The small 1500-word lexicon listed only function words and other irregular words. The morphological analyzer used inflectional and derivational suffixes to assign part-of-speech classes. These were run over words to produce candidate parts of speech which were then disambiguated by a set of 500 context rules by relying on surrounding islands of unambiguous words. For example, one rule said that between an ARTICLE and a VERB, the only allowable sequences were ADJ-NOUN, NOUN-ADVERB, or NOUN-NOUN. The TAGGIT tagger (Greene and Rubin, 1971) used the same architecture as Klein and Simmons (1963), with a bigger dictionary and more tags (87). TAGGIT was applied to the Brown corpus and, according to Francis and Kučera (1982, p. 9), accurately tagged 77% of the corpus; the remainder of the Brown corpus was then tagged by hand. All these early algorithms were based on a two-stage architecture in which a dictionary was first used to assign each word a set of potential parts of speech, and then lists of handwritten disambiguation rules winnowed the set down to a single part of speech per word.

Probabilities were used in tagging by Stolz et al. (1965) and a complete probabilistic tagger with Viterbi decoding was sketched by Bahl and Mercer (1976). The Lancaster-Oslo/Bergen (LOB) corpus, a British English equivalent of the Brown corpus, was tagged in the early 1980’s with the CLAWS tagger (Marshall 1983; Marshall 1987; Garside 1987), a probabilistic algorithm that approximated a simplified HMM tagger. The algorithm used tag bigram probabilities, but instead of storing the word likelihood of each tag, the algorithm marked tags either as rare \( P(t|w) < .01 \) or infrequent \( P(t|w) < .10 \) or normally frequent \( P(t|w) > .10 \). DeRose (1988) developed a quasi-HMM algorithm, including the use of dynamic programming, although computing \( P(t|w)P(w) \) instead of \( P(w|t)P(w) \). The same year, the probabilistic PARTS tagger of Church 1988, 1989 was probably the first implemented HMM tagger, described correctly in Church (1989), although Church (1988) also described the computation incorrectly as \( P(t|w)P(w) \) instead of \( P(w|t)P(w) \). Church (p.c.) explained that he had simplified for pedagogical purposes because using the probability \( P(t|w) \) made the idea seem more understandable as “storing a lexicon in an almost standard form”.

Later taggers explicitly introduced the use of the hidden Markov model (Kupiec 1992; Weischedel et al. 1993; Schütze and Singer 1994). Merialdo (1994) showed that fully unsupervised EM didn’t work well for the tagging task and that reliance on hand-labeled data was important. Charniak et al. (1993) showed the importance of the most frequent tag baseline; the 92.3% number we give above was from Abney et al. (1999). See Brants (2000) for HMM tagger implementation details, including the extension to trigram contexts, and the use of sophisticated unknown word features; its performance is still close to state of the art taggers.
Log-linear models for POS tagging were introduced by Ratnaparkhi (1996), who introduced a system called MXPOST which implemented a maximum entropy Markov model (MEMM), a slightly simpler version of a CRF. Around the same time, sequence labelers were applied to the task of named entity tagging, first with HMMs (Bikel et al., 1997) and MEMMs (McCallum et al., 2000), and then once CRFs were developed (Lafferty et al. 2001), they were also applied to NER (McCallum and Li, 2003). A wide exploration of features followed (Zhou et al., 2005). Neural approaches to NER mainly follow from the pioneering results of Collobert et al. (2011), who applied a CRF on top of a convolutional net. BiLSTMs with word and character-based embeddings as input followed shortly and became a standard neural algorithm for NER (Huang et al. 2015, Ma and Hovy 2016, Lample et al. 2016) followed by the more recent use of Transformers and BERT.

The idea of using letter suffixes for unknown words is quite old; the early Klein and Simmons (1963) system checked all final letter suffixes of lengths 1-5. The unknown word features described on page 178 come mainly from Ratnaparkhi (1996), with augmentations from Toutanova et al. (2003) and Manning (2011).

State of the art POS taggers use neural algorithms, either bidirectional RNNs or Transformers like BERT; see Chapter 9 and Chapter 11. HMM (Brants 2000; Thede and Harper 1999) and CRF tagger accuracies are likely just a tad lower.

Manning (2011) investigates the remaining 2.7% of errors in a high-performing tagger (Toutanova et al., 2003). He suggests that a third or half of these remaining errors are due to errors or inconsistencies in the training data, a third might be solvable with richer linguistic models, and for the remainder the task is underspecified or unclear.

Supervised tagging relies heavily on in-domain training data hand-labeled by experts. Ways to relax this assumption include unsupervised algorithms for clustering words into part-of-speech-like classes, summarized in Christodoulopoulos et al. (2010), and ways to combine labeled and unlabeled data, for example by co-training (Clark et al. 2003; Søgaard 2010).


**Exercises**

8.1 Find one tagging error in each of the following sentences that are tagged with the Penn Treebank tagset:

1. I/PRP need/VBP a/DT flight/NN from/IN Atlanta/NN
2. Does/VBZ this/DT flight/NN serve/VB dinner/NNS
3. I/PRP have/VB a/DT friend/NN living/VBG in/IN Denver/NNP
4. Can/VBP you/PRP list/VB the/DT nonstop/JJ afternoon/NN flights/NNS

8.2 Use the Penn Treebank tagset to tag each word in the following sentences from Damon Runyon’s short stories. You may ignore punctuation. Some of these are quite difficult; do your best.

1. It is a nice night.
2. This crap game is over a garage in Fifty-second Street...
3. ...Nobody ever takes the newspapers she sells...
4. He is a tall, skinny guy with a long, sad, mean-looking kisser, and a mournful voice.
5. ... I am sitting in Mindy’s restaurant putting on the gefillte fish, which is a dish I am very fond of, ...
6. When a guy and a doll get to taking peeks back and forth at each other, why there you are indeed.

8.3 Now compare your tags from the previous exercise with one or two friend’s answers. On which words did you disagree the most? Why?

8.4 Implement the “most likely tag” baseline. Find a POS-tagged training set, and use it to compute for each word the tag that maximizes $p(t|w)$. You will need to implement a simple tokenizer to deal with sentence boundaries. Start by assuming that all unknown words are NN and compute your error rate on known and unknown words. Now write at least five rules to do a better job of tagging unknown words, and show the difference in error rates.

8.5 Build a bigram HMM tagger. You will need a part-of-speech-tagged corpus. First split the corpus into a training set and test set. From the labeled training set, train the transition and observation probabilities of the HMM tagger directly on the hand-tagged data. Then implement the Viterbi algorithm so you can decode a test sentence. Now run your algorithm on the test set. Report its error rate and compare its performance to the most frequent tag baseline.

8.6 Do an error analysis of your tagger. Build a confusion matrix and investigate the most frequent errors. Propose some features for improving the performance of your tagger on these errors.

8.7 Develop a set of regular expressions to recognize the character shape features described on page 178.

8.8 The BIO and other labeling schemes given in this chapter aren’t the only possible one. For example, the B tag can be reserved only for those situations where an ambiguity exists between adjacent entities. Propose a new set of BIO tags for use with your NER system. Experiment with it and compare its performance with the schemes presented in this chapter.

8.9 Names of works of art (books, movies, video games, etc.) are quite different from the kinds of named entities we’ve discussed in this chapter. Collect a list of names of works of art from a particular category from a Web-based source (e.g., gutenberg.org, amazon.com, imdb.com, etc.). Analyze your list and give examples of ways that the names in it are likely to be problematic for the techniques described in this chapter.

8.10 Develop an NER system specific to the category of names that you collected in the last exercise. Evaluate your system on a collection of text likely to contain instances of these named entities.
Language is an inherently temporal phenomenon. Spoken language is a sequence of acoustic events over time, and we comprehend and produce both spoken and written language as a continuous input stream. The temporal nature of language is reflected in the metaphors we use: we talk of the flow of conversations, news feeds, and twitter streams, all of which emphasize that language is a sequence that unfolds in time.

This temporal nature is reflected in some language processing algorithms. For example, the Viterbi algorithm we introduced for HMM part-of-speech tagging proceeds through the input a word at a time, carrying forward information gleaned along the way. Yet other machine learning approaches, like those we’ve studied for sentiment analysis or other text classification tasks don’t have this temporal nature – they assume simultaneous access to all aspects of their input.

The feedforward networks of Chapter 7 also assumed simultaneous access, although they also had a simple model for time. Recall that we applied feedforward networks to language modeling by having them look only at a fixed-size window of words, and then sliding this window over the input, making independent predictions along the way. This sliding-window approach is also used in the transformer architecture we will introduce in Chapter 10.

This chapter introduces a deep learning architecture that offers an alternative way of representing time: recurrent neural networks (RNNs), and their variants like LSTMs. RNNs have a mechanism that deals directly with the sequential nature of language, allowing them to handle the temporal nature of language without the use of arbitrary fixed-sized windows. The recurrent network offers a new way to represent the prior context, in its recurrent connections, allowing the model’s decision to depend on information from hundreds of words in the past. We’ll see how to apply the model to the task of language modeling, to sequence modeling tasks like part-of-speech tagging, and to text classification tasks like sentiment analysis.

### 9.1 Recurrent Neural Networks

A recurrent neural network (RNN) is any network that contains a cycle within its network connections, meaning that the value of some unit is directly, or indirectly, dependent on its own earlier outputs as an input. While powerful, such networks are difficult to reason about and to train. However, within the general class of recurrent networks there are constrained architectures that have proven to be extremely effective when applied to language. In this section, we consider a class of recurrent networks referred to as Elman Networks (Elman, 1990) or simple recurrent net-
works. These networks are useful in their own right and serve as the basis for more complex approaches like the Long Short-Term Memory (LSTM) networks discussed later in this chapter. In this chapter when we use the term RNN we’ll be referring to these simpler more constrained networks (although you will often see the term RNN to mean any net with recurrent properties including LSTMs).

Fig. 9.1 illustrates the structure of an RNN. As with ordinary feedforward networks, an input vector representing the current input, \( x_t \), is multiplied by a weight matrix and then passed through a non-linear activation function to compute the values for a layer of hidden units. This hidden layer is then used to calculate a corresponding output, \( y_t \). In a departure from our earlier window-based approach, sequences are processed by presenting one item at a time to the network. We’ll use subscripts to represent time, thus \( x_t \) will mean the input vector \( x \) at time \( t \). The key difference from a feedforward network lies in the recurrent link shown in the figure with the dashed line. This link augments the input to the computation at the hidden layer with the value of the hidden layer from the preceding point in time.

The hidden layer from the previous time step provides a form of memory, or context, that encodes earlier processing and informs the decisions to be made at later points in time. Critically, this approach does not impose a fixed-length limit on this prior context; the context embodied in the previous hidden layer can include information extending back to the beginning of the sequence.

Adding this temporal dimension makes RNNs appear to be more complex than non-recurrent architectures. But in reality, they’re not all that different. Given an input vector and the values for the hidden layer from the previous time step, we’re still performing the standard feedforward calculation introduced in Chapter 7. To see this, consider Fig. 9.2 which clarifies the nature of the recurrence and how it factors into the computation at the hidden layer. The most significant change lies in the new set of weights, \( U \), that connect the hidden layer from the previous time step to the current hidden layer. These weights determine how the network makes use of past context in calculating the output for the current input. As with the other weights in the network, these connections are trained via backpropagation.

### 9.1.1 Inference in RNNs

Forward inference (mapping a sequence of inputs to a sequence of outputs) in an RNN is nearly identical to what we’ve already seen with feedforward networks. To compute an output \( y_t \) for an input \( x_t \), we need the activation value for the hidden layer \( h_t \). To calculate this, we multiply the input \( x_t \) with the weight matrix \( W \), and the hidden layer from the previous time step \( h_{t-1} \) with the weight matrix \( U \). We add these values together and pass them through a suitable activation function, \( g \), to arrive at the activation value for the current hidden layer, \( h_t \). Once we have the
values for the hidden layer, we proceed with the usual computation to generate the output vector.

\[
\begin{align*}
    h_t &= g(Uh_{t-1} + Wx_t) \\
    y_t &= f(Vh_t)
\end{align*}
\]  

(9.1) (9.2)

It’s worthwhile here to be careful about specifying the dimensions of the input, hidden and output layers, as well as the weight matrices to make sure these calculations are correct. Let’s refer to the input, hidden and output layer dimensions as \(d_{in}\), \(d_h\), and \(d_{out}\) respectively. Given this, our three parameter matrices are: \(W \in \mathbb{R}^{d_h \times d_{in}}\), \(U \in \mathbb{R}^{d_h \times d_h}\), and \(V \in \mathbb{R}^{d_{out} \times d_h}\).

In the commonly encountered case of soft classification, computing \(y_t\) consists of a softmax computation that provides a probability distribution over the possible output classes.

\[
    y_t = \text{softmax}(Vh_t)
\]

(9.3)

The fact that the computation at time \(t\) requires the value of the hidden layer from time \(t-1\) mandates an incremental inference algorithm that proceeds from the start of the sequence to the end as illustrated in Fig. 9.3. The sequential nature of simple recurrent networks can also be seen by unrolling the network in time as is shown in Fig. 9.4. In this figure, the various layers of units are copied for each time step to illustrate that they will have differing values over time. However, the various weight matrices are shared across time.

```
function FORWARDRNN(x, network) returns output sequence y
    h_0 ← 0
    for i ← 1 to LENGTH(x) do
        h_i ← g(Uh_{i-1} + Wx_i)
        y_i ← f(Vh_i)
    return y
```

Figure 9.3 Forward inference in a simple recurrent network. The matrices \(U\), \(V\) and \(W\) are shared across time, while new values for \(h\) and \(y\) are calculated with each time step.
9.1.2 Training

As with feedforward networks, we’ll use a training set, a loss function, and backpropagation to obtain the gradients needed to adjust the weights in these recurrent networks. As shown in Fig. 9.2, we now have 3 sets of weights to update: \( W \), the weights from the input layer to the hidden layer, \( U \), the weights from the previous hidden layer to the current hidden layer, and finally \( V \), the weights from the hidden layer to the output layer.

Fig. 9.4 highlights two considerations that we didn’t have to worry about with backpropagation in feedforward networks. First, to compute the loss function for the output at time \( t \) we need the hidden layer from time \( t - 1 \). Second, the hidden layer at time \( t \) influences both the output at time \( t \) and the hidden layer at time \( t + 1 \) (and hence the output and loss at \( t + 1 \)). It follows from this that to assess the error accruing to \( h_t \), we’ll need to know its influence on both the current output as well as the ones that follow.

Tailoring the backpropagation algorithm to this situation leads to a two-pass algorithm for training the weights in RNNs. In the first pass, we perform forward inference, computing \( h_t, y_t \), accumulating the loss at each step in time, saving the value of the hidden layer at each step for use at the next time step. In the second phase, we process the sequence in reverse, computing the required gradients as we go, computing and saving the error term for use in the hidden layer for each step backward in time. This general approach is commonly referred to as backpropagation through time (Werbos 1974, Rumelhart et al. 1986, Werbos 1990).

Fortunately, with modern computational frameworks and adequate computing resources, there is no need for a specialized approach to training RNNs. As illustrated in Fig. 9.4, explicitly unrolling a recurrent network into a feedforward computational graph eliminates any explicit recurrences, allowing the network weights to be trained directly. In such an approach, we provide a template that specifies the basic structure of the network, including all the necessary parameters for the input,
output, and hidden layers, the weight matrices, as well as the activation and output functions to be used. Then, when presented with a specific input sequence, we can generate an unrolled feedforward network specific to that input, and use that graph to perform forward inference or training via ordinary backpropagation.

For applications that involve much longer input sequences, such as speech recognition, character-level processing, or streaming continuous inputs, unrolling an entire input sequence may not be feasible. In these cases, we can unroll the input into manageable fixed-length segments and treat each segment as a distinct training item.

### 9.2 RNNs as Language Models

Let’s see how to apply RNNs to the language modeling task. Recall from Chapter 3 that language models predict the next word in a sequence given some preceding context. For example, if the preceding context is “Thanks for all the” and we want to know how likely the next word is “fish” we would compute:

\[ P(\text{fish}|\text{Thanks for all the}) \]

Language models give us the ability to assign such a conditional probability to every possible next word, giving us a distribution over the entire vocabulary. We can also assign probabilities to entire sequences by combining these conditional probabilities with the chain rule:

\[ P(w_1:n) = \prod_{i=1}^{n} P(w_i|w_{<i}) \]

The n-gram language models of Chapter 3 compute the probability of a word given counts of its occurrence with the \( n-1 \) prior words. The context is thus of size \( n-1 \). For the feedforward language models of Chapter 7, the context is the window size.

RNN language models (Mikolov et al., 2010) process the input sequence one word at a time, attempting to predict the next word from the current word and the previous hidden state. RNNs thus don’t have the limited context problem that n-gram models have, or the fixed context that feedforward language models have, since the hidden state can in principle represent information about all of the preceding words all the way back to the beginning of the sequence. Fig. 9.5 sketches this difference between a FFN language model and an RNN language model, showing that the RNN language model uses \( h_{t-1} \), the hidden state from the previous time step, as a representation of the past context.

#### 9.2.1 Forward Inference in an RNN language model

Forward inference in a recurrent language model proceeds exactly as described in Section 9.1.1. The input sequence \( X = [x_1; \ldots; x_t; \ldots; x_N] \) consists of a series of words each represented as a one-hot vector of size \( |V| \times 1 \), and the output prediction, \( y \), is a vector representing a probability distribution over the vocabulary. At each step, the model uses the word embedding matrix \( E \) to retrieve the embedding for the current word, and then combines it with the hidden layer from the previous step to compute a new hidden layer. This hidden layer is then used to generate an output layer which is passed through a softmax layer to generate a probability distribution over the entire
vocabulary. That is, at time $t$:

\begin{align*}
\mathbf{e}_t &= \mathbf{E} \mathbf{x}_t \quad (9.4) \\
\mathbf{h}_t &= g((\mathbf{U} \mathbf{h}_{t-1} + \mathbf{W} \mathbf{e}_t) \quad (9.5) \\
\mathbf{y}_t &= \text{softmax}(\mathbf{V} \mathbf{h}_t) \quad (9.6)
\end{align*}

The vector resulting from $\mathbf{V} \mathbf{h}$ can be thought of as a set of scores over the vocabulary given the evidence provided in $\mathbf{h}$. Passing these scores through the softmax normalizes the scores into a probability distribution. The probability that a particular word $l$ in the vocabulary is the next word is represented by $\mathbf{y}_t[k]$, the $k$th component of $\mathbf{y}_t$:

$$P(w_{t+1} = k | w_1, \ldots, w_t) = \mathbf{y}_t[k] \quad (9.7)$$

The probability of an entire sequence is just the product of the probabilities of each item in the sequence, where we’ll use $\mathbf{y}_i[w_i]$ to mean the probability of the true word $w_i$ at time step $i$.

$$P(w_1^{n}) = \prod_{i=1}^{n} P(w_i | w_1^{i-1}) = \prod_{i=1}^{n} \mathbf{y}_i[w_i] \quad (9.8)$$

$$L_{CE} = -\sum_{w \in \mathcal{V}} \mathbf{y}_t[w] \log \hat{\mathbf{y}}_t[w] \quad (9.10)$$

In the case of language modeling, the correct distribution $\mathbf{y}_t$ comes from knowing the next word. This is represented as a one-hot vector corresponding to the vocabulary.
where the entry for the actual next word is 1, and all the other entries are 0. Thus, the cross-entropy loss for language modeling is determined by the probability the model assigns to the correct next word. So at time $t$ the CE loss is the negative log probability the model assigns to the next word in the training sequence.

$$L_{CE}(\hat{y}_t, y_t) = -\log \hat{y}_t[w_{t+1}]$$ (9.11)

Thus at each word position $t$ of the input, the model takes as input the correct sequence of tokens $w_1:t$, and uses them to compute a probability distribution over possible next words so as to compute the model’s loss for the next token $w_{t+1}$. Then we move to the next word, we ignore what the model predicted for the next word and instead use the correct sequence of tokens $w_1:t+1$ to estimate the probability of token $w_{t+2}$. This idea that we always give the model the correct history sequence to predict the next word (rather than feeding the model its best case from the previous time step) is called teacher forcing.

The weights in the network are adjusted to minimize the average CE loss over the training sequence via gradient descent. Fig. 9.6 illustrates this training regimen.

### 9.2.3 Weight Tying

Careful readers may have noticed that the input embedding matrix $E$ and the final layer matrix $V$, which feeds the output softmax, are quite similar. The columns of $E$ represent the word embeddings for each word in the vocabulary learned during the training process with the goal that words that have similar meaning and function will have similar embeddings. And, since the length of these embeddings corresponds to the size of the hidden layer $d_h$, the shape of the embedding matrix $E$ is $d_h \times |V|$.

The final layer matrix $V$ provides a way to score the likelihood of each word in the vocabulary given the evidence present in the final hidden layer of the network through the calculation of $Vh$. This results in dimensionality $|V| \times d_h$. That is, the rows of $V$ provide a second set of learned word embeddings that capture relevant aspects of word meaning. This leads to an obvious question – is it even necessary to have both? **Weight tying** is a method that dispenses with this redundancy and simply uses a single set of embeddings at the input and softmax layers. That is, we
dispense with $V$ and use $E$ in both the start and end of the computation.

\begin{align*}
    e_t &= Ex_t \\
    h_t &= g(Uh_{t-1} + We_t) \\
    y_t &= \text{softmax}(E^t h_t)
\end{align*}

In addition to providing improved model perplexity, this approach significantly reduces the number of parameters required for the model.

9.3 RNNs for other NLP tasks

Now that we’ve seen the basic RNN architecture, let’s consider how to apply it to three types of NLP tasks: sequence classification tasks like sentiment analysis and topic classification, sequence labeling tasks like part-of-speech tagging, and text generation tasks, including with a new architecture called the encoder-decoder.

9.3.1 Sequence Labeling

In sequence labeling, the network’s task is to assign a label chosen from a small fixed set of labels to each element of a sequence, like the part-of-speech tagging and named entity recognition tasks from Chapter 8. In an RNN approach to sequence labeling, inputs are word embeddings and the outputs are tag probabilities generated by a softmax layer over the given tagset, as illustrated in Fig. 9.7.

In this figure, the inputs at each time step are pretrained word embeddings corresponding to the input tokens. The RNN block is an abstraction that represents an unrolled simple recurrent network consisting of an input layer, hidden layer, and output layer at each time step, as well as the shared $U$, $V$ and $W$ weight matrices that comprise the network. The outputs of the network at each time step represent the distribution over the POS tagset generated by a softmax layer.
To generate a sequence of tags for a given input, we run forward inference over the input sequence and select the most likely tag from the softmax at each step. Since we’re using a softmax layer to generate the probability distribution over the output tagset at each time step, we will again employ the cross-entropy loss during training.

### 9.3.2 RNNs for Sequence Classification

Another use of RNNs is to classify entire sequences rather than the tokens within them. This is the set of tasks commonly called text classification, like sentiment analysis or spam detection, in which we classify a text into two or three classes (like positive or negative), as well as classification tasks with a large number of categories, like document-level topic classification, or message routing for customer service applications.

To apply RNNs in this setting, we pass the text to be classified through the RNN a word at a time generating a new hidden layer at each time step. We can then take the hidden layer for the last token of the text, $h_n$, to constitute a compressed representation of the entire sequence. We can pass this representation $h_n$ to a feedforward network that chooses a class via a softmax over the possible classes. Fig. 9.8 illustrates this approach.

![Figure 9.8](image)

**Figure 9.8** Sequence classification using a simple RNN combined with a feedforward network. The final hidden state from the RNN is used as the input to a feedforward network that performs the classification.

Note that in this approach we don’t need intermediate outputs for the words in the sequence preceding the last element. Therefore, there are no loss terms associated with those elements. Instead, the loss function used to train the weights in the network is based entirely on the final text classification task. The output from the softmax output from the feedforward classifier together with a cross-entropy loss drives the training. The error signal from the classification is backpropagated all the way through the weights in the feedforward classifier through, to its input, and then through to the three sets of weights in the RNN as described earlier in Section 9.1.2. The training regimen that uses the loss from a downstream application to adjust the weights all the way through the network is referred to as end-to-end training.

Another option, instead of using just the last token $h_n$ to represent the whole sequence, is to use some sort of pooling function of all the hidden states $h_i$ for each word $i$ in the sequence. For example, we can create a representation that pools all...
the $n$ hidden states by taking their element-wise mean:

$$\mathbf{h}_{\text{mean}} = \frac{1}{n} \sum_{i=1}^{n} \mathbf{h}_i$$  \hspace{1cm} (9.15)

Or we can take the element-wise max; the element-wise max of a set of $n$ vectors is a new vector whose $k$th element is the max of the $k$th elements of all the $n$ vectors.

### 9.3.3 Generation with RNN-Based Language Models

RNN-based language models can also be used to generate text. Text generation is of enormous practical importance, part of tasks like question answering, machine translation, text summarization, grammar correction, story generation, and conversational dialogue; any task where a system needs to produce text, conditioned on some other text. This use of a language model to generate text is one of the areas in which the impact of neural language models on NLP has been the largest. Text generation, along with image generation and code generation, constitute a new area of AI that is often called **generative AI**.

Recall back in Chapter 3 we saw how to generate text from an n-gram language model by adapting a *sampling* technique suggested at about the same time by Claude Shannon (Shannon, 1951) and the psychologists George Miller and Jennifer Selfridge (Miller and Selfridge, 1950). We first randomly sample a word to begin a sequence based on its suitability as the start of a sequence. We then continue to sample words *conditioned on our previous choices* until we reach a pre-determined length, or an end of sequence token is generated.

Today, this approach of using a language model to incrementally generate words by repeatedly sampling the next word conditioned on our previous choices is called **autoregressive generation** or **causal LM generation**. The procedure is basically the same as that described on page 42, but adapted to a neural context:

- Sample a word in the output from the softmax distribution that results from using the beginning of sentence marker, $<$s$, as the first input.
- Use the word embedding for that first word as the input to the network at the next time step, and then sample the next word in the same fashion.
- Continue generating until the end of sentence marker, $</s$, is sampled or a fixed length limit is reached.

Technically an **autoregressive** model is a model that predicts a value at time $t$ based on a linear function of the previous values at times $t-1, t-2$, and so on. Although language models are not linear (since they have many layers of non-linearities), we loosely refer to this generation technique as **autoregressive generation** since the word generated at each time step is conditioned on the word selected by the network from the previous step. Fig. 9.9 illustrates this approach. In this figure, the details of the RNN’s hidden layers and recurrent connections are hidden within the blue block.

This simple architecture underlies state-of-the-art approaches to applications such as machine translation, summarization, and question answering. The key to these approaches is to prime the generation component with an appropriate context. That is, instead of simply using $<$s$ to get things started we can provide a richer task-appropriate context; for translation the context is the sentence in the source language; for summarization it’s the long text we want to summarize.
9.4 Stacked and Bidirectional RNN architectures

Recurrent networks are quite flexible. By combining the feedforward nature of unrolled computational graphs with vectors as common inputs and outputs, complex networks can be treated as modules that can be combined in creative ways. This section introduces two of the more common network architectures used in language processing with RNNs.

9.4.1 Stacked RNNs

In our examples thus far, the inputs to our RNNs have consisted of sequences of word or character embeddings (vectors) and the outputs have been vectors useful for predicting words, tags or sequence labels. However, nothing prevents us from using the entire sequence of outputs from one RNN as an input sequence to another one. **Stacked RNNs** consist of multiple networks where the output of one layer serves as the input to a subsequent layer, as shown in Fig. 9.10.
Stacked RNNs generally outperform single-layer networks. One reason for this success seems to be that the network induces representations at differing levels of abstraction across layers. Just as the early stages of the human visual system detect edges that are then used for finding larger regions and shapes, the initial layers of stacked networks can induce representations that serve as useful abstractions for further layers—representations that might prove difficult to induce in a single RNN. The optimal number of stacked RNNs is specific to each application and to each training set. However, as the number of stacks is increased the training costs rise quickly.

### 9.4.2 Bidirectional RNNs

The RNN uses information from the left (prior) context to make its predictions at time $t$. But in many applications we have access to the entire input sequence; in those cases we would like to use words from the context to the right of $t$. One way to do this is to run two separate RNNs, one left-to-right, and one right-to-left, and concatenate their representations.

In the left-to-right RNNs we’ve discussed so far, the hidden state at a given time $t$ represents everything the network knows about the sequence up to that point. The state is a function of the inputs $x_1,...,x_t$ and represents the context of the network to the left of the current time.

$$h_f^t = \text{RNN}_{\text{forward}}(x_1,...,x_t)$$  \hspace{1cm} (9.16)

This new notation $h_f^t$ simply corresponds to the normal hidden state at time $t$, representing everything the network has gleaned from the sequence so far.

To take advantage of context to the right of the current input, we can train an RNN on a reversed input sequence. With this approach, the hidden state at time $t$ represents information about the sequence to the right of the current input:

$$h_b^t = \text{RNN}_{\text{backward}}(x_t,...,x_n)$$  \hspace{1cm} (9.17)

Here, the hidden state $h_b^t$ represents all the information we have discerned about the sequence from $t$ to the end of the sequence.

A bidirectional RNN (Schuster and Paliwal, 1997) combines two independent RNNs, one where the input is processed from the start to the end, and the other from the end to the start. We then concatenate the two representations computed by the networks into a single vector that captures both the left and right contexts of an input at each point in time. Here we use either the semicolon “;” or the equivalent symbol $\oplus$ to mean vector concatenation:

$$h_t = [h_f^t ; h_b^t] = h_f^t \oplus h_b^t$$  \hspace{1cm} (9.18)

Fig. 9.11 illustrates such a bidirectional network that concatenates the outputs of the forward and backward pass. Other simple ways to combine the forward and backward contexts include element-wise addition or multiplication. The output at each step in time thus captures information to the left and to the right of the current input. In sequence labeling applications, these concatenated outputs can serve as the basis for a local labeling decision.

Bidirectional RNNs have also proven to be quite effective for sequence classification. Recall from Fig. 9.8 that for sequence classification we used the final hidden
state of the RNN as the input to a subsequent feedforward classifier. A difficulty with this approach is that the final state naturally reflects more information about the end of the sentence than its beginning. Bidirectional RNNs provide a simple solution to this problem; as shown in Fig. 9.12, we simply combine the final hidden states from the forward and backward passes (for example by concatenation) and use that as input for follow-on processing.
9.5 The LSTM

In practice, it is quite difficult to train RNNs for tasks that require a network to make use of information distant from the current point of processing. Despite having access to the entire preceding sequence, the information encoded in hidden states tends to be fairly local, more relevant to the most recent parts of the input sequence and recent decisions. Yet distant information is critical to many language applications. Consider the following example in the context of language modeling.

(9.19) The flights the airline was canceling were full.

Assigning a high probability to was following airline is straightforward since airline provides a strong local context for the singular agreement. However, assigning an appropriate probability to were is quite difficult, not only because the plural flights is quite distant, but also because the singular noun airline is closer in the intervening context. Ideally, a network should be able to retain the distant information about plural flights until it is needed, while still processing the intermediate parts of the sequence correctly.

One reason for the inability of RNNs to carry forward critical information is that the hidden layers, and, by extension, the weights that determine the values in the hidden layer, are being asked to perform two tasks simultaneously: provide information useful for the current decision, and updating and carrying forward information required for future decisions.

A second difficulty with training RNNs arises from the need to backpropagate the error signal back through time. Recall from Section 9.1.2 that the hidden layer at time $t$ contributes to the loss at the next time step since it takes part in that calculation. As a result, during the backward pass of training, the hidden layers are subject to repeated multiplications, as determined by the length of the sequence. A frequent result of this process is that the gradients are eventually driven to zero, a situation called the vanishing gradients problem.

To address these issues, more complex network architectures have been designed to explicitly manage the task of maintaining relevant context over time, by enabling the network to learn to forget information that is no longer needed and to remember information required for decisions still to come.

The most commonly used such extension to RNNs is the long short-term memory (LSTM) network (Hochreiter and Schmidhuber, 1997). LSTMs divide the context management problem into two subproblems: removing information no longer needed from the context, and adding information likely to be needed for later decision making. The key to solving both problems is to learn how to manage this context rather than hard-coding a strategy into the architecture. LSTMs accomplish this by first adding an explicit context layer to the architecture (in addition to the usual recurrent hidden layer), and through the use of specialized neural units that make use of gates to control the flow of information into and out of the units that comprise the network layers. These gates are implemented through the use of additional weights that operate sequentially on the input, and previous hidden layer, and previous context layers.

The gates in an LSTM share a common design pattern; each consists of a feed-forward layer, followed by a sigmoid activation function, followed by a pointwise multiplication with the layer being gated. The choice of the sigmoid as the activation function arises from its tendency to push its outputs to either 0 or 1. Combining this with a pointwise multiplication has an effect similar to that of a binary mask. Values
in the layer being gated that align with values near 1 in the mask are passed through nearly unchanged; values corresponding to lower values are essentially erased.

The first gate we’ll consider is the **forget gate**. The purpose of this gate is to delete information from the context that is no longer needed. The forget gate computes a weighted sum of the previous state’s hidden layer and the current input and passes that through a sigmoid. This mask is then multiplied element-wise by the context vector to remove the information from context that is no longer required. Element-wise multiplication of two vectors (represented by the operator $\odot$, and sometimes called the **Hadamard product**) is the vector of the same dimension as the two input vectors, where each element $i$ is the product of element $i$ in the two input vectors:

$$f_t = \sigma(U_f h_{t-1} + W_f x_t) \quad (9.20)$$

The next task is to compute the actual information we need to extract from the previous hidden state and current inputs—the same basic computation we’ve been using for all our recurrent networks.

$$g_t = \tanh(U_g h_{t-1} + W_g x_t) \quad (9.22)$$

Next, we generate the mask for the **add gate** to select the information to add to the current context.

$$i_t = \sigma(U_i h_{t-1} + W_i x_t) \quad (9.23)$$

$$j_t = g_t \odot i_t \quad (9.24)$$

Next, we add this to the modified context vector to get our new context vector.

$$c_t = j_t + k_t \quad (9.25)$$

The final gate we’ll use is the **output gate** which is used to decide what information is required for the current hidden state (as opposed to what information needs to be preserved for future decisions).

$$o_t = \sigma(U_o h_{t-1} + W_o x_t) \quad (9.26)$$

$$h_t = o_t \odot \tanh(c_t) \quad (9.27)$$

Fig. 9.13 illustrates the complete computation for a single LSTM unit. Given the appropriate weights for the various gates, an LSTM accepts as input the context layer, and hidden layer from the previous time step, along with the current input vector. It then generates updated context and hidden vectors as output.

It is the hidden state, $h_t$, that provides the output for the LSTM at each time step. This output can be used as the input to subsequent layers in a stacked RNN, or at the final layer of a network $h_T$ can be used to provide the final output of the LSTM.

### 9.5.1 Gated Units, Layers and Networks

The neural units used in LSTMs are obviously much more complex than those used in basic feedforward networks. Fortunately, this complexity is encapsulated within the basic processing units, allowing us to maintain modularity and to easily experiment with different architectures. To see this, consider Fig. 9.14 which illustrates the inputs and outputs associated with each kind of unit.
At the far left, (a) is the basic feedforward unit where a single set of weights and a single activation function determine its output, and when arranged in a layer there are no connections among the units in the layer. Next, (b) represents the unit in a simple recurrent network. Now there are two inputs and an additional set of weights to go with it. However, there is still a single activation function and output.

The increased complexity of the LSTM units is encapsulated within the unit itself. The only additional external complexity for the LSTM over the basic recurrent unit (b) is the presence of the additional context vector as an input and output.

This modularity is key to the power and widespread applicability of LSTM units. LSTM units (or other varieties, like GRUs) can be substituted into any of the network architectures described in Section 9.4. And, as with simple RNNs, multi-layered networks making use of gated units can be unrolled into deep feedforward networks and trained in the usual fashion with backpropagation. In practice, therefore, LSTMs rather than RNNs have become the standard unit for any modern system that makes use of recurrent networks.
9.6 Summary: Common RNN NLP Architectures

We’ve now introduced the RNN, seen advanced components like stacking multiple layers and using the LSTM version, and seen how the RNN can be applied to various tasks. Let’s take a moment to summarize the architectures for these applications.

Fig. 9.15 shows the three architectures we’ve discussed so far: sequence labeling, sequence classification, and language modeling. In sequence labeling (for example for part of speech tagging), we train a model to produce a label for each input word or token. In sequence classification, for example for sentiment analysis, we ignore the output for each token, and only take the value from the end of the sequence (and similarly the model’s training signal comes from backpropagation from that last token). In language modeling, we train the model to predict the next word at each token step. In the next section we’ll introduce a fourth architecture, the encoder-decoder.

![Figure 9.15](image)

**Figure 9.15** Four architectures for NLP tasks. In sequence labeling (POS or named entity tagging) we map each input token \( x_i \) to an output token \( y_i \). In sequence classification we map the entire input sequence to a single class. In language modeling we output the next token conditioned on previous tokens. In the encoder model we have two separate RNN models, one of which maps from an input sequence \( x \) to an intermediate representation we call the context, and a second of which maps from the context to an output sequence \( y \).

9.7 The Encoder-Decoder Model with RNNs

In this section we introduce a new model, the encoder-decoder model, which is used when we are taking an input sequence and translating it to an output sequence that is of a different length than the input, and doesn’t align with it in a word-to-word way. Recall that in the sequence labeling task, we have two sequences, but they are the...
same length (for example in part-of-speech tagging each token gets an associated
tag), each input is associated with a specific output, and the labeling for that output
takes mostly local information. Thus deciding whether a word is a verb or a noun,
we look mostly at the word and the neighboring words.

By contrast, encoder-decoder models are used especially for tasks like machine
translation, where the input sequence and output sequence can have different lengths
and the mapping between a token in the input and a token in the output can be very
indirect (in some languages the verb appears at the beginning of the sentence; in
other languages at the end). We’ll introduce machine translation in detail in Chap-
ter 13, but for now we’ll just point out that the mapping for a sentence in English to
a sentence in Tagalog or Yoruba can have very different numbers of words, and the
words can be in a very different order.

Encoder-decoder networks, sometimes called sequence-to-sequence networks,
are models capable of generating contextually appropriate, arbitrary length, output
sequences given an input sequence. Encoder-decoder networks have been applied
to a very wide range of applications including summarization, question answering,
and dialogue, but they are particularly popular for machine translation.

The key idea underlying these networks is the use of an encoder network that
takes an input sequence and creates a contextualized representation of it, often called
the context. This representation is then passed to a decoder which generates a task-
specific output sequence. Fig. 9.16 illustrates the architecture.

Encoder-decoder networks consist of three conceptual components:

1. An encoder that accepts an input sequence, \( x_{1:n} \), and generates a correspond-
ing sequence of contextualized representations, \( h_{1:n} \). LSTMs, convolutional
networks, and transformers can all be employed as encoders.

2. A context vector, \( c \), which is a function of \( h_{1:n} \), and conveys the essence of
the input to the decoder.

3. A decoder, which accepts \( c \) as input and generates an arbitrary length se-
quence of hidden states \( h_{1:m} \), from which a corresponding sequence of output
states \( y_{1:m} \), can be obtained. Just as with encoders, decoders can be realized
by any kind of sequence architecture.

In this section we’ll describe an encoder-decoder network based on a pair of
RNNs, but we’ll see in Chapter 13 how to apply them to transformers as well. We’ll
build up the equations for encoder-decoder models by starting with the conditional
RNN language model \( p(y) \), the probability of a sequence \( y \).

Recall that in any language model, we can break down the probability as follows:

\[
p(y) = p(y_1)p(y_2|y_1)p(y_3|y_1, y_2)\cdots p(y_m|y_1, \ldots, y_{m-1}) \tag{9.28}
\]
9.7 • The Encoder-Decoder Model with RNNs

In RNN language modeling, at a particular time \( t \), we pass the prefix of \( t - 1 \) tokens through the language model, using forward inference to produce a sequence of hidden states, ending with the hidden state corresponding to the last word of the prefix. We then use the final hidden state of the prefix as our starting point to generate the next token.

More formally, if \( g \) is an activation function like \( \tanh \) or ReLU, a function of the input at time \( t \) and the hidden state at time \( t - 1 \), and \( f \) is a softmax over the set of possible vocabulary items, then at time \( t \) the output \( y_t \) and hidden state \( h_t \) are computed as:

\[
\begin{align*}
    h_t &= g(h_{t-1}, x_t) \quad (9.29) \\
    y_t &= f(h_t) \quad (9.30)
\end{align*}
\]

We only have to make one slight change to turn this language model with autoregressive generation into an encoder-decoder model that is a translation model that can translate from a source text in one language to a target text in a second: add a sentence separation marker at the end of the source text, and then simply concatenate the target text.

Let’s use \(<s>\) for our sentence separator token, and let’s think about translating an English source text (“the green witch arrived”), to a Spanish sentence (“\( \text{llegó la bruja verde} \)” (which can be glossed word-by-word as ‘arrived the witch green’)). We could also illustrate encoder-decoder models with a question-answer pair, or a text-summarization pair.

Let’s use \( x \) to refer to the source text (in this case in English) plus the separator token \(<s>\), and \( y \) to refer to the target text \( y \) (in this case in Spanish). Then an encoder-decoder model computes the probability \( p(y|x) \) as follows:

\[
p(y|x) = p(y_1|x)p(y_2|y_1, x)p(y_3|y_1, y_2, x)\ldots p(y_m|y_1, \ldots, y_{m-1}, x) \quad (9.31)
\]

Fig. 9.17 shows the setup for a simplified version of the encoder-decoder model (we’ll see the full model, which requires the new concept of attention, in the next section).

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\]

We only have to make one slight change to turn this language model with autoregressive generation into an encoder-decoder model that is a translation model that can translate from a source text in one language to a target text in a second: add a sentence separation marker at the end of the source text, and then simply concatenate the target text.

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\[
p(y|x) = p(y_1|x)p(y_2|y_1, x)p(y_3|y_1, y_2, x)\ldots p(y_m|y_1, \ldots, y_{m-1}, x) \quad (9.31)
\]

Fig. 9.17 shows the setup for a simplified version of the encoder-decoder model (we’ll see the full model, which requires the new concept of attention, in the next section).

Fig. 9.17 shows the setup for a simplified version of the encoder-decoder approach to machine translation. Source and target sentences are concatenated with a separator token in between, and the decoder uses context information from the encoder’s last hidden state.

Fig. 9.17 shows an English source text (“the green witch arrived”), a sentence separator token (<s>), and a Spanish target text (“\( \text{llegó la bruja verde} \)”). To trans-
late a source text, we run it through the network performing forward inference to
generate hidden states until we get to the end of the source. Then we begin autore-
gressive generation, asking for a word in the context of the hidden layer from the
end of the source input as well as the end-of-sentence marker. Subsequent words
are conditioned on the previous hidden state and the embedding for the last word
generated.

Let’s formalize and generalize this model a bit in Fig. 9.18. (To help keep things
straight, we’ll use the superscripts e and d where needed to distinguish the hidden
states of the encoder and the decoder.) The elements of the network on the left
process the input sequence \( x \) and comprise the encoder. While our simplified figure
shows only a single network layer for the encoder, stacked architectures are the
norm, where the output states from the top layer of the stack are taken as the final
representation, and the encoder consists of stacked biLSTMs where the hidden states
from top layers from the forward and backward passes are concatenated to provide
the contextualized representations for each time step.

The entire purpose of the encoder is to generate a contextualized representation
of the input. This representation is embodied in the final hidden state of the encoder,
\( h^n_e \). This representation, also called \( c \) for context, is then passed to the decoder.

The simplest version of the decoder network would takes this state and use it
just to initialize the first hidden state of the decoder; the first decoder RNN cell
would use \( c \) as its prior hidden state \( h^d_0 \). The decoder would then autoregressively
generates a sequence of outputs, an element at a time, until an end-of-sequence
marker is generated. Each hidden state is conditioned on the previous hidden state
and the output generated in the previous state.

As Fig. 9.18 shows, we do something more complex: we make the context vector
\( c \) available to more than just the first decoder hidden state, to ensure that the influence
of the context vector, \( c \), doesn’t wane as the output sequence is generated. We do
this by adding \( c \) as a parameter to the computation of the current hidden state. using
the following equation:

\[
h^d_t = g(y_{t-1}, h^d_{t-1}, c)
\] (9.32)

Now we’re ready to see the full equations for this version of the decoder in the basic
encoder-decoder model, with context available at each decoding timestep. Recall
that $g$ is a stand-in for some flavor of RNN and $\hat{y}_{t-1}$ is the embedding for the output sampled from the softmax at the previous step:

$$c = h^n_e$$
$$h^d_0 = c$$
$$h^d_t = g(\hat{y}_{t-1}, h^d_{t-1}, c)$$
$$z_t = f(h^d_t)$$
$$y_t = \text{softmax}(z_t)$$

Finally, as shown earlier, the output $y$ at each time step consists of a softmax computation over the set of possible outputs (the vocabulary, in the case of language modeling or MT). We compute the most likely output at each time step by taking the argmax over the softmax output:

$$\hat{y}_t = \text{argmax}_{w \in V} P(w | y_1 ... y_{t-1}, x)$$

### 9.7.1 Training the Encoder-Decoder Model

Encoder-decoder architectures are trained end-to-end. Each training example is a tuple of paired strings, a source and a target. Concatenated with a separator token, these source-target pairs can now serve as training data.

For MT, the training data typically consists of sets of sentences and their translations. These can be drawn from standard datasets of aligned sentence pairs, as we’ll discuss in Section 13.2.2. Once we have a training set, the training itself proceeds as with any RNN-based language model. The network is given the source text and then starting with the separator token is trained autoregressively to predict the next word, as shown in Fig. 9.19.

![Diagram](image_url)

**Figure 9.19** Training the basic RNN encoder-decoder approach to machine translation. Note that in the decoder we usually don’t propagate the model’s softmax outputs $\hat{y}_t$, but use **teacher forcing** to force each input to the correct gold value for training. We compute the softmax output distribution over $\hat{y}_t$ in the decoder in order to compute the loss at each token, which can then be averaged to compute a loss for the sentence.
Note the differences between training (Fig. 9.19) and inference (Fig. 9.17) with respect to the outputs at each time step. The decoder during inference uses its own estimated output $\hat{y}_t$ as the input for the next time step $x_{t+1}$. Thus the decoder will tend to deviate more and more from the gold target sentence as it keeps generating more tokens. In training, therefore, it is more common to use teacher forcing in the decoder. Teacher forcing means that we force the system to use the gold target token from training as the next input $x_{t+1}$, rather than allowing it to rely on the (possibly erroneous) decoder output $\hat{y}_t$. This speeds up training.

### 9.8 Attention

The simplicity of the encoder-decoder model is its clean separation of the encoder—which builds a representation of the source text—from the decoder, which uses this context to generate a target text. In the model as we’ve described it so far, this context vector is $h_n$, the hidden state of the last ($n^{th}$) time step of the source text. This final hidden state is thus acting as a bottleneck: it must represent absolutely everything about the meaning of the source text, since the only thing the decoder knows about the source text is what’s in this context vector (Fig. 9.20). Information at the beginning of the sentence, especially for long sentences, may not be equally well represented in the context vector.

![Diagram of encoder-decoder model](image)

The attention mechanism is a solution to the bottleneck problem, a way of allowing the decoder to get information from all the hidden states of the encoder, not just the last hidden state.

In the attention mechanism, as in the vanilla encoder-decoder model, the context vector $c$ is a single vector that is a function of the hidden states of the encoder, that is, $c = f(h_1^{e} \ldots h_{n}^{e})$. Because the number of hidden states varies with the size of the input, we can’t use the entire set of encoder hidden state vectors directly as the context for the decoder.

The idea of attention is instead to create the single fixed-length vector $c$ by taking a weighted sum of all the encoder hidden states. The weights focus on (‘attend to’) a particular part of the source text that is relevant for the token the decoder is currently producing. Attention thus replaces the static context vector with one that is dynamically derived from the encoder hidden states, different for each token in decoding.

This context vector, $c_i$, is generated anew with each decoding step $i$ and takes all of the encoder hidden states into account in its derivation. We then make this context available during decoding by conditioning the computation of the current decoder hidden state on it (along with the prior hidden state and the previous output generated by the decoder), as we see in this equation (and Fig. 9.21):

$$ h_d^i = g(\hat{y}_{i-1}, h_{i-1}^d, c_i) $$ (9.35)
The attention mechanism allows each hidden state of the decoder to see a different, dynamic, context, which is a function of all the encoder hidden states.

The first step in computing $c_i$ is to compute how much to focus on each encoder state, how relevant each encoder state is to the decoder state captured in $h_{d-1}^i$. We capture relevance by computing—at each state $i$ during decoding—a score($h_{d-1}^i, h_j^i$) for each encoder state $j$.

The simplest such score, called **dot-product attention**, implements relevance as similarity: measuring how similar the decoder hidden state is to an encoder hidden state, by computing the dot product between them:

$$\text{score}(h_{d-1}^i, h_j^i) = h_{d-1}^i \cdot h_j^i \quad (9.36)$$

The score that results from this dot product is a scalar that reflects the degree of similarity between the two vectors. The vector of these scores across all the encoder hidden states gives us the relevance of each encoder state to the current step of the decoder.

To make use of these scores, we’ll normalize them with a softmax to create a vector of weights, $\alpha_{ij}$, that tells us the proportional relevance of each encoder hidden state $j$ to the prior hidden decoder state, $h_{d-1}^i$.

$$\alpha_{ij} = \text{softmax}(\text{score}(h_{d-1}^i, h_j^i)) = \frac{\exp(\text{score}(h_{d-1}^i, h_j^i))}{\sum_k \exp(\text{score}(h_{d-1}^i, h_k^i))} \quad (9.37)$$

Finally, given the distribution in $\alpha$, we can compute a fixed-length context vector for the current decoder state by taking a weighted average over all the encoder hidden states.

$$c_i = \sum_j \alpha_{ij} h_j^i \quad (9.38)$$

With this, we finally have a fixed-length context vector that takes into account information from the entire encoder state that is dynamically updated to reflect the needs of the decoder at each step of decoding. Fig. 9.22 illustrates an encoder-decoder network with attention, focusing on the computation of one context vector $c_i$.

It’s also possible to create more sophisticated scoring functions for attention models. Instead of simple dot product attention, we can get a more powerful function that computes the relevance of each encoder hidden state to the decoder hidden state by parameterizing the score with its own set of weights, $W_s$.

$$\text{score}(h_{d-1}^i, h_j^i) = h_{d-1}^i W_s h_j^i$$

The weights $W_s$, which are then trained during normal end-to-end training, give the network the ability to learn which aspects of similarity between the decoder and
encoder states are important to the current application. This bilinear model also allows the encoder and decoder to use different dimensional vectors, whereas the simple dot-product attention requires that the encoder and decoder hidden states have the same dimensionality.

We’ll return to the concept of attention when we defined the transformer architecture in Chapter 10, which is based on a slight modification of attention called self-attention.

9.9 Summary

This chapter has introduced the concepts of recurrent neural networks and how they can be applied to language problems. Here’s a summary of the main points that we covered:

- In simple Recurrent Neural Networks sequences are processed one element at a time, with the output of each neural unit at time \( t \) based both on the current input at \( t \) and the hidden layer from time \( t - 1 \).
- RNNs can be trained with a straightforward extension of the backpropagation algorithm, known as backpropagation through time (BPTT).
- Simple recurrent networks fail on long inputs because of problems like vanishing gradients; instead modern systems use more complex gated architectures such as LSTMs that explicitly decide what to remember and forget in their hidden and context layers.
- Common language-based applications for RNNs include:
  - Probabilistic language modeling: assigning a probability to a sequence, or to the next element of a sequence given the preceding words.
  - Auto-regressive generation using a trained language model.
  - Sequence labeling like part-of-speech tagging, where each element of a sequence is assigned a label.
– Sequence classification, where an entire text is assigned to a category, as in spam detection, sentiment analysis or topic classification.
– Encoder-decoder architectures, where an input is mapped to an output of different length and alignment.

Bibliographical and Historical Notes

Influential investigations of RNNs were conducted in the context of the Parallel Distributed Processing (PDP) group at UC San Diego in the 1980’s. Much of this work was directed at human cognitive modeling rather than practical NLP applications (Rumelhart and McClelland 1986c, McClelland and Rumelhart 1986). Models using recurrence at the hidden layer in a feedforward network (Elman networks) were introduced by Elman (1990). Similar architectures were investigated by Jordan (1986) with a recurrence from the output layer, and Mathis and Mozer (1995) with the addition of a recurrent context layer prior to the hidden layer. The possibility of unrolling a recurrent network into an equivalent feedforward network is discussed in (Rumelhart and McClelland, 1986c).

In parallel with work in cognitive modeling, RNNs were investigated extensively in the continuous domain in the signal processing and speech communities (Giles et al. 1994, Robinson et al. 1996). Schuster and Paliwal (1997) introduced bidirectional RNNs and described results on the TIMIT phoneme transcription task.

While theoretically interesting, the difficulty with training RNNs and managing context over long sequences impeded progress on practical applications. This situation changed with the introduction of LSTMs in Hochreiter and Schmidhuber (1997) and Gers et al. (2000). Impressive performance gains were demonstrated on tasks at the boundary of signal processing and language processing including phoneme recognition (Graves and Schmidhuber, 2005), handwriting recognition (Graves et al., 2007) and most significantly speech recognition (Graves et al., 2013).

Interest in applying neural networks to practical NLP problems surged with the work of Collobert and Weston (2008) and Collobert et al. (2011). These efforts made use of learned word embeddings, convolutional networks, and end-to-end training. They demonstrated near state-of-the-art performance on a number of standard shared tasks including part-of-speech tagging, chunking, named entity recognition and semantic role labeling without the use of hand-engineered features.

Approaches that married LSTMs with pretrained collections of word-embeddings based on word2vec (Mikolov et al., 2013a) and GloVe (Pennington et al., 2014) quickly came to dominate many common tasks: part-of-speech tagging (Ling et al., 2015), syntactic chunking (Søgaard and Goldberg, 2016), named entity recognition (Chiu and Nichols, 2016; Ma and Hovy, 2016), opinion mining (Irsoy and Cardie, 2014), semantic role labeling (Zhou and Xu, 2015a) and AMR parsing (Foland and Martin, 2016). As with the earlier surge of progress involving statistical machine learning, these advances were made possible by the availability of training data provided by CONLL, SemEval, and other shared tasks, as well as shared resources such as Ontonotes (Pradhan et al., 2007b), and PropBank (Palmer et al., 2005).

The modern neural encoder-decoder approach was pioneered by Kalchbrenner and Blunsom (2013), who used a CNN encoder and an RNN decoder. Cho et al. (2014) (who coined the name “encoder-decoder”) and Sutskever et al. (2014) then showed how to use extended RNNs for both encoder and decoder. The idea that a
generative decoder should take as input a soft weighting of the inputs, the central idea of attention, was first developed by Graves (2013) in the context of handwriting recognition. Bahdanau et al. (2015) extended the idea, named it “attention” and applied it to MT.
Fluent speakers of a language bring an enormous amount of knowledge to bear during comprehension and production. This knowledge is embodied in many forms, perhaps most obviously in the vocabulary, the rich representations we have of words and their meanings and usage. This makes the vocabulary a useful lens to explore the acquisition of knowledge from text, by both people and machines.

Estimates of the size of adult vocabularies vary widely both within and across languages. For example, estimates of the vocabulary size of young adult speakers of American English range from 30,000 to 100,000 depending on the resources used to make the estimate and the definition of what it means to know a word. What is agreed upon is that the vast majority of words that mature speakers use in their day-to-day interactions are acquired early in life through spoken interactions with caregivers and peers, usually well before the start of formal schooling. This active vocabulary is extremely limited compared to the size of the adult vocabulary (usually on the order of 2000 words for young speakers) and is quite stable, with very few additional words learned via casual conversation beyond this early stage. Obviously, this leaves a very large number of words to be acquired by other means.

A simple consequence of these facts is that children have to learn about 7 to 10 words a day, every single day, to arrive at observed vocabulary levels by the time they are 20 years of age. And indeed empirical estimates of vocabulary growth in late elementary through high school are consistent with this rate. How do children achieve this rate of vocabulary growth? Most of this growth is not happening through direct vocabulary instruction in school, which is not deployed at the rate that would be required to result in sufficient vocabulary growth.

The most likely explanation is that the bulk of this knowledge acquisition happens as a by-product of reading, as part of the rich processing and reasoning that we perform when we read. Research into the average amount of time children spend reading, and the lexical diversity of the texts they read, indicate that it is possible to achieve the desired rate. But the mechanism behind this rate of learning must be remarkable indeed, since at some points during learning the rate of vocabulary growth exceeds the rate at which new words are appearing to the learner!

Many of these facts have motivated approaches to word learning based on the *distributional hypothesis*, introduced in Chapter 6. This is the idea that something about what we’re loosely calling word meanings can be learned even without any grounding in the real world, solely based on the content of the texts we encounter over our lives. This knowledge is based on the complex association of words with the words they co-occur with (and with the words that those words occur with).

The crucial insight of the distributional hypothesis is that the knowledge that we acquire through this process can be brought to bear long after its initial acquisition.
Of course, adding grounding from vision or from real-world interaction can help build even more powerful models, but even text alone is remarkably useful.

In this chapter we formalize this idea of pretraining—learning knowledge about language and the world from vast amounts of text—and call the resulting pretrained language models large language models. Large language models exhibit remarkable performance on all sorts of natural language tasks because of the knowledge they learn in pretraining, and they will play a role throughout the rest of this book. They have been especially transformative for tasks where we need to produce text, like summarization, machine translation, question answering, or chatbots.

The standard architecture for building large language models is the transformer. We thus begin this chapter by introducing this architecture in detail. The transformer makes use of a novel mechanism called self-attention, which developed out of the idea of attention that was introduced for RNNs in Chapter 9. Self-attention can be thought of a way to build contextual representations of a word’s meaning that integrate information from surrounding words, helping the model learn how words relate to each other over large spans of text.

We’ll then see how to apply the transformer to language modeling, in a setting often called causal or autoregressive language models, in which we iteratively predict words left-to-right from earlier words. These language models, like the feedforward and RNN language models we have already seen, are thus self-trained: given a large corpus of text, we iteratively teach the model to guess the next word in the text from the prior words. In addition to training, we’ll introduce algorithms for generating texts, including important methods like greedy decoding, beam search, and sampling. And we’ll talk about the components of popular large language models like the GPT family.

Finally, we’ll see the great power of language models: almost any NLP task can be modeled as word prediction, if we think about it in the right way. We’ll work through an example of using large language models to solve one NLP task of summarization (generating a short text that summarizes some larger document). The use of a large language model to generate text is one of the areas in which the impact of the last decade of neural algorithms for NLP has been the largest. Indeed, text generation, along with image generation and code generation, constitute a new area of AI that is often called generative AI.

We’ll save three more areas of large language models for the next three chapters; Chapter 11 will introduce the bidirectional transformer encoder and the method of masked language modeling, used for the popular BERT family of models. Chapter 12 will introduce the most powerful way to interact with large language models: prompting them to perform other NLP tasks by simply giving directions or instructions in natural language to a transformer that is pretrained on language modeling. And Chapter 13 will introduce the use of the encoder-decoder architecture for transformers in the context of machine translation.

10.1 The Transformer: A Self-Attention Network

In this section we introduce the architecture of the transformer, the algorithm that underlies most modern NLP systems. When used for causal language modeling, the input to a transformer is a sequence of words, and the output is a prediction for what word comes next, as well as a sequence of contextual embedding that represents the contextual meaning of each of the input words. Like the LSTMs of Chapter 9,
Transformers are a neural architecture that can handle distant information. But unlike LSTMs, transformers are not based on recurrent connections (which can be hard to parallelize), which means that transformers can be more efficient to implement at scale.

Transformers are made up of stacks of transformer **blocks**, each of which is a multilayer network that maps sequences of input vectors \((x_1, \ldots, x_n)\) to sequences of output vectors \((z_1, \ldots, z_n)\) of the same length. These blocks are made by combining simple linear layers, feedforward networks, and **self-attention** layers, the key innovation of transformers. Self-attention allows a network to directly extract and use information from arbitrarily large contexts. We'll start by describing how self-attention works and then return to how it fits into larger transformer blocks. Finally, we'll describe how to use the transformer block together with some input and output mechanisms as a language model, to predict upcoming words from prior words in the context.

### 10.1.1 Transformers: the intuition

The intuition of a transformer is that across a series of layers, we build up richer and richer contextualized representations of the meanings of input words or tokens (we will refer to the input as a sequence of words for convenience, although technically the input is first tokenized by an algorithm like BPE, so it is a series of tokens rather than words). At each layer of a transformer, to compute the representation of a word \(i\) we combine information from the representation of \(i\) at the previous layer with information from the representations of the neighboring words. The goal is to produce a contextualized representation for each word at each position. We can think of these representations as a contextualized version of the static vectors we saw in Chapter 6, which each represented the meaning of a word type. By contrast, our goal in transformers is to produce a contextualized version, something that represents what this word means in the particular context in which it occurs.

We thus need a mechanism that tells us how to weigh and combine the representations of the different words from the context at the prior level in order to compute our representation at this layer. This mechanism must be able to look broadly in the context, since words have rich linguistic relationships with words that can be many sentences away. Even within the sentence, words have important linguistic relationships with contextual words. Consider these examples, each exhibiting linguistic relationships that we’ll discuss in more depth in later chapters:

1. **(10.1)** The **keys** to the cabinet **are** on the table.
2. **(10.2)** The **chicken** crossed the road because **it** wanted to get to the other side.
3. **(10.3)** I walked along the **pond**, and noticed that one of the trees along the **bank** had fallen into the **water** after the storm.

In (10.1), the phrase *The keys* is the subject of the sentence, and in English and many languages, must agree in grammatical number with the verb *are*; in this case both are plural. In English we can’t use a singular verb like *is* with a plural subject like *keys*; we’ll discuss agreement more in Chapter 17. In (10.2), the pronoun *it* corefers to the chicken; it’s the chicken that wants to get to the other side. We’ll discuss coreference more in Chapter 26. In (10.3), the way we know that *bank* refers to the side of a pond or river and not a financial institution is from the context, including words like *pond* and *water*. We’ll discuss word senses more in Chapter 23. These helpful contextual words can be quite far way in the sentence or paragraph,
so we need a mechanism that can look broadly in the context to help compute representations for words.

Self-attention is just such a mechanism: it allows us to look broadly in the context and tells us how to integrate the representation from words in that context from layer \( k - 1 \) to build the representation for words in layer \( k \).

![Figure 10.1](image)

Fig. 10.1 shows a schematic example simplified from a real transformer (Uszkoreit, 2017). Here we want to compute a contextual representation for the word *it* at layer 6. In computing the representation for *it*, we attend differently to the various words at layer 5, with darker shades indicating higher self-attention values. Note that the transformer is attending highly to *animal*, a sensible result, since in this example *it* corefers with the animal, and so we’d like the representation for *it* to draw on the representation for *animal*. Figure simplified from (Uszkoreit, 2017).

10.1.2 Causal or backward-looking self-attention

The concept of context can be used in two ways in self-attention. In causal, or backward looking self-attention, the context is any of the prior words. In general bidirectional self-attention, the context can include future words. In this chapter we focus on causal, backward looking self-attention; we’ll introduce bidirectional self-attention in Chapter 11.

Fig. 10.2 thus illustrates the flow of information in a single causal, or backward looking, self-attention layer. As with the overall transformer, a self-attention layer maps input sequences \((x_1, \ldots, x_n)\) to output sequences of the same length \((a_1, \ldots, a_n)\). When processing each item in the input, the model has access to all of the inputs up to and including the one under consideration, but no access to information about inputs beyond the current one. In addition, the computation performed for each item is independent of all the other computations. The first point ensures that we can use this approach to create language models and use them for autoregressive generation, and the second point means that we can easily parallelize both forward inference and training of such models.
10.1.3 Self-attention more formally

We’ve given the intuition of self-attention (as a way to compute representations of a word at a given layer by integrating information from words at the previous layer) and we’ve defined context as all the prior words in the input. Let’s now introduce the self-attention computation itself.

The core intuition of attention is the idea of comparing an item of interest to a collection of other items in a way that reveals their relevance in the current context. In the case of self-attention for language, the set of comparisons are to other words (or tokens) within a given sequence. The result of these comparisons is then used to compute an output sequence for the current input sequence. For example, returning to Fig. 10.2, the computation of $a_3$ is based on a set of comparisons between the input $x_3$ and its preceding elements $x_1$ and $x_2$, and to $x_3$ itself.

How shall we compare words to other words? Since our representations for words are vectors, we’ll make use of our old friend the dot product that we used for computing word similarity in Chapter 6, and also played a role in attention in Chapter 9. Let’s refer to the result of this comparison between words $i$ and $j$ as a score (we’ll be updating this equation to add attention to the computation of this score):

$$
Verson 1: \, \text{score}(x_i, x_j) = x_i \cdot x_j \quad (10.4)
$$

The result of a dot product is a scalar value ranging from $-\infty$ to $\infty$, the larger the value the more similar the vectors that are being compared. Continuing with our example, the first step in computing $y_3$ would be to compute three scores: $x_3 \cdot x_1$, $x_3 \cdot x_2$ and $x_3 \cdot x_3$. Then to make effective use of these scores, we’ll normalize them with a softmax to create a vector of weights, $\alpha_{ij}$, that indicates the proportional relevance of each input to the input element $i$ that is the current focus of attention.

$$
\alpha_{ij} = \text{softmax}(\text{score}(x_i, x_j)) \ \forall j \leq i \quad (10.5)
$$

$$
= \frac{\exp(\text{score}(x_i, x_j))}{\sum_{k=1}^{i} \exp(\text{score}(x_i, x_k))} \ \forall j \leq i \quad (10.6)
$$

Of course, the softmax weight will likely be highest for the current focus element $i$, since vec$x_i$ is very similar to itself, resulting in a high dot product. But other context words may also be similar to $i$, and the softmax will also assign some weight to those words.

Given the proportional scores in $\alpha$, we generate an output value $a_i$ by summing
the inputs seen so far, each weighted by its $\alpha$ value.

$$a_i = \sum_{j \leq i} \alpha_{ij} x_j \quad (10.7)$$

The steps embodied in Equations 10.4 through 10.7 represent the core of an attention-based approach: a set of comparisons to relevant items in some context, a normalization of those scores to provide a probability distribution, followed by a weighted sum using this distribution. The output $a$ is the result of this straightforward computation over the inputs.

This kind of simple attention can be useful, and indeed we saw in Chapter 9 how to use this simple idea of attention for LSTM-based encoder-decoder models for machine translation. But transformers allow us to create a more sophisticated way of representing how words can contribute to the representation of longer inputs.

Consider the three different roles that each input embedding plays during the course of the attention process.

- As the current focus of attention when being compared to all of the other preceding inputs. We’ll refer to this role as a query.
- In its role as a preceding input being compared to the current focus of attention. We’ll refer to this role as a key.
- And finally, as a value used to compute the output for the current focus of attention.

To capture these three different roles, transformers introduce weight matrices $W^Q$, $W^K$, and $W^V$. These weights will be used to project each input vector $x_i$ into a representation of its role as a key, query, or value.

$$q_i = x_i W^Q; \quad k_i = x_i W^K; \quad v_i = x_i W^V \quad (10.8)$$

The ensuing softmax calculation resulting in $\alpha_{i,j}$ remains the same, but the output calculation for $a_i$ is now based on a weighted sum over the value vectors $v$.

$$a_i = \sum_{j \leq i} \alpha_{ij} v_j \quad (10.10)$$

Again, the softmax weight $\alpha_{i,j}$ will likely be highest for the current focus element $i$, and so the value for $y_i$ will be most influenced by $v_i$. But the model will also pay attention to other contextual words if they are similar to $i$, allowing their values to
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6. Sum the weighted value vectors
4. Turn into weights via softmax
3. Divide score by $d_k$
2. Compare $x_3$'s query with the keys for $x_1$, $x_2$, and $x_3$
1. Generate key, query, value vectors

Output of self-attention

5. Weigh each value vector

Figure 10.3 Calculating the value of $a_3$, the third element of a sequence using causal (left-to-right) self-attention.

Also influence the final value of $v_j$. Context words that are not similar to $i$ will have their values downweighted and won’t contribute to the final value.

There is one final part of the self-attention model. The result of a dot product can be an arbitrarily large (positive or negative) value. Exponentiating large values can lead to numerical issues and to an effective loss of gradients during training. To avoid this, we scale down the result of the dot product, by dividing it by a factor related to the size of the embeddings. A typical approach is to divide by the square root of the dimensionality of the query and key vectors ($d_k$), leading us to update our scoring function one more time, replacing Eq. 10.4 and Eq. 10.9 with Eq. 10.12.

Here’s a final set of equations for computing self-attention for a single self-attention output vector $a_i$ from a single input vector $x_i$, illustrated in Fig. 10.3 for the case of calculating the value of the third output $a_3$ in a sequence.

\[
q_i = x_i W^Q, \quad k_i = x_i W^K, \quad v_i = x_i W^V \quad (10.11)
\]

**Final version:**

\[
\text{score}(x_i, x_j) = \frac{q_i \cdot k_j}{\sqrt{d_k}} \quad (10.12)
\]

\[
\alpha_{i,j} = \text{softmax}(\text{score}(x_i, x_j)) \quad \forall j \leq i \quad (10.13)
\]

\[
a_i = \sum_{j \leq i} \alpha_{i,j} v_j \quad (10.14)
\]

10.1.4 Parallelizing self-attention using a single matrix $X$

This description of the self-attention process has been from the perspective of computing a single output at a single time step $i$. However, since each output, $y_i$, is computed independently, this entire process can be parallelized, taking advantage of
efficient matrix multiplication routines by packing the input embeddings of the $N$ tokens of the input sequence into a single matrix $X \in \mathbb{R}^{N \times d}$. That is, each row of $X$ is the embedding of one token of the input. Transformers for large language models can have an input length $N = 1024$, $2048$, or $4096$ tokens, so $X$ has between $1K$ and $4K$ rows, each of the dimensionality of the embedding $d$.

We then multiply $X$ by the key, query, and value matrices (all of dimensionality $d \times d$) to produce matrices $Q \in \mathbb{R}^{N \times d}$, $K \in \mathbb{R}^{N \times d}$, and $V \in \mathbb{R}^{N \times d}$, containing all the key, query, and value vectors:

$$Q = XW_Q; \quad K = XW_K; \quad V = XW_V$$  \hspace{1cm} (10.15)

Given these matrices we can compute all the requisite query-key comparisons simultaneously by multiplying $Q$ and $K^\top$ in a single matrix multiplication (the product is of shape $N \times N$; Fig. 10.4 shows a visualization). Taking this one step further, we can scale these scores, take the softmax, and then multiply the result by $V$ resulting in a matrix of shape $N \times d$: a vector embedding representation for each token in the input. We’ve reduced the entire self-attention step for an entire sequence of $N$ tokens to the following computation:

$$A = \text{SelfAttention}(Q, K, V) = \text{softmax} \left( \frac{QK^\top}{\sqrt{d_k}} \right) V$$  \hspace{1cm} (10.16)

**10.1.5 Masking out the future**

The self-attention computation as we’ve described it has a problem: the calculation in $QK^\top$ results in a score for each query value to every key value, including those that follow the query. This is inappropriate in the setting of language modeling: guessing the next word is pretty simple if you already know it! To fix this, the elements in the upper-triangular portion of the matrix are zeroed out (set to $-\infty$), thus eliminating any knowledge of words that follow in the sequence. Fig. 10.4 shows this masked $QK^\top$ matrix. (we’ll see in Chapter 11 how to make use of words in the future for tasks that need it).

![Figure 10.4](image_url) 

*Figure 10.4* The $N \times N$ $QK^\top$ matrix showing the $q_i \cdot k_j$ values, with the upper-triangle portion of the comparisons matrix zeroed out (set to $-\infty$, which the softmax will turn to zero).

Fig. 10.4 also makes it clear that attention is quadratic in the length of the input, since at each layer we need to compute dot products between each pair of tokens in the input. This makes it expensive for the input to a transformer to consist of very long documents (like entire novels). Nonetheless modern large language models manage to use quite long contexts of up to 4096 tokens.
10.2 Multihead Attention

Transformers actually compute a more complex kind of attention than the single self-attention calculation we’ve seen so far. This is because the different words in a sentence can relate to each other in many different ways simultaneously. For example, distinct syntactic, semantic, and discourse relationships can hold between verbs and their arguments in a sentence. It would be difficult for a single self-attention model to learn to capture all of the different kinds of parallel relations among its inputs. Transformers address this issue with multihead self-attention layers. These are sets of self-attention layers, called heads, that reside in parallel layers at the same depth in a model, each with its own set of parameters. By using these distinct sets of parameters, each head can learn different aspects of the relationships among inputs at the same level of abstraction.

To implement this notion, each head, $i$, in a self-attention layer is provided with its own set of key, query and value matrices: $W^K_i$, $W^Q_i$ and $W^V_i$. These are used to project the inputs into separate key, value, and query embeddings separately for each head, with the rest of the self-attention computation remaining unchanged.

In multi-head attention, as with self-attention, the model dimension $d$ is still used for the input and output, the key and query embeddings have dimensionality $d_k$, and the value embeddings are of dimensionality $d_v$ (again, in the original transformer paper $d_k = d_v = 64$, $h = 8$, and $d = 512$). Thus for each head $i$, we have weight layers $W^Q_i \in \mathbb{R}^{d \times d_k}$, $W^K_i \in \mathbb{R}^{d \times d_k}$, and $W^V_i \in \mathbb{R}^{d \times d_v}$, and these get multiplied by the inputs packed into $X$ to produce $Q \in \mathbb{R}^{N \times d_k}$, $K \in \mathbb{R}^{N \times d_k}$, and $V \in \mathbb{R}^{N \times d_v}$. The output of each of the $h$ heads is of shape $N \times d_v$, and so the output of the multi-head layer with $h$ heads consists of $h$ matrices of shape $N \times d_v$. To make use of these matrices in further processing, they are concatenated to produce a single output with dimensionality $N \times hd_v$. Finally, we use yet another linear projection $W^O \in \mathbb{R}^{hd_v \times d}$, that reshape it to the original output dimension for each token. Multiplying the concatenated $N \times hd_v$ matrix output by $W^O \in \mathbb{R}^{hd_v \times d}$ yields the self-attention output $A$ of shape $[N \times d]$, suitable to be passed through residual connections and layer norm.

$$Q = XW^Q_i; K = XW^K_i; V = XW^V_i$$ (10.17)

$$\text{head}_i = \text{SelfAttention}(Q, K, V)$$ (10.18)

$$A = \text{MultiHeadAttention}(X) = (\text{head}_1 \oplus \text{head}_2 \ldots \oplus \text{head}_h)W^O$$ (10.19)

Fig. 10.5 illustrates this approach with 4 self-attention heads. In general in transformers, the multihead layer is used instead of a self-attention layer.

10.3 Transformer Blocks

The self-attention calculation lies at the core of what’s called a transformer block, which, in addition to the self-attention layer, includes three other kinds of layers: (1) a feedforward layer, (2) residual connections, and (3) normalizing layers (colloquially called “layer norm”).

Fig. 10.6 illustrates a standard transformer block consisting of a single attention layer followed by a position-wise feedforward layer with residual connections and layer normalizations following each.
Multihead Attention Layer with $h=4$ heads

**Figure 10.5** Multihead self-attention: Each of the multihead self-attention layers is provided with its own set of key, query and value weight matrices. The outputs from each of the layers are concatenated and then projected to $d$, thus producing an output of the same size as the input so the attention can be followed by layer norm and feedforward and layers can be stacked.

Feedforward layer The feedforward layer contains $N$ position-wise networks, one at each position. Each is a fully-connected 2-layer network, i.e., one hidden layer, two weight matrices, as introduced in Chapter 7. The weights are the same for each position, but the parameters are different from layer to layer. Unlike attention, the feedforward networks are independent for each position and so can be computed in parallel. It is common to make the dimensionality $d_{ff}$ of the hidden layer of the feedforward network be larger than the model dimensionality $d$. (For example in the original transformer model, $d = 512$ and $d_{ff} = 2048$.)

Residual connections Residual connections are connections that pass information from a lower layer to a higher layer without going through the intermediate
layer. Allowing information from the activation going forward and the gradient going backwards to skip a layer improves learning and gives higher level layers direct access to information from lower layers (He et al., 2016). Residual connections in transformers are implemented simply by adding a layer’s input vector to its output vector before passing it forward. In the transformer block shown in Fig. 10.6, residual connections are used with both the attention and feedforward sublayers.

**Layer Norm** These summed vectors are then normalized using layer normalization (Ba et al., 2016). Layer normalization (usually called layer norm) is one of many forms of normalization that can be used to improve training performance in deep neural networks by keeping the values of a hidden layer in a range that facilitates gradient-based training. Layer norm is a variation of the standard score, or z-score, from statistics applied to a single vector in a hidden layer. The input to layer norm is a single vector, for a particular token position $i$, and the output is that vector normalized. Thus layer norm takes as input a single vector of dimensionality $d$ and produces as output a single vector of dimensionality $d$. The first step in layer normalization is to calculate the mean, $\mu$, and standard deviation, $\sigma$, over the elements of the vector to be normalized. Given a hidden layer with dimensionality $d_h$, these values are calculated as follows.

$$\mu = \frac{1}{d_h} \sum_{i=1}^{d_h} x_i$$  \hspace{1cm} (10.20)

$$\sigma = \sqrt{\frac{1}{d_h} \sum_{i=1}^{d_h} (x_i - \mu)^2}$$  \hspace{1cm} (10.21)

Given these values, the vector components are normalized by subtracting the mean from each and dividing by the standard deviation. The result of this computation is a new vector with zero mean and a standard deviation of one.

$$\hat{x} = \frac{x - \mu}{\sigma}$$  \hspace{1cm} (10.22)

Finally, in the standard implementation of layer normalization, two learnable parameters, $\gamma$ and $\beta$, representing gain and offset values, are introduced.

$$\text{LayerNorm} = \gamma \hat{x} + \beta$$  \hspace{1cm} (10.23)

**Putting it all together** The function computed by a transformer block can be expressed as:

$$O = \text{LayerNorm}(X + \text{SelfAttention}(X))$$  \hspace{1cm} (10.24)

$$H = \text{LayerNorm}(O + \text{FFN}(O))$$  \hspace{1cm} (10.25)

Or we can break it down with one equation for each component computation, using $T$ (of shape $[N \times d]$) to stand for transformer and superscripts to demarcate each computation inside the block:

$$T^1 = \text{SelfAttention}(X)$$  \hspace{1cm} (10.26)

$$T^2 = X + T^1$$  \hspace{1cm} (10.27)

$$T^3 = \text{LayerNorm}(T^2)$$  \hspace{1cm} (10.28)

$$T^4 = \text{FFN}(T^3)$$  \hspace{1cm} (10.29)

$$T^5 = T^4 + T^3$$  \hspace{1cm} (10.30)

$$H = \text{LayerNorm}(T^5)$$  \hspace{1cm} (10.31)
Crucially, the input and output dimensions of transformer blocks are matched so they can be stacked. Each token $x_i$ at the input to the block has dimensionality $d$, and so the input $X$ and output $H$ are both of shape $[N \times d]$.

Transformers for large language models stack many of these blocks, from 12 layers (used for the T5 or GPT-3-small language models) to 96 layers (used for GPT-3 large), to even more for more recent models. We’ll come back to this issue of stacking in a bit.

### 10.4 The Residual Stream view of the Transformer Block

The previous sections viewed the transformer block as applied to the entire $N$-token input $X$ of shape $[N \times d]$, producing an output also of shape $[N \times d]$.

While packing everything this way is a computationally efficient way to implement the transformer block, it’s not always the most perspicuous way to understand what the transformer is doing. It’s often clearer to instead visualize what is happening to an individual token vector $x_i$ in the input as it is processed through each transformer block. After all, most of the components of the transformer are designed to take a single vector of dimensionality $d$, corresponding to a single token, and produce an output vector also of dimensionality $d$. For example, the feedforward layer takes a single $d$-dimensional vector and produces a single $d$-dimensional vector. Over the $N$ tokens in a batch, we simply use the identical feedforward layer weights ($W_1, W_2, b_1$ and $b_2$) for each token $i$. Similarly, the layer norm function takes a single $d$-dimensional vector and produces a normalized $d$-dimensional version.

![Figure 10.7](image-url) The residual stream for token $x_i$, showing how the input to the transformer block $x_i$ is passed up through residual connections, the output of the feedforward and multi-head attention layers are added in, and processed by layer norm, to produce the output of this block, $h_i$, which is used as the input to the next layer transformer block. Note that of all the components, only the MultiHeadAttention component reads information from the other residual streams in the context.

We can therefore talk about the processing of an individual token through all
these layers as a stream of $d$-dimensional representations, called the **residual stream** and visualized in Fig. 10.7. The input at the bottom of the stream is an embedding for a token, which has dimensionality $d$. That initial embedding is passed up by the residual connections and the outputs of feedforward and attention layers get added into it. For each token $i$, at each block and layer we are passing up an embedding of shape $[1 \times d]$. The residual layers are constantly copying information up from earlier embeddings (hence the metaphor of ‘residual stream’), so we can think of the other components as adding new views of this representation back into this constant stream. Feedforward networks add in a different view of the earlier embedding.

Here are the equations for the transformer block, now viewed from this embedding stream perspective.

$$
\begin{align*}
    \mathbf{t}_1^1 &= \text{MultiHeadAttention}(\mathbf{x}_i, [\mathbf{x}_1, \cdots, \mathbf{x}_N]) \\
    \mathbf{t}_1^2 &= \mathbf{t}_1^1 + \mathbf{x}_i \\
    \mathbf{t}_1^3 &= \text{LayerNorm}(\mathbf{t}_1^2) \\
    \mathbf{t}_1^4 &= \text{FFN}(\mathbf{t}_1^3) \\
    \mathbf{t}_1^5 &= \mathbf{t}_1^4 + \mathbf{t}_1^3 \\
    \mathbf{h}_i &= \text{LayerNorm}(\mathbf{t}_1^5)
\end{align*}
$$

Notice that the only component that takes as input information from other tokens (other residual streams) is multi-head attention, which (as we see from (10.32)) looks at all the neighboring tokens in the context. The output from attention, however, is then added into this token’s embedding stream. In fact, Elhage et al. (2021) show that we can view attention heads as literally moving attention from the residual stream of a neighboring token into the current stream. The high-dimensional embedding space at each position thus contains information about the current token and about neighboring tokens, albeit in different subspaces of the vector space. Fig. 10.8 shows a visualization of this movement.

Equation (10.32) and following are just just the equation for a single transformer block, but the residual stream metaphor goes through all the transformer layers, from the first transformer blocks to the 12th, in a 12-layer transformer. At the earlier transformer blocks, the residual stream is representing the current token. At the highest transformer blocks, the residual stream is usual representing the following token, since at the very end it’s being trained to predict the next token.

**Pre-norm vs. post-norm architecture** There is an alternative form of the transformer architecture that is commonly used because it performs better in many cases. In this **prenorm transformer** architecture, the layer norm happens in a slightly dif-
different place: before the attention layer and before the feedforward layer, rather than afterwards. Fig. 10.9 shows this architecture, with the equations below:

\[
\begin{align*}
t_1^i &= \text{LayerNorm}(x_i) \quad (10.38) \\
t_2^i &= \text{MultiHeadAttention}(t_1^i, [t_1^1, \ldots, x_N]) \quad (10.39) \\
t_3^i &= t_2^i + x_i \quad (10.40) \\
t_4^i &= \text{LayerNorm}(t_3^i) \quad (10.41) \\
t_5^i &= \text{FFN}(t_4^i) \quad (10.42) \\
h_i &= t_5^i + t_3^i \quad (10.43)
\end{align*}
\]

Figure 10.9 The architecture of the prenorm transformer block. Here the nature of the residual stream, passing up information from the input, is even clearer.

The prenorm transformer has one extra requirement: at the very end of the last (highest) transformer block, there is a single extra layer norm that is run on the last \(h_i\) of each token stream (just below the language model head layer that we will define below).

10.5 The input: embeddings for token and position

Let’s talk about where the input \(X\) comes from. Given a sequence of \(N\) tokens (\(N\) is the context length in tokens), the matrix \(X\) of shape \([N \times d]\) has an embedding for each word in the context. The transformer does this by separately computing two embeddings: an input token embedding, and an input positional embedding.

A token embedding, introduced in Chapter 7 and Chapter 9, is a vector of dimension \(d\) that will be our initial representation for the input token. (As we pass vectors up through the transformer layers in the residual stream, this embedding representation will change and grow, incorporating context and playing a different
role depending on the kind of language model we are building.) The set of initial embeddings are stored in the embedding matrix \( E \), which has a row for each of the \(|V|\) tokens in the vocabulary. Thus each word is a row vector of \( d \) dimensions, and \( E \) has shape \([|V| \times d]\).

Given an input token string like *Thanks for all the* we first convert the tokens into vocabulary indices (these were created when we first tokenized the input using BPE or SentencePiece). So the representation of *thanks for all the* might be \( w = [5, 4000, 10532, 2224] \). Next we use indexing to select the corresponding rows from \( E \), (row 5, row 4000, row 10532, row 2224).

Another way to think about selecting token embeddings from the embedding matrix is to represent tokens as one-hot vectors of shape \([1 \times |V|]\), i.e., with one dimension for each word in the vocabulary. Recall that in a one-hot vector all the elements are 0 except one, the element whose dimension is the word’s index in the vocabulary, which has value 1. So if the word “thanks” has index 5 in the vocabulary, \( x_5 = 1 \), and \( x_i = 0 \ \forall i \neq 5 \), as shown here:

\[
\begin{bmatrix}
0 & 0 & 0 & 0 & 1 & 0 & 0 & \ldots & 0 & 0 & 0 & 0 \\
1 & 2 & 3 & 4 & 5 & 6 & 7 & \ldots & \ldots & |V|
\end{bmatrix}
\]

Multiplying by a one-hot vector that has only one non-zero element \( x_i = 1 \) simply selects out the relevant row vector for word \( i \), resulting in the embedding for word \( i \), as depicted in Fig. 10.10.

![Figure 10.10](image)

Figure 10.10  Selecting the embedding vector for word \( V_5 \) by multiplying the embedding matrix \( E \) with a one-hot vector with a 1 in index 5.

We can extend this idea to represent the entire token sequence as a matrix of one-hot vectors, one for each of the \( N \) positions in the transformer’s context window, as shown in Fig. 10.11.

![Figure 10.11](image)

Figure 10.11  Selecting the embedding matrix for the input sequence of token ids \( W \) by multiplying a one-hot matrix corresponding to \( W \) by the embedding matrix \( E \).

These token embeddings are not position-dependent. To represent the position of each token in the sequence, we combine these token embeddings with **positional embeddings** specific to each position in an input sequence.

Where do we get these positional embeddings? The simplest method, called **absolute position**, is to start with randomly initialized embeddings corresponding to each possible input position up to some maximum length. For example, just as we have an embedding for the word *fish*, we’ll have an embedding for the position 3.
As with word embeddings, these positional embeddings are learned along with other parameters during training. We can store them in a matrix $E_{\text{pos}}$ of shape $[1 \times N]$.

To produce an input embedding that captures positional information, we just add the word embedding for each input to its corresponding positional embedding. The individual token and position embeddings are both of size $[1 \times d]$, so their sum is also $[1 \times d]$. This new embedding serves as the input for further processing. Fig. 10.12 shows the idea.

![Positional Embeddings](image)

Figure 10.12 A simple way to model position: add an embedding of the absolute position to the token embedding to produce a new embedding of the same dimensionality.

The final representation of the input, the matrix $X$, is an $[N \times d]$ matrix in which each row $i$ is the representation of the $i$th token in the input, computed by adding $E[id(i)]$—the embedding of the id of the token that occurred at position $i$—, to $P[i]$, the positional embedding of position $i$.

A potential problem with the simple absolute position embedding approach is that there will be plenty of training examples for the initial positions in our inputs and correspondingly fewer at the outer length limits. These latter embeddings may be poorly trained and may not generalize well during testing. An alternative approach to absolute positional embeddings is to choose a static function that maps integer inputs to real-valued vectors in a way that captures the inherent relationships among the positions. That is, it captures the fact that position 4 in an input is more closely related to position 5 than it is to position 17. A combination of sine and cosine functions with differing frequencies was used in the original transformer work. Even more complex positional embedding methods exist, such as ones that represent relative position instead of absolute position, often implemented in the attention mechanism at each layer rather than being added once at the initial input.

### 10.6 The Language Modeling Head

The last component of the transformer we must introduce is the language modeling head. When we apply pretrained transformer models to various tasks, we use the term head to mean the additional neural circuitry we add on top of the basic transformer architecture to enable that task. The language modeling head is the circuitry we need to do language modeling.

Recall that language models, from the simple n-gram models of Chapter 3 through the feedforward and RNN language models of Chapter 7 and Chapter 9, are word predictors. Given a context of words, they assign a probability to each possible next
word. For example, if the preceding context is “Thanks for all the” and we want to know how likely the next word is “fish” we would compute:

$$P(\text{fish} | \text{Thanks for all the})$$

Language models give us the ability to assign such a conditional probability to every possible next word, giving us a distribution over the entire vocabulary. The n-gram language models of Chapter 3 compute the probability of a word given counts of its occurrence with the $n-1$ prior words. The context is thus of size $n-1$. For transformer language models, the context is the size of the transformer’s context window, which can be quite large: up to 2048 or even 4096 tokens for large models.

The job of the language modeling head is to take the output of the final transformer layer from the last token $\text{N}$ and use it to predict the upcoming word at position $\text{N} + 1$. Fig. 10.13 shows how to accomplish this task, taking the output of the last token at the last layer (the $d$-dimensional output embedding of shape $[1 \times d]$) and producing a probability distribution over words (from which we will choose one to generate).

![Figure 10.13](image)

**Figure 10.13** The language modeling head: the circuit at the top of a transformer that maps from the output embedding for token $\text{N}$ from the last transformer layer ($h^L_N$) to a probability distribution over words in the vocabulary $V$.

The first module in Fig. 10.13 is a linear layer, whose job is to project from the output $h^L_N$, which represents the output token embedding at position $\text{N}$ from the final block $L$, (hence of shape $[1 \times d]$) to the logit vector, or score vector, that will have a single score for each of the $|V|$ possible words in the vocabulary $V$. The logit vector $u$ is thus of dimensionality $1 \times |V|$.

This linear layer can be learned, but more commonly we tie this matrix to (the transpose of) the embedding matrix $E$. Recall that in **weight tying**, we use the same weights for two different matrices in the model. Thus at the input stage of the transformer the embedding matrix (of shape $[|V| \times d]$) is used to map from a one-hot vector over the vocabulary (of shape $[1 \times |V|]$) to an embedding (of shape $[1 \times d]$). And then in the language model head, $E^T$, the transpose of the embedding matrix (of shape $[d \times |V|]$) is used to map back from an embedding (shape $[1 \times d]$) to a vector over the vocabulary (shape $[1 \times |V|]$). In the learning process, $E$ will be optimized to be good at doing both of these mappings. We therefore sometimes call the transpose $E^T$ the **unembedding** layer because it is performing this reverse mapping.
A softmax layer turns the logits $u$ into the probabilities $y$ over the vocabulary.

$$u = h_N^T E$$  \hspace{1cm} (10.44)  
$$y = \text{softmax}(u)$$  \hspace{1cm} (10.45)

We can use these probabilities to do things like help assign a probability to a given text. But the most important usage to generate text, which we do by sampling a word from these probabilities $y$. We might sample the highest probability word (‘greedy’ decoding), or use another of the sampling methods we’ll introduce in Section 10.8. In either case, whatever entry $y_k$ we choose from the probability vector $y$, we generate the word that has that index $k$.

**Figure 10.14** A final transformer decoder-only model, stacking post-norm transformer blocks and mapping from a set of input tokens $w_1$ to $w_N$ to a predicted next word $w_{N+1}$.

Fig. 10.14 shows the total stacked architecture. Note that the input to the first transformer block is represented as $X$, which is the $N$ indexed word embeddings + position embeddings, $E[w] + P$, but the input to all the other layers is the output $H$ from the layer just below the current one).

Now that we see all these transformer layers spread out on the page, we can point out another useful feature of the unembedding layer: as a tool for interpretability of
the internals of the transformer that we call the logit lens (Nostalgebraist, 2020). We can take a vector from any layer of the transformer and, pretending that it is the prefinal embedding, simply multiply it by the unembedding layer to get logits, and compute a softmax to see the distribution over words that that vector might be representing. This can be a useful window into the internal representations of the model. Since the network wasn’t trained to make the internal representations function in this way, the logit lens doesn’t always work perfectly, but this can still be a useful trick.

Anyhow, the Fig. 10.14 thus sketches out the entire process of taking a series of words \( w_1 \ldots w_N \) and using the model to predict the next word \( w_{N+1} \).

A terminological note before we conclude: You will sometimes see a transformer used for this kind of unidirectional causal language model called a decoder-only model. This is because this model constitutes roughly half of the encoder-decoder model for transformers that we’ll see how to apply to machine translation in Chapter 13. (Confusingly, the original introduction of the transformer had an encoder-decoder architecture, and it was only later that the standard paradigm for causal language model was defined by using only the decoder part of this original architecture).

In the next sections we’ll introduce what kind of tasks large language models can be used for, discuss various generation methods for sampling possible next words, and show how to train a transformer-based large language model. In the following chapters we’ll expand on these ideas to introduce fine-tuning, prompting, and encoder-decoder architectures for transformer-based large language models.

10.7 Large Language Models with Transformers

We’ve now seen most of the components of a transformer for language modeling (what remains is sampling and training, which we’ll get to in the following sections). Before we do that, we use this section to talk about why and how we apply transformer-based large language models to NLP tasks.

All of these tasks are cases of conditional generation, the task of generating text conditioned on an input piece of text, a prompt. The fact that transformers have such long contexts (1024 or even 4096 tokens) makes them very powerful for conditional generation, because they can look back so far into the prompting text.

Consider the simple task of text completion, illustrated in Fig. 10.15. Here a language model is given a text prefix and is asked to generate a possible completion. Note that as the generation process proceeds, the model has direct access to the priming context as well as to all of its own subsequently generated outputs (at least as much as fits in the large context window). This ability to incorporate the entirety of the earlier context and generated outputs at each time step is the key to the power of large language models built from transformers.

So why should we care about predicting upcoming words? The insight of large language modeling is that many practical NLP tasks can be cast as word prediction, and that a powerful-enough language model can solve them with a high degree of accuracy. For example, we can cast sentiment analysis as language modeling by giving a language model a context like:

The sentiment of the sentence “I like Jackie Chan” is:

and comparing the following conditional probability of the words “positive” and the
word “negative” to see which is higher:

\[ P(\text{positive} | \text{The sentiment of the sentence “I like Jackie Chan” is:}) \]
\[ P(\text{negative} | \text{The sentiment of the sentence “I like Jackie Chan” is:}) \]

If the word “positive” is more probable, we say the sentiment of the sentence is positive, otherwise we say the sentiment is negative.

We can also cast more complex tasks as word prediction. Consider the task of answering simple questions, a task we return to in Chapter 14. In this task the system is given some question and must give a textual answer. We can cast the task of question answering as word prediction by giving a language model a question and a token like A: suggesting that an answer should come next:

Q: Who wrote the book “The Origin of Species”? A:

If we ask a language model to compute

\[ P(w | Q: \text{Who wrote the book “The Origin of Species”? A:}) \]

and look at which words \( w \) have high probabilities, we might expect to see that Charles is very likely, and then if we choose Charles and continue and ask

\[ P(w | Q: \text{Who wrote the book “The Origin of Species”? A: Charles}) \]

we might now see that Darwin is the most probable word, and select it.

Conditional generation can even be used to accomplish tasks that must generate longer responses. Consider the task of text summarization, which is to take a long text, such as a full-length article, and produce an effective shorter summary of it. We can cast summarization as language modeling by giving a large language model a text, and follow the text by a token like tl;dr; this token is short for something like ‘too long; don’t read’ and in recent years people often use this token, especially in informal work emails, when they are going to give a short summary. We can then do conditional generation: give the language model this prefix, and then ask...
it to generate the following words, one by one, and take the entire response as a summary. Fig. 10.16 shows an example of a text and a human-produced summary from a widely-used summarization corpus consisting of CNN and Daily Mirror news articles.

Original Article

The only thing crazier than a guy in snowbound Massachusetts boxing up the powdery white stuff and offering it for sale online? People are actually buying it. For $89, self-styled entrepreneur Kyle Waring will ship you 6 pounds of Boston-area snow in an insulated Styrofoam box – enough for 10 to 15 snowballs, he says. But not if you live in New England or surrounding states. “We will not ship snow to any states in the northeast!” says Waring’s website, ShipSnowYo.com. “We’re in the business of expunging snow!”

His website and social media accounts claim to have filled more than 133 orders for snow – more than 30 on Tuesday alone, his busiest day yet. With more than 45 total inches, Boston has set a record this winter for the snowiest month in its history. Most residents see the huge piles of snow choking their yards and sidewalks as a nuisance, but Waring saw an opportunity. According to Boston.com, it all started a few weeks ago, when Waring and his wife were shoveling deep snow from their yard in Manchester-by-the-Sea, a coastal suburb north of Boston. He joked about shipping the stuff to friends and family in warmer states, and an idea was born. His business slogan: “Our nightmare is your dream!” At first, ShipSnowYo sold snow packed into empty 16.9-ounce water bottles for $19.99, but the snow usually melted before it reached its destination...

Summary

Kyle Waring will ship you 6 pounds of Boston-area snow in an insulated Styrofoam box – enough for 10 to 15 snowballs, he says. But not if you live in New England or surrounding states.

If we take this full article and append the token `tl;dr`, we can use this as the context to prime the generation process to produce a summary as illustrated in Fig. 10.17. Again, what makes transformers able to succeed at this task (as compared, say, to the primitive n-gram language model) is that the ability of self-attention to incorporate information from the large context windows means that the model has access to the original article as well as to the newly generated text throughout the process.

Which words do we generate at each step? One simple way to generate words is to always generate the most likely word given the context. Generating the most likely word given the context is called greedy decoding. A greedy algorithm is one that make a choice that is locally optimal, whether or not it will turn out to have been the best choice with hindsight. Thus in greedy decoding, at each time step in generation, the output $y_t$ is chosen by computing the probability for each possible outputs (every word in the vocabulary) and then choosing the highest probability word (the argmax):

$$\hat{w}_t = \arg\max_{w \in V} P(w | w_{<t})$$

In practice, however, we don’t use greedy decoding with large language models. A major problem with greedy decoding is that because the words it chooses are (by definition) extremely predictable, the resulting text is generic and often quite repetitive. Indeed, greedy decoding is so predictable that it is deterministic; if the context
is identical, and the probabilistic model is the same, greedy decoding will always result in generating exactly the same string. We’ll see in Chapter 13 that an extension to greedy decoding called beam search works well in tasks like machine translation, which are very constrained in that we are always generating a text in one language conditioned on a very specific text in another language. In most other tasks, however, people prefer text which has been generated by more sophisticated methods, called sampling methods, that introduce a bit more diversity into the generations. We’ll see how to do that in the next few sections.

### 10.8 Large Language Models: Generation by Sampling

The core of the generation process for large language models is the task of choosing the single word to generate next based on the context and based on the probabilities that the model assigns to possible words. This task of choosing a word to generate based on the model’s probabilities is called decoding. Decoding from a language model in a left-to-right manner (or right-to-left for languages like Arabic in which we read from right to left), and thus repeatedly choosing the next word conditioned on our previous choices is called autoregressive generation or causal LM generation. As we’ll see, alternatives like the masked language models of Chapter 11 are non-causal because they can predict words based on both past and future words.

The most common method for decoding in large language models is sampling. Recall from Chapter 3 that sampling from a model’s distribution over words means to choose random words according to their probability assigned by the model. That is, we iteratively choose a word to generate according to its probability in context.

---

1 Technically an autoregressive model predicts a value at time $t$ based on a linear function of the values at times $t-1, t-2$, and so on. Although language models are not linear (since they have many layers of non-linearities), we loosely refer to this generation technique as autoregressive since the word generated at each time step is conditioned on the word selected by the network from the previous step.
as defined by the model. Thus we are more likely to generate words that the model
thinks have a high probability in the context and less likely to generate words that
the model thinks have a low probability.

We saw back in Chapter 3 on page 42 how to generate text from a unigram lan-
guage model, by repeatedly randomly sampling words according to their probability
until we either reach a pre-determined length or select the end-of-sentence token. To
generate text from a trained transformer language model we’ll just generalize this
model a bit: at each step we’ll sample words according to their probability condi-
tioned on our previous choices, and we’ll use a transformer language model as the
probability model that tells us this probability.

We can formalize this algorithm for generating a sequence of words $W = w_1, w_2, \ldots, w_N$
until we hit the end-of-sequence token, using $x \sim p(x)$ to mean ’choose $x$ by sam-
pling from the distribution $p(x)$:

\[
\begin{align*}
  i & \leftarrow 1 \\
  w_i & \sim p(w) \\
  \text{while } w_i & \neq \text{EOS} \\
  & i \leftarrow i + 1 \\
  w_i & \sim p(w_i | w_{<i})
\end{align*}
\]

The algorithm above is called random sampling, and it turns out random sam-
pling doesn’t work well enough. The problem is that even though random sampling
is mostly going to generate sensible, high-probable words, there are many odd, low-
probability words in the tail of the distribution, and even though each one is low-
probability, if you add up all the rare words, they constitute a large enough portion
of the distribution that they get chosen often enough to result in generating weird
sentences. For this reason, instead of random sampling, we usually use sampling
methods that avoid generating the very unlikely words.

The sampling methods we introduce below each have parameters that enable
trading off two important factors in generation: quality and diversity. Methods
that emphasize the most probable words tend to produce generations that are rated
by people as more accurate, more coherent, and more factual, but also more boring
and more repetitive. Methods that give a bit more weight to the middle-probability
words tend to be more creative and more diverse, but less factual and more likely to
be incoherent or otherwise low-quality.

### 10.8.1 Top-$k$ sampling

Top-$k$ sampling is a simple generalization of greedy decoding. Instead of choosing
the single most probable word to generate, we first truncate the distribution to the
top $k$ most likely words, renormalize to produce a legitimate probability distribution,
and then randomly sample from within these $k$ words according to their renormalized
probabilities. More formally:

1. Choose in advance a number of words $k$
2. For each word in the vocabulary $V$, use the language model to compute the
   likelihood of this word given the context $p(w_i | w_{<i})$
3. Sort the words by their likelihood, and throw away any word that is not one of
   the top $k$ most probable words.
4. Renormalize the scores of the $k$ words to be a legitimate probability distribu-
tion.
5. Randomly sample a word from within these remaining $k$ most-probable words according to its probability.

When $k = 1$, top-$k$ sampling is identical to greedy decoding. Setting $k$ to a larger number than 1 leads us to sometimes select a word which is not necessarily the most probable, but is still probable enough, and whose choice results in generating more diverse but still high-enough-quality text.

### 10.8.2 Nucleus or top-$p$ sampling

One problem with top-$k$ sampling is that $k$ is fixed, but the shape of the probability distribution over words differs in different contexts. If we set $k = 10$, sometimes the top 10 words will be very likely and include most of the probability mass, but other times the probability distribution will be flatter and the top 10 words will only include a small part of the probability mass.

An alternative, called top-$p$ sampling or nucleus sampling (Holtzman et al., 2020), is to keep not the top $k$ words, but the top $p$ percent of the probability mass. The goal is the same; to truncate the distribution to remove the very unlikely words. But by measuring probability rather than the number of words, the hope is that the measure will be more robust in very different contexts, dynamically increasing and decreasing the pool of word candidates.

Given a distribution $P(w_t|w_{<t})$, the top-$p$ vocabulary $V(p)$ is the smallest set of words such that

$$
\sum_{w \in V(p)} P(w_t|w_{<t}) \geq p. \tag{10.47}
$$

### 10.8.3 Temperature sampling

In temperature sampling, we don’t truncate the distribution, but instead reshape it. The intuition for temperature sampling comes from thermodynamics, where a system at a high temperature is very flexible and can explore many possible states, while a system at a lower temperature is likely to explore a subset of lower energy (better) states. In low-temperature sampling, we smoothly increase the probability of the most probable words and decrease the probability of the rare words.

We implement this intuition by simply dividing the logit by a temperature parameter $\tau$ before we normalize it by passing it through the softmax. In low-temperature sampling, $\tau \in (0, 1]$. Thus instead of computing the probability distribution over the vocabulary directly from the logit as in the following (repeated from (10.45):

$$
y = \text{softmax}(u) \tag{10.48}
$$

we instead first divide the logits by $\tau$, computing the probability vector $y$ as

$$
y = \text{softmax}(u/\tau) \tag{10.49}
$$

Why does this work? When $\tau$ is close to 1 the distribution doesn’t change much. But the lower $\tau$ is, the larger the scores being passed to the softmax (dividing by a smaller fraction $\tau \leq 1$ results in making each score larger). Recall that one of the useful properties of a softmax is that it tends to push high values toward 1 and low values toward 0. Thus when larger numbers are passed to a softmax the result is a distribution with increased probabilities of the most high-probability words and decreased probabilities of the low probability words, making the distribution more greedy. As $\tau$ approaches 0 the probability of the most likely word approaches 1.
10.9 Large Language Models: Training Transformers

How do we teach a transformer to be a language model? What is the algorithm and what data do we train on?

### 10.9.1 Self-supervised training algorithm

To train a transformer as a language model, we use the same self-supervision (or self-training) algorithm we saw in Section 9.2.2: we take a corpus of text as training material and at each time step \( t \) ask the model to predict the next word. We call such a model self-supervised because we don’t have to add any special gold labels to the data; the natural sequence of words is its own supervision! We simply train the model to minimize the error in predicting the true next word in the training sequence, using cross-entropy as the loss function.

Recall that the cross-entropy loss measures the difference between a predicted probability distribution and the correct distribution.

\[
L_{CE} = -\sum_{w \in V} y_t[w] \log \hat{y}_t[w]
\]  

(10.50)

In the case of language modeling, the correct distribution \( y_t \) comes from knowing the next word. This is represented as a one-hot vector corresponding to the vocabulary where the entry for the actual next word is 1, and all the other entries are 0. Thus, the cross-entropy loss for language modeling is determined by the probability the model assigns to the correct next word. So at time \( t \) the CE loss in (10.50) can be simplified as the negative log probability the model assigns to the next word in the training sequence.

\[
L_{CE}(\hat{y}_t, y_t) = -\log \hat{y}_t[w_{t+1}]
\]  

(10.51)

Thus at each word position \( t \) of the input, the model takes as input the correct sequence of tokens \( w_{1:t} \), and uses them to compute a probability distribution over possible next words so as to compute the model’s loss for the next token \( w_{t+1} \). Then we move to the next word, we ignore what the model predicted for the next word and instead use the correct sequence of tokens \( w_{1:t+1} \) to estimate the probability of token \( w_{t+2} \). This idea that we always give the model the correct history sequence to predict the next word (rather than feeding the model its best case from the previous time step) is called teacher forcing.

Fig. 10.18 illustrates the general training approach. At each step, given all the preceding words, the final transformer layer produces an output distribution over the entire vocabulary. During training, the probability assigned to the correct word is used to calculate the cross-entropy loss for each item in the sequence. As with RNNs, the loss for a training sequence is the average cross-entropy loss over the entire sequence. The weights in the network are adjusted to minimize the average CE loss over the training sequence via gradient descent.
Note the key difference between this figure and the earlier RNN-based version shown in Fig. 9.6. There the calculation of the outputs and the losses at each step was inherently serial given the recurrence in the calculation of the hidden states. With transformers, each training item can be processed in parallel since the output for each element in the sequence is computed separately.

Large models are generally trained by filling the full context window (for example 2048 or 4096 tokens for GPT3 or GPT4) with text. If documents are shorter than this, multiple documents are packed into the window with a special end-of-text token between them. The batch size for gradient descent is usually quite large (the largest GPT-3 model uses a batch size of 3.2 million tokens).

## 10.9.2 Training corpora for large language models

Large language models are mainly trained on text scraped from the web, augmented by more carefully curated data. Because these training corpora are so large, they are likely to contain many natural examples that can be helpful for NLP tasks, such as question and answer pairs (for example from FAQ lists), translations of sentences between various languages, documents together with their summaries, and so on.

Web text is usually taken from corpora of automatically-crawled web pages like the common crawl, a series of snapshots of the entire web produced by the non-profit Common Crawl (https://commoncrawl.org/) that each have billions of webpages. Various cleanups of common crawl data exist, such as the Colossal Clean Crawled Corpus (C4; Raffel et al. 2020), a corpus of 156 billion tokens of English that is filtered in various ways (deduplicated, removing non-natural language like code, sentences with offensive words from a blocklist). What is in this data? An analysis suggests that in large part it’s patent text documents, Wikipedia, and news sites (Dodge et al., 2021). Wikipedia plays a role in lots of language model training, as do corpora of books. The GPT3 models, for example, are trained mostly on the web (429 billion tokens), some text from books (67 billion tokens) and Wikipedia (3 billion tokens).
10.9.3 Scaling laws

The performance of large language models has shown to be mainly determined by 3 factors: model size (the number of parameters not counting embeddings), dataset size (the amount of training data), and the amount of computer used for training. That is, we can improve a model by adding parameters (adding more layers or having wider contexts or both), by training on more data, or by training for more iterations.

The relationships between these factors and performance are known as scaling laws. Roughly speaking, the performance of a large language model (the loss) scales as a power-law with each of these three properties of model training.

For example, Kaplan et al. (2020) found the following three relationships for loss $L$ as a function of the number of non-embedding parameters $N$, the dataset size $D$, and the compute budget $C$, for models training with limited parameters, dataset, or compute budget, if in each case the other two properties are held constant:

$$L(N) = \left( \frac{N_c}{N} \right)^{\alpha_N}$$

$$L(D) = \left( \frac{D_c}{D} \right)^{\alpha_D}$$

$$L(C) = \left( \frac{C_c}{C} \right)^{\alpha_C}$$

The number of (non-embedding) parameters $N$ can be roughly computed as follows (ignoring biases, and with $d$ as the input and output dimensionality of the model, $d_{\text{attn}}$ as the self-attention layer size, and $d_{\text{ff}}$ the size of the feedforward layer):

$$N \approx 2 \times n_{\text{layer}} \times (2 \times d_{\text{attn}} + d_{\text{ff}})$$

$$\approx 12 \times n_{\text{layer}} \times d^2$$

(assuming $d_{\text{attn}} = d_{\text{ff}}/4 = d$)

Thus GPT-3, with $n = 96$ layers and dimensionality $d = 12288$, has $12 \times 96 \times 12288^2 \approx 175$ billion parameters.

The values of $N_c$, $D_c$, $C_c$, $\alpha_N$, $\alpha_D$, and $\alpha_C$ depend on the exact transformer architecture, tokenization, and vocabulary size, so rather than all the precise values, scaling laws focus on the relationship with loss.²

Scaling laws can be useful in deciding how to train a model to a particular performance, for example by looking at early in the training curve, or performance with smaller amounts of data, to predict what the loss would be if we were to add more data or increase model size. Other aspects of scaling laws can also tell us how much data we need to add when scaling up a model.

10.10 Potential Harms from Language Models

Large pretrained neural language models exhibit many of the potential harms discussed in Chapter 4 and Chapter 6. Many of these harms become realized when pretrained language models are used for any downstream task, particularly those

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² For the initial experiment in Kaplan et al. (2020) the precise values were $\alpha_N = 0.076$, $N_c = 8.8 \times 10^{13}$ (parameters), $\alpha_D = 0.095$, $D_c = 5.4 \times 10^{13}$ (tokens), $\alpha_C = 0.050$, $C_c = 3.1 \times 10^8$ (petaflop-days).
involving text generation, whether question answering, machine translation, or in assistive technologies like writing aids or web search query completion, or predictive typing for email (Olteanu et al., 2020).

For example, language models are prone to saying things that are false, a problem called hallucination. Language models are trained to generate text that is predictable and coherent, but the training algorithms we have seen so far don’t have any way to enforce that the text that is generated is correct or true. This causes enormous problems for any application where the facts matter!

A second source of harm is that language models can generate toxic language. Gehman et al. (2020) show that even completely non-toxic prompts can lead large language models to output hate speech and abuse their users. Language models also generate stereotypes (Cheng et al., 2023) and negative attitudes (Brown et al., 2020; Sheng et al., 2019) about many demographic groups.

One source of biases is the training data. Gehman et al. (2020) shows that large language model training datasets include toxic text scraped from banned sites. There are other biases than toxicity: the training data is disproportionately generated by authors from the US and from developed countries. Such biased population samples likely skew the resulting generation toward the perspectives or topics of this group alone. Furthermore, language models can amplify demographic and other biases in training data, just as we saw for embedding models in Chapter 6.

Language models can also be used by malicious actors for generating text for misinformation, phishing, or other socially harmful activities (Brown et al., 2020). McGuffie and Newhouse (2020) show how large language models generate text that emulates online extremists, with the risk of amplifying extremist movements and their attempt to radicalize and recruit.

Language models also present privacy issues since they can leak information about their training data. It is thus possible for an adversary to extract training-data text from a language model such as an individual person’s name, phone number, and address (Henderson et al. 2017, Carlini et al. 2021). This is a problem if large language models are trained on private datasets such as electronic health records.

Related to privacy is the issue of copyright. Large language models are trained on text that is copyrighted. In some countries, like the United States, the fair use doctrine allows copyrighted content to be used to build language models, but possibly not if they are used to generate text that competes with the market for the text they are trained on.

Finding ways to mitigate all these harms is an important current research area in NLP. At the very least, carefully analyzing the data used to pretrain large language models is important as a way of understanding issues of toxicity, bias, privacy, and fair use, making it extremely important that language models include datasheets (page 16) or model cards (page 78) giving full replicable information on the corpora used to train them. Open-source models can specify their exact training data. Requirements that models are transparent in such ways is also in the process of being incorporated into the regulations of various national governments.

10.11 Summary

This chapter has introduced the transformer, and how it can be applied to build large language models. Here’s a summary of the main points that we covered:
• Transformers are non-recurrent networks based on **self-attention**. A self-attention layer maps input sequences to output sequences of the same length, using attention heads that model how the surrounding words are relevant for the processing of the current word.

• A transformer block consists of a single attention layer followed by a feed-forward layer with residual connections and layer normalizations following each. Transformer blocks can be stacked to make deeper and more powerful networks.

• Language models can be built out of stacks of transformer blocks, with a linear and softmax max layer at the top.

• Transformer-based language models have a wide context window (as wide as 4096 tokens for current models) allowing them to draw on enormous amounts of context to predict upcoming words.

• Many NLP tasks—such as question answering, summarization, sentiment, and machine translation—can be cast as tasks of word prediction and hence addressed with Large language models.

• The choice of which word to generate in large language models is generally done by using a **sampling** algorithm.

• Because of their ability to be used in so many ways, language models also have the potential to cause harms. Some harms include hallucinations, bias, stereotypes, misinformation and propaganda, and violations of privacy and copyright.

**Bibliographical and Historical Notes**

The transformer (Vaswani et al., 2017) was developed drawing on two lines of prior research: **self-attention** and **memory networks**. Encoder-decoder attention, the idea of using a soft weighting over the encodings of input words to inform a generative decoder (see Chapter 13) was developed by Graves (2013) in the context of handwriting generation, and Bahdanau et al. (2015) for MT. This idea was extended to self-attention by dropping the need for separate encoding and decoding sequences and instead seeing attention as a way of weighting the tokens in collecting information passed from lower layers to higher layers (Ling et al., 2015; Cheng et al., 2016; Liu et al., 2016). Other aspects of the transformer, including the terminology of key, query, and value, came from **memory networks**, a mechanism for adding an external read-write memory to networks, by using an embedding of a query to match keys representing content in an associative memory (Sukhbaatar et al., 2015; Weston et al., 2015; Graves et al., 2014).

MORE HISTORY TBD IN NEXT DRAFT.
Fine-Tuning and Masked Language Models

*Larvatus prodeo [Masked, I go forward]*
Descartes

In the previous chapter we saw how to pretrain transformer language models, and how these pretrained models can be used as a tool for many kinds of NLP tasks, by casting the tasks as word prediction. The models we introduced in Chapter 10 to do this task are causal or left-to-right transformer models.

In this chapter we’ll introduce a second paradigm for pretrained language models, called the bidirectional transformer encoder, trained via masked language modeling, a method that allows the model to see entire texts at a time, including both the right and left context. We’ll introduce the most widely-used version of the masked language modeling architecture, the BERT model (Devlin et al., 2019).

We’ll also introduce two important ideas that are often used with these masked language models. The first is the idea of fine-tuning. Fine-tuning is the process of taking the network learned by these pretrained models, and further training the model, often via an added neural net classifier that takes the top layer of the network as input, to perform some downstream task like named entity tagging or question answering or coreference. The intuition is that the pretraining phase learns a language model that instantiates rich representations of word meaning, that thus enables the model to more easily learn (‘be fine-tuned to’) the requirements of a downstream language understanding task. The pretrain-finetune paradigm is an instance of what is called transfer learning in machine learning: the method of acquiring knowledge from one task or domain, and then applying it (transferring it) to solve a new task.

The second idea that we introduce in this chapter is the idea of contextual embeddings: representations for words in context. The methods of Chapter 6 like word2vec or GloVe learned a single vector embedding for each unique word $w$ in the vocabulary. By contrast, with contextual embeddings, such as those learned by masked language models like BERT, each word $w$ will be represented by a different vector each time it appears in a different context. While the causal language models of Chapter 10 also use contextual embeddings, the embeddings created by masked language models seem to function particularly well as representations.

### 11.1 Bidirectional Transformer Encoders

Let’s begin by introducing the bidirectional transformer encoder that underlies models like BERT and its descendants like RoBERTa (Liu et al., 2019) or SpanBERT (Joshi et al., 2020). In Chapter 10 we explored causal (left-to-right) transformers that can serve as the basis for powerful language models—models that can easily be applied to autoregressive generation problems such as contextual generation, summarization and machine translation. However, when applied to sequence classification and labeling problems causal models have obvious shortcomings since they
are based on an incremental, left-to-right processing of their inputs. If we want to assign the correct named-entity tag to each word in a sentence, or other sophisticated linguistic labels like the parse tags we’ll introduce in later chapters, we’ll want to be able to take into account information from the right context as we process each element. Fig. 11.1a, reproduced here from Chapter 10, illustrates the information flow in the purely left-to-right approach of Chapter 10. As can be seen, the hidden state computation at each point in time is based solely on the current and earlier elements of the input, ignoring potentially useful information located to the right of each tagging decision.

![Diagram of causal and bidirectional self-attention layers](image)

**Figure 11.1** (a) The causal, backward looking, transformer model we saw in Chapter 10. Each output is computed independently of the others using only information seen earlier in the context. (b) Information flow in a bidirectional self-attention model. In processing each element of the sequence, the model attends to all inputs, both before and after the current one.

Bidirectional encoders overcome this limitation by allowing the self-attention mechanism to range over the entire input, as shown in Fig. 11.1b.

Why bidirectional encoders? The causal models of Chapter 10 are generative models, designed to easily generate the next token in a sequence. But the focus of bidirectional encoders is instead on computing contextualized representations of the input tokens. Bidirectional encoders use self-attention to map sequences of input embeddings \((x_1, ..., x_n)\) to sequences of output embeddings the same length \((y_1, ..., y_n)\), where the output vectors have been contextualized using information from the entire input sequence. These output embeddings are contextualized representations of each input token that are generally useful across a range of downstream applications. The models of Chapter 10 are sometimes called **decoder-only**; the models of this chapter are sometimes called **encoder-only**, because they produce an encoding for each input token but generally aren’t used to produce running text by decoding/sampling.

### 11.1.1 The architecture for bidirectional models

Bidirectional models use the same self-attention mechanism as causal models. The first step is to generate a set of key, query and value embeddings for each element of the input vector \(x\) through the use of learned weight matrices \(W^Q\), \(W^K\), and \(W^V\). These weights project each input vector \(x_i\) into its specific role as a key, query, or value.

\[
q_i = W^Q x_i; \quad k_i = W^K x_i; \quad v_i = W^V x_i
\]

The output vector \(y_i\) corresponding to each input element \(x_i\) is a weighted sum of all
the input value vectors \( \mathbf{v} \), as follows:

\[
y_i = \sum_{j=1}^{n} \alpha_{ij} \mathbf{v}_j
\]  

(11.2)

The \( \alpha \) weights are computed via a softmax over the comparison scores between every element of an input sequence considered as a query and every other element as a key, where the comparison scores are computed using dot products.

\[
\alpha_{ij} = \frac{\exp(\text{score}_{ij})}{\sum_{k=1}^{n} \exp(\text{score}_{ik})}
\]  

(11.3)

\[
\text{score}_{ij} = \mathbf{q}_i \cdot \mathbf{k}_j
\]  

(11.4)

As with the models of Chapter 10, since each output vector, \( \mathbf{y}_i \), is computed independently, the processing of an entire sequence can be parallelized via matrix operations. The first step is to pack the input embeddings \( \mathbf{x}_i \) into a matrix \( \mathbf{X} \in \mathbb{R}^{N \times d_h} \). That is, each row of \( \mathbf{X} \) is the embedding of one token of the input. We then multiply \( \mathbf{X} \) by the key, query, and value weight matrices (all of dimensionality \( d \times d \)) to produce matrices \( \mathbf{Q} \in \mathbb{R}^{N \times d} \), \( \mathbf{K} \in \mathbb{R}^{N \times d} \), and \( \mathbf{V} \in \mathbb{R}^{N \times d} \), containing all the key, query, and value vectors in a single step.

\[
\mathbf{Q} = \mathbf{XW}^Q; \quad \mathbf{K} = \mathbf{XW}^K; \quad \mathbf{V} = \mathbf{XW}^V
\]  

(11.5)

Given these matrices we can compute all the requisite query-key comparisons simultaneously by multiplying \( \mathbf{Q} \) and \( \mathbf{K}^\top \) in a single operation. Fig. 11.2 illustrates the result of this operation for an input with length 5.

Finally, we can scale these scores, take the softmax, and then multiply the result by \( \mathbf{V} \) resulting in a matrix of shape \( N \times d \) where each row contains a contextualized output embedding corresponding to each token in the input.

\[
\text{SelfAttention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax}\left( \frac{\mathbf{QK}^\top}{\sqrt{d_k}} \right) \mathbf{V}
\]  

(11.6)

The key architecture difference is in bidirectional models we don’t mask the future. As shown in Fig. 11.2, the full set of self-attention scores represented by \( \mathbf{QK}^\top \) constitute an all-pairs comparison between the keys and queries for each element of the input. In the case of causal language models in Chapter 10, we masked the
upper triangular portion of this matrix (in Fig. 10.4) to eliminate information about future words since this would make the language modeling training task trivial. With bidirectional encoders we simply skip the mask, allowing the model to contextualize each token using information from the entire input.

Beyond this simple change, all of the other elements of the transformer architecture remain the same for bidirectional encoder models. Inputs to the model are segmented using subword tokenization and are combined with positional embeddings before being passed through a series of standard transformer blocks consisting of self-attention and feedforward layers augmented with residual connections and layer normalization, as shown in Fig. 11.3.

To make this more concrete, the original English-only bidirectional transformer encoder model, BERT (Devlin et al., 2019), consisted of the following:

- An English-only subword vocabulary consisting of 30,000 tokens generated using the WordPiece algorithm (Schuster and Nakajima, 2012).
- Hidden layers of size of 768,
- 12 layers of transformer blocks, with 12 multihead attention layers each.
- The resulting model has about 100M parameters.

The larger multilingual XLM-RoBERTa model, trained on 100 languages, has

- A multilingual subword vocabulary with 250,000 tokens generated using the SentencePiece Unigram LM algorithm (Kudo and Richardson, 2018b).
- 24 layers of transformer blocks, with 16 multihead attention layers each
- Hidden layers of size 1024
- The resulting model has about 550M parameters.

The use of WordPiece or SentencePiece Unigram LM tokenization (two of the large family of subword tokenization algorithms that includes the BPE algorithm we saw in Chapter 2) means that—like the large language models of Chapter 10—BERT and its descendants are based on subword tokens rather than words. Every input sentence first has to be tokenized, and then all further processing takes place on subword tokens rather than words. This will require, as we’ll see, that for some
NLP tasks that require notions of words (like named entity tagging, or parsing) we will occasionally need to map subwords back to words.

As with causal transformers, the size of the input layer dictates the complexity of the model. Both the time and memory requirements in a transformer grow quadratically with the length of the input. It’s necessary, therefore, to set a fixed input length that is long enough to provide sufficient context for the model to function and yet still be computationally tractable. For BERT and XLR-RoBERTa, a fixed input size of 512 subword tokens was used.

11.2 Training Bidirectional Encoders

We trained causal transformer language models in Chapter 10 by making them iteratively predict the next word in a text. But eliminating the causal mask makes the guess-the-next-word language modeling task trivial since the answer is now directly available from the context, so we’re in need of a new training scheme. Fortunately, the traditional learning objective suggests an approach that can be used to train bidirectional encoders. Instead of trying to predict the next word, the model learns to perform a fill-in-the-blank task, technically called the cloze task (Taylor, 1953). To see this, let’s return to the motivating example from Chapter 3. Instead of predicting which words are likely to come next in this example:

```
Please turn your homework ____ .
```

we’re asked to predict a missing item given the rest of the sentence.

```
Please turn ____ homework in.
```

That is, given an input sequence with one or more elements missing, the learning task is to predict the missing elements. More precisely, during training the model is deprived of one or more elements of an input sequence and must generate a probability distribution over the vocabulary for each of the missing items. We then use the cross-entropy loss from each of the model’s predictions to drive the learning process.

This approach can be generalized to any of a variety of methods that corrupt the training input and then asks the model to recover the original input. Examples of the kinds of manipulations that have been used include masks, substitutions, reorderings, deletions, and extraneous insertions into the training text.

11.2.1 Masking Words

The original approach to training bidirectional encoders is called Masked Language Modeling (MLM) (Devlin et al., 2019). As with the language model training methods we’ve already seen, MLM uses unannotated text from a large corpus. Here, the model is presented with a series of sentences from the training corpus where a random sample of tokens from each training sequence is selected for use in the learning task. Once chosen, a token is used in one of three ways:

- It is replaced with the unique vocabulary token [MASK].
- It is replaced with another token from the vocabulary, randomly sampled based on token unigram probabilities.
- It is left unchanged.
In BERT, 15% of the input tokens in a training sequence are sampled for learning. Of these, 80% are replaced with [MASK], 10% are replaced with randomly selected tokens, and the remaining 10% are left unchanged.

The MLM training objective is to predict the original inputs for each of the masked tokens using a bidirectional encoder of the kind described in the last section. The cross-entropy loss from these predictions drives the training process for all the parameters in the model. Note that all of the input tokens play a role in the self-attention process, but only the sampled tokens are used for learning.

More specifically, the original input sequence is first tokenized using a subword model. The sampled items which drive the learning process are chosen from among the set of tokenized inputs. Word embeddings for all of the tokens in the input are retrieved from the word embedding matrix and then combined with positional embeddings to form the input to the transformer.

**Figure 11.4** Masked language model training. In this example, three of the input tokens are selected, two of which are masked and the third is replaced with an unrelated word. The probabilities assigned by the model to these three items are used as the training loss. The other 5 words don’t play a role in training loss. (In this and subsequent figures we display the input as words rather than subword tokens; the reader should keep in mind that BERT and similar models actually use subword tokens instead.)

Fig. 11.4 illustrates this approach with a simple example. Here, *long*, *thanks* and *the* have been sampled from the training sequence, with the first two masked and *the* replaced with the randomly sampled token *apricot*. The resulting embeddings are passed through a stack of bidirectional transformer blocks. To produce a probability distribution over the vocabulary for each of the masked tokens, the output vector $z_i$ from the final transformer layer for each masked token $i$ is multiplied by a learned set of classification weights $W_V \in \mathbb{R}^{V \times d_h}$ and then through a softmax to yield the required predictions over the vocabulary.

$$y_i = \text{softmax}(W_V z_i)$$

With a predicted probability distribution for each masked item, we can use cross-entropy to compute the loss for each masked item— the negative log probability assigned to the actual masked word, as shown in Fig. 11.4. More formally, for a given vector of input tokens in a sentence or batch be $x$, let the set of tokens that are
masked be \( M \), the version of that sentence with some tokens replaced by masks be \( x^{\text{mask}} \), and the sequence of output vectors be \( z \). For a given input token \( x_i \), such as the word \textit{long} in Fig. 11.4, the loss is the probability of the correct word \textit{long}, given \( x^{\text{mask}} \) (as summarized in the single output vector \( z_i \)):

\[
L_{\text{MLM}}(x_i) = - \log P(x_i | z_i)
\]

The gradients that form the basis for the weight updates are based on the average loss over the sampled learning items from a single training sequence (or batch of sequences).

\[
L_{\text{MLM}} = - \frac{1}{|M|} \sum_{i \in M} \log P(x_i | z_i)
\]

Note that only the tokens in \( M \) play a role in learning; the other words play no role in the loss function, so in that sense BERT and its descendents are inefficient; only 15% of the input samples in the training data are actually used for training weights.

### 11.2.2 Next Sentence Prediction

The focus of mask-based learning is on predicting words from surrounding contexts with the goal of producing effective word-level representations. However, an important class of applications involves determining the relationship between pairs of sentences. These include tasks like paraphrase detection (detecting if two sentences have similar meanings), entailment (detecting if the meanings of two sentences entail or contradict each other) or discourse coherence (deciding if two neighboring sentences form a coherent discourse).

To capture the kind of knowledge required for applications such as these, some models in the BERT family include a second learning objective called Next Sentence Prediction (NSP). In this task, the model is presented with pairs of sentences and is asked to predict whether each pair consists of an actual pair of adjacent sentences from the training corpus or a pair of unrelated sentences. In BERT, 50% of the training pairs consisted of positive pairs, and in the other 50% the second sentence of a pair was randomly selected from elsewhere in the corpus. The NSP loss is based on how well the model can distinguish true pairs from random pairs.

To facilitate NSP training, BERT introduces two new tokens to the input representation (tokens that will prove useful for fine-tuning as well). After tokenizing the input with the subword model, the token [CLS] is prepended to the input sentence pair, and the token [SEP] is placed between the sentences and after the final token of the second sentence. Finally, embeddings representing the first and second segments of the input are added to the word and positional embeddings to allow the model to more easily distinguish the input sentences.

During training, the output vector from the final layer associated with the [CLS] token represents the next sentence prediction. As with the MLM objective, a learned set of classification weights \( W_{\text{NSP}} \in \mathbb{R}^{2 \times d_h} \) is used to produce a two-class prediction from the raw [CLS] vector.

\[
y_i = \text{softmax}(W_{\text{NSP}} h_i)
\]

1 There are members of the BERT family like ELECTRA that do use all examples for training (Clark et al., 2020b).
Cross entropy is used to compute the NSP loss for each sentence pair presented to the model. Fig. 11.5 illustrates the overall NSP training setup. In BERT, the NSP loss was used in conjunction with the MLM training objective to form final loss.

**11.2.3 Training Regimes**

BERT and other early transformer-based language models were trained on about 3.3 billion words (a combination of English Wikipedia and a corpus of book texts called BooksCorpus (Zhu et al., 2015) that is no longer used for intellectual property reasons). Modern masked language models are now trained on much larger datasets of web text, filtered a bit, and augmented by higher-quality data like Wikipedia, the same as those we discussed for the causal large language models of Chapter 10. Multilingual models similarity use webtext and multilingual Wikipedia. For example the XLM-R model was trained on about 300 billion tokens in 100 languages, taken from the web via Common Crawl (https://commoncrawl.org/).

To train the original BERT models, pairs of text segments were selected from the training corpus according to the next sentence prediction 50/50 scheme. Pairs were sampled so that their combined length was less than the 512 token input. Tokens within these sentence pairs were then masked using the MLM approach with the combined loss from the MLM and NSP objectives used for a final loss. Approximately 40 passes (epochs) over the training data was required for the model to converge.

Some models, like the RoBERTa model, drop the next sentence prediction objective, and therefore change the training regime a bit. Instead of sampling pairs of sentence, the input is simply a series of contiguous sentences. If the document runs out before 512 tokens are reached, an extra separator token is added, and sentences from the next document are packed in, until we reach a total of 512 tokens. Usually large batch sizes are used, between 8K and 32K tokens.

Multilingual models have an additional decision to make: what data to use to build the vocabulary? Recall that all language models use subword tokenization (BPE or SentencePiece Unigram LM are the two most common algorithms). What text should be used to learn this multilingual tokenization, given that it’s easier to get much more text in some languages than others? One option would be to create this vocabulary-learning dataset by sampling sentences from our training data (perhaps
web text from Common Crawl), randomly. In that case we will choose a lot of sentences from languages like languages with lots of web representation like English, and the tokens will be biased toward rare English tokens instead of creating frequent tokens from languages with less data. Instead, it is common to divide the training data into subcorpora of \( N \) different languages, compute the number of sentences \( n_i \) of each language \( i \), and readjust these probabilities so as to upweight the probability of less-represented languages (Lample and Conneau, 2019). The new probability of selecting a sentence from each of the \( N \) languages (whose prior frequency is \( n_i \)) is \( \{q_i\}_{i=1...N} \), where:

\[
q_i = \frac{p_i^\alpha}{\sum_{j=1}^N p_j^\alpha} \quad \text{with} \quad p_i = \frac{n_i}{\sum_{k=1}^N n_k}
\]  

(11.7)

Recall from (6.32) in Chapter 6 that an \( \alpha \) value between 0 and 1 will give higher weight to lower probability samples. Conneau et al. (2020) show that \( \alpha = 0.3 \) works well to give rare languages more inclusion in the tokenization, resulting in better multilingual performance overall.

The result of this pretraining process consists of both learned word embeddings, as well as all the parameters of the bidirectional encoder that are used to produce contextual embeddings for novel inputs.

For many purposes, a pretrained multilingual model is more practical than a monolingual model, since it avoids the need to build many (!) separate monolingual models. And multilingual models can improve performance on low-resourced languages by leveraging linguistic information from a similar language in the training data that happens to have more resources. Nonetheless, when the number of languages grows very large, multilingual models exhibit what has been called the curse of multilinguality (Conneau et al., 2020): the performance on each language degrades compared to a model training on fewer languages. Another problem with multilingual models is that they ‘have an accent’: grammatical structures in higher-resource languages (often English) bleed into lower-resource languages; the vast amount of English language in training makes the model’s representations for low-resource languages slightly more English-like (Papadimitriou et al., 2023).

### 11.3 Contextual Embeddings

Given a pretrained language model and a novel input sentence, we can think of the sequence of model outputs as constituting contextual embeddings for each token in the input. These contextual embeddings are vectors representing some aspect of the meaning of a token in context, and can be used for any task requiring the meaning of tokens or words. More formally, given a sequence of input tokens \( x_1, ..., x_n \), we can use the output vector \( z_i \) from the final layer of the model as a representation of the meaning of token \( x_i \) in the context of sentence \( x_1, ..., x_n \). Or instead of just using the vector \( z_i \) from the final layer of the model, it’s common to compute a representation for \( x_i \) by averaging the output tokens \( z_j \) from each of the last four layers of the model.

Just as we used static embeddings like word2vec in Chapter 6 to represent the meaning of words, we can use contextual embeddings as representations of word meanings in context for any task that might require a model of word meaning. Where static embeddings represent the meaning of word types (vocabulary entries), contextual embeddings represent the meaning of word instances: instances of a particular
word type in a particular context. Thus where word2vec had a single vector for each word type, contextual embeddings provide a single vector for each instance of that word type in its sentential context. Contextual embeddings can thus be used for tasks like measuring the semantic similarity of two words in context, and are useful in linguistic tasks that require models of word meaning.

### 11.3.1 Contextual Embeddings and Word Sense

**Words are ambiguous**: the same word can be used to mean different things. In Chapter 6 we saw that the word “mouse” can mean (1) a small rodent, or (2) a hand-operated device to control a cursor. The word “bank” can mean: (1) a financial institution or (2) a sloping mound. We say that the words ‘mouse’ or ‘bank’ are *polysemous* (from Greek ‘many senses’, *poly-* ‘many’ + *sema*, ‘sign, mark’).²

A *sense* (or *word sense*) is a discrete representation of one aspect of the meaning of a word. We can represent each sense with a superscript: **bank**¹ and **bank**², **mouse**¹ and **mouse**². These senses can be found listed in online thesauruses (or thesauri) like *WordNet* (Fellbaum, 1998), which has datasets in many languages listing the senses of many words. In context, it’s easy to see the different meanings:

**mouse**¹ : .... a *mouse* controlling a computer system in 1968.

**mouse**² : .... a quiet animal like a *mouse*

**bank**¹ : .... a *bank* can hold the investments in a custodial account ...

**bank**² : .... as agriculture burgeons on the east *bank*, the river ...

This fact that context disambiguates the senses of *mouse* and *bank* above can also be visualized geometrically. Fig. 11.7 shows a two-dimensional project of many instances of the BERT embeddings of the word *die* in English and German. Each point in the graph represents the use of *die* in one input sentence. We can clearly see at least two different English senses of *die* (the singular of *dice* and the verb *to die*, as well as the German article, in the BERT embedding space.

Thus while thesauruses like WordNet give discrete lists of senses, embeddings (whether static or contextual) offer a continuous high-dimensional model of meaning.

---

² The word *polysemy* itself is ambiguous; you may see it used in a different way, to refer only to cases where a word’s senses are related in some structured way, reserving the word *homonymy* to mean sense ambiguities with no relation between the senses (Haber and Poesio, 2020). Here we will use ‘polysemy’ to mean any kind of sense ambiguity, and ‘structured polysemy’ for polysemy with sense relations.
that, although it can be clustered, doesn’t divide up into fully discrete senses.

**Word Sense Disambiguation**

The task of selecting the correct sense for a word is called **word sense disambiguation**, or **WSD**. WSD algorithms take as input a word in context and a fixed inventory of potential word senses (like the ones in WordNet) and outputs the correct word sense in context. Fig. 11.8 sketches out the task.

**Figure 11.8** The all-words WSD task, mapping from input words \( x \) to WordNet senses \( y \). Figure inspired by Chaplot and Salakhutdinov (2018).

WSD can be a useful analytic tool for text analysis in the humanities and social sciences, and word senses can play a role in model interpretability for word representations. Word senses also have interesting distributional properties. For example a word often is used in roughly the same sense through a discourse, an observation called the **one sense per discourse** rule (Gale et al., 1992a).
The best performing WSD algorithm is a simple 1-nearest-neighbor algorithm using contextual word embeddings, due to Melamud et al. (2016) and Peters et al. (2018). At training time we pass each sentence in some sense-labeled dataset (like the SemCore or SenseEval datasets in various languages) through any contextual embedding (e.g., BERT) resulting in a contextual embedding for each labeled token. (There are various ways to compute this contextual embedding \( v_i \) for a token \( i \); for BERT it is common to pool multiple layers by summing the vector representations of \( i \) from the last four BERT layers). Then for each sense \( s \) of any word in the corpus, for each of the \( n \) tokens of that sense, we average their \( n \) contextual representations \( v_i \) to produce a contextual sense embedding \( v_s \) for \( s \):

\[
v_s = \frac{1}{n} \sum_i v_i, \quad \forall v_i \in \text{tokens}(s)
\]  

(11.8)

At test time, given a token of a target word \( t \) in context, we compute its contextual embedding \( t \) and choose its nearest neighbor sense from the training set, i.e., the sense whose sense embedding has the highest cosine with \( t \):

\[
\text{sense}(t) = \arg \max_{s \in \text{senses}(t)} \cosine(t, v_s)
\]  

(11.9)

Fig. 11.9 illustrates the model.

![Figure 11.9](image)

**Figure 11.9** The nearest-neighbor algorithm for WSD. In green are the contextual embeddings precomputed for each sense of each word; here we just show a few of the senses for *find*. A contextual embedding is computed for the target word *found*, and then the nearest neighbor sense (in this case *find*\(^9\)) is chosen. Figure inspired by Loureiro and Jorge (2019).

### 11.3.2 Contextual Embeddings and Word Similarity

In Chapter 6 we introduced the idea that we could measure the similarity of two words by considering how close they are geometrically, by using the cosine as a similarity function. The idea of meaning similarity is also clear geometrically in the meaning clusters in Fig. 11.7; the representation of a word which has a particular sense in a context is closer to other instances of the same sense of the word. Thus we often measure the similarity between two instances of two words in context (or two instances of the same word in two different contexts) by using the cosine between their contextual embeddings.

Usually some transformations to the embeddings are required before computing cosine. This is because contextual embeddings (whether from masked language
models or from autoregressive ones) have the property that the vectors for all words are extremely similar. If we look at the embeddings from the final layer of BERT or other models, embeddings for instances of any two randomly chosen words will have extremely high cosines that can be quite close to 1, meaning all word vectors tend to point in the same direction. The property of vectors in a system all tending to point in the same direction is known as anisotropy. Ethayarajh (2019) defines the anisotropy of a model as the expected cosine similarity of any pair of words in a corpus. The word ‘isotropy’ means uniformity in all directions, so in an isotropic model, the collection of vectors should point in all directions and the expected cosine between a pair of random embeddings would be zero. Timkey and van Schijndel (2021) show that one cause of anisotropy is that cosine measures are dominated by a small number of dimensions of the contextual embedding whose values are very different than the others: these rogue dimensions have very large magnitudes and very high variance.

Timkey and van Schijndel (2021) shows that we can make the embeddings more isotropic by standardizing (z-scoring) the vectors, i.e., subtracting the mean and dividing by the variance. Given a set $C$ of all the embeddings in some corpus, each with dimensionality $d$ (i.e., $x \in \mathbb{R}^d$), the mean vector $\mu \in \mathbb{R}^d$ is:

$$\mu = \frac{1}{|C|} \sum_{x \in C} x$$  \hspace{1cm} (11.10)

The standard deviation in each dimension $\sigma \in \mathbb{R}^d$ is:

$$\sigma = \sqrt{\frac{1}{|C|} \sum_{x \in C} (x - \mu)^2}$$  \hspace{1cm} (11.11)

Then each word vector $x$ is replaced by a standardized version $z$:

$$z = \frac{x - \mu}{\sigma}$$  \hspace{1cm} (11.12)

One problem with cosine that is not solved by standardization is that cosine tends to underestimate human judgments on similarity of word meaning for very frequent words (Zhou et al., 2022).

In the next section we’ll see the most common use of contextual representations: as representations of words or even entire sentences that can be the inputs to classifiers in the fine-tuning process for downstream NLP applications.

### 11.4 Fine-Tuning Language Models

The power of pretrained language models lies in their ability to extract generalizations from large amounts of text—generalizations that are useful for myriad downstream applications. There are two ways to make practical use of the generalizations. One way is to use natural language to prompt the model, putting it in a state where it contextually generates what we want. We’ll introduce prompting in Chapter 12. An alternative is to create interfaces from pretrained language models to downstream applications through a process called fine-tuning. In fine-tuning, we create applications on top of pretrained models by adding a small set of application-specific parameters. The fine-tuning process consists of using labeled data about
the application to train these additional application-specific parameters. Typically, this training will either freeze or make only minimal adjustments to the pretrained language model parameters.

The following sections introduce fine-tuning methods for the most common applications including sequence classification, sequence labeling, sentence-pair inference, and span-based operations.

### 11.4.1 Sequence Classification

Sequence classification applications often represent an input sequence with a single consolidated representation. With RNNs, we used the hidden layer associated with the final input element to stand for the entire sequence. A similar approach is used with transformers. An additional vector is added to the model to stand for the entire sequence. This vector is sometimes called the sentence embedding since it refers to the entire sequence, although the term ‘sentence embedding’ is also used in other ways. In BERT, the [CLS] token plays the role of this embedding. This unique token is added to the vocabulary and is prepended to the start of all input sequences, both during pretraining and encoding. The output vector in the final layer of the model for the [CLS] input represents the entire input sequence and serves as the input to a classifier head, a logistic regression or neural network classifier that makes the relevant decision.

As an example, let’s return to the problem of sentiment classification. A simple approach to fine-tuning a classifier for this application involves learning a set of weights, $W_C$, to map the output vector for the [CLS] token—$z_{CLS}$—to a set of scores over the possible sentiment classes. Assuming a three-way sentiment classification task (positive, negative, neutral) and dimensionality $d_h$ for the size of the language model hidden layers gives $W_C \in \mathbb{R}^{3 \times d_h}$. Classification of unseen documents proceeds by passing the input text through the pretrained language model to generate $z_{CLS}$, multiplying it by $W_C$, and finally passing the resulting vector through a softmax.

$$y = \text{softmax}(W_C z_{CLS})$$ (11.13)

Fine-tuning the values in $W_C$ requires supervised training data consisting of input sequences labeled with the appropriate class. Training proceeds in the usual way; cross-entropy loss between the softmax output and the correct answer is used to drive the learning that produces $W_C$.

A key difference from what we’ve seen earlier with neural classifiers is that this loss can be used to not only learn the weights of the classifier, but also to update the weights for the pretrained language model itself. In practice, reasonable classification performance is typically achieved with only minimal changes to the language model parameters, often limited to updates over the final few layers of the transformer. Fig. 11.10 illustrates this overall approach to sequence classification.

### 11.4.2 Pair-Wise Sequence Classification

As mentioned in Section 11.2.2, an important type of problem involves the classification of pairs of input sequences. Practical applications that fall into this class include paraphrase detection (are the two sentences paraphrases of each other?), logical entailment (does sentence A logically entail sentence B?), and discourse coherence (how coherent is sentence B as a follow-on to sentence A?).
Fine-tuning an application for one of these tasks proceeds just as with pretraining using the NSP objective. During fine-tuning, pairs of labeled sentences from the supervised training data are presented to the model, and run through all the layers of the model to produce the $z$ outputs for each input token. As with sequence classification, the output vector associated with the prepended [CLS] token represents the model’s view of the input pair. And as with NSP training, the two inputs are separated by the [SEP] token. To perform classification, the [CLS] vector is multiplied by a set of learning classification weights and passed through a softmax to generate label predictions, which are then used to update the weights.

As an example, let’s consider an entailment classification task with the Multi-Genre Natural Language Inference (MultiNLI) dataset (Williams et al., 2018). In the task of natural language inference or NLI, also called recognizing textual entailment, a model is presented with a pair of sentences and must classify the relationship between their meanings. For example in the MultiNLI corpus, pairs of sentences are given one of 3 labels: entails, contradicts and neutral. These labels describe a relationship between the meaning of the first sentence (the premise) and the meaning of the second sentence (the hypothesis). Here are representative examples of each class from the corpus:

- **Neutral**
  a: Jon walked back to the town to the smithy.
  b: Jon traveled back to his hometown.

- **Contradicts**
  a: Tourist Information offices can be very helpful.
  b: Tourist Information offices are never of any help.

- **Entails**
  a: I’m confused.
  b: Not all of it is very clear to me.

A relationship of *contradicts* means that the premise contradicts the hypothesis; *entails* means that the premise entails the hypothesis; *neutral* means that neither is necessarily true. The meaning of these labels is looser than strict logical entailment.
or contradiction indicating that a typical human reading the sentences would most likely interpret the meanings in this way.

To fine-tune a classifier for the MultiNLI task, we pass the premise/hypothesis pairs through a bidirectional encoder as described above and use the output vector for the [CLS] token as the input to the classification head. As with ordinary sequence classification, this head provides the input to a three-way classifier that can be trained on the MultiNLI training corpus.

### 11.4.3 Sequence Labelling

Sequence labelling tasks, such as part-of-speech tagging or BIO-based named entity recognition, follow the same basic classification approach. Here, the final output vector corresponding to each input token is passed to a classifier that produces a softmax distribution over the possible set of tags. Again, assuming a simple classifier consisting of a single feedforward layer followed by a softmax, the set of weights to be learned for this additional layer is $W_k \in \mathbb{R}^{k \times d_h}$, where $k$ is the number of possible tags for the task. As with RNNs, a greedy approach, where the argmax tag for each token is taken as a likely answer, can be used to generate the final output tag sequence. Fig. 11.11 illustrates an example of this approach.

$$y_i = \text{softmax}(W_k z_i)$$  \hfill (11.14)

$$t_i = \text{argmax}_k(y_i)$$  \hfill (11.15)

Alternatively, the distribution over labels provided by the softmax for each input token can be passed to a conditional random field (CRF) layer which can take global tag-level transitions into account.

![Figure 11.11](image)

**Figure 11.11** Sequence labeling for part-of-speech tagging with a bidirectional transformer encoder. The output vector for each input token is passed to a simple $k$-way classifier.

A complication with this approach arises from the use of subword tokenization such as WordPiece, SentencePiece Unigram LM or Byte Pair Encoding. Supervised training data for tasks like named entity recognition (NER) is typically in the form of BIO tags associated with text segmented at the word level. For example the following sentence containing two named entities:
(11.16) **Mt. Sanitas is in Sunshine Canyon.**

Unfortunately, the WordPiece tokenization for this sentence yields the following sequence of tokens which doesn’t align directly with BIO tags in the ground truth annotation:

'Mt', '.', 'San', '##itas', 'is', 'in', 'Sunshine', 'Canyon' '. '

To deal with this misalignment, we need a way to assign BIO tags to subword tokens during training and a corresponding way to recover word-level tags from subwords during decoding. For training, we can just assign the gold-standard tag associated with each word to all of the subword tokens derived from it. For decoding, the simplest approach is to use the argmax BIO tag associated with the first subword token of a word. Thus, in our example, the BIO tag assigned to “Mt” would be assigned to “Mt.” and the tag assigned to “San” would be assigned to “Sanitas”, effectively ignoring the information in the tags assigned to “.” and “##itas”. More complex approaches combine the distribution of tag probabilities across the subwords in an attempt to find an optimal word-level tag.

### 11.5 Advanced: Span-based Masking

For many NLP applications, the natural unit of interest may be larger than a single word (or token). Question answering, syntactic parsing, coreference and semantic role labeling applications all involve the identification and classification of longer phrases. This suggests that a span-oriented masked learning objective might provide improved performance on such tasks.

#### 11.5.1 Masking Spans

A span is a contiguous sequence of one or more words selected from a training text, prior to subword tokenization. In span-based masking, a set of randomly selected spans from a training sequence are chosen. In the SpanBERT work that originated this technique (Joshi et al., 2020), a span length is first chosen by sampling from a geometric distribution that is biased towards shorter spans and with an upper bound of 10. Given this span length, a starting location consistent with the desired span length and the length of the input is sampled uniformly.

Once a span is chosen for masking, all the tokens within the span are substituted according to the same regime used in BERT: 80% of the time the span elements are substituted with the [MASK] token, 10% of the time they are replaced by randomly sampled tokens from the vocabulary, and 10% of the time they are left as is. Note that this substitution process is done at the span level—all the tokens in a given span are substituted using the same method. As with BERT, the total token substitution is limited to 15% of the training sequence input. Having selected and masked the training span, the input is passed through the standard transformer architecture to generate contextualized representations of the input tokens.
Downstream span-based applications rely on span representations derived from the tokens within the span, as well as the start and end points, or the boundaries, of a span. Representations for these boundaries are typically derived from the first and last tokens of a span, the tokens immediately preceding and following the span, or some combination of them. The SpanBERT learning objective augments the MLM objective with a boundary oriented component called the Span Boundary Objective (SBO). The SBO relies on a model’s ability to predict the tokens within a masked span from the tokens immediately preceding and following the span.

Let the sequence of output from the transformer encoder for the \( n \) input tokens \( s_1, \ldots, s_n \) be \( z_1, \ldots, z_n \). A token \( x_i \) in a masked span of tokens \( (x_s, \ldots, x_e) \), i.e., starting with token \( x_s \) and ending with token \( x_e \), is represented by concatenating 3 embeddings. The first two are the embeddings of two external boundary tokens \( x_{s-1} \) and \( x_{e+1} \), i.e., the token preceding \( x_s \), the token following \( x_e \). The third embedding that is concatenated is the relative position embedding of the target token \( p_{i-s+1} \). The position embeddings \( p_1, p_2, \ldots \) represent relative positions of the tokens with respect to the left boundary token \( x_{s-1} \).

\[
L(x) = L_{MLM}(x) + L_{SBO}(x)
\]

This probability for token \( x_i \) is formed by passing the concatenation of these embeddings through a 2-layer feedforward network to get the probability distribution over the whole vocabulary at \( i \):

\[
s_i = \text{FFN}(z_{s-1}; z_{e+1}; p_{i-s+1})
\]

\[
y_i = \text{softmax}(W_V s_i)
\]

We then use \( s_i \), the output of the vector representation of token \( i \) in the span, to predict the token \( x_i \) by reshaping it and passing it through a softmax to get a probability distribution \( y_i \) over the vocabulary, and select from it the probability for input token \( x_i \).

The final loss is the sum of the BERT MLM loss and the SBO loss.

Fig. 11.12 illustrates this with one of our earlier examples. Here the span selected is and thanks for which spans from position 3 to 5. The total loss associated with the masked token thanks is the sum of the cross-entropy loss generated from the prediction of thanks from the output \( z_4 \), plus the cross-entropy loss from the prediction of thanks from the output vectors from the left external boundary \( z_2 \), the right external boundary \( z_6 \), and the embedding for relative position 2 in the span.

### 11.5.2 Fine-tuning for Span-Based Applications

Span-oriented applications operate in a middle ground between sequence level and token level tasks. That is, in span-oriented applications the focus is on generating and operating with representations of contiguous sequences of tokens. Typical operations include identifying spans of interest, classifying spans according to some labeling scheme, and determining relations among discovered spans. Applications include named entity recognition, question answering, syntactic parsing, semantic role labeling and coreference resolution.

Formally, given an input sequence \( x \) consisting of \( T \) tokens, \( (x_1, x_2, \ldots, x_T) \), a span is a contiguous sequence of tokens with start \( i \) and end \( j \) such that \( 1 <= i <= j <= T \). This formulation results in a total set of spans equal to \( \frac{T(T+1)}{2} \). For practical
Figure 11.12  Span-based language model training. In this example, a span of length 3 is selected for training and all of the words in the span are masked. The figure illustrates the loss computed for word thanks; the loss for the entire span is the sum of the loss for the three words in the span.

purposes, span-based models often impose an application-specific length limit \( L \), so the legal spans are limited to those where \( j - i < L \). In the following, we’ll refer to the enumerated set of legal spans in \( x \) as \( S(x) \).

The first step in fine-tuning a pretrained language model for a span-based application is using the contextualized input embeddings from the model to generate representations for all the spans in the input. Most schemes for representing spans make use of two primary components: representations of the span boundaries and summary representations of the contents of each span. To compute a unified span representation, we concatenate the boundary representations with the summary representation.

In the simplest possible approach, we can use the contextual embeddings of the start and end tokens of a span as the boundaries, and the average of the output embeddings within the span as the summary representation.

\[
g_{ij} = \frac{1}{(j-i)+1} \sum_{k=i}^{j} z_k \quad (11.21)
\]

\[
\text{spanRep}_{ij} = [z_i; z_j; g_{ij}] \quad (11.22)
\]

A weakness of this approach is that it doesn’t distinguish the use of a word’s embedding as the beginning of a span from its use as the end of one. Therefore, more elaborate schemes for representing the span boundaries involve learned representations for start and end points through the use of two distinct feedforward networks:

\[
s_i = \text{FFN}_{\text{start}}(z_i) \quad (11.23)
\]

\[
e_j = \text{FFN}_{\text{end}}(z_j) \quad (11.24)
\]

\[
\text{spanRep}_{ij} = [s_i; e_j; g_{ij}] \quad (11.25)
\]
Similarly, a simple average of the vectors in a span is unlikely to be an optimal representation of a span since it treats all of a span’s embeddings as equally important. For many applications, a more useful representation would be centered around the head of the phrase corresponding to the span. One method for getting at such information in the absence of a syntactic parse is to use a standard self-attention layer to generate a span representation.

$$g_{ij} = \text{SelfAttention}(z_{i,j})$$  \hspace{1cm} (11.26)

Now, given span representations $g$ for each span in $S(x)$, classifiers can be fine-tuned to generate application-specific scores for various span-oriented tasks: binary span identification (is this a legitimate span of interest or not?), span classification (what kind of span is this?), and span relation classification (how are these two spans related?).

To ground this discussion, let’s return to named entity recognition (NER). Given a scheme for representing spans and a set of named entity types, a span-based approach to NER is a straightforward classification problem where each span in an input is assigned a class label. More formally, given an input sequence $x_1, \ldots, x_n$, we want to assign a label $y$, from the set of valid NER labels, to each of the spans in $S(x)$. Since most of the spans in a given input will not be named entities we’ll add the label NULL to the set of types in $Y$.

$$y_{ij} = \text{softmax}(\text{FFN}(\text{spanRep}_{ij}))$$  \hspace{1cm} (11.27)

With this approach, fine-tuning entails using supervised training data to learn the parameters of the final classifier, as well as the weights used to generate the boundary representations, and the weights in the self-attention layer that generates the span content representation. During training, the model’s predictions for all spans are compared to their gold-standard labels and cross-entropy loss is used to drive the training.

During decoding, each span is scored using a softmax over the final classifier output to generate a distribution over the possible labels, with the argmax score for each span taken as the correct answer. Fig. 11.13 illustrates this approach with an
example. A variation on this scheme designed to improve precision adds a calibrated threshold to the labeling of a span as anything other than NULL.

There are two significant advantages to a span-based approach to NER over a BIO-based per-word labeling approach. The first advantage is that BIO-based approaches are prone to a labeling mis-match problem. That is, every label in a longer named entity must be correct for an output to be judged correct. Returning to the example in Fig. 11.13, the following labeling would be judged entirely wrong due to the incorrect label on the first item. Span-based approaches only have to make one classification for each span.

(11.28) Jane Villanueva of United Airlines Holding discussed ...
B-PER I-PER O I-ORG I-ORG I-ORG O

The second advantage to span-based approaches is that they naturally accommodate embedded named entities. For example, in this example both United Airlines and United Airlines Holding are legitimate named entities. The BIO approach has no way of encoding this embedded structure. But the span-based approach can naturally label both since the spans are labeled separately.

### 11.6 Summary

This chapter has introduced the topic of transfer learning from pretrained language models. Here’s a summary of the main points that we covered:

- Bidirectional encoders can be used to generate contextualized representations of input embeddings using the entire input context.
- Pretrained language models based on bidirectional encoders can be learned using a masked language model objective where a model is trained to guess the missing information from an input.
- Pretrained language models can be fine-tuned for specific applications by adding lightweight classifier layers on top of the outputs of the pretrained model.

### Bibliographical and Historical Notes
CHAPTER 12
Prompting, In-Context Learning, and Instruct Tuning
In this second part of the book we introduce fundamental NLP applications: machine translation, information retrieval, question answering, dialogue systems, and speech recognition.
“I want to talk the dialect of your people. It’s no use of talking unless people understand what you say.”

Zora Neale Hurston, *Moses, Man of the Mountain* 1939, p. 121

This chapter introduces machine translation (MT), the use of computers to translate from one language to another.

Of course translation, in its full generality, such as the translation of literature, or poetry, is a difficult, fascinating, and intensely human endeavor, as rich as any other area of human creativity.

Machine translation in its present form therefore focuses on a number of very practical tasks. Perhaps the most common current use of machine translation is for information access. We might want to translate some instructions on the web, perhaps the recipe for a favorite dish, or the steps for putting together some furniture. Or we might want to read an article in a newspaper, or get information from an online resource like Wikipedia or a government webpage in some other language. MT for information access is probably one of the most common uses of NLP technology, and Google Translate alone (shown above) translates hundreds of billions of words a day between over 100 languages. Improvements in machine translation can thus help reduce what is often called the digital divide in information access: the fact that much more information is available in English and other languages spoken in wealthy countries. Web searches in English return much more information than searches in other languages, and online resources like Wikipedia are much larger in English and other higher-resourced languages. High-quality translation can help provide information to speakers of lower-resourced languages.

Another common use of machine translation is to aid human translators. MT systems are routinely used to produce a draft translation that is fixed up in a post-editing phase by a human translator. This task is often called computer-aided translation or CAT. CAT is commonly used as part of localization: the task of adapting content or a product to a particular language community.

Finally, a more recent application of MT is to in-the-moment human communication needs. This includes incremental translation, translating speech on-the-fly before the entire sentence is complete, as is commonly used in simultaneous interpretation. Image-centric translation can be used for example to use OCR of the text on a phone camera image as input to an MT system to translate menus or street signs.

The standard algorithm for MT is the encoder-decoder network, an architecture that we introduced in Chapter 9 for RNNs. Recall that encoder-decoder or sequence-to-sequence models are used for tasks in which we need to map an input sequence to an output sequence that is a complex function of the entire input sequence. Indeed,
in machine translation, the words of the target language don’t necessarily agree with
the words of the source language in number or order. Consider translating the fol-
lowing made-up English sentence into Japanese.

(13.1) English:  He wrote a letter to a friend

Japanese:  tomodachi ni tegami-o kaita
friend to letter wrote

Note that the elements of the sentences are in very different places in the different
languages. In English, the verb is in the middle of the sentence, while in Japanese,
the verb kaita comes at the end. The Japanese sentence doesn’t require the pronoun
he, while English does.

Such differences between languages can be quite complex. In the following ac-
tual sentence from the United Nations, notice the many changes between the Chinese
sentence (we’ve given in red a word-by-word gloss of the Chinese characters) and
its English equivalent produced by human translators.

(13.2) 大会/General Assembly 在/on 1982年/1982 12月/December 10日/10 通过了/adopted 第37号/37th 决议/resolution，核准了/approved 第二
次/second 探索/exploration 及/and 和平/peaceful 利用/fusing 外层空间/outer space 会议/conference 的/of 各项/ various 建议/suggestions

On 10 December 1982, the General Assembly adopted resolution 37 in
which it endorsed the recommendations of the Second United Nations
Conference on the Exploration and Peaceful Uses of Outer Space.

Note the many ways the English and Chinese differ. For example the order-
ding differs in major ways; the Chinese order of the noun phrase is “peaceful using
outer space conference of suggestions” while the English has “suggestions of the ...
conference on peaceful use of outer space”). And the order differs in minor ways
(the date is ordered differently). English requires the in many places that Chinese
doesn’t, and adds some details (like “in which” and “it”) that aren’t necessary in
Chinese. Chinese doesn’t grammatically mark plurality on nouns (unlike English,
which has the “-s” in “recommendations”), and so the Chinese must use the modi-
ifier 各项/ various to make it clear that there is not just one recommendation. English
capitalizes some words but not others. Encoder-decoder networks are very success-
ful at handling these sorts of complicated cases of sequence mappings.

We’ll begin in the next section by considering the linguistic background about
how languages vary, and the implications this variance has for the task of MT. Then
we’ll sketch out the standard algorithm, give details about things like input tokeniza-
tion and creating training corpora of parallel sentences, give some more low-level
details about the encoder-decoder network, and finally discuss how MT is evaluated,
introducing the simple chrF metric.

13.1 Language Divergences and Typology

There are about 7,000 languages in the world. Some aspects of human language
seem to be universal, holding true for every one of these languages, or are statistical
universals, holding true for most of these languages. Many universals arise from the
functional role of language as a communicative system by humans. Every language,
for example, seems to have words for referring to people, for talking about eating and
drinking, for being polite or not. There are also structural linguistic universals; for example, every language seems to have nouns and verbs (Chapter 8), has ways to ask questions, or issue commands, has linguistic mechanisms for indicating agreement or disagreement.

Yet languages also differ in many ways (as has been pointed out since ancient times; see Fig. 13.1). Understanding what causes such translation divergences (Dorr, 1994) can help us build better MT models. We often distinguish the idiosyncratic and lexical differences that must be dealt with one by one (the word for “dog” differs wildly from language to language), from systematic differences that we can model in a general way (many languages put the verb before the grammatical object; others put the verb after the grammatical object). The study of these systematic cross-linguistic similarities and differences is called linguistic typology. This section sketches some typological facts that impact machine translation; the interested reader should also look into WALS, the World Atlas of Language Structures, which gives many typological facts about languages (Dryer and Haspelmath, 2013).

### 13.1.1 Word Order Typology

As we hinted at in our example above comparing English and Japanese, languages differ in the basic word order of verbs, subjects, and objects in simple declarative clauses. German, French, English, and Mandarin, for example, are all SVO (Subject-Verb-Object) languages, meaning that the verb tends to come between the subject and object. Hindi and Japanese, by contrast, are SOV languages, meaning that the verb tends to come at the end of basic clauses, and Irish and Arabic are VSO languages. Two languages that share their basic word order type often have other similarities. For example, VO languages generally have prepositions, whereas OV languages generally have postpositions.
Let’s look in more detail at the example we saw above. In this SVO English sentence, the verb *wrote* is followed by its object *a letter* and the prepositional phrase *to a friend*, in which the preposition *to* is followed by its argument *a friend*. Arabic, with a VSO order, also has the verb before the object and prepositions. By contrast, in the Japanese example that follows, each of these orderings is reversed; the verb is *preceded* by its arguments, and the postposition follows its argument.

(13.3) **English:** He wrote a letter to a friend  
**Japanese:** tomodachi ni tegami-o kaita  
**Arabic:** katabt risāla li ṣadq  
   wrote  letter  to  friend

Other kinds of ordering preferences vary idiosyncratically from language to language. In some SVO languages (like English and Mandarin) adjectives tend to appear before nouns, while in others languages like Spanish and Modern Hebrew, adjectives appear after the noun:

(13.4) **Spanish** bruja verde **English** green witch

Fig. 13.2 shows examples of other word order differences. All of these word order differences between languages can cause problems for translation, requiring the system to do huge structural reorderings as it generates the output.

13.1.2 Lexical Divergences

Of course we also need to translate the individual words from one language to another. For any translation, the appropriate word can vary depending on the context. The English source-language word *bass*, for example, can appear in Spanish as the fish *lubina* or the musical instrument *bajo*. German uses two distinct words for what in English would be called a *wall*: *Wand* for walls inside a building, and *Mauer* for walls outside a building. Where English uses the word *brother* for any male sibling, Chinese and many other languages have distinct words for *older brother* (Mandarin *gege*) and *younger brother* (*didi*). In all these cases, translating *bass, wall, or brother* from English would require a kind of specialization, disambiguating the different uses of a word. For this reason the fields of MT and Word Sense Disambiguation (Chapter 23) are closely linked.

Sometimes one language places more grammatical constraints on word choice than another. We saw above that English marks nouns for whether they are singular or plural. Mandarin doesn’t. Or French and Spanish, for example, mark grammatical gender on adjectives, so an English translation into French requires specifying adjective gender.
The way that languages differ in lexically dividing up conceptual space may be more complex than this one-to-many translation problem, leading to many-to-many mappings. For example, Fig. 13.3 summarizes some of the complexities discussed by Hutchins and Somers (1992) in translating English *leg*, *foot*, and *paw*, to French. For example, when *leg* is used about an animal it’s translated as French *jambe*; but about the leg of a journey, as French *etape*; if the leg is of a chair, we use French *pied*.

Further, one language may have a **lexical gap**, where no word or phrase, short of an explanatory footnote, can express the exact meaning of a word in the other language. For example, English does not have a word that corresponds neatly to Mandarin *xiăo* or Japanese *oyakō* (in English one has to make do with awkward phrases like *filial piety* or *loving child*, or *good son/daughter* for both).

![Figure 13.3](image)

**Figure 13.3** The complex overlap between English *leg*, *foot*, etc., and various French translations as discussed by Hutchins and Somers (1992).

Finally, languages differ systematically in how the conceptual properties of an event are mapped onto specific words. Talmy (1985, 1991) noted that languages can be characterized by whether direction of motion and manner of motion are marked on the verb or on the “satellites”: particles, prepositional phrases, or adverbial phrases. For example, a bottle floating out of a cave would be described in English with the direction marked on the particle *out*, while in Spanish the direction would be marked on the verb:

(13.5) English: *The bottle floated out.*

Spanish: La botella salió flotando.

The bottle exited floating.

**Verb-framed** languages mark the direction of motion on the verb (leaving the satellites to mark the manner of motion), like Spanish *acercar* ‘approach’, *alcanzar* ‘reach’, *entrar* ‘enter’, *salir* ‘exit’. **Satellite-framed** languages mark the direction of motion on the satellite (leaving the verb to mark the manner of motion), like English *crawl out*, *float off*, *jump down*, *run after*. Languages like Japanese, Tamil, and the many languages in the Romance, Semitic, and Mayan languages families, are verb-framed; Chinese as well as non-Romance Indo-European languages like English, Swedish, Russian, Hindi, and Farsi are satellite framed (Talmy 1991, Slobin 1996).

### 13.1.3 Morphological Typology

**Morphologically**, languages are often characterized along two dimensions of variation. The first is the number of morphemes per word, ranging from **isolating** languages like Vietnamese and Cantonese, in which each word generally has one morpheme, to **polysynthetic** languages like Siberian Yupik ("Eskimo"), in which a single word may have very many morphemes, corresponding to a whole sentence in
English. The second dimension is the degree to which morphemes are segmentable, ranging from agglutinative languages like Turkish, in which morphemes have relatively clean boundaries, to fusion languages like Russian, in which a single affix may conflate multiple morphemes, like -om in the word stolom (table-SG-INSTR-DECL1), which fuses the distinct morphological categories instrumental, singular, and first declension.

Translating between languages with rich morphology requires dealing with structure below the word level, and for this reason modern systems generally use subword models like the wordpiece or BPE models of Section 13.2.1.

13.1.4 Referential density

Finally, languages vary along a typological dimension related to the things they tend to omit. Some languages, like English, require that we use an explicit pronoun when talking about a referent that is given in the discourse. In other languages, however, we can sometimes omit pronouns altogether, as the following example from Spanish shows:

(13.6) [El jefe] dio con un libro. 0 Mostró su hallazgo a un descifrador ambulante.

[The boss] came upon a book. [He] showed his find to a wandering decoder.

Languages that can omit pronouns are called pro-drop languages. Even among the pro-drop languages, there are marked differences in frequencies of omission. Japanese and Chinese, for example, tend to omit far more than does Spanish. This dimension of variation across languages is called the dimension of referential density. We say that languages that tend to use more pronouns are more referentially dense than those that use more zeros. Referentially sparse languages, like Chinese or Japanese, that require the hearer to do more inferential work to recover antecedents are also called cold languages. Languages that are more explicit and make it easier for the hearer are called hot languages. The terms hot and cold are borrowed from Marshall McLuhan’s 1964 distinction between hot media like movies, which fill in many details for the viewer, versus cold media like comics, which require the reader to do more inferential work to fill out the representation (Bickel, 2003).

Translating from languages with extensive pro-drop, like Chinese or Japanese, to non-pro-drop languages like English can be difficult since the model must somehow identify each zero and recover who or what is being talked about in order to insert the proper pronoun.

13.2 Machine Translation using Encoder-Decoder

The standard architecture for MT is the encoder-decoder transformer or sequence-to-sequence model, an architecture we saw for RNNs in Chapter 9. We’ll see the details of how to apply this architecture to transformers in Section 13.3, but first let’s talk about the overall task.

Most machine translation tasks make the simplification that we can translate each sentence independently, so we’ll just consider individual sentences for now. Given a sentence in a source language, the MT task is then to generate a corresponding sentence in a target language. For example, an MT system is given an English sentence like

1 Here we use the θ-notation; we’ll introduce this and discuss this issue further in Chapter 26
The green witch arrived
and must translate it into the Spanish sentence:

Llegó la bruja verde

MT uses supervised machine learning: at training time the system is given a large set of parallel sentences (each sentence in a source language matched with a sentence in the target language), and learns to map source sentences into target sentences. In practice, rather than using words (as in the example above), we split the sentences into a sequence of subword tokens (tokens can be words, or subwords, or individual characters). The systems are then trained to maximize the probability of the sequence of tokens in the target language $y_1, \ldots, y_m$ given the sequence of tokens in the source language $x_1, \ldots, x_n$:

$$P(y_1, \ldots, y_m|x_1, \ldots, x_n)$$ (13.7)

Rather than use the input tokens directly, the encoder-decoder architecture consists of two components, an encoder and a decoder. The encoder takes the input words $x = [x_1, \ldots, x_n]$ and produces an intermediate context $h$. At decoding time, the system takes $h$ and, word by word, generates the output $y$:

$$h = \text{encoder}(x)$$ (13.8)

$$y_{i+1} = \text{decoder}(h, y_1, \ldots, y_i) \quad \forall i \in [1, \ldots, m]$$ (13.9)

In the next two sections we’ll talk about subword tokenization, and then how to get parallel corpora for training, and then we’ll introduce the details of the encoder-decoder architecture.

### 13.2.1 Tokenization

Machine translation systems use a vocabulary that is fixed in advance, and rather than using space-separated words, this vocabulary is generated with subword tokenization algorithms, like the BPE algorithm sketched in Chapter 2. A shared vocabulary is used for the source and target languages, which makes it easy to copy tokens (like names) from source to target. Using subword tokenization with tokens shared between languages makes it natural to translate between languages like English or Hindi that use spaces to separate words, and languages like Chinese or Thai that don’t.

We build the vocabulary by running a subword tokenization algorithm on a corpus that contains both source and target language data.

Rather than the simple BPE algorithm from Fig. 2.13, modern systems often use more powerful tokenization algorithms. Some systems (like BERT) use a variant of BPE called the wordpiece algorithm, which instead of choosing the most frequent set of tokens to merge, chooses merges based on which one most increases the language model probability of the tokenization. Wordpieces use a special symbol at the beginning of each token; here’s a resulting tokenization from the Google MT system (Wu et al., 2016):

- **words**: Jet makers feud over seat width with big orders at stake
- **wordpieces**: J et _makers _fe ud _over _seat _width _with _big _orders _at _stake

The wordpiece algorithm is given a training corpus and a desired vocabulary size $V$, and proceeds as follows:
1. Initialize the wordpiece lexicon with characters (for example a subset of Unicode characters, collapsing all the remaining characters to a special unknown character token).

2. Repeat until there are V wordpieces:
   (a) Train an n-gram language model on the training corpus, using the current set of wordpieces.
   (b) Consider the set of possible new wordpieces made by concatenating two wordpieces from the current lexicon. Choose the one new wordpiece that most increases the language model probability of the training corpus.

Recall that with BPE we had to specify the number of merges to perform; in wordpiece, by contrast, we specify the total vocabulary, which is a more intuitive parameter. A vocabulary of 8K to 32K word pieces is commonly used.

An even more commonly used tokenization algorithm is (somewhat ambiguously) called the unigram algorithm (Kudo, 2018) or sometimes the SentencePiece algorithm, and is used in systems like ALBERT (Lan et al., 2020) and T5 (Raffel et al., 2020). (Because unigram is the default tokenization algorithm used in a library called SentencePiece that adds a useful wrapper around tokenization algorithms (Kudo and Richardson, 2018b), authors often say they are using SentencePiece tokenization but really mean they are using the unigram algorithm).

In unigram tokenization, instead of building up a vocabulary by merging tokens, we start with a huge vocabulary of every individual unicode character plus all frequent sequences of characters (including all space-separated words, for languages with spaces), and iteratively remove some tokens to get to a desired final vocabulary size. The algorithm is complex (involving suffix-trees for efficiently storing many tokens, and the EM algorithm for iteratively assigning probabilities to tokens), so we don’t give it here, but see Kudo (2018) and Kudo and Richardson (2018b). Roughly speaking the algorithm proceeds iteratively by estimating the probability of each token, tokenizing the input data using various tokenizations, then removing a percentage of tokens that don’t occur in high-probability tokenization, and then iterates until the vocabulary has been reduced down to the desired number of tokens.

Why does unigram tokenization work better than BPE? BPE tends to creates lots of very small non-meaningful tokens (because BPE can only create larger words or morphemes by merging characters one at a time), and it also tends to merge very common tokens, like the suffix ed, onto their neighbors. We can see from these examples from Bostrom and Durrett (2020) that unigram tends to produce tokens that are more semantically meaningful:

<table>
<thead>
<tr>
<th>Original:</th>
<th>Unigram:</th>
</tr>
</thead>
<tbody>
<tr>
<td>corrupted</td>
<td>corrupt ed</td>
</tr>
<tr>
<td>BPE: cor rupted</td>
<td>BPE: Complete tely prep ost erous suggest ions</td>
</tr>
<tr>
<td>Unigram: corrupt ed</td>
<td>Unigram: Complete ly pre post er ous suggestion s</td>
</tr>
</tbody>
</table>

13.2.2 Creating the Training data

Machine translation models are trained on a parallel corpus, sometimes called a bitext, a text that appears in two (or more) languages. Large numbers of parallel corpora are available. Some are governmental; the Europarl corpus (Koehn, 2005), extracted from the proceedings of the European Parliament, contains between 400,000 and 2 million sentences each from 21 European languages. The United Nations Parallel Corpus contains on the order of 10 million sentences in the six official languages of the United Nations (Arabic, Chinese, English, French, Russian, Spanish) Ziemski et al. (2016). Other parallel corpora have been made from movie and
13.2 • Machine Translation using Encoder-Decoder

TV subtitles, like the OpenSubtitles corpus (Lison and Tiedemann, 2016), or from general web text, like the ParaCrawl corpus of 223 million sentence pairs between 23 EU languages and English extracted from the CommonCrawl (Banón et al. 2020).

Sentence alignment

Standard training corpora for MT come as aligned pairs of sentences. When creating new corpora, for example for underresourced languages or new domains, these sentence alignments must be created. Fig. 13.4 gives a sample hypothetical sentence alignment.

Given two documents that are translations of each other, we generally need two steps to produce sentence alignments:

- a cost function that takes a span of source sentences and a span of target sentences and returns a score measuring how likely these spans are to be translations.
- an alignment algorithm that takes these scores to find a good alignment between the documents.

To score the similarity of sentences across languages, we need to make use of a **multilingual embedding space**, in which sentences from different languages are in the same embedding space (Artetxe and Schwenk, 2019). Given such a space, cosine similarity of such embeddings provides a natural scoring function (Schwenk, 2018). Thompson and Koehn (2019) give the following cost function between two sentences or spans $x, y$ from the source and target documents respectively:

$$
c(x, y) = \frac{(1 - \cos(x, y)) \cdot \text{nSents}(x) \cdot \text{nSents}(y)}{\sum_{i=1}^{n} 1 - \cos(x, i) + \sum_{i=1}^{n} 1 - \cos(x, i)}
$$

(13.10)

where nSents() gives the number of sentences (this biases the metric toward many alignments of single sentences instead of aligning very large spans). The denominator helps to normalize the similarities, and so $x_1, ..., x_n, y_1, ..., y_n$, are randomly selected sentences sampled from the respective documents.

Usually dynamic programming is used as the alignment algorithm (Gale and Church, 1993), in a simple extension of the minimum edit distance algorithm we introduced in Chapter 2.

| E1: “Good morning,” said the little prince. | F1: -Bonjour, dit le petit prince. |
| E2: “Good morning,” said the merchant. | F2: -Bonjour, dit le marchand de pilules perfectionnées qui apaisent la soif. |
| E3: This was a merchant who sold pills that had been perfected to quench thirst. | F3: On en avale une par semaine et l'on n'éprouve plus le besoin de boire. |
| E4: You just swallow one pill a week and you won't feel the need for anything to drink. | F4: -C’est une grosse économie de temps, dit le marchand. |
| E5: “They save a huge amount of time,” said the merchant. | F5: Les experts ont fait des calculs. |
| E7: “If I had fifty–three minutes to spend?” said the little prince to himself. | F7: “Moi, se dit le petit prince, si j’avais cinquante-trois minutes à dépenser, je marcherais tout doucement vers une fontaine...” |
| E8: “I would take a stroll to a spring of fresh water” | |

Figure 13.4 A sample alignment between sentences in English and French, with sentences extracted from Antoine de Saint-Exupery’s Le Petit Prince and a hypothetical translation. Sentence alignment takes sentences $e_1, ..., e_n$, and $f_1, ..., f_n$ and finds minimal sets of sentences that are translations of each other, including single sentence mappings like $(e_1, f_1)$, $(e_4, f_4)$, $(e_5, f_5)$, $(e_6, f_6)$ as well as 2-1 alignments $(e_2/e_3, f_2)$, $(e_7/e_8, f_7)$, and null alignments $(f_5)$.
Finally, it’s helpful to do some corpus cleanup by removing noisy sentence pairs. This can involve handwritten rules to remove low-precision pairs (for example removing sentences that are too long, too short, have different URLs, or even pairs that are too similar, suggesting that they were copies rather than translations). Or pairs can be ranked by their multilingual embedding cosine score and low-scoring pairs discarded.

### 13.3 Details of the Encoder-Decoder Model

The standard architecture for MT is the encoder-decoder transformer. The encoder-decoder architecture was introduced already for RNNs in Chapter 9, and the transformer version has the same idea. Fig. 13.5 shows the intuition of the architecture at a high level. You’ll see that the encoder-decoder architecture is made up of two transformers: an **encoder**, which is the same as the basic transformers from Chapter 10, and a **decoder**, which is augmented with a special new layer called the **cross-attention** layer. The encoder takes the source language input words \( X = x_1, \ldots, x_T \) and maps them to an output representation \( H^{enc} = h_1, \ldots, h_T \); usually via \( N = 6 \) stacked encoder blocks.

The decoder is essentially a conditional language model that attends to the encoder representation and generates the target words one by one, at each timestep conditioning on the source sentence and the previously generated target language words to generate a token. Decoding can use any of the decoding methods discussed in Chapter 10 like greedy, or temperature or nucleus sampling. But the most common decoding algorithm for MT is the beam search algorithm that we’ll introduce in Section 13.4.

But the components of the architecture differ somewhat from the RNN and also from the transformer block we’ve seen. First, in order to attend to the source language, the transformer blocks in the decoder have an extra **cross-attention** layer. Recall that the transformer block of Chapter 10 consists of a self-attention layer that attends to the input from the previous layer, followed by layer norm, a feed forward layer, and another layer norm. The decoder transformer block includes an extra layer with a special kind of attention, **cross-attention** (also sometimes called **encoder-decoder attention** or **source attention**). Cross-attention has the same form as the multi-headed self-attention in a normal transformer block, except that while
the queries as usual come from the previous layer of the decoder, the keys and values come from the output of the encoder.

![Diagram](image.png)

**Figure 13.6** The transformer block for the encoder and the decoder. The final output of the encoder $H^{e_{nc}} = h_1, \ldots, h_T$ is the context used in the decoder. The decoder is a standard transformer except with one extra layer, the cross-attention layer, which takes that decoder output $H^{e_{nc}}$ and uses it to form its $K$ and $V$ inputs.

That is, the final output of the encoder $H^{e_{nc}} = h_1, \ldots, h_T$ is multiplied by the cross-attention layer’s key weights $W^K$ and value weights $W^V$, but the output from the prior decoder layer $H^{d_{ec}[i-1]}$ is multiplied by the cross-attention layer’s query weights $W^Q$:

$$Q = W^Q H^{d_{ec}[i-1]}; \quad K = W^K H^{e_{nc}}; \quad V = W^V H^{e_{nc}}$$  \hspace{1cm} (13.11)

$$\text{CrossAttention}(Q, K, V) = \text{softmax} \left( \frac{QK^T}{\sqrt{d_k}} \right) V$$  \hspace{1cm} (13.12)

The cross attention thus allows the decoder to attend to each of the source language words as projected into the entire encoder final output representations. The other attention layer in each decoder block, the self-attention layer, is the same causal (left-to-right) self-attention that we saw in Chapter 9. The self-attention in the encoder, however, is allowed to look ahead at the entire source language text.

To train an encoder-decoder model, we use the same self-supervision model we used for training encoder-decoders RNNs in Chapter 9. The network is given the source text and then starting with the separator token is trained autoregressively to predict the next token $y_t$, using cross-entropy loss:

$$L_{CE}(\hat{y}_t, y_t) = -\log \hat{y}_t[w_{t+1}]$$  \hspace{1cm} (13.13)
As in that case, we use teacher forcing in the decoder. Recall that in teacher forcing, at each time step in decoding we force the system to use the gold target token from training as the next input $x_{t+1}$, rather than allowing it to rely on the (possibly erroneous) decoder output $\hat{y}_t$.

### 13.4 Decoding in MT: Beam Search

Recall the greedy decoding algorithm from Chapter 10: at each time step $t$ in generation, the output $y_t$ is chosen by computing the probability for each word in the vocabulary and then choosing the highest probability word (the argmax):

$$\hat{w}_t = \arg\max_{w \in V} P(w|w_{<t})$$

A problem with greedy decoding is that what looks high probability at word $t$ might turn out to have been the wrong choice once we get to word $t+1$. The beam search algorithm maintains multiple choices until later when we can see which one is best.

In beam search we model decoding as searching the space of possible generations, represented as a search tree whose branches represent actions (generating a token), and nodes represent states (having generated a particular prefix). We search for the best action sequence, i.e., the string with the highest probability.

#### An illustration of the problem

Fig. 13.7 shows a made-up example. The most probable sequence is *ok ok EOS* (its probability is $0.4 \times 0.7 \times 1.0$). But greedy search doesn’t find it, incorrectly choosing *yes* as the first word since it has the highest local probability (0.5).

![Search Tree](image)

**Figure 13.7** A search tree for generating the target string $T = t_1, t_2, \ldots$ from vocabulary $V = \{\text{yes, ok, <s>}\}$, showing the probability of generating each token from that state. Greedy search chooses *yes* followed by *yes*, instead of the globally most probable sequence *ok ok*.

Recall from Chapter 8 that for part-of-speech tagging we used dynamic programming search (the Viterbi algorithm) to address this problem. Unfortunately, dynamic programming is not applicable to generation problems with long-distance dependencies between the output decisions. The only method guaranteed to find the best solution is exhaustive search: computing the probability of every one of the $V^T$ possible sentences (for some length value $T$) which is obviously too slow.
The solution: beam search

Instead, MT systems generally decode using beam search, a heuristic search method first proposed by Lowerre (1976). In beam search, instead of choosing the best token to generate at each timestep, we keep \( k \) possible tokens at each step. This fixed-size memory footprint \( k \) is called the beam width, on the metaphor of a flashlight beam that can be parameterized to be wider or narrower.

Thus at the first step of decoding, we compute a softmax over the entire vocabulary, assigning a probability to each word. We then select the \( k \)-best options from this softmax output. These initial \( k \) outputs are the search frontier and these \( k \) initial words are called hypotheses. A hypothesis is an output sequence, a translation-so-far, together with its probability.

At subsequent steps, each of the \( k \) best hypotheses is extended incrementally by being passed to distinct decoders, which each generate a softmax over the entire vocabulary to extend the hypothesis to every possible next token. Each of these \( k \times V \) hypotheses is scored by \( P(y_i|x,y_{<i}) \): the product of the probability of the current word choice multiplied by the probability of the path that led to it. We then prune the \( k \times V \) hypotheses down to the \( k \) best hypotheses, so there are never more than \( k \)
hypotheses at the frontier of the search, and never more than \(k\) decoders. Fig. 13.8 illustrates this with a beam width of 2 for the beginning of *The green witch arrived*.

This process continues until an EOS is generated indicating that a complete candidate output has been found. At this point, the completed hypothesis is removed from the frontier and the size of the beam is reduced by one. The search continues until the beam has been reduced to 0. The result will be \(k\) hypotheses.

To score each node by its log probability, we use the chain rule of probability to break down \(p(y | x)\) into the product of the probability of each word given its prior context, which we can turn into a sum of logs (for an output string of length \(t\)):

\[
score(y) = \log P(y | x) = \log \left( P(y_1 | x) P(y_2 | y_1, x) P(y_3 | y_1, y_2, x) \cdots P(y_t | y_1, \ldots, y_{t-1}, x) \right)
= \sum_{i=1}^{t} \log P(y_i | y_1, \ldots, y_{i-1}, x) \tag{13.15}
\]

Thus at each step, to compute the probability of a partial sentence, we simply add the log probability of the prefix sentence so far to the log probability of generating the next token. Fig. 13.9 shows the scoring for the example sentence shown in Fig. 13.8, using some simple made-up probabilities. Log probabilities are negative or 0, and the max of two log probabilities is the one that is greater (closer to 0).

Fig. 13.10 gives the algorithm. One problem with this version of the algorithm is that the completed hypotheses may have different lengths. Because language models generally assign lower probabilities to longer strings, a naive algorithm would choose shorter strings for \(y\). (This is not an issue during the earlier steps of decoding; since beam search is breadth-first, all the hypotheses being compared had the same length.) For this reason we often apply length normalization methods, like...
function \textsc{BeamDecode}(c, beam\_width) \textbf{returns} best paths

\begin{verbatim}
\begin{align*}
y_0, h_0 &\leftarrow 0 \\
path &\leftarrow () \\
\text{complete\_paths} &\leftarrow () \\
state &\leftarrow (c, y_0, h_0, \text{path}) \\
f\text{frontier} &\leftarrow \langle \text{state} \rangle \\
while & \text{frontier contains incomplete paths and beamwidth > 0} \\
& \text{extended\_frontier} &\leftarrow () \\
& \text{for each} \ state &\in \text{frontier} \do \\
& y &\leftarrow \textsc{Decode}(\text{state}) \\
& \text{for each word} \ i &\in \text{Vocabulary} \do \\
& \text{successor} &\leftarrow \textsc{NewState}(\text{state}, i, y) \\
& \text{extended\_frontier} &\leftarrow \textsc{AddToBeam}(\text{successor, extended\_frontier, beam\_width}) \\
& \text{for each} \ state &\in \text{extended\_frontier} \do \\
& &\text{if state is complete} \do \\
& &\text{complete\_paths} &\leftarrow \textsc{Append}(\text{complete\_paths, state}) \\
& &\text{extended\_frontier} &\leftarrow \textsc{Remove}(\text{extended\_frontier, state}) \\
& &\text{beam\_width} &\leftarrow \text{beam\_width} - 1 \\
& &\text{frontier} &\leftarrow \text{extended\_frontier} \\
& return &\text{complete\_paths} \\
\end{align*}
\end{verbatim}

\begin{verbatim}
function \textsc{NewState}(state, word, word\_prob) \textbf{returns} new state

function \textsc{AddToBeam}(state, frontier, width) \textbf{returns} updated frontier

\begin{verbatim}
\begin{align*}
& \text{if} \ \text{Length}(\text{frontier}) < \text{width} \ \text{then} \\
& \ \text{frontier} &\leftarrow \textsc{Insert}(\text{state, frontier}) \\
& \text{else if} &\ \text{Score}(\text{state}) > \text{Score}(\text{WorstOf}(\text{frontier})) \\
& \ \text{frontier} &\leftarrow \textsc{Remove}(\text{WorstOf}(\text{frontier})) \\
& \ \text{frontier} &\leftarrow \textsc{Insert}(\text{state, frontier}) \\
& return &\text{frontier} \\
\end{align*}
\end{verbatim}
\end{verbatim}

For MT we generally use beam widths \( k \) between 5 and 10, giving us \( k \) hypotheses at the end. We can pass all \( k \) to the downstream application with their respective scores, or if we just need a single translation we can pass the most probable hypothesis.

\subsection{Minimum Bayes Risk Decoding}

Minimum Bayes risk or MBR decoding is an alternative decoding algorithm that can work even better than beam search and also tends to be better than the other decoding algorithms like temperature sampling introduced in Section 10.8.

The intuition of minimum Bayes risk is that instead of trying to choose the translation which is most probable, we choose the one that is likely have the least error.
For example, we might want our decoding algorithm to find the translation which has the highest score on some evaluation metric. For example in Section 13.6 we will introduce metrics like chrF or BERTScore that measure the goodness-of-fit between a candidate translation and a set of reference human translations. A translation that maximizes this score, especially with a hypothetically huge set of perfect human translations is likely to be a good one (have minimum risk) even if it is not the most probable translation by our particular probability estimator.

In practice, we don’t know the perfect set of translations for a given sentence. So the standard simplification used in MBR decoding algorithms is to instead choose the candidate translation which is most similar (by some measure of goodness-of-fit) with some set of candidate translations. We’re essentially approximating the enormous space of all possible translations \( \mathcal{U} \) with a smaller set of possible candidate translations \( \mathcal{Y} \).

Given this set of possible candidate translations \( \mathcal{Y} \), and some similarity or alignment function \( \text{util} \), we choose the best translation \( \hat{y} \) as the translation which is most similar to all the other candidate translations:

\[
\hat{y} = \arg\max_{y \in \mathcal{Y}} \sum_{c \in \mathcal{Y}} \text{util}(y, c) \tag{13.17}
\]

Various \( \text{util} \) functions can be used, like chrF or BERTscore or BLEU. We can get the set of candidate translations by sampling using one of the basic sampling algorithms of Section 10.8 like temperature sampling; good results can be obtained with as few as 32 or 64 candidates.

Minimum Bayes risk decoding can also be used for other NLP tasks; indeed it was widely applied to speech recognition (Stolcke et al., 1997; Goel and Byrne, 2000) before being applied to machine translation (Kumar and Byrne, 2004), and has been shown to work well across many other generation tasks as well (e.g., summarization, dialogue, and image captioning (Suzgun et al., 2023)).

### 13.5 Translating in low-resource situations

For some languages, and especially for English, online resources are widely available. There are many large parallel corpora that contain translations between English and many languages. But the vast majority of the world’s languages do not have large parallel training texts available. An important ongoing research question is how to get good translation with lesser resourced languages. The resource problem can even be true for high resource languages when we need to translate into low resource domains (for example in a particular genre that happens to have very little bitext).

Here we briefly introduce two commonly used approaches for dealing with this data sparsity: backtranslation, which is a special case of the general statistical technique called data augmentation, and multilingual models, and also discuss some socio-technical issues.

#### 13.5.1 Data Augmentation

Data augmentation is a statistical technique for dealing with insufficient training data, by adding new synthetic data that is generated from the current natural data.
13.5 Translating in low-resource situations

The most common data augmentation technique for machine translation is called **backtranslation**. Backtranslation relies on the intuition that while parallel corpora may be limited for particular languages or domains, we can often find a large (or at least larger) monolingual corpus, to add to the smaller parallel corpora that are available. The algorithm makes use of monolingual corpora in the target language by creating synthetic bitexts.

In backtranslation, our goal is to improve source-to-target MT, given a small parallel text (a bitext) in the source/target languages, and some monolingual data in the target language. We first use the bitext to train a MT system in the reverse direction: a target-to-source MT system. We then use it to translate the monolingual target data to the source language. Now we can add this synthetic bitext (natural target sentences, aligned with MT-produced source sentences) to our training data, and retrain our source-to-target MT model. For example suppose we want to translate from Navajo to English but only have a small Navajo-English bitext, although of course we can find lots of monolingual English data. We use the small bitext to build an MT engine going the other way (from English to Navajo). Once we translate the monolingual English text to Navajo, we can add this synthetic Navajo/English bitext to our training data.

Backtranslation has various parameters. One is how we generate the backtranslated data; we can run the decoder in greedy inference, or use beam search. Or we can do sampling, like the temperature sampling algorithm we saw in Chapter 10. Another parameter is the ratio of backtranslated data to natural bitext data; we can choose to upsample the bitext data (include multiple copies of each sentence). In general backtranslation works surprisingly well; one estimate suggests that a system trained on backtranslated text gets about 2/3 of the gain as would training on the same amount of natural bitext (Edunov et al., 2018).

13.5.2 Multilingual models

The models we’ve described so far are for bilingual translation: one source language, one target language. It’s also possible to build a **multilingual** translator.

In a multilingual translator, we train the system by giving it parallel sentences in many different pairs of languages. That means we need to tell the system which language to translate from and to! We tell the system which language is which by adding a special token $l_s$ to the encoder specifying the source language we’re translating from, and a special token $l_t$ to the decoder telling it the target language we’d like to translate into.

Thus we slightly update Eq. 13.9 above to add these tokens in Eq. 13.19:

\[
\begin{align*}
  h &= \text{encoder}(x, l_s) \quad (13.18) \\
  y_{i+1} &= \text{decoder}(h, l_t, y_1, \ldots, y_i) \quad \forall i \in [1, \ldots, m] \quad (13.19)
\end{align*}
\]

One advantage of a multilingual model is that they can improve the translation of lower-resourced languages by drawing on information from a similar language in the training data that happens to have more resources. Perhaps we don’t know the meaning of a word in Galician, but the word appears in the similar and higher-resourced language Spanish.

13.5.3 Sociotechnical issues

Many issues in dealing with low-resource languages go beyond the purely technical. One problem is that for low-resource languages, especially from low-income
countries, native speakers are often not involved as the curators for content selection, as the language technologists, or as the evaluators who measure performance (∀ et al., 2020). Indeed, one well-known study that manually audited a large set of parallel corpora and other major multilingual datasets found that for many of the corpora, less than 50% of the sentences were of acceptable quality, with a lot of data consisting of repeated sentences with web boilerplate or incorrect translations, suggesting that native speakers may not have been sufficiently involved in the data process (Kreutzer et al., 2022).

Other issues, like the tendency of many MT approaches to focus on the case where one of the languages is English (Anastasopoulos and Neubig, 2020), have to do with allocation of resources. Where most large multilingual systems were trained on bitexts in which English was one of the two languages, recent huge corporate systems like those of Fan et al. (2021) and Costa-jussá et al. (2022) and datasets like Schwenk et al. (2021) attempt to handle large numbers of languages (up to 200 languages) and create bitexts between many more pairs of languages and not just through English.

At the smaller end, ∀ et al. (2020) propose a participatory design process to encourage content creators, curators, and language technologists who speak these low-resourced languages to participate in developing MT algorithms. They provide online groups, mentoring, and infrastructure, and report on a case study on developing MT algorithms for low-resource African languages. Among their conclusions was perform MT evaluation by post-editing rather than direct evaluation, since having labelers edit an MT system and then measure the distance between the MT output and its post-edited version both was simpler to train evaluators and makes it easier to measure true errors in the MT output and not differences due to linguistic variation (Bentivogli et al., 2018).

13.6 MT Evaluation

Translations are evaluated along two dimensions:

1. **adequacy**: how well the translation captures the exact meaning of the source sentence. Sometimes called faithfulness or fidelity.

2. **fluency**: how fluent the translation is in the target language (is it grammatical, clear, readable, natural).

Using humans to evaluate is most accurate, but automatic metrics are also used for convenience.

13.6.1 Using Human Raters to Evaluate MT

The most accurate evaluations use human raters, such as online crowdworkers, to evaluate each translation along the two dimensions. For example, along the dimension of fluency, we can ask how intelligible, how clear, how readable, or how natural the MT output (the target text) is. We can give the raters a scale, for example, from 1 (totally unintelligible) to 5 (totally intelligible), or 1 to 100, and ask them to rate each sentence or paragraph of the MT output.

We can do the same thing to judge the second dimension, adequacy, using raters to assign scores on a scale. If we have bilingual raters, we can give them the source sentence and a proposed target sentence, and rate, on a 5-point or 100-point scale,
how much of the information in the source was preserved in the target. If we only have monolingual raters but we have a good human translation of the source text, we can give the monolingual raters the human reference translation and a target machine translation and again rate how much information is preserved. An alternative is to do ranking: give the raters a pair of candidate translations, and ask them which one they prefer.

Training of human raters (who are often online crowdworkers) is essential; raters without translation expertise find it difficult to separate fluency and adequacy, and so training includes examples carefully distinguishing these. Raters often disagree (source sentences may be ambiguous, raters will have different world knowledge, raters may apply scales differently). It is therefore common to remove outlier raters, and (if we use a fine-grained enough scale) normalizing raters by subtracting the mean from their scores and dividing by the variance.

As discussed above, an alternative way of using human raters is to have them post-edit translations, taking the MT output and changing it minimally until they feel it represents a correct translation. The difference between their post-edited translations and the original MT output can then be used as a measure of quality.

13.6.2 Automatic Evaluation

While humans produce the best evaluations of machine translation output, running a human evaluation can be time consuming and expensive. For this reason automatic metrics are often used as temporary proxies. Automatic metrics are less accurate than human evaluation, but can help test potential system improvements, and even be used as an automatic loss function for training. In this section we introduce two families of such metrics, those based on character- or word-overlap and those based on embedding similarity.

Automatic Evaluation by Character Overlap: chrF

The simplest and most robust metric for MT evaluation is called chrF, which stands for character F-score (Popović, 2015). chrF (along with many other earlier related metrics like BLEU, METEOR, TER, and others) is based on a simple intuition derived from the pioneering work of Miller and Beebe-Center (1956): a good machine translation will tend to contain characters and words that occur in a human translation of the same sentence. Consider a test set from a parallel corpus, in which each source sentence has both a gold human target translation and a candidate MT translation we’d like to evaluate. The chrF metric ranks each MT target sentence by a function of the number of character n-gram overlaps with the human translation. Given the hypothesis and the reference, chrF is given a parameter \( k \) indicating the length of character n-grams to be considered, and computes the average of the \( k \) precisions (unigram precision, bigram, and so on) and the average of the \( k \) recalls (unigram recall, bigram recall, etc.):

\[
\text{chrP} \quad \text{percentage of character 1-grams, 2-grams, ...}, \ k \text{-grams in the hypothesis that occur in the reference, averaged.}
\]

\[
\text{chrR} \quad \text{percentage of character 1-grams, 2-grams, ...}, \ k \text{-grams in the reference that occur in the hypothesis, averaged.}
\]

The metric then computes an F-score by combining chrP and chrR using a weighting parameter \( \beta \). It is common to set \( \beta = 2 \), thus weighing recall twice as much as...
For \( \beta = 2 \), that would be:

\[
\text{chrF}_2 = \frac{5 \cdot \text{chrP} \cdot \text{chrR}}{4 \cdot \text{chrP} + \text{chrR}}
\]

For example, consider two hypotheses that we’d like to score against the reference translation \textit{witness for the past}. Here are the hypotheses along with chrF values computed using parameters \( k = \beta = 2 \) (in real examples, \( k \) would be a higher number like 6):

\[
\begin{align*}
\text{REF:} & \quad \text{witness for the past}, \\
\text{HYP1:} & \quad \text{witness of the past}, \quad \text{chrF}_{2,2} = .86 \\
\text{HYP2:} & \quad \text{past witness} \quad \text{chrF}_{2,2} = .62
\end{align*}
\]

Let’s see how we computed that chrF value for HYP1 (we’ll leave the computation of the chrF value for HYP2 as an exercise for the reader). First, chrF ignores spaces, so we’ll remove them from both the reference and hypothesis:

\[
\begin{align*}
\text{REF:} & \quad \text{witnessforthe past}, \quad (18 \text{ unigrams}, 17 \text{ bigrams}) \\
\text{HYP1:} & \quad \text{witnessofthepast}, \quad (17 \text{ unigrams}, 16 \text{ bigrams})
\end{align*}
\]

Next let’s see how many unigrams and bigrams match between the reference and hypothesis:

- unigrams that match: \textit{w i t n e s s f o t h e p a s t}, (17 unigrams)
- bigrams that match: \textit{w i t t n e s s f o t h e p a s t}, (13 bigrams)

We use that to compute the unigram and bigram precisions and recalls:

\[
\begin{align*}
\text{unigram P:} & \quad 17/17 = 1 \quad \text{unigram R:} \quad 17/18 = .944 \\
\text{bigram P:} & \quad 13/16 = .813 \quad \text{bigram R:} \quad 13/17 = .765
\end{align*}
\]

Finally we average to get chrP and chrR, and compute the F-score:

\[
\begin{align*}
\text{chrP} & = \frac{17/17 + 13/16}{2} = .906 \\
\text{chrR} & = \frac{17/18 + 13/17}{2} = .855 \\
\text{chrF}_{2,2} & = \frac{5 \cdot \text{chrP} \cdot \text{chrR}}{4 \cdot \text{chrP} + \text{chrR}} = .86
\end{align*}
\]

chrF is simple, robust, and correlates very well with human judgments in many languages (Kocmi et al., 2021).

**Alternative overlap metric: BLEU**

There are various alternative overlap metrics. For example, before the development of chrF, it was common to use a word-based overlap metric called \textbf{BLEU} (for BiLingual Evaluation Understudy), that is purely precision-based rather than combining precision and recall (Papineni et al., 2002). The BLEU score for a corpus of candidate translation sentences is a function of the \textbf{n-gram word precision} over all the sentences combined with a brevity penalty computed over the corpus as a whole.

What do we mean by n-gram precision? Consider a corpus composed of a single sentence. The unigram precision for this corpus is the percentage of unigram tokens
in the candidate translation that also occur in the reference translation, and ditto for bigrams and so on, up to 4-grams. BLEU extends this unigram metric to the whole corpus by computing the numerator as the sum over all sentences of the counts of all the unigram types that also occur in the reference translation, and the denominator is the total of the counts of all unigrams in all candidate sentences. We compute this n-gram precision for unigrams, bigrams, trigrams, and 4-grams and take the geometric mean. BLEU has many further complications, including a brevity penalty for penalizing candidate translations that are too short, and it also requires the n-gram counts be clipped in a particular way.

Because BLEU is a word-based metric, it is very sensitive to word tokenization, making it impossible to compare different systems if they rely on different tokenization standards, and doesn’t work as well in languages with complex morphology. Nonetheless, you will sometimes still see systems evaluated by BLEU, particularly for translation into English. In such cases it’s important to use packages that enforce standardization for tokenization like SACREBLEU (Post, 2018).

**Statistical Significance Testing for MT evals**

Character or word overlap-based metrics like chrF (or BLEU, or etc.) are mainly used to compare two systems, with the goal of answering questions like: did the new algorithm we just invented improve our MT system? To know if the difference between the chrF scores of two MT systems is a significant difference, we use the paired bootstrap test, or the similar randomization test.

To get a confidence interval on a single chrF score using the bootstrap test, recall from Section 4.9 that we take our test set (or devset) and create thousands of pseudo-testsets by repeatedly sampling with replacement from the original test set. We now compute the chrF score of each of the pseudo-testsets. If we drop the top 2.5% and bottom 2.5% of the scores, the remaining scores will give us the 95% confidence interval for the chrF score of our system.

To compare two MT systems A and B, we draw the same set of pseudo-testsets, and compute the chrF scores for each of them. We then compute the percentage of pseudo-test-sets in which A has a higher chrF score than B.

**chrF: Limitations**

While automatic character and word-overlap metrics like chrF or BLEU are useful, they have important limitations. chrF is very local: a large phrase that is moved around might barely change the chrF score at all, and chrF can’t evaluate cross-sentence properties of a document like its discourse coherence (Chapter 27). chrF and similar automatic metrics also do poorly at comparing very different kinds of systems, such as comparing human-aided translation against machine translation, or different machine translation architectures against each other (Callison-Burch et al., 2006). Instead, automatic overlap metrics like chrF are most appropriate when evaluating changes to a single system.

**13.6.3 Automatic Evaluation: Embedding-Based Methods**

The chrF metric is based on measuring the exact character n-grams a human reference and candidate machine translation have in common. However, this criterion is overly strict, since a good translation may use alternate words or paraphrases. A solution first pioneered in early metrics like METEOR (Banerjee and Lavie, 2005) was to allow synonyms to match between the reference \( x \) and candidate \( \tilde{x} \). More
recent metrics use BERT or other embeddings to implement this intuition.

For example, in some situations we might have datasets that have human assessments of translation quality. Such datasets consists of tuples \((x, \hat{x}, r)\), where \(x = (x_1, \ldots, x_n)\) is a reference translation, \(\hat{x} = (\hat{x}_1, \ldots, \hat{x}_m)\) is a candidate machine translation, and \(r \in \mathbb{R}\) is a human rating that expresses the quality of \(\hat{x}\) with respect to \(x\). Given such data, algorithms like COMET (Rei et al., 2020) BLEURT (Sellam et al., 2020) train a predictor on the human-labeled datasets, for example by passing \(x\) and \(\hat{x}\) through a version of BERT (trained with extra pretraining, and then fine-tuned on the human-labeled sentences), followed by a linear layer that is trained to predict \(r\). The output of such models correlates highly with human labels.

In other cases, however, we don’t have such human-labeled datasets. In that case we can measure the similarity of \(x\) and \(\hat{x}\) by the similarity of their embeddings. The BERTSCORE algorithm (Zhang et al., 2020) shown in Fig. 13.11, for example, passes the reference \(x\) and the candidate \(\hat{x}\) through BERT, computing a BERT embedding for each token \(x_i\) and \(\hat{x}_j\). Each pair of tokens \((x_i, \hat{x}_j)\) is scored by its cosine distance \(\frac{x_i \cdot \hat{x}_j}{|x_i||\hat{x}_j|}\). Each token in \(x\) is matched to a token in \(\hat{x}\) to compute recall, and each token in \(\hat{x}\) is matched to a token in \(x\) to compute precision (with each token greedily matched to the most similar token in the corresponding sentence). BERTSCORE provides precision and recall (and hence \(F_1\)):

\[
R_{\text{BERT}} = \frac{1}{|x|} \sum_{x_i \in x} \max_{\hat{x}_j \in \hat{x}} x_i \cdot \hat{x}_j \quad P_{\text{BERT}} = \frac{1}{|\hat{x}|} \sum_{\hat{x}_j \in \hat{x}} \max_{x_i \in x} x_i \cdot \hat{x}_j \quad (13.21)
\]

![Figure 13.11](image.png)

Figure 13.11 The computation of BERTSCORE recall from reference \(x\) and candidate \(\hat{x}\), from Figure 1 in Zhang et al. (2020). This version shows an extended version of the metric in which tokens are also weighted by their idf values.

### 13.7 Bias and Ethical Issues

Machine translation raises many of the same ethical issues that we’ve discussed in earlier chapters. For example, consider MT systems translating from Hungarian (which has the gender neutral pronoun \(\sigma\)) or Spanish (which often drops pronouns) into English (in which pronouns are obligatory, and they have grammatical gender). When translating a reference to a person described without specified gender, MT systems often default to male gender (Schiebinger 2014, Prates et al. 2019). And MT systems often assign gender according to culture stereotypes of the sort we saw in Section 6.11. Fig. 13.12 shows examples from Prates et al. (2019), in which Hungarian gender-neutral \(\sigma\) is a nurse is translated with she, but gender-neutral \(\sigma\) is a CEO is translated with he. Prates et al. (2019) find that these stereotypes can’t completely be accounted for by gender bias in US labor statistics, because the biases are...
amplified by MT systems, with pronouns being mapped to male or female gender with a probability higher than if the mapping was based on actual labor employment statistics.

<table>
<thead>
<tr>
<th>Hungarian (gender neutral) source</th>
<th>English MT output</th>
</tr>
</thead>
<tbody>
<tr>
<td>ö egy ápoló</td>
<td>she is a nurse</td>
</tr>
<tr>
<td>ö egy tudós</td>
<td>he is a scientist</td>
</tr>
<tr>
<td>ö egy mérnök</td>
<td>he is an engineer</td>
</tr>
<tr>
<td>ö egy pék</td>
<td>he is a baker</td>
</tr>
<tr>
<td>ö egy tanár</td>
<td>she is a teacher</td>
</tr>
<tr>
<td>ö egy esküvőszervező</td>
<td>she is a wedding organizer</td>
</tr>
<tr>
<td>ö egy vezérigazgató</td>
<td>he is a CEO</td>
</tr>
</tbody>
</table>

Similarly, a recent challenge set, the WinoMT dataset (Stanovsky et al., 2019) shows that MT systems perform worse when they are asked to translate sentences that describe people with non-stereotypical gender roles, like “The doctor asked the nurse to help her in the operation”.

Many ethical questions in MT require further research. One open problem is developing metrics for knowing what our systems don’t know. This is because MT systems can be used in urgent situations where human translators may be unavailable or delayed: in medical domains, to help translate when patients and doctors don’t speak the same language, or in legal domains, to help judges or lawyers communicate with witnesses or defendants. In order to ‘do no harm’, systems need ways to assign confidence values to candidate translations, so they can abstain from giving incorrect translations that may cause harm.

13.8 Summary

Machine translation is one of the most widely used applications of NLP, and the encoder-decoder model, first developed for MT is a key tool that has applications throughout NLP.

- Languages have divergences, both structural and lexical, that make translation difficult.
- The linguistic field of typology investigates some of these differences; languages can be classified by their position along typological dimensions like whether verbs precede their objects.
- Encoder-decoder networks (for transformers just as we saw in Chapter 9 for RNNs) are composed of an encoder network that takes an input sequence and creates a contextualized representation of it, the context. This context representation is then passed to a decoder which generates a task-specific output sequence.
- Cross-attention allows the transformer decoder to view information from all the hidden states of the encoder.
- Machine translation models are trained on a parallel corpus, sometimes called a bitext, a text that appears in two (or more) languages.
Backtranslation is a way of making use of monolingual corpora in the target language by running a pilot MT engine backwards to create synthetic bitexts. MT is evaluated by measuring a translation’s adequacy (how well it captures the meaning of the source sentence) and fluency (how fluent or natural it is in the target language). Human evaluation is the gold standard, but automatic evaluation metrics like chrF, which measure character n-gram overlap with human translations, or more recent metrics based on embedding similarity, are also commonly used.

Bibliographical and Historical Notes

MT was proposed seriously by the late 1940s, soon after the birth of the computer (Weaver, 1949/1955). In 1954, the first public demonstration of an MT system prototype (Dostert, 1955) led to great excitement in the press (Hutchins, 1997). The next decade saw a great flowering of ideas, prefiguring most subsequent developments. But this work was ahead of its time—implementations were limited by, for example, the fact that pending the development of disks there was no good way to store dictionary information.

As high-quality MT proved elusive (Bar-Hillel, 1960), there grew a consensus on the need for better evaluation and more basic research in the new fields of formal and computational linguistics. This consensus culminated in the famously critical ALPAC (Automatic Language Processing Advisory Committee) report of 1966 (Pierce et al., 1966) that led in the mid 1960s to a dramatic cut in funding for MT in the US. As MT research lost academic respectability, the Association for Machine Translation and Computational Linguistics dropped MT from its name. Some MT developers, however, persevered, and there were early MT systems like Météo, which translated weather forecasts from English to French (Chandioux, 1976), and industrial systems like Systran.

In the early years, the space of MT architectures spanned three general models. In direct translation, the system proceeds word-by-word through the source-language text, translating each word incrementally. Direct translation uses a large bilingual dictionary, each of whose entries is a small program with the job of translating one word. In transfer approaches, we first parse the input text and then apply rules to transform the source-language parse into a target language parse. We then generate the target language sentence from the parse tree. In interlingua approaches, we analyze the source language text into some abstract meaning representation, called an interlingua. We then generate into the target language from this interlingual representation. A common way to visualize these three early approaches was the Vauquois triangle shown in Fig. 13.13. The triangle shows the increasing depth of analysis required (on both the analysis and generation end) as we move from the direct approach through transfer approaches to interlingual approaches. In addition, it shows the decreasing amount of transfer knowledge needed as we move up the triangle, from huge amounts of transfer at the direct level (almost all knowledge is transfer knowledge for each word) through transfer (transfer rules only for parse trees or thematic roles) through interlingua (no specific transfer knowledge). We can view the encoder-decoder network as an interlingual approach, with attention acting as an integration of direct and transfer, allowing words or their representations to be directly accessed by the decoder.
Statistical methods began to be applied around 1990, enabled first by the development of large bilingual corpora like the Hansard corpus of the proceedings of the Canadian Parliament, which are kept in both French and English, and then by the growth of the Web. Early on, a number of researchers showed that it was possible to extract pairs of aligned sentences from bilingual corpora, using words or simple cues like sentence length (Kay and Röšcheisen 1988, Gale and Church 1991, Gale and Church 1993, Kay and Röšcheisen 1993).

At the same time, the IBM group, drawing directly on the noisy channel model for speech recognition, proposed two related paradigms for statistical MT. These include the generative algorithms that became known as IBM Models 1 through 5, implemented in the Candide system. The algorithms (except for the decoder) were published in full detail—encouraged by the US government who had partially funded the work—which gave them a huge impact on the research community (Brown et al. 1990, Brown et al. 1993).

The group also developed a discriminative approach, called MaxEnt (for maximum entropy, an alternative formulation of logistic regression), which allowed many features to be combined discriminatively rather than generatively (Berger et al., 1996), which was further developed by Och and Ney (2002).

By the turn of the century, most academic research on machine translation used statistical MT, either in the generative or discriminative mode. An extended version of the generative approach, called phrase-based translation was developed, based on inducing translations for phrase-pairs (Och 1998, Marcu and Wong 2002, Koehn et al. (2003), Och and Ney 2004, Deng and Byrne 2005, inter alia).

Once automatic metrics like BLEU were developed (Papineni et al., 2002), the discriminative log linear formulation (Och and Ney, 2004), drawing from the IBM MaxEnt work (Berger et al., 1996), was used to directly optimize evaluation metrics like BLEU in a method known as Minimum Error Rate Training, or MERT (Och, 2003), also drawing from speech recognition models (Chou et al., 1993). Toolkits like GIZA (Och and Ney, 2003) and Moses (Koehn et al. 2006, Zens and Ney 2007) were widely used.

There were also approaches around the turn of the century that were based on syntactic structure (Chapter 17). Models based on transduction grammars (also called synchronous grammars) assign a parallel syntactic tree structure to a pair of sentences in different languages, with the goal of translating the sentences by applying reordering operations on the trees. From a generative perspective, we can view a transduction grammar as generating pairs of aligned sentences in two languages. Some of the most widely used models included the inversion transduction grammar (Wu, 1996) and synchronous context-free grammars (Chiang, 2005).
Neural networks had been applied at various times to various aspects of machine translation; for example Schwenk et al. (2006) showed how to use neural language models to replace n-gram language models in a Spanish-English system based on IBM Model 4. The modern neural encoder-decoder approach was pioneered by Kalchbrenner and Blunsom (2013), who used a CNN encoder and an RNN decoder, and was first applied to MT by Bahdanau et al. (2015). The transformer encoder-decoder was proposed by Vaswani et al. (2017) (see the History section of Chapter 10).

Research on evaluation of machine translation began quite early. Miller and Beebe-Center (1956) proposed a number of methods drawing on work in psycholinguistics. These included the use of cloze and Shannon tasks to measure intelligibility as well as a metric of edit distance from a human translation, the intuition that underlies all modern overlap-based automatic evaluation metrics. The ALPAC report included an early evaluation study conducted by John Carroll that was extremely influential (Pierce et al., 1966, Appendix 10). Carroll proposed distinct measures for fidelity and intelligibility, and had raters score them subjectively on 9-point scales. Much early evaluation work focuses on automatic word-overlap metrics like BLEU (Papineni et al., 2002), NIST (Doddington, 2002), TER (Translation Error Rate) (Snover et al., 2006), Precision and Recall (Turian et al., 2003), and METEOR (Banerjee and Lavie, 2005); character n-gram overlap methods like chrF (Popović, 2015) came later. More recent evaluation work, echoing the ALPAC report, has emphasized the importance of careful statistical methodology and the use of human evaluation (Kocmi et al., 2021; Marie et al., 2021).


Exercises

13.1 Compute by hand the chrF2.2 score for HYP2 on page 286 (the answer should round to .62).
The quest for knowledge is deeply human, and so it is not surprising that practically as soon as there were computers we were asking them questions. By the early 1960s, systems used the two major paradigms of question answering—retrieval-based and knowledge-based—to answer questions about baseball statistics or scientific facts. Even imaginary computers got into the act. Deep Thought, the computer that Douglas Adams invented in *The Hitchhiker’s Guide to the Galaxy*, managed to answer “the Ultimate Question Of Life, The Universe, and Everything”.¹ In 2011, IBM’s Watson question-answering system won the TV game-show *Jeopardy!*, surpassing humans at answering questions like:

```
WILLIAM WILKINSON’S “AN ACCOUNT OF THE PRINCIPALITIES OF WALLACHIA AND MOLDOVIA” INSPIRED THIS AUTHOR’S MOST FAMOUS NOVEL
```

Question answering systems are designed to fill human information needs that might arise in situations like talking to a virtual assistant or a chatbot, interacting with a search engine, or querying a database. Question answering systems often focus on a particular subset of these information needs: factoid questions, questions that can be answered with simple facts expressed in short texts, like the following:

(14.1) Where is the Louvre Museum located?
(14.2) What is the average age of the onset of autism?

One way to do question answering is just to directly ask a large language model. For example, we could use the techniques of Chapter 12, prompting a large pre-trained causal language model with a string like

```
Q: Where is the Louvre Museum located? A:
```

have it do conditional generation given this prefix, and take the response as the answer. The idea is that huge pretrained language models have read a lot of facts in their pretraining data, presumably including the location of the Louvre, and have encoded this information in their parameters.

For some general factoid questions this can be a useful approach and is used in practice. But prompting a large language model is not yet a solution for question answering. The main problem is that large language models often give the wrong answer! Large language models hallucinate. A hallucination is a response that is not faithful to the facts of the world. That is, when asked questions, large language models simply make up answers that sound reasonable. For example, (Dahl et al., 2024) found that when asked questions about the legal domain (like about particular legal cases), large language models had hallucination rates ranging from 69% to 88%.

¹ The answer was 42, but unfortunately the details of the question were never revealed.
² The answer, of course, is ‘Who is Bram Stoker’, and the novel was *Dracula*. 

Sometime there are ways to tell that language models are hallucinating, but often there aren’t. One problem is that language model estimates of their confidence in their answers aren’t well-calibrated. In a calibrated system, the confidence of a system in the correctness of its answer is highly correlated with the probability of an answer being correct. So if the system is wrong, at least it might hedge its answer or tell us to go check another source. But since language models are not well-calibrated, they often give a very wrong answer with complete certainty.

A second problem is that simply prompting a large language model doesn’t allow us to ask questions about proprietary data. A common use of question-answering is to query private data, like asking an assistant about our email or private documents, or asking a question about our own medical records. Or a company may have internal documents that contain answers for customer service or internal use. Or legal firms need to ask questions about legal discovery from proprietary documents. Furthermore, the use of internal datasets, or even the web itself, can be especially useful for rapidly changing or dynamic information; by contrast, large language models are often only released at long increments of many months and so may not have up-to-date information.

For this reason the current dominant solution for question-answering is the two-stage retriever/reader model (Chen et al., 2017a), and that is the method we will focus on in this chapter. In a retriever/reader model, we use information retrieval techniques to first retrieve documents that are likely to have information that might help answer the question. Then we either extract an answer from spans of text in the documents, or use large language models to generate an answer given these documents, sometimes called retrieval-augmented generation.

Basing our answers on retrieved documents can solve the above-mentioned problems with using simple prompting to answer questions. First, we can ensure that the answer is grounded in facts from some curated dataset. And we can give the answer accompanied by the context of the passage or document the answer came from. This information can help users have confidence in the accuracy of the answer (or help them spot when it is wrong!). And we can use our retrieval techniques on any proprietary data we want, such as legal or medical data for those applications.

We’ll begin by introducing information retrieval, the task of choosing the most relevant document from a document set given a user’s query expressing their information need. We’ll see the classic method based on cosines of sparse tf-idf vectors, as well as modern neural IR using dense retriever, in which we run documents through BERT or other language models to get neural representations, and use cosine between dense representations of the query and document.

We then introduce retriever-based question answering, via the retriever/reader model. This algorithm most commonly relies on the vast amount of text on the web, in which case it is sometimes called open domain QA, or on collections of proprietary data, or scientific papers like PubMed. We’ll go through the two types of readers, span extractors and retrieval-augmented generation.

### 14.1 Information Retrieval

**Information retrieval** or IR is the name of the field encompassing the retrieval of all manner of media based on user information needs. The resulting IR system is often called a search engine. Our goal in this section is to give a sufficient overview of IR to see its application to question answering. Readers with more interest specifically
in information retrieval should see the Historical Notes section at the end of the chapter and textbooks like Manning et al. (2008).

The IR task we consider is called **ad hoc retrieval**, in which a user poses a **query** to a retrieval system, which then returns an ordered set of **documents** from some **collection**. A **document** refers to whatever unit of text the system indexes and retrieves (web pages, scientific papers, news articles, or even shorter passages like paragraphs). A **collection** refers to a set of documents being used to satisfy user requests. A **term** refers to a word in a collection, but it may also include phrases. Finally, a **query** represents a user’s information need expressed as a set of terms.

The high-level architecture of an ad hoc retrieval engine is shown in Fig. 14.1.

![Figure 14.1](image)

The architecture of an ad hoc IR system.

The basic IR architecture uses the vector space model we introduced in Chapter 6, in which we map queries and document to vectors based on unigram word counts, and use the cosine similarity between the vectors to rank potential documents (Salton, 1971). This is thus an example of the **bag-of-words** model introduced in Chapter 4, since words are considered independently of their positions.

### 14.1.1 Term weighting and document scoring

Let’s look at the details of how the match between a document and query is scored.

We don’t use raw word counts in IR, instead computing a **term weight** for each document word. Two term weighting schemes are common: the **tf-idf** weighting introduced in Chapter 6, and a slightly more powerful variant called **BM25**.

We’ll reintroduce tf-idf here so readers don’t need to look back at Chapter 6. Tf-idf (the ‘-’ here is a hyphen, not a minus sign) is the product of two terms, the term frequency $tf$ and the inverse document frequency $idf$.

The term frequency tells us how frequent the word is; words that occur more often in a document are likely to be informative about the document’s contents. We usually use the $\log_{10}$ of the word frequency, rather than the raw count. The intuition is that a word appearing 100 times in a document doesn’t make that word 100 times more likely to be relevant to the meaning of the document. We also need to do something special with counts of 0, since we can’t take the log of 0.\(^3\)

$$
\text{tf}_{t,d} = \begin{cases} 
1 + \log_{10}\text{count}(t,d) & \text{if } \text{count}(t,d) > 0 \\
0 & \text{otherwise}
\end{cases} 
$$ (14.3)

If we use log weighting, terms which occur 0 times in a document would have $tf = 0$.

\(^3\) We can also use this alternative formulation, which we have used in earlier editions: $\text{tf}_{t,d} = \log_{10}(\text{count}(t,d) + 1)$.
1 times in a document \( tf = 1 + \log_{10}(1) = 1 + 0 = 1 \), 10 times in a document \( tf = 1 + \log_{10}(10) = 2 \), 100 times \( tf = 1 + \log_{10}(100) = 3 \), 1000 times \( tf = 4 \), and so on.

The **document frequency** \( df_t \) of a term \( t \) is the number of documents it occurs in. Terms that occur in only a few documents are useful for discriminating those documents from the rest of the collection; terms that occur across the entire collection aren’t as helpful. The **inverse document frequency** or **idf** term weight (Sparck Jones, 1972) is defined as:

\[
idf_t = \log_{10} \frac{N}{df_t} \tag{14.4}
\]

where \( N \) is the total number of documents in the collection, and \( df_t \) is the number of documents in which term \( t \) occurs. The fewer documents in which a term occurs, the higher this weight; the lowest weight of 0 is assigned to terms that occur in every document.

Here are some idf values for some words in the corpus of Shakespeare plays, ranging from extremely informative words that occur in only one play like *Romeo*, to those that occur in a few like *salad* or *Falstaff*, to those that are very common like *fool* or so common as to be completely non-discriminative since they occur in all 37 plays like *good* or *sweet*.\(^4\)

<table>
<thead>
<tr>
<th>Word</th>
<th>df</th>
<th>idf</th>
</tr>
</thead>
<tbody>
<tr>
<td>Romeo</td>
<td>1</td>
<td>1.57</td>
</tr>
<tr>
<td>salad</td>
<td>2</td>
<td>1.27</td>
</tr>
<tr>
<td>Falstaff</td>
<td>4</td>
<td>0.967</td>
</tr>
<tr>
<td>forest</td>
<td>12</td>
<td>0.489</td>
</tr>
<tr>
<td>battle</td>
<td>21</td>
<td>0.246</td>
</tr>
<tr>
<td>wit</td>
<td>34</td>
<td>0.037</td>
</tr>
<tr>
<td>fool</td>
<td>36</td>
<td>0.012</td>
</tr>
<tr>
<td>good</td>
<td>37</td>
<td>0</td>
</tr>
<tr>
<td>sweet</td>
<td>37</td>
<td>0</td>
</tr>
</tbody>
</table>

The \( \text{tf-idf} \) value for word \( t \) in document \( d \) is then the product of term frequency \( tf_{t,d} \) and IDF:

\[
\text{tf-idf}(t, d) = tf_{t,d} \cdot \idf_t \tag{14.5}
\]

### 14.1.2 Document Scoring

We score document \( d \) by the cosine of its vector \( \mathbf{d} \) with the query vector \( \mathbf{q} \):

\[
\text{score}(q, d) = \cos(q, d) = \frac{\mathbf{q} \cdot \mathbf{d}}{|\mathbf{q}| \cdot |\mathbf{d}|} \tag{14.6}
\]

Another way to think of the cosine computation is as the dot product of unit vectors; we first normalize both the query and document vector to unit vectors, by dividing by their lengths, and then take the dot product:

\[
\text{score}(q, d) = \cos(q, d) = \frac{\mathbf{q}}{|\mathbf{q}|} \cdot \frac{\mathbf{d}}{|\mathbf{d}|} \tag{14.7}
\]

\(^4\) *Sweet* was one of Shakespeare’s favorite adjectives, a fact probably related to the increased use of sugar in European recipes around the turn of the 16th century (Jurafsky, 2014, p. 175).
We can spell out Eq. 14.7, using the tf-idf values and spelling out the dot product as a sum of products:

\[
\text{score}(q, d) = \sum_{t \in q} \frac{\text{tf-idf}(t, q)}{\sqrt{\sum_{q_i \in q} \text{tf-idf}^2(q_i, q)}} \cdot \frac{\text{tf-idf}(t, d)}{\sqrt{\sum_{d_i \in d} \text{tf-idf}^2(d_i, d)}} \tag{14.8}
\]

Now let’s use (14.8) to walk through an example of a tiny query against a collection of 4 nano documents, computing tf-idf values and seeing the rank of the documents. We’ll assume all words in the following query and documents are downcased and punctuation is removed:

**Query:** sweet love

**Doc 1:** Sweet sweet nurse! Love?

**Doc 2:** Sweet sorrow

**Doc 3:** How sweet is love?

**Doc 4:** Nurse!

Fig. 14.2 shows the computation of the tf-idf cosine between the query and Document 1, and the query and Document 2. The cosine is the normalized dot product of tf-idf values, so for the normalization we must need to compute the document vector lengths \(|q|\), \(|d_1|\), and \(|d_2|\) for the query and the first two documents using Eq. 14.3, Eq. 14.4, Eq. 14.5, and Eq. 14.8 (computations for Documents 3 and 4 are also needed but are left as an exercise for the reader). The dot product between the vectors is the sum over dimensions of the product, for each dimension, of the values of the two tf-idf vectors for that dimension. This product is only non-zero where both the query and document have non-zero values, so for this example, in which only *sweet* and *love* have non-zero values in the query, the dot product will be the sum of the products of those elements of each vector.

Document 1 has a higher cosine with the query (0.747) than Document 2 has with the query (0.0779), and so the tf-idf cosine model would rank Document 1 above Document 2. This ranking is intuitive given the vector space model, since Document 1 has both terms including two instances of *sweet*, while Document 2 is missing one of the terms. We leave the computation for Documents 3 and 4 as an exercise for the reader.

In practice, there are many variants and approximations to Eq. 14.8. For example, we might choose to simplify processing by removing some terms. To see this, let’s start by expanding the formula for tf-idf in Eq. 14.8 to explicitly mention the tf and idf terms from (14.5):

\[
\text{score}(q, d) = \sum_{t \in q} \frac{\text{tf}_t \cdot \text{idf}_t}{\sqrt{\sum_{q_i \in q} \text{tf-idf}^2(q_i, q)}} \cdot \frac{\text{tf}_t \cdot \text{idf}_t}{\sqrt{\sum_{d_i \in d} \text{tf-idf}^2(d_i, d)}} \tag{14.9}
\]

In one common variant of tf-idf cosine, for example, we drop the idf term for the document. Eliminating the second copy of the idf term (since the identical term is already computed for the query) turns out to sometimes result in better performance:

\[
\text{score}(q, d) = \sum_{t \in q} \frac{\text{tf}_t \cdot \text{idf}_t}{\sqrt{\sum_{q_i \in q} \text{tf-idf}^2(q_i, q)}} \cdot \frac{\text{tf}_t \cdot \text{idf}_t}{\sqrt{\sum_{d_i \in d} \text{tf-idf}^2(d_i, d)}} \tag{14.10}
\]

Other variants of tf-idf eliminate various other terms.

A slightly more complex variant in the tf-idf family is the **BM25** weighting
Figure 14.2 Computation of tf-idf cosine score between the query and nano-documents 1 (0.747) and 2 (0.0779), using Eq. 14.3, Eq. 14.4, Eq. 14.5 and Eq. 14.8.

scheme (sometimes called Okapi BM25 after the Okapi IR system in which it was introduced (Robertson et al., 1995)). BM25 adds two parameters: $k$, a knob that adjust the balance between term frequency and IDF, and $b$, which controls the importance of document length normalization. The BM25 score of a document $d$ given a query $q$ is:

$$
\sum_{t \in q} \text{IDF} \cdot \frac{\text{weighted tf}}{k \left( 1 - b + b \left( \frac{|d|}{|d_{\text{avg}}|} \right) \right) + \text{tf}_{t,d}}
$$

(14.11)

where $|d_{\text{avg}}|$ is the length of the average document. When $k$ is 0, BM25 reverts to no use of term frequency, just a binary selection of terms in the query (plus idf). A large $k$ results in raw term frequency (plus idf). $b$ ranges from 1 (scaling by document length) to 0 (no length scaling). Manning et al. (2008) suggest reasonable values are $k = [1.2, 2]$ and $b = 0.75$. Kamphuis et al. (2020) is a useful summary of the many minor variants of BM25.

Stop words In the past it was common to remove high-frequency words from both the query and document before representing them. The list of such high-frequency words to be removed is called a stop list. The intuition is that high-frequency terms (often function words like the, a, to) carry little semantic weight and may not help with retrieval, and can also help shrink the inverted index files we describe below. The downside of using a stop list is that it makes it difficult to search for phrases that contain words in the stop list. For example, common stop lists would reduce the phrase to be or not to be to the phrase not. In modern IR systems, the use of stop lists is much less common, partly due to improved efficiency and partly because much of their function is already handled by IDF weighting, which downweights function
words that occur in every document. Nonetheless, stop word removal is occasionally useful in various NLP tasks so is worth keeping in mind.

### 14.1.3 Inverted Index

In order to compute scores, we need to efficiently find documents that contain words in the query. (Any document that contains none of the query terms will have a score of 0 and can be ignored.) The basic search problem in IR is thus to find all documents \( d \in C \) that contain a term \( q \in Q \).

The data structure for this task is the **inverted index**, which we use for making this search efficient, and also conveniently storing useful information like the document frequency and the count of each term in each document.

An inverted index, given a query term, gives a list of documents that contain the term. It consists of two parts, a **dictionary** and the **postings**. The dictionary is a list of terms (designed to be efficiently accessed), each pointing to a postings list for the term. A postings list is the list of document IDs associated with each term, which can also contain information like the term frequency or even the exact positions of terms in the document. The dictionary can also start the document frequency for each term. For example, a simple inverted index for our 4 sample documents above, with each word containing its document frequency in \{ \}, and a pointer to a postings list that contains document IDs and term counts in [], might look like the following:

<table>
<thead>
<tr>
<th>Term</th>
<th>Dictionary</th>
<th>Postings</th>
</tr>
</thead>
<tbody>
<tr>
<td>how</td>
<td>{1} → 3 [1]</td>
<td></td>
</tr>
<tr>
<td>is</td>
<td>{1} → 3 [1]</td>
<td></td>
</tr>
<tr>
<td>love</td>
<td>{2} → 1 [1] → 3 [1]</td>
<td></td>
</tr>
<tr>
<td>nurse</td>
<td>{2} → 1 [1] → 4 [1]</td>
<td></td>
</tr>
<tr>
<td>sorry</td>
<td>{1} → 2 [1]</td>
<td></td>
</tr>
</tbody>
</table>

Given a list of terms in query, we can very efficiently get lists of all candidate documents, together with the information necessary to compute the tf-idf scores we need.

There are alternatives to the inverted index. For the question-answering domain of finding Wikipedia pages to match a user query, Chen et al. (2017a) show that indexing based on bigrams works better than unigrams, and use efficient hashing algorithms rather than the inverted index to make the search efficient.

### 14.1.4 Evaluation of Information-Retrieval Systems

We measure the performance of ranked retrieval systems using the same **precision** and **recall** metrics we have been using. We make the assumption that each document returned by the IR system is either **relevant** to our purposes or **not relevant**. Precision is the fraction of the returned documents that are relevant, and recall is the fraction of all relevant documents that are returned. More formally, let’s assume a system returns \( T \) ranked documents in response to an information request, a subset \( R \) of these are relevant, a disjoint subset, \( N \), are the remaining irrelevant documents, and \( U \) documents in the collection as a whole are relevant to this request. Precision and recall are then defined as:

\[
\text{Precision} = \frac{|R|}{|T|} \quad \text{Recall} = \frac{|R|}{|U|}
\]

(14.12)

Unfortunately, these metrics don’t adequately measure the performance of a system that ranks the documents it returns. If we are comparing the performance of two
ranked retrieval systems, we need a metric that prefers the one that ranks the relevant documents higher. We need to adapt precision and recall to capture how well a system does at putting relevant documents higher in the ranking.

<table>
<thead>
<tr>
<th>Rank</th>
<th>Judgment</th>
<th>Precision\textsubscript{Rank}</th>
<th>Recall\textsubscript{Rank}</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>R</td>
<td>1.0</td>
<td>.11</td>
</tr>
<tr>
<td>2</td>
<td>N</td>
<td>.50</td>
<td>.11</td>
</tr>
<tr>
<td>3</td>
<td>R</td>
<td>.66</td>
<td>.22</td>
</tr>
<tr>
<td>4</td>
<td>N</td>
<td>.50</td>
<td>.22</td>
</tr>
<tr>
<td>5</td>
<td>R</td>
<td>.60</td>
<td>.33</td>
</tr>
<tr>
<td>6</td>
<td>R</td>
<td>.66</td>
<td>.44</td>
</tr>
<tr>
<td>7</td>
<td>N</td>
<td>.57</td>
<td>.44</td>
</tr>
<tr>
<td>8</td>
<td>R</td>
<td>.63</td>
<td>.55</td>
</tr>
<tr>
<td>9</td>
<td>N</td>
<td>.55</td>
<td>.55</td>
</tr>
<tr>
<td>10</td>
<td>N</td>
<td>.50</td>
<td>.55</td>
</tr>
<tr>
<td>11</td>
<td>R</td>
<td>.55</td>
<td>.66</td>
</tr>
<tr>
<td>12</td>
<td>N</td>
<td>.50</td>
<td>.66</td>
</tr>
<tr>
<td>13</td>
<td>N</td>
<td>.46</td>
<td>.66</td>
</tr>
<tr>
<td>14</td>
<td>N</td>
<td>.43</td>
<td>.66</td>
</tr>
<tr>
<td>15</td>
<td>R</td>
<td>.47</td>
<td>.77</td>
</tr>
<tr>
<td>16</td>
<td>N</td>
<td>.44</td>
<td>.77</td>
</tr>
<tr>
<td>17</td>
<td>N</td>
<td>.44</td>
<td>.77</td>
</tr>
<tr>
<td>18</td>
<td>R</td>
<td>.44</td>
<td>.88</td>
</tr>
<tr>
<td>19</td>
<td>N</td>
<td>.42</td>
<td>.88</td>
</tr>
<tr>
<td>20</td>
<td>N</td>
<td>.40</td>
<td>.88</td>
</tr>
<tr>
<td>21</td>
<td>N</td>
<td>.38</td>
<td>.88</td>
</tr>
<tr>
<td>22</td>
<td>N</td>
<td>.36</td>
<td>.88</td>
</tr>
<tr>
<td>23</td>
<td>N</td>
<td>.35</td>
<td>.88</td>
</tr>
<tr>
<td>24</td>
<td>N</td>
<td>.33</td>
<td>.88</td>
</tr>
<tr>
<td>25</td>
<td>R</td>
<td>.36</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Figure 14.3  Rank-specific precision and recall values calculated as we proceed down through a set of ranked documents (assuming the collection has 9 relevant documents).

Let’s turn to an example. Assume the table in Fig. 14.3 gives rank-specific precision and recall values calculated as we proceed down through a set of ranked documents for a particular query; the precisions are the fraction of relevant documents seen at a given rank, and recalls the fraction of relevant documents found at the same rank. The recall measures in this example are based on this query having 9 relevant documents in the collection as a whole.

Note that recall is non-decreasing; when a relevant document is encountered, recall increases, and when a non-relevant document is found it remains unchanged. Precision, on the other hand, jumps up and down, increasing when relevant documents are found, and decreasing otherwise. The most common way to visualize precision and recall is to plot precision against recall in a precision-recall curve, like the one shown in Fig. 14.4 for the data in table 14.3.

Fig. 14.4 shows the values for a single query. But we’ll need to combine values for all the queries, and in a way that lets us compare one system to another. One way of doing this is to plot averaged precision values at 11 fixed levels of recall (0 to 100, in steps of 10). Since we’re not likely to have datapoints at these exact levels, we use interpolated precision values for the 11 recall values from the data points we do have. We can accomplish this by choosing the maximum precision value achieved at any level of recall at or above the one we’re calculating. In other words,

\[
\text{IntPrecision}(r) = \max_{i \geq r} \text{Precision}(i) \tag{14.13}
\]
This interpolation scheme not only lets us average performance over a set of queries, but also helps smooth over the irregular precision values in the original data. It is designed to give systems the benefit of the doubt by assigning the maximum precision value achieved at higher levels of recall from the one being measured. Fig. 14.5 and Fig. 14.6 show the resulting interpolated data points from our example.

<table>
<thead>
<tr>
<th>Interpolated Precision</th>
<th>Recall</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>0.0</td>
</tr>
<tr>
<td>1.0</td>
<td>.10</td>
</tr>
<tr>
<td>.66</td>
<td>.20</td>
</tr>
<tr>
<td>.66</td>
<td>.30</td>
</tr>
<tr>
<td>.66</td>
<td>.40</td>
</tr>
<tr>
<td>.63</td>
<td>.50</td>
</tr>
<tr>
<td>.55</td>
<td>.60</td>
</tr>
<tr>
<td>.47</td>
<td>.70</td>
</tr>
<tr>
<td>.44</td>
<td>.80</td>
</tr>
<tr>
<td>.36</td>
<td>.90</td>
</tr>
<tr>
<td>.36</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Given curves such as that in Fig. 14.6 we can compare two systems or approaches by comparing their curves. Clearly, curves that are higher in precision across all recall values are preferred. However, these curves can also provide insight into the overall behavior of a system. Systems that are higher in precision toward the left may favor precision over recall, while systems that are more geared towards recall will be higher at higher levels of recall (to the right).

A second way to evaluate ranked retrieval is **mean average precision** (MAP), which provides a single metric that can be used to compare competing systems or approaches. In this approach, we again descend through the ranked list of items, but now we note the precision only at those points where a relevant item has been encountered (for example at ranks 1, 3, 5, 6 but not 2 or 4 in Fig. 14.3). For a single query, we average these individual precision measurements over the return set (up to some fixed cutoff). More formally, if we assume that \( R_q \) is the set of relevant
documents at or above \( r \), then the **average precision** (AP) for a single query is

\[
AP = \frac{1}{|R_r|} \sum_{d \in R_r} \text{Precision}_r(d)
\]

(14.14)

where \( \text{Precision}_r(d) \) is the precision measured at the rank at which document \( d \) was found. For an ensemble of queries \( Q \), we then average over these averages, to get our final MAP measure:

\[
\text{MAP} = \frac{1}{|Q|} \sum_{q \in Q} \text{AP}(q)
\]

(14.15)

The MAP for the single query (hence = AP) in Fig. 14.3 is 0.6.

### 14.2 Information Retrieval with Dense Vectors

The classic tf-idf or BM25 algorithms for IR have long been known to have a conceptual flaw: they work only if there is exact overlap of words between the query and document. In other words, the user posing a query (or asking a question) needs to guess exactly what words the writer of the answer might have used, an issue called the **vocabulary mismatch problem** (Furnas et al., 1987).

The solution to this problem is to use an approach that can handle synonymy: instead of (sparse) word-count vectors, using (dense) embeddings. This idea was first proposed for retrieval in the last century under the name of Latent Semantic Indexing approach (Deerwester et al., 1990), but is implemented in modern times via encoders like BERT.

The most powerful approach is to present both the query and the document to a single encoder, allowing the transformer self-attention to see all the tokens of both
the query and the document, and thus building a representation that is sensitive to the meanings of both query and document. Then a linear layer can be put on top of the [CLS] token to predict a similarity score for the query/document tuple:

\[
\mathbf{z} = \text{BERT}(\mathbf{q}; [\text{SEP}]; \mathbf{d})[\text{CLS}]
\]

\[
\text{score}(q, d) = \text{softmax}(\mathbf{U}(\mathbf{z}))
\]  

This architecture is shown in Fig. 14.7a. Usually the retrieval step is not done on an entire document. Instead documents are broken up into smaller passages, such as non-overlapping fixed-length chunks of say 100 tokens, and the retriever encodes and retrieves these passages rather than entire documents. The query and document have to be made to fit in the BERT 512-token window, for example by truncating the query to 64 tokens and truncating the document if necessary so that it, the query, [CLS], and [SEP] fit in 512 tokens. The BERT system together with the linear layer \( \mathbf{U} \) can then be fine-tuned for the relevance task by gathering a tuning dataset of relevant and non-relevant passages.

![Image](image-url)

Figure 14.7 Two ways to do dense retrieval, illustrated by using lines between layers to schematically represent self-attention: (a) Use a single encoder to jointly encode query and document and finetune to produce a relevance score with a linear layer over the CLS token. This is too compute-expensive to use except in rescoring (b) Use separate encoders for query and document, and use the dot product between CLS token outputs for the query and document as the score. This is less compute-expensive, but not as accurate.

The problem with the full BERT architecture in Fig. 14.7a is the expense in computation and time. With this architecture, every time we get a query, we have to pass every single single document in our entire collection through a BERT encoder jointly with the new query! This enormous use of resources is impractical for real cases.

At the other end of the computational spectrum is a much more efficient architecture, the **bi-encoder**. In this architecture we can encode the documents in the collection only one time by using two separate encoder models, one to encode the query and one to encode the document. We encode each document, and store all the encoded document vectors in advance. When a query comes in, we encode just this query and then use the dot product between the query vector and the precomputed document vectors as the score for each candidate document (Fig. 14.7b). For example, if we used BERT, we would have two encoders \( \text{BERT}_Q \) and \( \text{BERT}_D \) and
we could represent the query and document as the [CLS] token of the respective encoders (Karpukhin et al., 2020):

\[
\begin{align*}
z_q &= \text{BERT}_Q(q) \text{[CLS]} \\
z_d &= \text{BERT}_D(d) \text{[CLS]}
\end{align*}
\]

\[
\text{score}(q, d) = z_q \cdot z_d
\]  
(14.17)

The bi-encoder is much cheaper than a full query/document encoder, but is also less accurate, since its relevance decision can’t take full advantage of all the possible meaning interactions between all the tokens in the query and the tokens in the document.

There are numerous approaches that lie in between the full encoder and the bi-encoder. One intermediate alternative is to use cheaper methods (like BM25) as the first pass relevance ranking for each document, take the top \(N\) ranked documents, and use expensive methods like the full BERT scoring to rerank only the top \(N\) documents rather than the whole set.

Another intermediate approach is the ColBERT approach of Khattab and Zaharia (2020) and Khattab et al. (2021), shown in Fig. 14.8. This method separately encodes the query and document, but rather than encoding the entire query or document into one vector, it separately encodes each of them into contextual representations for each token. These BERT representations of each document word can be pre-stored for efficiency. The relevance score between a query \(q\) and a document \(d\) is a sum of maximum similarity (MaxSim) operators between tokens in \(q\) and tokens in \(d\). Essentially, for each token in \(q\), ColBERT finds the most contextually similar token in \(d\), and then sums up these similarities. A relevant document will have tokens that are contextually very similar to the query.

More formally, a question \(q\) is tokenized as \([q_1, \ldots, q_n]\), prepended with a [CLS] and a special [Q] token, truncated to \(N=32\) tokens (or padded with [MASK] tokens if it is shorter), and passed through BERT to get output vectors \(q = [q_1, \ldots, q_N]\). The passage \(d\) with tokens \([d_1, \ldots, d_m]\), is processed similarly, including a [CLS] and special [D] token. A linear layer is applied on top of \(d\) and \(q\) to control the output dimension, so as to keep the vectors small for storage efficiency, and vectors are rescaled to unit length, producing the final vector sequences \(E_q\) (length \(N\)) and \(E_d\) (length \(m\)). The ColBERT scoring mechanism is:

\[
\text{score}(q, d) = \sum_{i=1}^{N} \max_{j=1}^{m} E_{q_i} \cdot E_{d_j}
\]  
(14.18)

While the interaction mechanism has no tunable parameters, the ColBERT architecture still needs to be trained end-to-end to fine-tune the BERT encoders and train the linear layers (and the special [Q] and [D] embeddings) from scratch. It is trained on triples \((q, d^+, d^-)\) of query \(q\), positive document \(d^+\) and negative document \(d^-\) to produce a score for each document using (14.18), optimizing model parameters using a cross-entropy loss.

All the supervised algorithms (like ColBERT or the full-interaction version of the BERT algorithm applied for reranking) need training data in the form of queries together with relevant and irrelevant passages or documents (positive and negative examples). There are various semi-supervised ways to get labels; some datasets (like MS MARCO Ranking, Section 14.3.1) contain gold positive examples. Negative examples can be sampled randomly from the top-1000 results from some existing IR system. If datasets don’t have labeled positive examples, iterative methods like
relevance-guided supervision can be used (Khattab et al., 2021) which rely on the fact that many datasets contain short answer strings. In this method, an existing IR system is used to harvest examples that do contain short answer strings (the top few are taken as positives) or don’t contain short answer strings (the top few are taken as negatives), these are used to train a new retriever, and then the process is iterated.

Efficiency is an important issue, since every possible document must be ranked for its similarity to the query. For sparse word-count vectors, the inverted index allows this very efficiently. For dense vector algorithms finding the set of dense document vectors that have the highest dot product with a dense query vector is an instance of the problem of nearest neighbor search. Modern systems therefore make use of approximate nearest neighbor vector search algorithms like Faiss (Johnson et al., 2017).

14.3 Using Neural IR for Question Answering

The goal of retrieval-based QA (sometimes called open domain QA) is to answer a user’s question by either finding short text segments from the web or some other large collection of documents, or by generating an answer based on them. Figure 14.9 shows some sample factoid questions with answers.

The dominant paradigm for retrieval-based QA is sometimes called the retrieve and read model shown in Fig. 14.10. In the first stage of this 2-stage model we retrieve relevant passages from a text collection, for example using the dense retrievers of the previous section.

The second stage, called the reader, is commonly implemented as either an ex-
tract or a generator. The first method is span extraction, using a neural reading comprehension algorithm that passes over each passage and is trained to find spans of text that answer the question. The second method is also known as retrieval-augmented generation: we take a large pretrained language model, give it some set of retrieved passages and other text as its prompt, and autoregressively generate a new answer token by token.

In the next few sections we’ll describe these two standard reader algorithms. But first, we’ll introduce some commonly-used question answering datasets.

### 14.3.1 Retrieval-based QA: Datasets

Datasets for retrieval-based QA are most commonly created by first developing reading comprehension datasets containing tuples of (passage, question, answer). Reading comprehension systems can use the datasets to train a reader that is given a passage and a question, and predicts a span in the passage as the answer. Including the passage from which the answer is to be extracted eliminates the need for reading comprehension systems to deal with IR.

For example the Stanford Question Answering Dataset (SQuAD) consists of passages from Wikipedia and associated questions whose answers are spans from the passage (Rajpurkar et al. 2016). Squad 2.0 in addition adds some questions that are designed to be unanswerable (Rajpurkar et al. 2018), with a total of just over 150,000 questions. Fig. 14.11 shows a (shortened) excerpt from a SQUAD 2.0 passage together with three questions and their gold answer spans.

SQuAD was built by having humans read a given Wikipedia passage, write questions about the passage, and choose a specific answer span.

Other datasets are created by similar techniques but try to make the questions more complex. The HotpotQA dataset (Yang et al., 2018) was created by showing
Beyoncé Giselle Knowles-Carter (born September 4, 1981) is an American singer, songwriter, record producer and actress. Born and raised in Houston, Texas, she performed in various singing and dancing competitions as a child, and rose to fame in the late 1990s as lead singer of R&B girl-group Destiny’s Child. Managed by her father, Mathew Knowles, the group became one of the world’s best-selling girl groups of all time. Their hiatus saw the release of Beyoncé’s debut album, Dangerously in Love (2003), which established her as a solo artist worldwide, earned five Grammy Awards and featured the Billboard Hot 100 number-one singles “Crazy in Love” and “Baby Boy.”

Q: “In what city and state did Beyoncé grow up?”
A: “Houston, Texas”

Q: “What areas did Beyoncé compete in when she was growing up?”
A: “singing and dancing”

Q: “When did Beyoncé release Dangerously in Love?”
A: “2003”

Figure 14.11 A (Wikipedia) passage from the SQuAD 2.0 dataset (Rajpurkar et al., 2018) with 3 sample questions and the labeled answer spans.

crowd workers multiple context documents and asked to come up with questions that require reasoning about all of the documents.

The fact that questions in datasets like SQuAD or HotpotQA are created by annotators who have first read the passage may make their questions easier to answer, since the annotator may (subconsciously) make use of words from the answer text.

A solution to this possible bias is to make datasets from questions that were not written with a passage in mind. The TriviaQA dataset (Joshi et al., 2017) contains 94K questions written by trivia enthusiasts, together with supporting documents from Wikipedia and the web resulting in 650K question-answer-evidence triples.

MS MARCO (Microsoft Machine Reading Comprehension) is a collection of datasets, including 1 million real anonymized questions from Microsoft Bing query logs together with a human generated answer and 9 million passages (Nguyen et al., 2016), that can be used both to test retrieval ranking and question answering. The Natural Questions dataset (Kwiatkowski et al., 2019) similarly incorporates real anonymized queries to the Google search engine. Annotators are presented a query, along with a Wikipedia page from the top 5 search results, and annotate a paragraph-length long answer and a short span answer, or mark null if the text doesn’t contain the paragraph. For example the question “When are hops added to the brewing process?” has the short answer the boiling process and a long answer which the surrounding entire paragraph from the Wikipedia page on Brewing. In using this dataset, a reading comprehension model is given a question and a Wikipedia page and must return a long answer, short answer, or ‘no answer’ response.

The above datasets are all in English. The TyDi QA dataset contains 204K question-answer pairs from 11 typologically diverse languages, including Arabic, Bengali, Kiswahili, Russian, and Thai (Clark et al., 2020a). In the TyDi QA task, a system is given a question and the passages from a Wikipedia article and must (a) select the passage containing the answer (or NULL if no passage contains the answer), and (b) mark the minimal answer span (or NULL). Many questions have no answer. The various languages in the dataset bring up challenges for QA systems like morphological variation between the question and the answer, or complex issue with word segmentation or multiple alphabets.

In the reading comprehension task, a system is given a question and the passage in which the answer should be found. In the full two-stage QA task, however, sys-
tems are not given a passage, but are required to do their own retrieval from some document collection. A common way to create open-domain QA datasets is to modify a reading comprehension dataset. For research purposes this is most commonly done by using QA datasets that annotate Wikipedia (like SQuAD or HotpotQA). For training, the entire \((\text{question, passage, answer})\) triple is used to train the reader. But at inference time, the passages are removed and system is given only the question, together with access to the entire Wikipedia corpus. The system must then do IR to find a set of pages and then read them.

### 14.3.2 Reader algorithms: Answer Span Extraction

The job of the reader is to take a passage as input and produce the answer. Here we introduce the span extraction style of reader, in which the answer is a span of text in the passage. For example, given a question like “How tall is Mt. Everest?” and a passage that contains the clause \(\text{Reaching 29,029 feet at its summit}\), a reader will output \(29,029\) feet.

The answer extraction task is commonly modeled by span labeling: identifying in the passage a span (a continuous string of text) that constitutes an answer. Neural algorithms for reading comprehension are given a question \(q\) of \(n\) tokens \(q_1, \ldots, q_n\) and a passage \(p\) of \(m\) tokens \(p_1, \ldots, p_m\). Their goal is thus to compute the probability \(P(a|q, p)\) that each possible span \(a\) is the answer.

If each span \(a\) starts at position \(a_s\) and ends at position \(a_e\), we make the simplifying assumption that this probability can be estimated as \(P(a|q, p) = P_{\text{start}}(a_s|q, p)P_{\text{end}}(a_e|q, p)\). Thus for for each token \(p_i\) in the passage we’ll compute two probabilities: \(P_{\text{start}}(i)\) that \(p_i\) is the start of the answer span, and \(P_{\text{end}}(i)\) that \(p_i\) is the end of the answer span.

A standard baseline algorithm for reading comprehension is to pass the question and passage to any encoder like BERT (Fig. 14.12), as strings separated with a \([\text{SEP}]\) token, resulting in an encoding token embedding for every passage token \(p_i\).

![Figure 14.12](image)

**Figure 14.12** An encoder model (using BERT) for span-based question answering from reading-comprehension-based question answering tasks.

For span-based question answering, we represent the question as the first sequence and the passage as the second sequence. We’ll also need to add a linear layer that will be trained in the fine-tuning phase to predict the start and end position of the answer span.
span. We’ll add two new special vectors: a span-start embedding $S$ and a span-end embedding $E$, which will be learned in fine-tuning. To get a span-start probability for each output token $p'_i$, we compute the dot product between $S$ and $p'_i$ and then use a softmax to normalize over all tokens $p'_i$ in the passage:

$$P_{\text{start}} = \frac{\exp(S \cdot p'_i)}{\sum_j \exp(S \cdot p'_j)} \quad (14.19)$$

We do the analogous thing to compute a span-end probability:

$$P_{\text{end}} = \frac{\exp(E \cdot p'_i)}{\sum_j \exp(E \cdot p'_j)} \quad (14.20)$$

The score of a candidate span from position $i$ to $j$ is $S \cdot p'_i + E \cdot p'_j$, and the highest scoring span in which $j \geq i$ is chosen is the model prediction.

The training loss for fine-tuning is the negative sum of the log-likelihoods of the correct start and end positions for each instance:

$$L = - \log P_{\text{start}} - \log P_{\text{end}} \quad (14.21)$$

Many datasets (like SQuAD 2.0 and Natural Questions) also contain (question, passage) pairs in which the answer is not contained in the passage. We thus also need a way to estimate the probability that the answer to a question is not in the document. This is standardly done by treating questions with no answer as having the [CLS] token as the answer, and hence the answer span start and end index will point at [CLS] (Devlin et al., 2019).

For many datasets the annotated documents/passages are longer than the maximum 512 input tokens BERT allows, such as Natural Questions whose gold passages are full Wikipedia pages. In such cases, following Alberti et al. (2019), we can create multiple pseudo-passage observations from the labeled Wikipedia page. Each observation is formed by concatenating [CLS], the question, [SEP], and tokens from the document. We walk through the document, sliding a window of size 512 (or rather, 512 minus the question length $n$ minus special tokens) and packing the window of tokens into each next pseudo-passage. The answer span for the observation is either labeled [CLS] (= no answer in this particular window) or the gold-labeled span is marked. The same process can be used for inference, breaking up each retrieved document into separate observation passages and labeling each observation. The answer can be chosen as the span with the highest probability (or nil if no span is more probable than [CLS]).

### 14.3.3 Reader algorithms: Retrieval-Augmented Generation

The second standard reader algorithm is to generate from a large language model, conditioned on the retrieved passages. This method is known as **retrieval-augmented generation**, or **RAG**.

Recall that in simple conditional generation, we can cast the task of question answering as word prediction by giving a language model a question and a token like A: suggesting that an answer should come next:

Q: Who wrote the book ‘‘The Origin of Species’’?  A:

Then we generate autoregressively conditioned on this text.
More formally, recall that simple autoregressive language modeling computes the probability of a string from the previous tokens:

\[ p(x_1, \ldots, x_n) = \prod_{i=1}^{n} p(x_i | x_{<i}) \]

And simple conditional generation for question answering adds a prompt like Q:, followed by a query \( q \), and A:, all concatenated:

\[ p(x_1, \ldots, x_n) = \prod_{i=1}^{n} p([Q:] ; q ; [A:] ; x_{<i}) \]

The advantage of using a large language model is the enormous amount of knowledge encoded in its parameters from the text it was pretrained on. But as we mentioned at the start of the chapter, while this kind of simple prompted generation can work fine for many simple factoid questions, it is not a general solution for QA, because it leads to hallucination, is unable to show users textual evidence to support the answer, and is unable to answer questions from proprietary data.

The idea of retrieval-augmented generation is to address these problems by conditioning on the retrieved passages as part of the prefix, perhaps with some prompt text like “Based on these texts, answer this question:”. Let’s suppose we have a query \( q \), and call the set of retrieved passages based on it \( R(q) \). For example, we could have a prompt like:

- retrieved passage 1
- retrieved passage 2
- ...
- retrieved passage n

Based on these texts, answer this question: Q: Who wrote the book "The Origin of Species"? A:

Or more formally,

\[ p(x_1, \ldots, x_n) = \prod_{i=1}^{n} p(x_i | R(q) ; \text{prompt} ; [Q:] ; q ; [A:] ; x_{<i}) \]

As with the span-based extraction reader, successfully applying the retrieval-augmented generation algorithm for QA requires a successful retriever, and often a two-stage retrieval algorithm is used in which the retrieval is reranked. Some complex questions may require multi-hop architectures, in which a query is used to retrieve documents, which are then appended to the original query for a second stage of retrieval. Details of prompt engineering also have to be worked out, like deciding whether to demarcate passages, for example with [SEP] tokens, and so on. Finally, combinations of private data and public data involving an externally hosted large language model may lead to privacy concerns that need to be worked out (Arora et al., 2023).
14.4 Evaluating Retrieval-based Question Answering

Question answering is commonly evaluated using **mean reciprocal rank**, or MRR (Voorhees, 1999). MRR is designed for systems that return a short ranked list of answers or passages for each test set question, which we can compare against the (human-labeled) correct answer. First, each test set question is scored with the reciprocal of the rank of the first correct answer. For example if the system returned five answers to a question but the first three are wrong (so the highest-ranked correct answer is ranked fourth), the reciprocal rank for that question is \( \frac{1}{4} \). The score for questions that return no correct answer is 0. The MRR of a system is the average of the scores for each question in the test set. In some versions of MRR, questions with a score of zero are ignored in this calculation. More formally, for a system returning ranked answers to each question in a test set \( Q \), (or in the alternate version, let \( Q \) be the subset of test set questions that have non-zero scores). MRR is then defined as

\[
\text{MRR} = \frac{1}{|Q|} \sum_{i=1}^{|Q|} \frac{1}{\text{rank}_i}
\]  

(14.22)

Alternatively, question answering systems can be evaluated with exact match, or with \( F_1 \) score. This is common for datasets like SQuAD which are evaluated (first ignoring punctuation and articles like \( a, an, the \)) via both (Rajpurkar et al., 2016):

- **Exact match**: The % of predicted answers that match the gold answer exactly.
- **\( F_1 \) score**: The average word/token overlap between predicted and gold answers. Treat the prediction and gold as a bag of tokens, and compute \( F_1 \) for each question, then return the average \( F_1 \) over all questions.

Other recent datasets include the AI2 Reasoning Challenge (ARC) (Clark et al., 2018) of multiple choice questions designed to be hard to answer from simple lexical methods, like this question:

Which property of a mineral can be determined just by looking at it?

(A) luster [correct] (B) mass (C) weight (D) hardness

in which the correct answer *luster* is unlikely to co-occur frequently with phrases like *looking at it*, while the word *mineral* is highly associated with the incorrect answer *hardness*.

14.5 Summary

This chapter introduced the tasks of **question answering** and **information retrieval**.

- **Question answering (QA)** is the task of answering a user’s questions.
- We focus in this chapter on the task of retrieval-based question answering, in which the user’s questions are intended to be answered by the material in some set of documents.
- **Information Retrieval (IR)** is the task of returning documents to a user based on their information need as expressed in a **query**. In ranked retrieval, the documents are returned in ranked order.
The match between a query and a document can be done by first representing each of them with a sparse vector that represents the frequencies of words, weighted by tf-idf or BM25. Then the similarity can be measured by cosine.

Documents or queries can instead be represented by dense vectors, by encoding the question and document with an encoder-only model like BERT, and in that case computing similarity in embedding space.

The inverted index is an storage mechanism that makes it very efficient to find documents that have a particular word.

Ranked retrieval is generally evaluated by mean average precision or interpolated precision.

Question answering systems generally use the retriever/reader architecture. In the retriever stage, an IR system is given a query and returns a set of documents.

The reader stage can either be a span-based extractor, that predicts a span of text in the retrieved documents to return as the answer, or a retrieval-augmented generator, in which a large language model is used to generate a novel answer after reading the documents and the query.

QA can be evaluated by exact match with a known answer if only a single answer is given, or with mean reciprocal rank if a ranked set of answers is given.

Bibliographical and Historical Notes

Question answering was one of the earliest NLP tasks, and early versions of the text-based and knowledge-based paradigms were developed by the very early 1960s. The text-based algorithms generally relied on simple parsing of the question and of the sentences in the document, and then looking for matches. This approach was used very early on (Phillips, 1960) but perhaps the most complete early system, and one that strikingly prefigures modern relation-based systems, was the Protosynthex system of Simmons et al. (1964). Given a question, Protosynthex first formed a query from the content words in the question, and then retrieved candidate answer sentences in the document, ranked by their frequency-weighted term overlap with the question. The query and each retrieved sentence were then parsed with dependency parsers, and the sentence whose structure best matches the question structure selected. Thus the question What do worms eat? would match worms eat grass: both have the subject worms as a dependent of eat, in the version of dependency grammar used at the time, while birds eat worms has birds as the subject:

![Diagram of dependency grammar](image)

The alternative knowledge-based paradigm was implemented in the BASEBALL system (Green et al., 1961). This system answered questions about baseball games like “Where did the Red Sox play on July 7” by querying a structured database of game information. The database was stored as a kind of attribute-value matrix with values for attributes of each game:
Each question was constituency-parsed using the algorithm of Zellig Harris’s TDAP project at the University of Pennsylvania, essentially a cascade of finite-state transducers (see the historical discussion in Joshi and Hopely 1999 and Karttunen 1999). Then in a content analysis phase each word or phrase was associated with a program that computed parts of its meaning. Thus the phrase ‘Where’ had code to assign the semantics Place = ?, with the result that the question “Where did the Red Sox play on July 7” was assigned the meaning

Place = ?
Team = Red Sox
Month = July
Day = 7

The question is then matched against the database to return the answer. Simmons (1965) summarizes other early QA systems.

Another important progenitor of the knowledge-based paradigm for question-answering is work that used predicate calculus as the meaning representation language. The LUNAR system (Woods et al. 1972, Woods 1978) was designed to be a natural language interface to a database of chemical facts about lunar geology. It could answer questions like Do any samples have greater than 13 percent aluminum by parsing them into a logical form

\[(\text{TEST} \ (\text{FOR SOME X16 / (SEQ SAMPLES) : T ; (CONTAIN’ X16 (NPR* X17 / (QUOTE AL203)) (GREATERTHAN 13 PCT))))}\]

By a couple decades later, drawing on new machine learning approaches in NLP, Zelle and Mooney (1996) proposed to treat knowledge-based QA as a semantic parsing task, by creating the Prolog-based GEOQUERY dataset of questions about US geography. This model was extended by Zettlemoyer and Collins (2005) and 2007. By a decade later, neural models were applied to semantic parsing (Dong and Lapatia 2016, Jia and Liang 2016), and then to knowledge-based question answering by mapping text to SQL (Iyer et al., 2017).

Meanwhile, the information-retrieval paradigm for question answering was influenced by the rise of the web in the 1990s. The U.S. government-sponsored TREC (Text REtrieval Conference) evaluations, run annually since 1992, provide a testbed for evaluating information-retrieval tasks and techniques (Voorhees and Harman, 2005). TREC added an influential QA track in 1999, which led to a wide variety of factoid and non-factoid systems competing in annual evaluations.

At that same time, Hirschman et al. (1999) introduced the idea of using children’s reading comprehension tests to evaluate machine text comprehension algorithms. They acquired a corpus of 120 passages with 5 questions each designed for 3rd-6th grade children, built an answer extraction system, and measured how well the answers given by their system corresponded to the answer key from the test’s publisher. Their algorithm focused on word overlap as a feature; later algorithms added named entity features and more complex similarity between the question and the answer span (Riloff and Thelen 2000, Ng et al. 2000).

The DeepQA component of the Watson Jeopardy! system was a large and sophisticated feature-based system developed just before neural systems became com-
mon. It is described in a series of papers in volume 56 of the IBM Journal of Research and Development, e.g., Ferrucci (2012).

Neural reading comprehension systems drew on the insight common to early systems that answer finding should focus on question-passage similarity. Many of the architectural outlines of these modern neural systems were laid out in Hermann et al. (2015a), Chen et al. (2017a), and Seo et al. (2017). These systems focused on datasets like Rajpurkar et al. (2016) and Rajpurkar et al. (2018) and their successors, usually using separate IR algorithms as input to neural reading comprehension systems. The paradigm of using dense retrieval with a span-based reader, often with a single end-to-end architecture, is exemplified by systems like Lee et al. (2019) or Karpukhin et al. (2020). An important research area with dense retrieval for open-domain QA is training data: using self-supervised methods to avoid having to label positive and negative passages (Sachan et al., 2023). Retrieval-augmented generation algorithms were first introduced as a way to improve language modeling (Khandelwal et al., 2019), but were quickly applied to question answering (Izacard et al., 2022; Ram et al., 2023; Shi et al., 2023).

Exercises
CHAPTER 15

Chatbots & Dialogue Systems

Les lois de la conversation sont en général de ne s’y appesantir sur aucun objet, mais de passer légèrement, sans effort et sans affectation, d’un sujet à un autre ; de savoir y parler de choses frivoles comme de choses sérieuses

[The rules of conversation are, in general, not to dwell on any one subject, but to pass lightly from one to another without effort and without affectation; to know how to speak about trivial topics as well as serious ones:]

The 18th C. Encyclopedia of Diderot, start of the entry on conversation

The literature of the fantastic abounds in inanimate objects magically endowed with the gift of speech. From Ovid’s statue of Pygmalion to Mary Shelley’s story about Frankenstein, we continually reinvent stories about creating something and then having a chat with it. Legend has it that after finishing his sculpture Moses, Michelangelo thought it so lifelike that he tapped it on the knee and commanded it to speak. Perhaps this shouldn’t be surprising. Language is the mark of humanity and sentience, and conversation or dialogue is the most fundamental arena of language. It is the first kind of language we learn as children, and the kind we engage in constantly, whether we are ordering lunch, buying train tickets, or talking with our families, friends, or coworkers.

This chapter introduces the fundamental algorithms of programs that use conversation to interact with users. We often distinguish between two kinds of architectures. Task-oriented dialogue systems converse with users to accomplish fixed tasks like controlling appliances or finding restaurants, relying on a data structure called the frame, which represents the knowledge a system needs to acquire from the user (like the time to set an alarm clock). Chatbots, by contrast, are designed to mimic the longer and more unstructured conversations or ‘chats’ characteristic of human-human interaction. Modern systems incorporate aspects of both; industrial chatbots like ChatGPT can carry on longer unstructured conversations; industrial digital assistants like Siri or Alexa are generally frame-based dialogue systems.

The fact that chatbots and dialogue systems are designed for human-computer interaction has strong implications for their design and use. Many of these implications already became clear in one of the earliest chatbots, ELIZA (Weizenbaum, 1966). ELIZA was designed to simulate a Rogerian psychologist, based on a branch of clinical psychology whose methods involve drawing the patient out by reflecting patient’s statements back at them. Rogerian interactions are the rare type of conversation in which, as Weizenbaum points out, one can “assume the pose of knowing almost nothing of the real world”. If a patient says “I went for a long boat ride” and the psychiatrist says “Tell me about boats”, you don’t assume she didn’t know what
Men are all alike.

**IN WHAT WAY**
They’re always bugging us about something or other.

**CAN YOU THINK OF A SPECIFIC EXAMPLE**
Well my boyfriend made me come here.

**YOUR BOYFRIEND MADE YOU COME HERE**
He says I’m depressed much of the time.

**I AM SORRY TO HEAR YOU ARE DEPRESSED**

![Figure 15.1](Image) Sample ELIZA dialogue from Weizenbaum (1966).

Weizenbaum made use of this property of Rogerian psychiatric conversations, along with clever regular expressions, to allow ELIZA to interact in ways that seemed deceptively human-like, as in the sample conversational fragment in Fig. 15.1.

As we foreshadowed in Chapter 2, ELIZA worked by simple rules roughly like:

\[
(.*) \text{ YOU (.*) ME} \rightarrow \text{WHAT MAKES YOU THINK I \2 YOU}
\]

to transform a user sentence like “You hate me” into a system response like

**WHAT MAKES YOU THINK I HATE YOU**

Among Weizenbaum’s clever tricks are the linking of each ELIZA pattern/rule to a keyword. Consider the following user sentence:

**I know everybody laughed at me**

Because it has the word “I”, this sentence could match the following rule whose keyword is **I**:

\[
I (.*) \rightarrow \text{You say you \1}
\]

producing:

**YOU SAY YOU KNOW EVERYBODY LAUGHED AT YOU**

Weizenbaum points out, however, that a more powerful response would rely on the keyword “everybody”, since someone using universals like *everybody* or *always* is probably thinking about a specific person or situation. So the ELIZA algorithm prefers to respond using patterns associated more specific keywords like *everybody*:

**WHO IN PARTICULAR ARE YOU THINKING OF?**

If no keyword matches, the algorithm chooses a non-committal response like “PLEASE GO ON”, “THAT’S VERY INTERESTING”, or “I SEE”.

ELIZA illustrates a number of important issues with chatbots. First, people became deeply emotionally involved and conducted very personal conversations, even to the extent of asking Weizenbaum to leave the room while they were typing. Reeves and Nass (1996) show that people tend to assign human characteristics to computers and interact with them in ways that are typical of human-human interactions. They interpret an utterance in the way they would if it had spoken by a human, (even though they are aware they are talking to a computer). This means that chatbots can have significant influences on people’s cognitive and emotional state.

A second related issue is privacy. When Weizenbaum suggested that he might want to store the ELIZA conversations, people immediately pointed out that this would violate people’s privacy. Modern chatbots in the home are likely to overhear

---

1 This is due to the Gricean principle of *relevance* that we’ll discuss in the next section.
private information, even if they aren’t used for counseling as ELIZA was. Indeed, if a chatbot is human-like, users are more likely to disclose private information, and yet less likely to worry about the harm of this disclosure (Ischen et al., 2019).

Both of these issues (emotional engagement and privacy) mean we need to think carefully about how we deploy chatbots and the people who are interacting with them. Dialogue research that uses human participants often requires getting permission from the Institutional Review Board (IRB) of your institution.

In the next section we introduce some basic properties of human conversation. We then turn in the rest of the chapter to the two basic paradigms for conversational interaction: frame-based dialogue systems and chatbots.

15.1 Properties of Human Conversation

Conversation between humans is an intricate and complex joint activity. Before we attempt to design a dialogue system to converse with humans, it is crucial to understand something about how humans converse with each other. Consider some of the phenomena that occur in the conversation between a human travel agent and a human client excerpted in Fig. 15.2.

![Figure 15.2](image)

A dialogue is a sequence of **turns** (C₁, A₂, C₃, and so on), each a single contribution from one speaker to the dialogue (as if in a game: I take a turn, then you take a turn, ...
then me, and so on). There are 20 turns in Fig. 15.2. A turn can consist of a sentence (like C₁), although it might be as short as a single word (C₁₃) or as long as multiple sentences (A₁₀).

Turn structure has important implications for spoken dialogue. A human has to know when to stop talking; the client interrupts (in A₁₆ and C₁₇), so a system that was performing this role must know to stop talking (and that the user might be making a correction). A system also has to know when to start talking. For example, most of the time in conversation, speakers start their turns almost immediately after the other speaker finishes, without a long pause, because people are can usually predict when the other person is about to finish talking. Spoken dialogue systems must also detect whether a user is done speaking, so they can process the utterance and respond. This task—called endpointing or endpoint detection—can be quite challenging because of noise and because people often pause in the middle of turns.

**Speech Acts**

A key insight into conversation—due originally to the philosopher Wittgenstein (1953) but worked out more fully by Austin (1962)—is that each utterance in a dialogue is a kind of action being performed by the speaker. These actions are commonly called speech acts or dialogue acts: here’s one taxonomy consisting of 4 major classes (Bach and Harnish, 1979):

<table>
<thead>
<tr>
<th>Speech acts</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constatives</td>
<td>committing the speaker to something’s being the case (answering, claiming, confirming, denying, disagreeing, stating)</td>
</tr>
<tr>
<td>Directives</td>
<td>attempts by the speaker to get the addressee to do something (advising, asking, forbidding, inviting, ordering, requesting)</td>
</tr>
<tr>
<td>Commissives</td>
<td>committing the speaker to some future course of action (promising, planning, vowing, betting, opposing)</td>
</tr>
<tr>
<td>Acknowledgments</td>
<td>express the speaker’s attitude regarding the hearer with respect to some social action (apologizing, greeting, thanking, accepting an acknowledgment)</td>
</tr>
</tbody>
</table>

A user asking a person or a dialogue system to do something (“Turn up the music”) is issuing a DIRECTIVE. Asking a question that requires an answer is also a way of issuing a DIRECTIVE: in a sense when the system says (A₂) “what day in May did you want to travel?” it’s as if the system is (very politely) commanding the user to answer. By contrast, a user stating a constraint (like C₁ ’I need to travel in May’) is issuing a CONSTATIVE. A user thanking the system is issuing an ACKNOWLEDGMENT. The speech act expresses an important component of the intention of the speaker (or writer) in saying what they said.

**Grounding**

A dialogue is not just a series of independent speech acts, but rather a collective act performed by the speaker and the hearer. Like all collective acts, it’s important for the participants to establish what they both agree on, called the common ground (Stalnaker, 1978). Speakers do this by grounding each other’s utterances. Grounding means acknowledging that the hearer has understood the speaker (Clark, 1996). (People need grounding for non-linguistic actions as well; the reason an elevator button lights up when it’s pressed is to acknowledge that the elevator has indeed been called, essentially grounding your action of pushing the button (Norman, 1988).)

Humans constantly ground each other’s utterances. We can ground by explicitly saying “OK”, as the agent does in A₈ or A₁₀. Or we can ground by repeating what the other person says; in utterance A₂ the agent repeats “in May”, demonstrating her
understanding to the client. Or notice that when the client answers a question, the agent begins the next question with “And”. The “And” implies that the new question is ‘in addition’ to the old question, again indicating to the client that the agent has successfully understood the answer to the last question.

Subdialogues and Dialogue Structure

Conversations have structure. Consider, for example, the local structure between speech acts discussed in the field of conversational analysis (Sacks et al., 1974). Questions set up an expectation for an answer. Proposals are followed by acceptance (or rejection). Compliments (“Nice jacket!”) often give rise to downplayers (“Oh, this old thing?”). These pairs, called adjacency pairs are composed of a first pair part and a second pair part (Schegloff, 1968), and these expectations can help systems decide what actions to take.

However, dialogue acts aren’t always followed immediately by their second pair part. The two parts can be separated by a side sequence (Jefferson 1972) or subdialogue. For example utterances C_{17} to A_{20} constitute a correction subdialogue (Litman 1985, Litman and Allen 1987, Chu-Carroll and Carberry 1998):

C_{17}: #Act. . . actually#, what day of the week is the 15th?
A_{18}: It’s a Friday.
C_{19}: Uh hmm. I would consider staying there an extra day til Sunday.
A_{20}: OK . . . OK. On Sunday I have . . .

The question in C_{17} interrupts the prior discourse, in which the agent was looking for a May 15 return flight. The agent must answer the question and also realize that “I would consider staying...til Sunday” means that the client would probably like to change their plan, and now go back to finding return flights, but for the 17th.

Another side sequence is the clarification question, which can form a subdialogue between a request and a response. This is especially common in dialogue systems where speech recognition errors causes the system to have to ask for clarifications or repetitions like the following:

User: What do you have going to UNKNOWN WORD on the 5th?
System: Let’s see, going where on the 5th?
User: Going to Hong Kong.
System: OK, here are some flights...

In addition to side-sequences, questions often have presequences, like the following example where a user starts with a question about the system’s capabilities (“Can you make train reservations”) before making a request.

User: Can you make train reservations?
System: Yes I can.
User: Great, I’d like to reserve a seat on the 4pm train to New York.

Initiative

Sometimes a conversation is completely controlled by one participant. For example a reporter interviewing a chef might ask questions, and the chef responds. We say that the reporter in this case has the conversational initiative (Carbonell, 1970; Nickerson, 1976). In normal human-human dialogue, however, it’s more common for initiative to shift back and forth between the participants, as they sometimes answer questions, sometimes ask them, sometimes take the conversations in new directions, sometimes not. You may ask me a question, and then I respond asking you
to clarify something you said, which leads the conversation in all sorts of ways. We call such interactions **mixed initiative** (Carbonell, 1970).

Full mixed initiative, while the norm for human-human conversations, can be difficult for dialogue systems. The most primitive dialogue systems tend to use **system-initiative**, where the system asks a question and the user can’t do anything until they answer it, or **user-initiative** like simple search engines, where the user specifies a query and the system passively responds. Even modern large language model-based dialogue systems, which come much closer to using full mixed initiative, often don’t have completely natural initiative switching. Getting this right is an important goal for modern systems.

**Inference and Implicature**

Inference is also important in dialogue understanding. Consider the client’s response $C_3$, repeated here:

$$A_2: \text{And, what day in May did you want to travel?}$$
$$C_3: \text{OK uh I need to be there for a meeting that’s from the 12th to the 15th.}$$

Notice that the client does not in fact answer the agent’s question. The client merely mentions a meeting at a certain time. What is it that licenses the agent to infer that the client is mentioning this meeting so as to inform the agent of the travel dates?

The speaker seems to expect the hearer to draw certain inferences; in other words, the speaker is communicating more information than seems to be present in the uttered words. This kind of example was pointed out by Grice (1975, 1978) as part of his theory of **conversational implicature**. **Implicature** means a particular class of licensed inferences. Grice proposed that what enables hearers to draw these inferences is that conversation is guided by a set of maxim*es*, general heuristics that play a guiding role in the interpretation of conversational utterances. One such maxim is the maxim of **relevance** which says that speakers attempt to be relevant, they don’t just utter random speech acts. When the client mentions a meeting on the 12th, the agent reasons ‘There must be some relevance for mentioning this meeting. What could it be?’. The agent knows that one precondition for having a meeting (at least before Web conferencing) is being at the place where the meeting is held, and therefore that maybe the meeting is a reason for the travel, and if so, then since people like to arrive the day before a meeting, the agent should infer that the flight should be on the 11th.

These subtle characteristics of human conversations (turns, speech acts, grounding, dialogue structure, initiative, and implicature) are among the reasons it is difficult to build dialogue systems that can carry on natural conversations with humans. Many of these challenges are active areas of dialogue systems research.

### 15.2 Frame-Based Dialogue Systems

A **task-based dialogue** system has the goal of helping a user solve a specific task like making a travel reservation or buying a product. Task-based dialogue systems are based around **frames**, first introduced in the early influential **GUS** system for travel planning (Bobrow et al., 1977). Frames are knowledge structures representing the details of the user’s task specification. Each frame consists of a collection of **slots**, each of which can take a set of possible **values**. Together a set of frames is
sometimes called a \textit{domain ontology}.

Here we’ll describe the most well-studied frame-based architecture, the \textit{dialogue-state} architecture, made up of the six components shown in Fig. 15.3. In the next sections we’ll introduce four of them, after introducing the idea of frames (deferring the speech recognition and synthesis components to Chapter 16).

15.2.1 \textbf{Frames and Slot Filling}

The frame and its slots in a task-based dialogue system specify what the system needs to know to perform its task. A hotel reservation system needs dates and locations. An alarm clock system needs a time. The system’s goal is to fill the slots in the frame with the fillers the user intends, and then perform the relevant action for the user (answering a question, or booking a flight).

Fig. 15.4 shows a sample frame for booking air travel, with some sample questions used for filling slots. In the simplest frame-based systems (including most commercial assistants until quite recently), these questions are pre-written templates, but in more sophisticated systems, questions are generated on-the-fly. The slot fillers are often constrained to a particular semantic type, like type \texttt{CITY} (taking on values like \textit{San Francisco}, or \textit{Hong Kong}) or \texttt{DATE}, \texttt{AIRLINE}, or \texttt{TIME}.

<table>
<thead>
<tr>
<th>Slot</th>
<th>Type</th>
<th>Example Question</th>
</tr>
</thead>
<tbody>
<tr>
<td>ORIGIN CITY</td>
<td>city</td>
<td>“From what city are you leaving?”</td>
</tr>
<tr>
<td>DESTINATION CITY</td>
<td>city</td>
<td>“Where are you going?”</td>
</tr>
<tr>
<td>DEPARTURE TIME</td>
<td>time</td>
<td>“When would you like to leave?”</td>
</tr>
<tr>
<td>DEPARTURE DATE</td>
<td>date</td>
<td>“What day would you like to leave?”</td>
</tr>
<tr>
<td>ARRIVAL TIME</td>
<td>time</td>
<td>“When do you want to arrive?”</td>
</tr>
<tr>
<td>ARRIVAL DATE</td>
<td>date</td>
<td>“What day would you like to arrive?”</td>
</tr>
</tbody>
</table>

Figure 15.4 \textit{A frame in a frame-based dialogue system, showing the type of each slot and a sample question used to fill the slot.}
Many domains require multiple frames. Besides frames for car or hotel reservations, we might need other frames for things like general route information (for questions like *Which airlines fly from Boston to San Francisco?*). That means the system must be able to disambiguate which slot of which frame a given input is supposed to fill.

The task of slot-filling is usually combined with two other tasks, to extract 3 things from each user utterance. The first is **domain classification**: is this user for example talking about airlines, programming an alarm clock, or dealing with their calendar? The second is user **intent determination**: what general task or goal is the user trying to accomplish? For example the task could be to Find a Movie, or Show a Flight, or Remove a Calendar Appointment. Together, the domain classification and intent determination tasks decide which frame we are filling. Finally, we need to do **slot filling** itself: extract the particular slots and fillers that the user intends the system to understand from their utterance with respect to their intent. From a user utterance like this:

```
Show me morning flights from Boston to San Francisco on Tuesday
```

a system might want to build a representation like:

```
DOMAIN: AIR-TRAVEL
INTENT: SHOW-FLIGHTS
ORIGIN-CITY: Boston
DEST-CITY: San Francisco
ORIGIN-DATE: Tuesday
ORIGIN-TIME: morning
```

Similarly an utterance like this:

```
Wake me tomorrow at 6
```

should give an intent like this:

```
DOMAIN: ALARM-CLOCK
INTENT: SET-ALARM
TIME: 2017-07-01 0600
```

The simplest dialogue systems use handwritten rules for slot-filling, like this regular expression for recognizing the SET-ALARM intent:

```
wake me (up) | set (the|an) alarm | get me up
```

But most systems use supervised machine-learning: each sentence in a training set is annotated with slots, domain, and intent, and a sequence model maps from input words to slot fillers, domain and intent. For example we’ll have pairs of sentences that are labeled for domain (AIRLINE) and intent (SHOWFLIGHT), and are also labeled with BIO representations for the slots and fillers. (Recall from Chapter 8 that in BIO tagging we introduce a tag for the beginning (B) and inside (I) of each slot label, and one for tokens outside (O) any slot label.)

```
0 0 0 0 0 B-DES I-DES 0 B-DEPTIME I-DEPTIME 0 AIRLINE-SHOWFLIGHT
```

Fig. 15.5 shows a typical architecture for inference. The input words $w_1...w_n$ are passed through a pretrained language model encoder, followed by a feedforward layer and a softmax at each token position over possible BIO tags, with the output a series of BIO tags $s_1...s_n$. We generally combine the domain-classification and intent-extraction tasks with slot-filling by adding a domain concatenated with an intent as the desired output for the final EOS token.

Once the sequence labeler has tagged the user utterance, a filler string can be extracted for each slot from the tags (e.g., “San Francisco”), and these word strings can then be normalized to the correct form in the ontology (perhaps the airport
code ‘SFO’), for example with dictionaries that specify that SF, SFO, and San Francisco are synonyms. Often in industrial contexts, combinations of rules and machine learning are used for each of these components.

We can make a very simple frame-based dialogue system by wrapping a small amount of code around this slot extractor. Mainly we just need to ask the user questions until all the slots are full, do a database query, then report back to the user, using hand-built templates for generating sentences.

### 15.2.2 Evaluating Task-Based Dialogue

**task error rate** We evaluate task-based systems by computing the task error rate, or task success rate: the percentage of times the system booked the right plane flight, or put the right event on the calendar. A more fine-grained, but less extrinsic metric is the slot error rate, the percentage of slots filled with the correct values:

$$\text{Slot Error Rate for a Sentence} = \frac{\text{# of inserted/deleted/substituted slots}}{\text{# of total reference slots for sentence}}$$

For example a system that extracted the slot structure below from this sentence:

(15.2) Make an appointment with Chris at 10:30 in Gates 104

<table>
<thead>
<tr>
<th>Slot</th>
<th>Filler</th>
</tr>
</thead>
<tbody>
<tr>
<td>PERSON</td>
<td>Chris</td>
</tr>
<tr>
<td>TIME</td>
<td>11:30 a.m.</td>
</tr>
<tr>
<td>ROOM</td>
<td>Gates 104</td>
</tr>
</tbody>
</table>

has a slot error rate of 1/3, since the TIME is wrong. Instead of error rate, slot precision, recall, and F-score can also be used. We can also measure efficiency costs like the length of the dialogue in seconds or turns.

### 15.3 Dialogue Acts and Dialogue State

While the naive slot-extractor system described above can handle simple dialogues, often we want more complex interactions. For example, we might want to confirm that we’ve understand the user, or ask them to repeat themselves. We can build a more sophisticated system using dialogue acts and dialogue state.
15.3.1 Dialogue Acts

Dialogue acts are a generalization of speech acts that also represent grounding. The set of acts can be general, or can be designed for particular dialogue tasks.

<table>
<thead>
<tr>
<th>Tag</th>
<th>Sys</th>
<th>User</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>HELLO(a = x, b = y, ... )</td>
<td>✓</td>
<td>✓</td>
<td>Open a dialogue and give info a = x, b = y, ...</td>
</tr>
<tr>
<td>INFORM(a = x, b = y, ... )</td>
<td>✓</td>
<td>✓</td>
<td>Give info a = x, b = y, ...</td>
</tr>
<tr>
<td>REQUEST(a, b = x, ...)</td>
<td>✓</td>
<td>✓</td>
<td>Request value for a given b = x, ...</td>
</tr>
<tr>
<td>REQALTS(a = x, ...)</td>
<td></td>
<td>✓</td>
<td>Request alternative with a = x, ...</td>
</tr>
<tr>
<td>CONFIRM(a = x, b = y, ...)</td>
<td>✓</td>
<td>✓</td>
<td>Explicitly confirm a = x, b = y, ...</td>
</tr>
<tr>
<td>CONFREQ(a = x, ..., d)</td>
<td>✓</td>
<td></td>
<td>Implicitly confirm a = x, ... and request value of d</td>
</tr>
<tr>
<td>SELECT(a = x, a = y)</td>
<td>✓</td>
<td></td>
<td>Implicitly confirm a = x, ... and request value of d</td>
</tr>
<tr>
<td>AFFIRM(a = x, b = y, ...)</td>
<td>✓</td>
<td>✓</td>
<td>Affirm and give further info a = x, b = y, ...</td>
</tr>
<tr>
<td>NEGATE(a = x)</td>
<td></td>
<td>✓</td>
<td>Negate and give corrected value a = x</td>
</tr>
<tr>
<td>DENY(a = x)</td>
<td></td>
<td>✓</td>
<td>Deny that a = x</td>
</tr>
<tr>
<td>BYE()</td>
<td>✓</td>
<td>✓</td>
<td>Close a dialogue</td>
</tr>
</tbody>
</table>

Figure 15.6 shows a tagset for a restaurant recommendation system, and Fig. 15.7 shows these tags labeling a sample dialogue from the HIS system (Young et al., 2010). This example also shows the content of each dialogue act, which are the slot fillers being communicated. So the user might INFORM the system that they want Italian food near a museum, or CONFIRM with the system that the price is reasonable.

<table>
<thead>
<tr>
<th>Utterance</th>
<th>Dialogue act</th>
</tr>
</thead>
<tbody>
<tr>
<td>U: Hi, I am looking for somewhere to eat.</td>
<td>hello(task = find, type=restaurant)</td>
</tr>
<tr>
<td>S: You are looking for a restaurant. What type of food do you like?</td>
<td>confreq(type = restaurant, food)</td>
</tr>
<tr>
<td>U: I’d like an Italian near the museum.</td>
<td>inform(food = Italian, near=museum)</td>
</tr>
<tr>
<td>S: Roma is a nice Italian restaurant near the museum.</td>
<td>inform(name = &quot;Roma&quot;, type = restaurant,</td>
</tr>
<tr>
<td></td>
<td>food = Italian, near = museum)</td>
</tr>
<tr>
<td>U: Is it reasonably priced?</td>
<td>confirm(pricerange = moderate)</td>
</tr>
<tr>
<td>S: Yes, Roma is in the moderate price range.</td>
<td>affirm(name = &quot;Roma&quot;, pricerange = moderate)</td>
</tr>
<tr>
<td>U: What is the phone number?</td>
<td>request(phone)</td>
</tr>
<tr>
<td>S: The number of Roma is 385456.</td>
<td>inform(name = &quot;Roma&quot;, phone = &quot;385456&quot;)</td>
</tr>
<tr>
<td>U: Ok, thank you goodby.</td>
<td>bye()</td>
</tr>
</tbody>
</table>

Figure 15.7 A dialogue from the HIS System of Young et al. (2010) using the dialogue acts in Fig. 15.6.

15.3.2 Dialogue State Tracking

The job of the dialogue-state tracker is to determine the current state of the frame (the fillers of each slot), and the user’s most recent dialogue act. The dialogue-state is not just the slot-fillers in the current sentence; it includes the entire state of the frame at this point, summarizing all of the user’s constraints. Fig. 15.8 from Mrkšić et al. (2017) shows the dialogue state after each turn.

Dialogue act detection is done just like domain or intent classification, by passing the input sentence through an encoder and adding an act classifier. Often passing in the prior dialogue act as well can improve classification. And since dialogue acts
place some constraints on the slots and values, the tasks of dialogue-act detection and slot-filling are often performed jointly. The state tracker can just take the output of a slot-filling sequence-model (Section 15.2.1) after each sentence, or do something more complicated like training a classifier to decide if a value has been changed.

**A special case: detecting correction acts.** If a dialogue system misrecognizes or misunderstands an utterance, users will repeat or reformulate the utterance. Detecting these user correction acts is quite important, especially for spoken language. Ironically, corrections are actually harder to recognize than normal sentences (Swerts et al., 2000), because users who are frustrated adjust their speech in a way that is difficult for speech recognizers (Goldberg et al., 2003). For example speakers often use a prosodic style for corrections called hyperarticulation, in which the utterance is louder or longer or exaggerated in pitch, such as *I said BAL-TI-MORE, not Boston* (Wade et al. 1992, Levow 1998, Hirschberg et al. 2001). Detecting acts can be part of the general dialogue act detection classifier, or can make use of special features beyond the words, like those shown below (Levow 1998, Litman et al. 1999, Hirschberg et al. 2001, Bulyko et al. 2005, Awadallah et al. 2015).

<table>
<thead>
<tr>
<th>features</th>
<th>examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>semantic</td>
<td>embedding similarity between correction and user’s prior utterance</td>
</tr>
<tr>
<td>phonetic</td>
<td>phonetic overlap between candidate correction act and user’s prior utterance (i.e. “WhatsApp” may be incorrectly recognized as “What’s up”)</td>
</tr>
<tr>
<td>prosodic</td>
<td>hyperarticulation, increases in F0 range, pause duration, and word duration</td>
</tr>
<tr>
<td>ASR</td>
<td>ASR confidence, language model probability</td>
</tr>
</tbody>
</table>

---

### 15.3.3 Dialogue Policy: Which act to generate

In early commercial frame-based systems, the dialogue policy is simple: ask questions until all the slots are full, do a database query, then report back to the user. A more sophisticated dialogue policy can help a system decide when to answer the user’s questions, when to instead ask the user a clarification question, and so on. A dialogue policy thus decides what dialogue act to generate. Choosing a dialogue act to generate, along with its arguments, is sometimes called content planning.

Let’s see how to do this for some important dialogue acts. Dialogue systems, especially speech systems, often misrecognize the users’ words or meaning. To ensure system and user share a common ground, systems must confirm understandings with the user or reject utterances that the system don’t understand. A system might use an explicit confirmation act to confirm with the user, like *Is that correct?* below:
When using an implicit confirmation act, a system instead grounds more implicitly, for example by repeating the system’s understanding as part of asking the next question, as *Shanghai* is confirmed in passing in this example:

U: I want to travel to to Shanghai
S: When do you want to travel to Shanghai?

There’s a tradeoff. Explicit confirmation makes it easier for users to correct misrecognitions by just answering “no” to the confirmation question. But explicit confirmation is time-consuming and awkward (Danieli and Gerbino 1995, Walker et al. 1998a). We also might want an act that expresses lack of understanding: rejection, for example with a prompt like *I’m sorry, I didn’t understand that*. To decide among these acts, we can make use of the fact that ASR systems often compute their confidence in their transcription (often based on the log-likelihood the system assigns the sentence). A system can thus choose to explicitly confirm only low-confidence sentences. Or systems might have a four-tiered level of confidence with three thresholds $\alpha$, $\beta$, and $\gamma$:

- $< \alpha$: low confidence reject
- $\geq \alpha$: above the threshold confirm explicitly
- $\geq \beta$: high confidence confirm implicitly
- $\geq \gamma$: very high confidence don’t confirm at all

15.3.4 Natural language generation: Sentence Realization

Once a dialogue act has been chosen, we need to generate the text of the response to the user. This part of the generation process is called sentence realization. Fig. 15.9 shows a sample input/output for the sentence realization phase. The content planner has chosen the dialogue act *RECOMMEND* and some slots (name, neighborhood, cuisine) and fillers. The sentence realizer generates a sentence like lines 1 or 2 (by training on examples of representation/sentence pairs from a corpus of labeled dialogues). Because we won’t see every restaurant or attribute in every possible wording, we can delexicalize: generalize the training examples by replacing specific slot value words in the training set with a generic placeholder token representing the slot. Fig. 15.10 shows the sentences in Fig. 15.9 delexicalized.

We can map from frames to delexicalized sentences with an encoder decoder model (Mrkšić et al. 2017, inter alia), trained on hand-labeled dialogue corpora like MultiWOZ (Budzianowski et al., 2018). The input to the encoder is a sequence of
15.4 Chatbots

Chatbots are systems that can carry on extended conversations with the goal of mimicking the unstructured conversations or ‘chats’ characteristic of informal human-human interaction. While early systems like ELIZA (Weizenbaum, 1966) or PARRY (Colby et al., 1971) had theoretical goals like testing theories of psychological counseling, for most of the last 50 years chatbots have been designed for entertainment. That changed with the recent rise of neural chatbots like ChatGPT, which incorporate solutions to NLP tasks like question answering, writing tools, or machine translation into a conversational interface. A conversation with ChatGPT is shown in Fig. 15.12. In this section we describe neural chatbot architectures and datasets.

15.4.1 Training chatbots

Data Chatbots are generally trained on a training set that includes standard large language model training data of the type discussed in Section 10.9.2: versions of the web from the Common Crawl, including news sites, Wikipedia, as well as books. For training chatbots, it is common to additionally add lots of dialogue data.

This can include datasets created specifically for training chatbots by hiring speakers of the language to have conversations, such as by having them take on personas or talk about knowledge provided to them. For example the Topical-Chat dataset has 11K crowdsourced conversations spanning 8 broad topics (Gopalakrishnan et al., 2019), the EMPATHETICDIALOGUES includes 25K crowdsourced con-
Conversations grounded in a specific situation where a speaker was feeling a specific emotion (Rashkin et al., 2019), and the SaFeRDialogues dataset (Ung et al., 2022) has 8k dialogues demonstrating graceful responses to conversational feedback about safety failures.

Such datasets are far too small to train a language model alone, and so it’s common to also pretrain on large datasets of pseudo-conversations drawn from Twitter (Ritter et al., 2010a), Reddit (Roller et al., 2021), Weibo (微博), and other social media platforms. To turn social media data into data that has the structure of a conversation, we can treat any post on the platform as the first turn in a conversation, and the sequence of comments/replies as subsequent turns in that conversation.

Datasets from the web can be enormously toxic, so it’s crucial to filter the dialogues first. This can be done by using the same toxicity classifiers we describe below in the fine-tuning section.

**Architecture**  For training chatbots, it’s most common to use the standard causal language model architecture, in which the model predicts each word given all the prior words, and the loss is the standard language modeling loss. Fig. 15.13 shows a standard training setup; no different than language model training in Chapter 10. The only difference is the data, which has the addition of significant conversation and pseudo-conversation data as described in the prior section. As usual, the left context can include the entire prior conversation (or as much as fits in the context window).

![Transformer Blocks](image)

**Figure 15.13** Training a causal (decoder-only) language model for a chatbot.

An alternative is to use the encoder-decoder architecture of Chapter 13. In this case the entire conversation up to the last turn (as much as fits in the context) is presented to the encoder, and the decoder generates the next turn.

![Encoder-Decoder](image)

**Figure 15.14** An alternative: an encoder-decoder language model for a chatbot.
In practice, dialogue systems require additional customization beyond just pre-training on dialogue data. In the next few sections we'll discuss various stages of fine-tuning that can be used for this customization.

15.4.2 Fine Tuning for Quality and Safety

It is a common practice for dialogue systems to use further labeled data for fine-tuning. One function of this fine-tuning step is to improve the quality of the dialogue, training the system to produce responses that are sensible and interesting. Another function might be to improve safety, keeping a dialogue system from suggesting harmful actions (like financial fraud, medical harm, inciting hatred, or abusing the user or other people).

In the simplest method for improving quality and safety, speakers of the language are given an initial prompt and instructions to have high-quality, safe dialogues. They then interact with an initial dialogue system and their responses are used to finetune the model, usually as part of the instruct tuning step we introduced in Chapter 12. Thus a dialogue system learns to answer questions, follow other instructions, and also carry on high-quality, safe dialogues, in a single multi-task learning format.

While fine-tuning on positive examples is helpful, it is generally insufficient and so it is common to add more discriminative data that specifically downweights low-quality or harmful responses. The simplest paradigm for this is to train a model to predict turn-level safety and quality values, by training on human-labeled ratings. Such ratings might be collected by first having speakers of the language carry on dialogues with a system, and then a second set of people act as labelers to label every system turn for its quality and safety, resulting in a binary label for quality and safety for each turn.

Once a dataset has been created with these labels, a language model can be used in a classification task to label the quality and safety of a turn. For example in the Lamda system (Cohen et al., 2022), a single language model is used in two phases, roughly corresponding to generative and discriminative tasks: first generating a response, and then generating a label. In the generative phase, the model is given the prior turn and a special RESPONSE token and generates the blue response turn. (In training, the training loss is given only for the blue response):

“What’s up? RESPONSE Not much.

In a second, discriminative phase, the model is fine-tuned to see an attribute (SENSIBLE, INTERESTING, UNSAFE) and then to predict a 0 or 1 value, again with training losses given only for the blue value.

What’s up? RESPONSE Not much. SENSIBLE 1
What’s up? RESPONSE Not much. INTERESTING 0
What’s up? RESPONSE Not much. UNSAFE 0

To use the system in inference, the model first generates a response given the context, and then it is given the attribute and asked to generate a rating. The result is a generated turn along with a label. This label isn’t shown to the user but can be use for filtering, either at training time or at deployment time. For example, the system can generate multiple potential responses, filter out any response that is unsafe, and return to the user the highest ranking response.
15.4.3 Learning to perform retrieval as part of responding

Modern chatbots are also trained to do retrieval (calls to Google or Bing or other search engines) as a component of generating a response. This is generally done by having a sort of fake dialogue participant called something like `Search Query` whose utterances are passed to a search engine. The system can be encouraged to do searches either by prompting or by fine-tuning.

For example in the Sparrow chatbot (Glaese et al., 2022), the prompt includes a few sample conversations that include two special users, `Search Query`, and `Search Results`:

<table>
<thead>
<tr>
<th>User:</th>
<th>What color is the sky?</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sparrow:</td>
<td>Blue.</td>
</tr>
<tr>
<td>User:</td>
<td>Why?</td>
</tr>
<tr>
<td>Search Query:</td>
<td>why is sky blue</td>
</tr>
<tr>
<td>Search Results:</td>
<td>Page title: Sky Except for direct sunlight, most of the light in the daytime sky is caused by scattering, which is dominated by a small-particle limit called Rayleigh scattering. The scattering due to molecule-sized particles (as in air) is greater in the directions both toward and away from the source of light than it is in directions perpendicular to the incident path. Scattering is significant for light at all visible wavelengths, but is stronger at the shorter (bluer) end of the visible spectrum, meaning that the scattered light is bluer than its source: the Sun. The remaining direct sunlight, having lost some of its shorter-wavelength components, appears slightly less blue.</td>
</tr>
<tr>
<td>Sparrow:</td>
<td>Because of the Rayleigh scattering. It causes short waves of blue light to be scattered more than the other colours in the spectrum.</td>
</tr>
<tr>
<td>User:</td>
<td>Who was Raleigh?</td>
</tr>
<tr>
<td>Search Query:</td>
<td>who was Raleigh?</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
</tr>
</tbody>
</table>

From these prompts, the system learns to generate texts with `Search Query` turns for fact-based questions from the user, and these are passed to a search engine to generate the `Search Results` turns.

Alternatively, systems can be finetuned to to know when to use a search engine. For example, labelers can interact with a system, fact check each of the responses, and whenever the system emits an incorrect response, perform the web search queries that the system should have used to check its answer, and then the iteration is recorded and used for fine-tuning. Or labelers can look at a transcript of a language model carrying on a dialogue, and similarly mark every place where a fact was wrong (or out-of-date) and write the set of search queries that would have been appropriate. A system is then finetuned to generate search query turns which are again passed to a search engine to generate the search responses. The set of pages or snippets returned by the search engine in the search response turn are then treated as the context for generation, similarly to the retrieval-based question-answering methods of Chapter 14.
15.4.4 RLHF

A more sophisticated family of methods uses reinforcement learning to learn to match human preferences for generated turns. In this method, RLHF for Reinforcement Learning from Human Feedback, we give a system a dialogue context and sample two possible turns from the language model. We then have humans label which of the two is better, creating a large dataset of sentence pairs with human preferences. These pairs are used to train a dialogue policy, and reinforcement learning is used to train the language model to generate turns that have higher rewards (Christiano et al., 2017; Ouyang et al., 2022). While using RLHF is the current state of the art at the time of this writing, a number of alternatives have been recently developed that don’t require reinforcement learning (Rafailov et al., 2023, e.g.,) and so this aspect of the field is changing very quickly.

15.4.5 Evaluating Chatbots

Chatbots are evaluated by humans, who assign a score. This can be the human who talked to the chatbot (participant evaluation) or a third party who reads a transcript of a human/chatbot conversation (observer evaluation). In the participant evaluation of See et al. (2019), the human evaluator chats with the model for six turns and rates the chatbot on 8 dimensions capturing conversational quality: avoiding repetition, interestingness, making sense, fluency, listening, inquisitiveness, humanness and engagingness on Likert scales like these:

**Engagingness** How much did you enjoy talking to this user?
- Not at all
- A little
- Somewhat
- A lot

**Making sense** How often did this user say something which did NOT make sense?
- Never made any sense
- Most responses didn’t make sense
- Some responses didn’t make sense
- Everything made perfect sense

Observer evaluations use third party annotators to look at the text of a complete conversation. Sometimes we’re interested in having raters assign a score to each system turn; for example (Artstein et al., 2009) have raters mark how **coherent** each turn is. Often, however, we just want a single high-level score to know if system A is better than system B. The **acute-eval** metric (Li et al., 2019a) is such an observer evaluation in which annotators look at two separate human-computer conversations and choose the system which performed better on four metrics: engagingness, interestingness, humanness, and knowledgability.

15.5 Dialogue System Design

Because of the important role of the user, the field of dialogue systems is closely linked with Human-Computer Interaction (HCI). This is especially true for task-oriented dialogue and assistants, where the design of dialogue strategies, sometimes called **voice user interface** design, generally follows **user-centered design** principles (Gould and Lewis, 1985):

1. **Study the user and task:** Understand the users and the task by interviewing users, investigating similar systems, and studying related human-human dialogues.

2. **Build simulations and prototypes:** A crucial tool in building dialogue systems is the **Wizard-of-Oz system**. In wizard systems, the users interact with what they
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think is a program but is in fact a human “wizard” disguised by a software interface (Gould et al. 1983, Good et al. 1984, Fraser and Gilbert 1991). The name comes from the children’s book The Wizard of Oz (Baum, 1900), in which the wizard turned out to be a simulation controlled by a man behind a curtain or screen. A wizard system can be used to test out an architecture before implementation; only the interface software and databases need to be in place. The wizard gets input from the user, uses a database interface to run queries based on the user utterance, and then outputs sentences, either by typing them or speaking them.

Wizard-of-Oz systems are not a perfect simulation, since the wizard doesn’t exactly simulate the errors or limitations of a real system; but wizard studies can still provide a useful first idea of the domain issues.

3. Iteratively test the design on users: An iterative design cycle with embedded user testing is essential in system design (Nielsen 1992, Cole et al. 1997, Yankelovich et al. 1995, Landauer 1995). For example in a well-known incident, an early dialogue system required the user to press a key to interrupt the system (Stifelman et al., 1993). But user testing showed users barged in (interrupted, talking over the system), which led to a redesign of the system to recognize overlapped speech. It’s also important to incorporate value sensitive design, in which we carefully consider during the design process the benefits, harms and possible stakeholders of the resulting system (Friedman et al. 2017, Friedman and Hendry 2019).

15.5.1 Ethical Issues in Dialogue System Design

Ethical issues have been key to how we think about designing artificial agents since well before we had dialogue systems. Mary Shelley (depicted below) centered her novel Frankenstein around the problem of creating artificial agents without considering ethical and humanistic concerns. One issue is the safety of users. If users seek information from dialogue systems in safety-critical situations like asking medical advice, or in emergency situations, or when indicating the intentions of self-harm, incorrect advice can be dangerous and even life-threatening. For example (Bickmore et al., 2018) gave participants medical problems to pose to three commercial dialogue systems (Siri, Alexa, Google Assistant) and asked them to determine an action to take based on the system responses; many of the proposed actions, if actually taken, would have led to harm or death.

A system can also harm users by verbally attacking them, or creating representational harms (Blodgett et al., 2020) by generating abusive or harmful stereotypes that demean particular groups of people. Both abuse and stereotypes can cause psychological harm to users. Microsoft’s 2016 Tay chatbot, for example, was taken offline 16 hours after it went live, when it began posting messages with racial slurs,
conspiracy theories, and personal attacks on its users. Tay had learned these biases and actions from its training data, including from users who seemed to be purposely teaching the system to repeat this kind of language (Neff and Nagy 2016). Henderson et al. (2017) examined dialogue datasets used to train corpus-based chatbots and found toxic and abusive language, especially in social media corpora like Twitter and Reddit, and indeed such language then appears in the text generated by language models and dialogue systems (Gehman et al. 2020; Xu et al. 2020) which can even amplify the bias from the training data (Dinan et al., 2020). Liu et al. (2020) developed another method for investigating bias, testing how neural dialogue systems responded to pairs of simulated user turns that are identical except for mentioning different genders or race. They found, for example, that simple changes like using the word ‘she’ instead of ‘he’ in a sentence caused systems to respond more offensively and with more negative sentiment.

Another important ethical issue is privacy. Already in the first days of ELIZA, Weizenbaum pointed out the privacy implications of people’s revelations to the chatbot. The ubiquity of in-home dialogue systems means they may often overhear private information (Henderson et al., 2017). If a chatbot is human-like, users are also more likely to disclose private information, and less likely to worry about the harm of this disclosure (Ischen et al., 2019). In general, chatbots that are trained on transcripts of human-human or human-machine conversation must anonymize personally identifiable information.

Finally, chatbots raise important issues of gender equality in addition to textual bias. Current chatbots are overwhelmingly given female names, likely perpetuating the stereotype of a subservient female servant (Paolino, 2017). And when users use sexually harassing language, most commercial chatbots evade or give positive responses rather than responding in clear negative ways (Fessler, 2017).

These ethical issues are an important area of investigation, including finding ways to mitigate problems of abuse and toxicity, like detecting and responding appropriately to toxic contexts (Wolf et al. 2017, Dinan et al. 2020, Xu et al. 2020). Value sensitive design, carefully considering possible harms in advance (Friedman et al. 2017, Friedman and Hendry 2019) is also important; (Dinan et al., 2021) give a number of suggestions for best practices in dialogue system design. For example getting informed consent from participants, whether they are used for training, or whether they are interacting with a deployed system is important. Because dialogue systems by definition involve human participants, researchers also work on these issues with the Institutional Review Boards (IRB) at their institutions, who help protect the safety of experimental subjects.

15.6 Summary

Chatbots and dialogue systems are crucial speech and language processing applications that are already widely used commercially.

- In human dialogue, speaking is a kind of action; these acts are referred to as speech acts or dialogue acts. Speakers also attempt to achieve common ground by acknowledging that they have understand each other. Conversation also is characterized by turn structure and dialogue structure.

- Chatbots are conversational systems designed to mimic the appearance of informal human conversation. Rule-based chatbots like ELIZA and its modern
descendants use rules to map user sentences into system responses. Corpus-based chatbots mine logs of human conversation to learn to automatically map user sentences into system responses.

- For task-based dialogue, most commercial dialogue systems use the GUS or frame-based architecture, in which the designer specifies frames consisting of slots that the system must fill by asking the user.

- The dialogue-state architecture augments the GUS frame-and-slot architecture with richer representations and more sophisticated algorithms for keeping track of user’s dialogue acts, policies for generating its own dialogue acts, and a natural language component.

- Dialogue systems are a kind of human-computer interaction, and general HCI principles apply in their design, including the role of the user, simulations such as Wizard-of-Oz systems, and the importance of iterative design and testing on real users.

**Bibliographical and Historical Notes**

The linguistic, philosophical, and psychological literature on dialogue is quite extensive. For example the idea that utterances in a conversation are a kind of **action** being performed by the speaker was due originally to the philosopher Wittgenstein (1953) but worked out more fully by Austin (1962) and his student John Searle. Various sets of speech acts have been defined over the years, and a rich linguistic and philosophical literature developed, especially focused on explaining the use of indirect speech acts. The idea of dialogue acts draws also from a number of other sources, including the ideas of adjacency pairs, pre-sequences, and other aspects of the interactional properties of human conversation developed in the field of **conversation analysis** (see Levinson (1983) for an introduction to the field). This idea that acts set up strong local dialogue expectations was also prefigured by Firth (1935, p. 70), in a famous quotation:

> Most of the give-and-take of conversation in our everyday life is stereotyped and very narrowly conditioned by our particular type of culture. It is a sort of roughly prescribed social ritual, in which you generally say what the other fellow expects you, one way or the other, to say.

Another important research thread modeled dialogue as a kind of collaborative behavior, including the ideas of common ground (Clark and Marshall, 1981), reference as a collaborative process (Clark and Wilkes-Gibbs, 1986), joint intention (Levesque et al., 1990), and shared plans (Grosz and Sidner, 1980).

The earliest conversational systems were simple pattern-action chatbots like ELIZA (Weizenbaum, 1966). ELIZA had a widespread influence on popular perceptions of artificial intelligence, and brought up some of the first ethical questions in natural language processing — such as the issues of privacy we discussed above as well the role of algorithms in decision-making — leading its creator Joseph Weizenbaum to fight for social responsibility in AI and computer science in general.

Computational-implemented theories of dialogue blossomed in the 1970. That period saw the very influential GUS system (Bobrow et al., 1977), which in the late 1970s established the frame-based paradigm that became the dominant industrial paradigm for dialogue systems for over 30 years.
Another influential line of research from that decade focused on modeling the hierarchical structure of dialogue. Grosz’s pioneering 1977b dissertation first showed that “task-oriented dialogues have a structure that closely parallels the structure of the task being performed” (p. 27), leading to her work with Sidner and others showing how to use similar notions of intention and plans to model discourse structure and coherence in dialogue. See, e.g., Lochbaum et al. (2000) for a summary of the role of intentional structure in dialogue.

Yet a third line, first suggested by Bruce (1975), suggested that since speech acts are actions, they should be planned like other actions, and drew on the AI planning literature (Fikes and Nilsson, 1971). A system seeking to find out some information can come up with the plan of asking the interlocutor for the information. A system hearing an utterance can interpret a speech act by running the planner “in reverse”, using inference rules to infer from what the interlocutor said what the plan might have been. Plan-based models of dialogue are referred to as BDI models because such planners model the beliefs, desires, and intentions (BDI) of the system and interlocutor. BDI models of dialogue were first introduced by Allen, Cohen, Perrault, and their colleagues in a number of influential papers showing how speech acts could be generated (Cohen and Perrault, 1979) and interpreted (Perrault and Allen 1980, Allen and Perrault 1980). At the same time, Wilensky (1983) introduced plan-based models of understanding as part of the task of interpreting stories.

In the 1990s, machine learning models that had first been applied to natural language processing began to be applied to dialogue tasks like slot filling (Miller et al. 1994, Pieraccini et al. 1991). This period also saw lots of analytic work on the linguistic properties of dialogue acts and on machine-learning-based methods for their detection. (Sag and Liberman 1975, Hinkelman and Allen 1989, Nagata and Morimoto 1994, Goodwin 1996, Chu-Carroll 1998, Shriberg et al. 1998, Stolcke et al. 2000, Gravano et al. 2012. This work strongly informed the development of the dialogue-state model (Larsson and Traum, 2000). Dialogue state tracking quickly became an important problem for task-oriented dialogue, and there has been an influential annual evaluation of state-tracking algorithms (Williams et al., 2016).

The turn of the century saw a line of work on applying reinforcement learning to dialogue, which first came out of AT&T and Bell Laboratories with work on MDP dialogue systems (Walker 2000, Levin et al. 2000, Singh et al. 2002) along with work on cue phrases, prosody, and rejection and confirmation. Reinforcement learning research turned quickly to the more sophisticated POMDP models (Roy et al. 2000, Lemon et al. 2006, Williams and Young 2007) applied to small slot-filling dialogue tasks. Neural reinforcement learning models have been used both for chatbot systems, for example simulating dialogues between two dialogue systems, rewarding good conversational properties like coherence and ease of answering (Li et al., 2016a), and for task-oriented dialogue (Williams et al., 2017).

By around 2010 the GUS architecture finally began to be widely used commercially in dialogue systems on phones like Apple’s Siri (Bellegarda, 2013) and other digital assistants.

The rise of the web gave rise to corpus-based chatbot architectures around the turn of the century, first using information retrieval models and then in the 2010s, after the rise of deep learning, with sequence-to-sequence models.

[TBD: Modern history of neural chatbots]

Other important dialogue areas include the study of affect in dialogue (Rashkin et al. 2019, Lin et al. 2019) and conversational interface design (Cohen et al. 2004, Harris 2005, Pearl 2017, Deibel and Evanhoe 2021).
Exercises

15.1 Write a finite-state automaton for a dialogue manager for checking your bank balance and withdrawing money at an automated teller machine.

15.2 A dispreferred response is a response that has the potential to make a person uncomfortable or embarrassed in the conversational context; the most common example dispreferred responses is turning down a request. People signal their discomfort with having to say no with surface cues (like the word well), or via significant silence. Try to notice the next time you or someone else utters a dispreferred response, and write down the utterance. What are some other cues in the response that a system might use to detect a dispreferred response? Consider non-verbal cues like eye gaze and body gestures.

15.3 When asked a question to which they aren’t sure they know the answer, people display their lack of confidence by cues that resemble other dispreferred responses. Try to notice some unsure answers to questions. What are some of the cues? If you have trouble doing this, read Smith and Clark (1993) and listen specifically for the cues they mention.

15.4 Implement a small air-travel help system based on text input. Your system should get constraints from users about a particular flight that they want to take, expressed in natural language, and display possible flights on a screen. Make simplifying assumptions. You may build in a simple flight database or you may use a flight information system on the Web as your backend.
I KNOW not whether
I see your meaning: if I do, it lies
Upon the wordy wavelets of your voice,
Dim as an evening shadow in a brook,
Thomas Lovell Beddoes, 1851

Understanding spoken language, or at least transcribing the words into writing, is one of the earliest goals of computer language processing. In fact, speech processing predates the computer by many decades! The first machine that recognized speech was a toy from the 1920s. “Radio Rex”, shown to the right, was a celluloid dog that moved (by means of a spring) when the spring was released by 500 Hz acoustic energy. Since 500 Hz is roughly the first formant of the vowel [eh] in “Rex”, Rex seemed to come when he was called (David, Jr. and Selfridge, 1962).

In modern times, we expect more of our automatic systems. The task of automatic speech recognition (ASR) is to map any waveform like this:

```
It’s time for lunch!
```

to the appropriate string of words:

```
It’s time for lunch!
```

Automatic transcription of speech by any speaker in any environment is still far from solved, but ASR technology has matured to the point where it is now viable for many practical tasks. Speech is a natural interface for communicating with smart home appliances, personal assistants, or cellphones, where keyboards are less convenient, in telephony applications like call-routing (“Accounting, please”) or in sophisticated dialogue applications (“I’d like to change the return date of my flight”). ASR is also useful for general transcription, for example for automatically generating captions for audio or video text (transcribing movies or videos or live discussions). Transcription is important in fields like law where dictation plays an important role. Finally, ASR is important as part of augmentative communication (interaction between computers and humans with some disability resulting in difficulties or inabilities in typing or audition). The blind Milton famously dictated Paradiso Lost to his daughters, and Henry James dictated his later novels after a repetitive stress injury.

What about the opposite problem, going from text to speech? This is a problem with an even longer history. In Vienna in 1769, Wolfgang von Kempelen built for
the Empress Maria Theresa the famous Mechanical Turk, a chess-playing automaton consisting of a wooden box filled with gears, behind which sat a robot mannequin who played chess by moving pieces with his mechanical arm. The Turk toured Europe and the Americas for decades, defeating Napoleon Bonaparte and even playing Charles Babbage. The Mechanical Turk might have been one of the early successes of artificial intelligence were it not for the fact that it was, alas, a hoax, powered by a human chess player hidden inside the box.

What is less well known is that von Kempelen, an extraordinarily prolific inventor, also built between 1769 and 1790 what was definitely not a hoax: the first full-sentence speech synthesizer, shown partially to the right. His device consisted of a bellows to simulate the lungs, a rubber mouthpiece and a nose aperture, a reed to simulate the vocal folds, various whistles for the fricatives, and a small auxiliary bellows to provide the puff of air for plosives. By moving levers with both hands to open and close apertures, and adjusting the flexible leather “vocal tract”, an operator could produce different consonants and vowels.

More than two centuries later, we no longer build our synthesizers out of wood and leather, nor do we need human operators. The modern task of speech synthesis, also called text-to-speech or TTS, is exactly the reverse of ASR; to map text:

It's time for lunch!

to an acoustic waveform:

Modern speech synthesis has a wide variety of applications. TTS is used in conversational agents that conduct dialogues with people, plays a role in devices that read out loud for the blind or in games, and can be used to speak for sufferers of neurological disorders, such as the late astrophysicist Steven Hawking who, after he lost the use of his voice because of ALS, spoke by manipulating a TTS system.

In the next sections we’ll show how to do ASR with encoder-decoders, introduce the CTC loss functions, the standard word error rate evaluation metric, and describe how acoustic features are extracted. We’ll then see how TTS can be modeled with almost the same algorithm in reverse, and conclude with a brief mention of other speech tasks.

16.1 The Automatic Speech Recognition Task

Before describing algorithms for ASR, let’s talk about how the task itself varies. One dimension of variation is vocabulary size. Some ASR tasks can be solved with extremely high accuracy, like those with a 2-word vocabulary (yes versus no) or an 11 word vocabulary like digit recognition (recognizing sequences of digits including zero to nine plus oh). Open-ended tasks like transcribing videos or human conversations, with large vocabularies of up to 60,000 words, are much harder.
A second dimension of variation is who the speaker is talking to. Humans speaking to machines (either dictating or talking to a dialogue system) are easier to recognize than humans speaking to humans. **Read speech**, in which humans are reading aloud, for example in audio books, is also relatively easy to recognize. Recognizing the speech of two humans talking to each other in **conversational speech**, for example, for transcribing a business meeting, is the hardest. It seems that when humans talk to machines, or read without an audience present, they simplify their speech quite a bit, talking more slowly and more clearly.

A third dimension of variation is channel and noise. Speech is easier to recognize if it’s recorded in a quiet room with head-mounted microphones than if it’s recorded by a distant microphone on a noisy city street, or in a car with the window open.

A final dimension of variation is accent or speaker-class characteristics. Speech is easier to recognize if the speaker is speaking the same dialect or variety that the system was trained on. Speech by speakers of regional or ethnic dialects, or speech by children can be quite difficult to recognize if the system is only trained on speakers of standard dialects, or only adult speakers.

A number of publicly available corpora with human-created transcripts are used to create ASR test and training sets to explore this variation; we mention a few of them here since you will encounter them in the literature. **LibriSpeech** is a large open-source read-speech 16 kHz dataset with over 1000 hours of audio books from the LibriVox project, with transcripts aligned at the sentence level (Panayotov et al., 2015). It is divided into an easier (“clean”) and a more difficult portion (“other”) with the clean portion of higher recording quality and with accents closer to US English. This was done by running a speech recognizer (trained on read speech from the Wall Street Journal) on all the audio, computing the WER for each speaker based on the gold transcripts, and dividing the speakers roughly in half, with recordings from lower-WER speakers called “clean” and recordings from higher-WER speakers “other”.

The **Switchboard** corpus of prompted telephone conversations between strangers was collected in the early 1990s; it contains 2430 conversations averaging 6 minutes each, totaling 240 hours of 8 kHz speech and about 3 million words (Godfrey et al., 1992). Switchboard has the singular advantage of an enormous amount of auxiliary hand-done linguistic labeling, including parses, dialogue act tags, phonetic and prosodic labeling, and discourse and information structure. The **CALLHOME** corpus was collected in the late 1990s and consists of 120 unscripted 30-minute telephone conversations between native speakers of English who were usually close friends or family (Canavan et al., 1997).

The Santa Barbara Corpus of Spoken American English (Du Bois et al., 2005) is a large corpus of naturally occurring everyday spoken interactions from all over the United States, mostly face-to-face conversation, but also town-hall meetings, food preparation, on-the-job talk, and classroom lectures. The corpus was anonymized by removing personal names and other identifying information (replaced by pseudonyms in the transcripts, and masked in the audio).

**CORAAL** is a collection of over 150 sociolinguistic interviews with African American speakers, with the goal of studying African American Language (AAL), the many variations of language used in African American communities (Kendall and Farrington, 2020). The interviews are anonymized with transcripts aligned at the utterance level. The **CHiME** Challenge is a series of difficult shared tasks with corpora that deal with robustness in ASR. The CHiME 5 task, for example, is ASR of conversational speech in real home environments (specifically dinner parties). The
corpus contains recordings of twenty different dinner parties in real homes, each with four participants, and in three locations (kitchen, dining area, living room), recorded both with distant room microphones and with body-worn mikes. The HKUST Mandarin Telephone Speech corpus has 1206 ten-minute telephone conversations between speakers of Mandarin across China, including transcripts of the conversations, which are between either friends or strangers (Liu et al., 2006). The AISHELL-1 corpus contains 170 hours of Mandarin read speech of sentences taken from various domains, read by different speakers mainly from northern China (Bu et al., 2017).

Figure 16.1 shows the rough percentage of incorrect words (the word error rate, or WER, defined on page 352) from state-of-the-art systems on some of these tasks. Note that the error rate on read speech (like the LibriSpeech audiobook corpus) is around 2%; this is a solved task, although these numbers come from systems that require enormous computational resources. By contrast, the error rate for transcribing conversations between humans is much higher; 5.8 to 11% for the Switchboard and CALLHOME corpora. The error rate is higher yet again for speakers of varieties like African American Vernacular English, and yet again for difficult conversational tasks like transcription of 4-speaker dinner party speech, which can have error rates as high as 81.3%. Character error rates (CER) are also much lower for read Mandarin speech than for natural conversation.

<table>
<thead>
<tr>
<th>English Tasks</th>
<th>WER%</th>
</tr>
</thead>
<tbody>
<tr>
<td>LibriSpeech audiobooks 960hour clean</td>
<td>1.4</td>
</tr>
<tr>
<td>LibriSpeech audiobooks 960hour other</td>
<td>2.6</td>
</tr>
<tr>
<td>Switchboard telephone conversations between strangers</td>
<td>5.8</td>
</tr>
<tr>
<td>CALLHOME telephone conversations between family</td>
<td>11.0</td>
</tr>
<tr>
<td>Sociolinguistic interviews, CORAAL (AAL)</td>
<td>27.0</td>
</tr>
<tr>
<td>CHiMe5 dinner parties with body-worn microphones</td>
<td>47.9</td>
</tr>
<tr>
<td>CHiMe5 dinner parties with distant microphones</td>
<td>81.3</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Chinese (Mandarin) Tasks</th>
<th>CER%</th>
</tr>
</thead>
<tbody>
<tr>
<td>AISHELL-1 Mandarin read speech corpus</td>
<td>6.7</td>
</tr>
<tr>
<td>HKUST Mandarin Chinese telephone conversations</td>
<td>23.5</td>
</tr>
</tbody>
</table>

Figure 16.1 Rough Word Error Rates (WER = % of words misrecognized) reported around 2020 for ASR on various American English recognition tasks, and character error rates (CER) for two Chinese recognition tasks.

16.2 Feature Extraction for ASR: Log Mel Spectrum

The first step in ASR is to transform the input waveform into a sequence of acoustic feature vectors, each vector representing the information in a small time window of the signal. Let’s see how to convert a raw wavefile to the most commonly used features, sequences of log mel spectrum vectors. A speech signal processing course is recommended for more details.

16.2.1 Sampling and Quantization

The input to a speech recognizer is a complex series of changes in air pressure. These changes in air pressure obviously originate with the speaker and are caused...
by the specific way that air passes through the glottis and out the oral or nasal cavities. We represent sound waves by plotting the change in air pressure over time. One metaphor which sometimes helps in understanding these graphs is that of a vertical plate blocking the air pressure waves (perhaps in a microphone in front of a speaker’s mouth, or the eardrum in a hearer’s ear). The graph measures the amount of compression or rarefaction (uncompression) of the air molecules at this plate. Figure 16.2 shows a short segment of a waveform taken from the Switchboard corpus of telephone speech of the vowel [iy] from someone saying “she just had a baby”.

The first step in digitizing a sound wave like Fig. 16.2 is to convert the analog representations (first air pressure and then analog electric signals in a microphone) into a digital signal. This analog-to-digital conversion has two steps: sampling and quantization. To sample a signal, we measure its amplitude at a particular time; the sampling rate is the number of samples taken per second. To accurately measure a wave, we must have at least two samples in each cycle: one measuring the positive part of the wave and one measuring the negative part. More than two samples per cycle increases the amplitude accuracy, but fewer than two samples causes the frequency of the wave to be completely missed. Thus, the maximum frequency wave that can be measured is one whose frequency is half the sample rate (since every cycle needs two samples). This maximum frequency for a given sampling rate is called the Nyquist frequency. Most information in human speech is in frequencies below 10,000 Hz; thus, a 20,000 Hz sampling rate would be necessary for complete accuracy. But telephone speech is filtered by the switching network, and only frequencies less than 4,000 Hz are transmitted by telephones. Thus, an 8,000 Hz sampling rate is sufficient for telephone-bandwidth speech like the Switchboard corpus, while 16,000 Hz sampling is often used for microphone speech.

Although using higher sampling rates produces higher ASR accuracy, we can’t combine different sampling rates for training and testing ASR systems. Thus if we are testing on a telephone corpus like Switchboard (8 KHz sampling), we must downsample our training corpus to 8 KHz. Similarly, if we are training on multiple corpora and one of them includes telephone speech, we downsample all the wideband corpora to 8Khz.

Amplitude measurements are stored as integers, either 8 bit (values from -128–127) or 16 bit (values from -32768–32767). This process of representing real-valued numbers as integers is called quantization; all values that are closer together than the minimum granularity (the quantum size) are represented identically. We refer to each sample at time index \( n \) in the digitized, quantized waveform as \( x[n] \).

Once data is quantized, it is stored in various formats. One parameter of these formats is the sample rate and sample size discussed above; telephone speech is often sampled at 8 kHz and stored as 8-bit samples, and microphone data is often sampled at 16 kHz and stored as 16-bit samples. Another parameter is the number of
channels. For stereo data or for two-party conversations, we can store both channels in the same file or we can store them in separate files. A final parameter is individual sample storage—linearly or compressed. One common compression format used for telephone speech is µ-law (often written u-law but still pronounced mu-law). The intuition of log compression algorithms like µ-law is that human hearing is more sensitive at small intensities than large ones; the log represents small values with more faithfulness at the expense of more error on large values. The linear (unlogged) values are generally referred to as linear PCM values (PCM stands for pulse code modulation, but never mind that). Here’s the equation for compressing a linear PCM sample value $x$ to 8-bit µ-law, (where $\mu = 255$ for 8 bits):

$$F(x) = \frac{\text{sgn}(x) \log(1 + \mu |x|)}{\log(1 + \mu)} \quad -1 \leq x \leq 1$$

(16.1)

There are a number of standard file formats for storing the resulting digitized waveform, such as Microsoft’s .wav and Apple’s AIFF all of which have special headers; simple headerless “raw” files are also used. For example, the .wav format is a subset of Microsoft’s RIFF format for multimedia files; RIFF is a general format that can represent a series of nested chunks of data and control information. Figure 16.3 shows a simple .wav file with a single data chunk together with its format chunk.

16.2.2 Windowing

From the digitized, quantized representation of the waveform, we need to extract spectral features from a small window of speech that characterizes part of a particular phoneme. Inside this small window, we can roughly think of the signal as stationary (that is, its statistical properties are constant within this region). (By contrast, in general, speech is a non-stationary signal, meaning that its statistical properties are not constant over time). We extract this roughly stationary portion of speech by using a window which is non-zero inside a region and zero elsewhere, running this window across the speech signal and multiplying it by the input waveform to produce a windowed waveform.

The speech extracted from each window is called a frame. The windowing is characterized by three parameters: the window size or frame size of the window (its width in milliseconds), the frame stride, (also called shift or offset) between successive windows, and the shape of the window.

To extract the signal we multiply the value of the signal at time $n$, $s[n]$ by the value of the window at time $n$, $w[n]$:

$$y[n] = w[n]s[n]$$

(16.2)

The window shape sketched in Fig. 16.4 is rectangular; you can see the extracted windowed signal looks just like the original signal. The rectangular window,
16.2  •  Feature Extraction for ASR: Log Mel Spectrum 343

Figure 16.4 Windowing, showing a 25 ms rectangular window with a 10 ms stride.

however, abruptly cuts off the signal at its boundaries, which creates problems when we do Fourier analysis. For this reason, for acoustic feature creation we more commonly use the Hamming window, which shrinks the values of the signal toward zero at the window boundaries, avoiding discontinuities. Figure 16.5 shows both; the equations are as follows (assuming a window that is \( L \) frames long):

\[
\text{rectangular} \quad w[n] = \begin{cases} 
1 & 0 \leq n \leq L - 1 \\
0 & \text{otherwise}
\end{cases}
\]  

(16.3)

\[
\text{Hamming} \quad w[n] = \begin{cases} 
0.54 - 0.46\cos\left(\frac{2\pi n}{L}\right) & 0 \leq n \leq L - 1 \\
0 & \text{otherwise}
\end{cases}
\]  

(16.4)

Figure 16.5 Windowing a sine wave with the rectangular or Hamming windows.

16.2.3 Discrete Fourier Transform

The next step is to extract spectral information for our windowed signal; we need to know how much energy the signal contains at different frequency bands. The tool
for extracting spectral information for discrete frequency bands for a discrete-time (sampled) signal is the discrete Fourier transform or DFT.

The input to the DFT is a windowed signal \( x[n] \ldots x[m] \), and the output, for each of \( N \) discrete frequency bands, is a complex number \( X[k] \) representing the magnitude and phase of that frequency component in the original signal. If we plot the magnitude against the frequency, we can visualize the spectrum that we introduced in Chapter 28. For example, Fig. 16.6 shows a 25 ms Hamming-windowed portion of a signal and its spectrum as computed by a DFT (with some additional smoothing).

![Figure 16.6](a) A 25 ms Hamming-windowed portion of a signal from the vowel [iy] and (b) its spectrum computed by a DFT.

We do not introduce the mathematical details of the DFT here, except to note that Fourier analysis relies on Euler’s formula, with \( j \) as the imaginary unit:

\[
e^{j\theta} = \cos \theta + j \sin \theta
\]

As a brief reminder for those students who have already studied signal processing, the DFT is defined as follows:

\[
X[k] = \sum_{n=0}^{N-1} x[n] e^{-j \frac{2\pi}{N} kn}
\]

A commonly used algorithm for computing the DFT is the fast Fourier transform or FFT. This implementation of the DFT is very efficient but only works for values of \( N \) that are powers of 2.

### 16.2.4 Mel Filter Bank and Log

The results of the FFT tell us the energy at each frequency band. Human hearing, however, is not equally sensitive at all frequency bands; it is less sensitive at higher frequencies. This bias toward low frequencies helps human recognition, since information in low frequencies (like formants) is crucial for distinguishing vowels or nasals, while information in high frequencies (like stop bursts or fricative noise) is less crucial for successful recognition. Modeling this human perceptual property improves speech recognition performance in the same way.

We implement this intuition by collecting energies, not equally at each frequency band, but according to the mel scale, an auditory frequency scale (Chapter 28). A mel (Stevens et al. 1937, Stevens and Volkmann 1940) is a unit of pitch. Pairs of sounds that are perceptually equidistant in pitch are separated by an equal number
of mels. The mel frequency \( m \) can be computed from the raw acoustic frequency by a log transformation:

\[
\text{mel}(f) = 1127 \ln(1 + \frac{f}{700})
\] (16.7)

We implement this intuition by creating a bank of filters that collect energy from each frequency band, spread logarithmically so that we have very fine resolution at low frequencies, and less resolution at high frequencies. Figure 16.7 shows a sample bank of triangular filters that implement this idea, that can be multiplied by the spectrum to get a mel spectrum.

Finally, we take the log of each of the mel spectrum values. The human response to signal level is logarithmic (like the human response to frequency). Humans are less sensitive to slight differences in amplitude at high amplitudes than at low amplitudes. In addition, using a log makes the feature estimates less sensitive to variations in input such as power variations due to the speaker’s mouth moving closer or further from the microphone.

16.3 Speech Recognition Architecture

The basic architecture for ASR is the encoder-decoder (implemented with either RNNs or Transformers), exactly the same architecture introduced for MT in Chapter 13. Generally we start from the log mel spectral features described in the previous section, and map to letters, although it’s also possible to map to induced morpheme-like chunks like wordpieces or BPE.

Fig. 16.8 sketches the standard encoder-decoder architecture, which is commonly referred to as the attention-based encoder decoder or AED, or listen attend and spell (LAS) after the two papers which first applied it to speech (Chorowski et al. 2014, Chan et al. 2016). The input is a sequence of \( t \) acoustic feature vectors \( F = f_1, f_2, ..., f_t \), one vector per 10 ms frame. The output can be letters or wordpieces; we’ll assume letters here. Thus the output sequence \( Y = (\langle \text{SOS} \rangle, y_1, ..., y_m \langle \text{EOS} \rangle) \), assuming special start of sequence and end of sequence tokens \( \langle \text{sos} \rangle \) and \( \langle \text{eos} \rangle \) and each \( y_i \) is a character; for English we might choose the set:

\[ y_i \in \{a, b, c, ..., z, 0, ..., 9, \langle \text{space} \rangle, \langle \text{comma} \rangle, \langle \text{period} \rangle, \langle \text{apostrophe} \rangle, \langle \text{unk} \rangle \} \]

Of course the encoder-decoder architecture is particularly appropriate when input and output sequences have stark length differences, as they do for speech, with
very long acoustic feature sequences mapping to much shorter sequences of letters or words. A single word might be 5 letters long but, supposing it lasts about 2 seconds, would take 200 acoustic frames (of 10ms each).

Because this length difference is so extreme for speech, encoder-decoder architectures for speech need to have a special compression stage that shortens the acoustic feature sequence before the encoder stage. (Alternatively, we can use a loss function that is designed to deal well with compression, like the CTC loss function we’ll introduce in the next section.)

The goal of the subsampling is to produce a shorter sequence $X = x_1, \ldots, x_n$ that will be the input to the encoder. The simplest algorithm is a method sometimes called low frame rate (Pundak and Sainath, 2016): for time $i$ we stack (concatenate) the acoustic feature vector $f_i$ with the prior two vectors $f_{i-1}$ and $f_{i-2}$ to make a new vector three times longer. Then we simply delete $f_{i-1}$ and $f_{i-2}$. Thus instead of (say) a 40-dimensional acoustic feature vector every 10 ms, we have a longer vector (say 120-dimensional) every 30 ms, with a shorter sequence length $n = \frac{t}{3}$.

After this compression stage, encoder-decoders for speech use the same architecture as for MT or other text, composed of either RNNs (LSTMs) or Transformers.

For inference, the probability of the output string $Y$ is decomposed as:

$$p(y_1, \ldots, y_n) = \prod_{i=1}^n p(y_i|y_1, \ldots, y_{i-1}, X) \quad (16.8)$$

We can produce each letter of the output via greedy decoding:

$$\hat{y}_i = \arg\max_{\text{char} \in \text{Alphabet}} P(\text{char}|y_1 \ldots y_{i-1}, X) \quad (16.9)$$

Alternatively we can use beam search as described in the next section. This is particularly relevant when we are adding a language model.

Adding a language model Since an encoder-decoder model is essentially a conditional language model, encoder-decoders implicitly learn a language model for the output domain of letters from their training data. However, the training data (speech...

---

1 There are also more complex alternatives for subsampling, like using a convolutional net that downsamples with max pooling, or layers of pyramidal RNNs, RNNs where each successive layer has half the number of RNNs as the previous layer.
paired with text transcriptions) may not include sufficient text to train a good language model. After all, it’s easier to find enormous amounts of pure text training data than it is to find text paired with speech. Thus we can can usually improve a model at least slightly by incorporating a very large language model.

The simplest way to do this is to use beam search to get a final beam of hypothesized sentences; this beam is sometimes called an **n-best list**. We then use a language model to **rescore** each hypothesis on the beam. The scoring is done by interpolating the score assigned by the language model with the encoder-decoder score used to create the beam, with a weight $\lambda$ tuned on a held-out set. Also, since most models prefer shorter sentences, ASR systems normally have some way of adding a length factor. One way to do this is to normalize the probability by the number of characters in the hypothesis $|Y|_c$. The following is thus a typical scoring function (Chan et al., 2016):

$$
\text{score}(Y|X) = \frac{1}{|Y|_c} \log P(Y|X) + \lambda \log P_{LM}(Y)
$$

(16.10)

### 16.3.1 Learning

Encoder-decoders for speech are trained with the normal cross-entropy loss generally used for conditional language models. At timestep $i$ of decoding, the loss is the log probability of the correct token (letter) $y_i$:

$$
L_{CE} = -\log p(y_i|y_1, \ldots, y_{i-1}, X)
$$

(16.11)

The loss for the entire sentence is the sum of these losses:

$$
L_{CE} = -\sum_{i=1}^{m} \log p(y_i|y_1, \ldots, y_{i-1}, X)
$$

(16.12)

This loss is then backpropagated through the entire end-to-end model to train the entire encoder-decoder.

As we described in Chapter 13, we normally use teacher forcing, in which the decoder history is forced to be the correct gold $y_i$ rather than the predicted $\hat{y}_i$. It’s also possible to use a mixture of the gold and decoder output, for example using the gold output 90% of the time, but with probability .1 taking the decoder output instead:

$$
L_{CE} = -\log p(y_i|y_1, \ldots, \hat{y}_{i-1}, X)
$$

(16.13)

### 16.4 CTC

We pointed out in the previous section that speech recognition has two particular properties that make it very appropriate for the encoder-decoder architecture, where the encoder produces an encoding of the input that the decoder uses attention to explore. First, in speech we have a very long acoustic input sequence $X$ mapping to a much shorter sequence of letters $Y$, and second, it’s hard to know exactly which part of $X$ maps to which part of $Y$.

In this section we briefly introduce an alternative to encoder-decoder: an algorithm and loss function called **CTC**, short for **Connectionist Temporal Classification**.
tion (Graves et al., 2006), that deals with these problems in a very different way. The intuition of CTC is to output a single character for every frame of the input, so that the output is the same length as the input, and then to apply a collapsing function that combines sequences of identical letters, resulting in a shorter sequence.

Let’s imagine inference on someone saying the word dinner, and let’s suppose we had a function that chooses the most probable letter for each input spectral frame representation \( x_i \). We’ll call the sequence of letters corresponding to each input frame an alignment, because it tells us where in the acoustic signal each letter aligns to. Fig. 16.9 shows one such alignment, and what happens if we use a collapsing function that just removes consecutive duplicate letters.

Well, that doesn’t work; our naive algorithm has transcribed the speech as diner, not dinner! Collapsing doesn’t handle double letters. There’s also another problem with our naive function; it doesn’t tell us what symbol to align with silence in the input. We don’t want to be transcribing silence as random letters!

The CTC algorithm solves both problems by adding to the transcription alphabet a special symbol for a blank, which we’ll represent as \( \omega \). The blank can be used in the alignment whenever we don’t want to transcribe a letter. Blank can also be used between letters; since our collapsing function collapses only consecutive duplicate letters, it won’t collapse across \( \omega \). More formally, let’s define the mapping \( B : a \rightarrow y \) between an alignment \( a \) and an output \( y \), which collapses all repeated letters and then removes all blanks. Fig. 16.10 sketches this collapsing function \( B \).

The CTC collapsing function is many-to-one; lots of different alignments map to the same output string. For example, the alignment shown in Fig. 16.10 is not the only alignment that results in the string dinner. Fig. 16.11 shows some other alignments that would produce the same output.

It’s useful to think of the set of all alignments that might produce the same output \( Y \). We’ll use the inverse of our \( B \) function, called \( B^{-1} \), and represent that set as
16.4 CTC Inference

Before we see how to compute $P_{CTC}(Y|X)$ let’s first see how CTC assigns a probability to one particular alignment $\hat{A} = \{\hat{a}_1, \ldots, \hat{a}_n\}$. CTC makes a strong conditional independence assumption: it assumes that, given the input $X$, the CTC model output $a_t$ at time $t$ is independent of the output labels at any other time $a_i$. Thus:

$$P_{CTC}(A|X) = \prod_{t=1}^{T} p(a_t|X) \tag{16.14}$$

Thus to find the best alignment $\hat{A} = \{\hat{a}_1, \ldots, \hat{a}_T\}$ we can greedily choose the character with the max probability at each time step $t$:

$$\hat{a}_t = \arg\max_{c \in C} p_t(c|X) \tag{16.15}$$

We then pass the resulting sequence $A$ to the CTC collapsing function $B$ to get the output sequence $Y$.

Let’s talk about how this simple inference algorithm for finding the best alignment $A$ would be implemented. Because we are making a decision at each time point, we can treat CTC as a sequence-modeling task, where we output one letter $\hat{y}_t$ at time $t$ corresponding to each input token $x_t$, eliminating the need for a full decoder. Fig. 16.12 sketches this architecture, where we take an encoder, produce a hidden state $h_t$ at each timestep, and decode by taking a softmax over the character vocabulary at each time step.

![Diagram of CTC Inference](image-url)
Alas, there is a potential flaw with the inference algorithm sketched in (Eq. 16.15) and Fig. 16.11. The problem is that we chose the most likely alignment \( A \), but the most likely alignment may not correspond to the most likely final collapsed output string \( Y \). That’s because there are many possible alignments that lead to the same output string, and hence the most likely output string might not correspond to the most probable alignment. For example, imagine the most probable alignment \( A \) for an input \( X = [x_1, x_2, x_3] \) is the string \([a b \epsilon] \) but the next two most probable alignments are \([b \epsilon b] \) and \([\epsilon b b] \). The output \( Y =[b b] \), summing over those two alignments, might be more probable than \( Y =[a b] \).

For this reason, the most probable output sequence \( Y \) is the one that has, not the single best CTC alignment, but the highest sum over the probability of all its possible alignments:

\[
P_{CTC}(Y|X) = \sum_{A \in B^{-1}(Y)} P(A|X)
\]

\[
= \sum_{A \in B^{-1}(Y)} \prod_{t=1}^{T} p(a_t|h_t)
\]

\[
\hat{Y} = \arg\max_{Y} P_{CTC}(Y|X) \tag{16.16}
\]

Alas, summing over all alignments is very expensive (there are a lot of alignments), so we approximate this sum by using a version of Viterbi beam search that cleverly keeps in the beam the high-probability alignments that map to the same output string, and sums those as an approximation of (Eq. 16.16). See Hannun (2017) for a clear explanation of this extension of beam search for CTC.

Because of the strong conditional independence assumption mentioned earlier (that the output at time \( t \) is independent of the output at time \( t - 1 \), given the input), CTC does not implicitly learn a language model over the data (unlike the attention-based encoder-decoder architectures). It is therefore essential when using CTC to interpolate a language model (and some sort of length factor \( L(Y) \)) using interpolation weights that are trained on a dev set:

\[
\text{score}_{CTC}(Y|X) = \log P_{CTC}(Y|X) + \lambda_1 \log P_{LM}(Y) + \lambda_2 L(Y) \tag{16.17}
\]

### 16.4.2 CTC Training

To train a CTC-based ASR system, we use negative log-likelihood loss with a special CTC loss function. Thus the loss for an entire dataset \( D \) is the sum of the negative log-likelihoods of the correct output \( Y \) for each input \( X \):

\[
L_{CTC} = \sum_{(X,Y) \in D} -\log P_{CTC}(Y|X) \tag{16.18}
\]

To compute CTC loss function for a single input pair \( (X,Y) \), we need the probability of the output \( Y \) given the input \( X \). As we saw in Eq. 16.16, to compute the probability of a given output \( Y \) we need to sum over all the possible alignments that would collapse to \( Y \). In other words:

\[
P_{CTC}(Y|X) = \sum_{A \in B^{-1}(Y)} \prod_{t=1}^{T} p(a_t|h_t) \tag{16.19}
\]
16.4 • CTC

Naively summing over all possible alignments is not feasible (there are too many alignments). However, we can efficiently compute the sum by using dynamic programming to merge alignments, with a version of the forward-backward algorithm also used to train HMMs (Appendix A) and CRFs. The original dynamic programming algorithms for both training and inference are laid out in (Graves et al., 2006); see (Hannun, 2017) for a detailed explanation of both.

16.4.3 Combining CTC and Encoder-Decoder

It’s also possible to combine the two architectures/loss functions we’ve described, the cross-entropy loss from the encoder-decoder architecture, and the CTC loss. Fig. 16.13 shows a sketch. For training, we can simply weight the two losses with a $\lambda$ tuned on a dev set:

$$L = -\lambda \log P_\text{enc\_dec}(Y|X) - (1-\lambda) \log P_\text{ctc}(Y|X)$$

(16.20)

For inference, we can combine the two with the language model (or the length penalty), again with learned weights:

$$\hat{Y} = \arg\max_Y [\lambda \log P_\text{enc\_dec}(Y|X) - (1-\lambda) \log P_\text{ctc}(Y|X) + \gamma \log P_\text{LM}(Y)]$$

(16.21)

16.4.4 Streaming Models: RNN-T for improving CTC

Because of the strong independence assumption in CTC (assuming that the output at time $t$ is independent of the output at time $t-1$), recognizers based on CTC don’t achieve as high an accuracy as the attention-based encoder-decoder recognizers. CTC recognizers have the advantage, however, that they can be used for streaming. Streaming means recognizing words on-line rather than waiting until the end of the sentence to recognize them. Streaming is crucial for many applications, from commands to dictation, where we want to start recognition while the user is still talking. Algorithms that use attention need to compute the hidden state sequence over the entire input first in order to provide the attention distribution context, before the decoder can start decoding. By contrast, a CTC algorithm can input letters from left to right immediately.

If we want to do streaming, we need a way to improve CTC recognition to remove the conditional independent assumption, enabling it to know about output history. The RNN-Transducer (RNN-T), shown in Fig. 16.14, is just such a model (Graves 2012, Graves et al. 2013). The RNN-T has two main components: a CTC
acoustic model, and a separate language model component called the **predictor** that conditions on the output token history. At each time step \(t\), the CTC encoder outputs a hidden state \(h_{\text{enc}}^t\) given the input \(x_1...x_t\). The language model predictor takes as input the previous output token (not counting blanks), outputting a hidden state \(h_{\text{pred}}^u\). The two are passed through another network whose output is then passed through a softmax to predict the next character.

\[
P_{\text{RNN-T}}(Y|X) = \sum_{A \in B^{-1}(Y)} P(A|X)
\]

\[
= \sum_{A \in B^{-1}(Y)} \prod_{t=1}^T p(a_t|h_{t},y_{<u})
\]

![Figure 16.14](image)

**Figure 16.14** The RNN-T model computing the output token distribution at time \(t\) by integrating the output of a CTC acoustic encoder and a separate ‘predictor’ language model.

### 16.5 ASR Evaluation: Word Error Rate

**word error**

The standard evaluation metric for speech recognition systems is the **word error rate**. The word error rate is based on how much the word string returned by the recognizer (the hypothesized word string) differs from a reference transcription. The first step in computing word error is to compute the **minimum edit distance** in words between the hypothesized and correct strings, giving us the minimum number of word **substitutions**, word **insertions**, and word **deletions** necessary to map between the correct and hypothesized strings. The word error rate (WER) is then defined as follows (note that because the equation includes insertions, the error rate can be greater than 100%):

\[
\text{Word Error Rate} = 100 \times \frac{\text{Insertions} + \text{Substitutions} + \text{Deletions}}{\text{Total Words in Correct Transcript}}
\]

**alignment**

Here is a sample **alignment** between a reference and a hypothesis utterance from the CallHome corpus, showing the counts used to compute the error rate:

<table>
<thead>
<tr>
<th>REF:</th>
<th>i *** ** UM the PHONE IS</th>
<th>i LEFT THE portable **** PHONE UPSTAIRS last night</th>
</tr>
</thead>
<tbody>
<tr>
<td>HYP:</td>
<td>i GOT IT TO the ***** FULLEST i LOVE TO portable FORM OF STORES last night</td>
<td></td>
</tr>
<tr>
<td>Eval:</td>
<td>I I S D S S S I S S</td>
<td></td>
</tr>
</tbody>
</table>

This utterance has six substitutions, three insertions, and one deletion:

\[
\text{Word Error Rate} = 100 \times \frac{6 + 3 + 1}{13} = 76.9\%
\]
The standard method for computing word error rates is a free script called sclite, available from the National Institute of Standards and Technologies (NIST) (NIST, 2005). Sclite is given a series of reference (hand-transcribed, gold-standard) sentences and a matching set of hypothesis sentences. Besides performing alignments, and computing word error rate, sclite performs a number of other useful tasks. For example, for error analysis it gives useful information such as confusion matrices showing which words are often misrecognized for others, and summarizes statistics of words that are often inserted or deleted. Sclite also gives error rates by speaker (if sentences are labeled for speaker ID), as well as useful statistics like the sentence error rate, the percentage of sentences with at least one word error.

Statistical significance for ASR: MAPSSWE or MacNemar

As with other language processing algorithms, we need to know whether a particular improvement in word error rate is significant or not.

The standard statistical tests for determining if two word error rates are different is the Matched-Pair Sentence Segment Word Error (MAPSSWE) test, introduced in Gillick and Cox (1989).

The MAPSSWE test is a parametric test that looks at the difference between the number of word errors the two systems produce, averaged across a number of segments. The segments may be quite short or as long as an entire utterance; in general, we want to have the largest number of (short) segments in order to justify the normality assumption and to maximize power. The test requires that the errors in one segment be statistically independent of the errors in another segment. Since ASR systems tend to use trigram LMs, we can approximate this requirement by defining a segment as a region bounded on both sides by words that both recognizers get correct (or by turn/utterance boundaries). Here’s an example from NIST (2007) with four regions:

<table>
<thead>
<tr>
<th>I</th>
<th>II</th>
<th>III</th>
<th>IV</th>
</tr>
</thead>
<tbody>
<tr>
<td>REF:</td>
<td>it was the best of times</td>
<td>it was the worst of times</td>
<td>it was</td>
</tr>
<tr>
<td>SYS A:</td>
<td>ITS</td>
<td>the best of times</td>
<td>IS the worst of times</td>
</tr>
<tr>
<td>SYS B:</td>
<td>it was the best</td>
<td>times it</td>
<td>WON the TEST</td>
</tr>
</tbody>
</table>

In region I, system A has two errors (a deletion and an insertion) and system B has zero; in region III, system A has one error (a substitution) and system B has two. Let’s define a sequence of variables \( Z_i \) representing the difference between the errors in the two systems as follows:

\[
N_A^i \quad \text{the number of errors made on segment } i \text{ by system A} \\
N_B^i \quad \text{the number of errors made on segment } i \text{ by system B} \\
Z = N_A^i - N_B^i, i = 1, 2, \ldots, n \quad \text{where } n \text{ is the number of segments}
\]

In the example above, the sequence of \( Z \) values is \( \{2, -1, -1, 1\} \). Intuitively, if the two systems are identical, we would expect the average difference, that is, the average of the \( Z \) values, to be zero. If we call the true average of the differences \( \mu_z \), we would thus like to know whether \( \mu_z = 0 \). Following closely the original proposal and notation of Gillick and Cox (1989), we can estimate the true average from our limited sample as \( \hat{\mu}_z = \sum_{i=1}^n Z_i / n \). The estimate of the variance of the \( Z_i \)’s is

\[
\sigma_z^2 = \frac{1}{n-1} \sum_{i=1}^n (Z_i - \hat{\mu}_z)^2
\] (16.22)
Let
\[ W = \frac{\mu_z}{\sigma_z / \sqrt{n}} \]  
(16.23)

For a large enough \( n (> 50) \), \( W \) will approximately have a normal distribution with unit variance. The null hypothesis is \( H_0 : \mu_z = 0 \), and it can thus be rejected if \( 2 \times P(Z \geq |w|) \leq 0.05 \) (two-tailed) or \( P(Z \geq |w|) \leq 0.05 \) (one-tailed), where \( Z \) is standard normal and \( w \) is the realized value \( W \); these probabilities can be looked up in the standard tables of the normal distribution.

Earlier work sometimes used McNemar’s test for significance, but McNemar’s is only applicable when the errors made by the system are independent, which is not true in continuous speech recognition, where errors made on a word are extremely dependent on errors made on neighboring words.

Could we improve on word error rate as a metric? It would be nice, for example, to have something that didn’t give equal weight to every word, perhaps valuing content words like Tuesday more than function words like a or of. While researchers generally agree that this would be a good idea, it has proved difficult to agree on a metric that works in every application of ASR. For dialogue systems, however, where the desired semantic output is more clear, a metric called slot error rate or concept error rate has proved extremely useful; it is discussed in Chapter 15 on page 323.

16.6 TTS

The goal of text-to-speech (TTS) systems is to map from strings of letters to waveforms, a technology that’s important for a variety of applications from dialogue systems to games to education.

Like ASR systems, TTS systems are generally based on the encoder-decoder architecture, either using LSTMs or Transformers. There is a general difference in training. The default condition for ASR systems is to be speaker-independent: they are trained on large corpora with thousands of hours of speech from many speakers because they must generalize well to an unseen test speaker. By contrast, in TTS, it’s less crucial to use multiple voices, and so basic TTS systems are speaker-dependent: trained to have a consistent voice, on much less data, but all from one speaker. For example, one commonly used public domain dataset, the LJ speech corpus, consists of 24 hours of one speaker, Linda Johnson, reading audio books in the LibriVox project (Ito and Johnson, 2017), much smaller than standard ASR corpora which are hundreds or thousands of hours.\(^2\)

We generally break up the TTS task into two components. The first component is an encoder-decoder model for spectrogram prediction: it maps from strings of letters to mel spectrographs: sequences of mel spectral values over time. Thus we

\(^2\) There is also recent TTS research on the task of multi-speaker TTS, in which a system is trained on speech from many speakers, and can switch between different voices.
might map from this string:

\[ \text{It's time for lunch!} \]

to the following mel spectrogram:

![](mel_spectrogram.png)

The second component maps from mel spectrograms to waveforms. Generating waveforms from intermediate representations like spectrograms is called **vocoding** and this second component is called a **vocoder**:

These standard encoder-decoder algorithms for TTS are still quite computationally intensive, so a significant focus of modern research is on ways to speed them up.

### 16.6.1 TTS Preprocessing: Text normalization

Before either of these two steps, however, TTS systems require text normalization preprocessing for handling **non-standard words**: numbers, monetary amounts, dates, and other concepts that are verbalized differently than they are spelled. A TTS system seeing a number like 151 needs to know to verbalize it as *one hundred fifty one* if it occurs as $151$ but as *one fifty one* if it occurs in the context 151 Chapultepec Ave. The number 1750 can be spoken in at least four different ways, depending on the context:

- **seventeen fifty:** (in “The European economy in 1750”)
- **one seven five zero:** (in “The password is 1750”)
- **seventeen hundred and fifty:** (in “1750 dollars”)
- **one thousand, seven hundred, and fifty:** (in “1750 dollars”)

Often the verbalization of a non-standard word depends on its meaning (what Taylor (2009) calls its **semiotic class**). Fig. 16.15 lays out some English non-standard word types.

Many classes have preferred realizations. A year is generally read as paired digits (e.g., **seventeen fifty** for 1750). $3.2$ billion must be read out with the word **dollars** at the end, as **three point two billion dollars**. Some abbreviations like **N.Y.** are expanded (to **New York**), while other acronyms like **GPU** are pronounced as letter sequences. In languages with grammatical gender, normalization may depend on morphological properties. In French, the phrase *1 mangue* (‘one mangue’) is normalized to *une mangue*, but *1 ananas* (‘one pineapple’) is normalized to *un ananas*. In German, *Heinrich IV* (‘Henry IV’) can be normalized to *Heinrich der Vierte*, *Heinrich des Vierten*, *Heinrich dem Vierten*, or *Heinrich den Vierten* depending on the grammatical case of the noun (Demberg, 2006).
Modern end-to-end TTS systems can learn to do some normalization themselves, but TTS systems are only trained on a limited amount of data (like the 220,000 words we mentioned above for the LJ corpus (Ito and Johnson, 2017)), and so a separate normalization step is important.

Normalization can be done by rule or by an encoder-decoder model. Rule-based normalization is done in two stages: tokenization and verbalization. In the tokenization stage we hand-write rules to detect non-standard words. These can be regular expressions, like the following for detecting years:

```
/([0-9][0-9][0-9])|(20[0-9][0-9])
```

A second pass of rules express how to verbalize each semiotic class. Larger TTS systems instead use more complex rule-systems, like the Kestral system of (Ebden and Sproat, 2015), which first classifies and parses each input into a normal form and then produces text using a verbalization grammar. Rules have the advantage that they don’t require training data, and they can be designed for high precision, but can be brittle, and require expert rule-writers so are hard to maintain.

The alternative model is to use encoder-decoder models, which have been shown to work better than rules for such transduction tasks, but do require expert-labeled training sets in which non-standard words have been replaced with the appropriate verbalization; such training sets for some languages are available (Sproat and Gorman 2018, Zhang et al. 2019).

In the simplest encoder-decoder setting, we simply treat the problem like machine translation, training a system to map from:

```
They live at 224 Mission St.
```

to

```
They live at two twenty four Mission Street
```

While encoder-decoder algorithms are highly accurate, they occasionally produce errors that are egregious; for example normalizing 45 minutes as forty five millimeters. To address this, more complex systems use mechanisms like lightweight covering grammars, which enumerate a large set of possible verbalizations but don’t try to disambiguate, to constrain the decoding to avoid such outputs (Zhang et al., 2019).

## 16.6.2 TTS: Spectrogram prediction

The exact same architecture we described for ASR—the encoder-decoder with attention—can be used for the first component of TTS. Here we’ll give a simplified overview.
of the Tacotron2 architecture (Shen et al., 2018), which extends the earlier Tacotron (Wang et al., 2017) architecture and the Wavenet vocoder (van den Oord et al., 2016). Fig. 16.16 sketches out the entire architecture.

The encoder’s job is to take a sequence of letters and produce a hidden representation representing the letter sequence, which is then used by the attention mechanism in the decoder. The Tacotron2 encoder first maps every input grapheme to a 512-dimensional character embedding. These are then passed through a stack of 3 convolutional layers, each containing 512 filters with shape 5 × 1, i.e., each filter spanning 5 characters, to model the larger letter context. The output of the final convolutional layer is passed through a biLSTM to produce the final encoding. It’s common to use a slightly higher quality (but slower) version of attention called location-based attention, in which the computation of the α values (Eq. 9.37 in Chapter 9) makes use of the α values from the prior time-state.

In the decoder, the predicted mel spectrum from the prior time slot is passed through a small pre-net as a bottleneck. This prior output is then concatenated with the encoder’s attention vector context and passed through 2 LSTM layers. The output of this LSTM is used in two ways. First, it is passed through a linear layer, and some output processing, to autoregressively predict one 80-dimensional log-mel filterbank vector frame (50 ms, with a 12.5 ms stride) at each step. Second, it is passed through another linear layer to a sigmoid to make a “stop token prediction” decision about whether to stop producing output.

The system is trained on gold log-mel filterbank features, using teacher forcing, that is the decoder is fed the correct log-model spectral feature at each decoder step instead of the predicted decoder output from the prior step.

### 16.6.3 TTS: Vocoder

The vocoder for Tacotron 2 is an adaptation of the Wavenet vocoder (van den Oord et al., 2016). Here we’ll give a somewhat simplified description of vocoding using WaveNet.

Recall that the goal of the vocoding process here will be to invert a log mel spectrum representations back into a time-domain waveform representation. WaveNet is an autoregressive network, like the language models we introduced in Chapter 9. It
takes spectrograms as input and produces audio output represented as sequences of 8-bit mu-law (page 342). The probability of a waveform, a sequence of 8-bit mu-law values \( Y = y_1, \ldots, y_t \), given an intermediate input mel spectrogram \( h \) is computed as:

\[
p(Y) = \prod_{t=1}^{T} P(y_t | y_1, \ldots, y_{t-1}, h_1, \ldots, h_t)
\]  

(16.24)

This probability distribution is modeled by a stack of special convolution layers, which include a specific convolutional structure called dilated convolutions, and a specific non-linearity function.

A dilated convolution is a subtype of causal convolutional layer. Causal or masked convolutions look only at the past input, rather than the future; the prediction of \( y_{t+1} \) can only depend on \( y_1, \ldots, y_t \), useful for autoregressive left-to-right processing. In dilated convolutions, at each successive layer we apply the convolutional filter over a span longer than its length by skipping input values. Thus at time \( t \) with a dilation value of 1, a convolutional filter of length 2 would see input values \( x_t \) and \( x_{t-1} \). But a filter with a distillation value of 2 would skip an input, so would see input values \( x_t \) and \( x_{t-1} \). Fig. 16.17 shows the computation of the output at time \( t \) with 4 dilated convolution layers with dilation values, 1, 2, 4, and 8.

![Dilated convolutions](image)

Figure 16.17 Dilated convolutions, showing one dilation cycle size of 4, i.e., dilation values of 1, 2, 4, 8. Figure from van den Oord et al. (2016).

The Tacotron 2 synthesizer uses 12 convolutional layers in two cycles with a dilation cycle size of 6, meaning that the first 6 layers have dilations of 1, 2, 4, 8, 16, and 32, and the next 6 layers again have dilations of 1, 2, 4, 8, 16, and 32. Dilated convolutions allow the vocoder to grow the receptive field exponentially with depth.

WaveNet predicts mu-law audio samples. Recall from page 342 that this is a standard compression for audio in which the values at each sampling timestep are compressed into 8-bits. This means that we can predict the value of each sample with a simple 256-way categorical classifier. The output of the dilated convolutions is thus passed through a softmax which makes this 256-way decision.

The spectrogram prediction encoder-decoder and the WaveNet vocoder are trained separately. After the spectrogram predictor is trained, the spectrogram prediction network is run in teacher-forcing mode, with each predicted spectral frame conditioned on the encoded text input and the previous frame from the ground truth spectrogram. This sequence of ground truth-aligned spectral features and gold audio output is then used to train the vocoder.

This has been only a high-level sketch of the TTS process. There are numerous important details that the reader interested in going further with TTS may want...
to look into. For example WaveNet uses a special kind of a gated activation function as its non-linearity, and contains residual and skip connections. In practice, predicting 8-bit audio values doesn’t as work as well as 16-bit, for which a simple softmax is insufficient, so decoders use fancier ways as the last step of predicting audio sample values, like mixtures of distributions. Finally, the WaveNet vocoder as we have described it would be so slow as to be useless; many different kinds of efficiency improvements are necessary in practice, for example by finding ways to do non-autoregressive generation, avoiding the latency of having to wait to generate each frame until the prior frame has been generated, and instead making predictions in parallel. We encourage the interested reader to consult the original papers and various version of the code.

16.6.4 TTS Evaluation

Speech synthesis systems are evaluated by human listeners. (The development of a good automatic metric for synthesis evaluation, one that would eliminate the need for expensive and time-consuming human listening experiments, remains an open and exciting research topic.)

We evaluate the quality of synthesized utterances by playing a sentence to listeners and ask them to give a mean opinion score (MOS), a rating of how good the synthesized utterances are, usually on a scale from 1–5. We can then compare systems by comparing their MOS scores on the same sentences (using, e.g., paired t-tests to test for significant differences).

If we are comparing exactly two systems (perhaps to see if a particular change actually improved the system), we can use AB tests. In AB tests, we play the same sentence synthesized by two different systems (an A and a B system). The human listeners choose which of the two utterances they like better. We do this for say 50 sentences (presented in random order) and compare the number of sentences preferred for each system.

16.7 Other Speech Tasks

While we have focused on speech recognition and TTS in this chapter, there are a wide variety of speech-related tasks.

The task of **wake word** detection is to detect a word or short phrase, usually in order to wake up a voice-enable assistant like Alexa, Siri, or the Google Assistant. The goal with wake words is build the detection into small devices at the computing edge, to maintain privacy by transmitting the least amount of user speech to a cloud-based server. Thus wake word detectors need to be fast, small footprint software that can fit into embedded devices. Wake word detectors usually use the same frontend feature extraction we saw for ASR, often followed by a whole-word classifier.

**Speaker diarization** is the task of determining ‘who spoke when’ in a long multi-speaker audio recording, marking the start and end of each speaker’s turns in the interaction. This can be useful for transcribing meetings, classroom speech, or medical interactions. Often diarization systems use voice activity detection (VAD) to find segments of continuous speech, extract speaker embedding vectors, and cluster the vectors to group together segments likely from the same speaker. More recent work is investigating end-to-end algorithms to map directly from input speech to a sequence of speaker labels for each frame.
Speaker recognition, is the task of identifying a speaker. We generally distinguish the subtasks of speaker verification, where we make a binary decision (is this speaker X or not?), such as for security when accessing personal information over the telephone, and speaker identification, where we make a one of N decision trying to match a speaker’s voice against a database of many speakers. These tasks are related to language identification, in which we are given a wavefile and must identify which language is being spoken; this is useful for example for automatically directing callers to human operators that speak appropriate languages.

16.8 Summary

This chapter introduced the fundamental algorithms of automatic speech recognition (ASR) and text-to-speech (TTS).

- The task of speech recognition (or speech-to-text) is to map acoustic waveforms to sequences of graphemes.
- The input to a speech recognizer is a series of acoustic waves, that are sampled, quantized, and converted to a spectral representation like the log mel spectrum.
- Two common paradigms for speech recognition are the encoder-decoder with attention model, and models based on the CTC loss function. Attention-based models have higher accuracies, but models based on CTC more easily adapt to streaming: outputting graphemes online instead of waiting until the acoustic input is complete.
- ASR is evaluated using the Word Error Rate; the edit distance between the hypothesis and the gold transcription.
- TTS systems are also based on the encoder-decoder architecture. The encoder maps letters to an encoding, which is consumed by the decoder which generates mel spectrogram output. A neural vocoder then reads the spectrogram and generates waveforms.
- TTS systems require a first pass of text normalization to deal with numbers and abbreviations and other non-standard words.
- TTS is evaluated by playing a sentence to human listeners and having them give a mean opinion score (MOS) or by doing AB tests.

Bibliographical and Historical Notes

ASR A number of speech recognition systems were developed by the late 1940s and early 1950s. An early Bell Labs system could recognize any of the 10 digits from a single speaker (Davis et al., 1952). This system had 10 speaker-dependent stored patterns, one for each digit, each of which roughly represented the first two vowel formants in the digit. They achieved 97%–99% accuracy by choosing the pattern that had the highest relative correlation coefficient with the input. Fry (1959) and Denes (1959) built a phoneme recognizer at University College, London, that recognized four vowels and nine consonants based on a similar pattern-recognition principle. Fry and Denes’s system was the first to use phoneme transition probabilities to constrain the recognizer.
The late 1960s and early 1970s produced a number of important paradigm shifts. First were a number of feature-extraction algorithms, including the efficient fast Fourier transform (FFT) (Cooley and Tukey, 1965), the application of cepstral processing to speech (Oppenheim et al., 1968), and the development of LPC for speech coding (Atal and Hanauer, 1971). Second were a number of ways of handling warping; stretching or shrinking the input signal to handle differences in speaking rate and segment length when matching against stored patterns. The natural algorithm for solving this problem was dynamic programming, and, as we saw in Appendix A, the algorithm was reinvented multiple times to address this problem. The first application to speech processing was by Vintsyuk (1968), although his result was not picked up by other researchers, and was reinvented by Velichko and Zagoruyko (1970) and Sakoe and Chiba (1971) (and 1984). Soon afterward, Itakura (1975) combined this dynamic programming idea with the LPC coefficients that had previously been used only for speech coding. The resulting system extracted LPC features from incoming words and used dynamic programming to match them against stored LPC templates. The non-probabilistic use of dynamic programming to match a template against incoming speech is called dynamic time warping.

The third innovation of this period was the rise of the HMM. Hidden Markov models seem to have been applied to speech independently at two laboratories around 1972. One application arose from the work of statisticians, in particular Baum and colleagues at the Institute for Defense Analyses in Princeton who applied HMMs to various prediction problems (Baum and Petrie 1966, Baum and Eagon 1967). James Baker learned of this work and applied the algorithm to speech processing (Baker, 1975a) during his graduate work at CMU. Independently, Frederick Jelinek and collaborators (drawing from their research in information-theoretical models influenced by the work of Shannon (1948)) applied HMMs to speech at the IBM Thomas J. Watson Research Center (Jelinek et al., 1975). One early difference was the decoding algorithm; Baker’s DRAGON system used Viterbi (dynamic programming) decoding, while the IBM system applied Jelinek’s stack decoding algorithm (Jelinek, 1969). Baker then joined the IBM group for a brief time before founding the speech-recognition company Dragon Systems.

The use of the HMM, with Gaussian Mixture Models (GMMs) as the phonetic component, slowly spread through the speech community, becoming the dominant paradigm by the 1990s. One cause was encouragement by ARPA, the Advanced Research Projects Agency of the U.S. Department of Defense. ARPA started a five-year program in 1971 to build 1000-word, constrained grammar, few speaker speech understanding (Klatt, 1977), and funded four competing systems of which Carnegie-Mellon University’s Harpy system (Lowerre, 1976), which used a simplified version of Baker’s HMM-based DRAGON system was the best of the tested systems. ARPA (and then DARPA) funded a number of new speech research programs, beginning with 1000-word speaker-independent read-speech tasks like “Resource Management” (Price et al., 1988), recognition of sentences read from the Wall Street Journal (WSJ), Broadcast News domain (LDC 1998, Graff 1997) (transcription of actual news broadcasts, including quite difficult passages such as on-the-street interviews) and the Switchboard, CallHome, CallFriend, and Fisher domains (Godfrey et al. 1992, Cieri et al. 2004) (natural telephone conversations between friends or strangers). Each of the ARPA tasks involved an approximately annual bakeoff at which systems were evaluated against each other. The ARPA competitions resulted in wide-scale borrowing of techniques among labs since it was easy to see which ideas reduced errors the previous year, and the competitions were probably an im-
important factor in the eventual spread of the HMM paradigm.

By around 1990 neural alternatives to the HMM/GMM architecture for ASR arose, based on a number of earlier experiments with neural networks for phoneme recognition and other speech tasks. Architectures included the time-delay neural network (TDNN)—the first use of convolutional networks for speech—(Waibel et al. 1989, Lang et al. 1990), RNNs (Robinson and Fallside, 1991), and the hybrid HMM/MLP architecture in which a feedforward neural network is trained as a phonetic classifier whose outputs are used as probability estimates for an HMM-based architecture (Morgan and Bourlard 1990, Bourlard and Morgan 1994, Morgan and Bourlard 1995).

While the hybrid systems showed performance close to the standard HMM/GMM models, the problem was speed: large hybrid models were too slow to train on the CPUs of that era. For example, the largest hybrid system, a feedforward network, was limited to a hidden layer of 4000 units, producing probabilities over only a few dozen monophones. Yet training this model still required the research group to design special hardware boards to do vector processing (Morgan and Bourlard, 1995). A later analytic study showed the performance of such simple feedforward MLPs for ASR increases sharply with more than 1 hidden layer, even controlling for the total number of parameters (Maas et al., 2017). But the computational resources of the time were insufficient for more layers.

Over the next two decades a combination of Moore’s law and the rise of GPUs allowed deep neural networks with many layers. Performance was getting close to traditional systems on smaller tasks like TIMIT phone recognition by 2009 (Mohamed et al., 2009), and by 2012, the performance of hybrid systems had surpassed traditional HMM/GMM systems (Jaitly et al. 2012, Dahl et al. 2012, inter alia). Originally it seemed that unsupervised pretraining of the networks using a technique like deep belief networks was important, but by 2013, it was clear that for hybrid HMM/GMM feedforward networks, all that mattered was to use a lot of data and enough layers, although a few other components did improve performance: using log mel features instead of MFCCs, using dropout, and using rectified linear units (Deng et al. 2013, Maas et al. 2013, Dahl et al. 2013).

Meanwhile early work had proposed the CTC loss function by 2006 (Graves et al., 2006), and by 2012 the RNN-Transducer was defined and applied to phone recognition (Graves 2012, Graves et al. 2013), and then to end-to-end speech recognition rescoring (Graves and Jaitly, 2014), and then recognition (Maas et al., 2015), with advances such as specialized beam search (Hannun et al., 2014). (Our description of CTC in the chapter draws on Hannun (2017), which we encourage the interested reader to follow).

The encoder-decoder architecture was applied to speech at about the same time by two different groups, in the Listen Attend and Spell system of Chan et al. (2016) and the attention-based encoder decoder architecture of Chorowski et al. (2014) and Bahdanau et al. (2016). By 2018 Transformers were included in this encoder-decoder architecture. Karita et al. (2019) is a nice comparison of RNNs vs Transformers in encoder-architectures for ASR, TTS, and speech-to-speech translation.

Popular toolkits for speech processing include Kaldi (Povey et al., 2011) and ESPnet (Watanabe et al. 2018, Hayashi et al. 2020).

TTS As we noted at the beginning of the chapter, speech synthesis is one of the earliest fields of speech and language processing. The 18th century saw a number of physical models of the articulation process, including the von Kempelen model mentioned above, as well as the 1773 vowel model of Kratzenstein in Copenhagen
using organ pipes.

The early 1950s saw the development of three early paradigms of waveform synthesis: formant synthesis, articulatory synthesis, and concatenative synthesis. Modern encoder-decoder systems are distant descendants of formant synthesizers. **Formant synthesizers** originally were inspired by attempts to mimic human speech by generating artificial spectrograms. The Haskins Laboratories Pattern Playback Machine generated a sound wave by painting spectrogram patterns on a moving transparent belt and using reflectance to filter the harmonics of a waveform (Cooper et al., 1951); other very early formant synthesizers include those of Lawrence (1953) and Fant (1951). Perhaps the most well-known of the formant synthesizers were the **Klatt formant synthesizer** and its successor systems, including the MITalk system (Allen et al., 1987) and the Klattalk software used in Digital Equipment Corporation’s DECtalk (Klatt, 1982). See Klatt (1975) for details.

A second early paradigm, concatenative synthesis, seems to have been first proposed by Harris (1953) at Bell Laboratories; he literally spliced together pieces of magnetic tape corresponding to phones. Soon afterwards, Peterson et al. (1958) proposed a theoretical model based on diphones, including a database with multiple copies of each diphone with differing prosody, each labeled with prosodic features including F0, stress, and duration, and the use of join costs based on F0 and formant distance between neighboring units. But such **diphone synthesis** models were not actually implemented until decades later (Dixon and Maxey 1968, Olive 1977). The 1980s and 1990s saw the invention of **unit selection synthesis**, based on larger units of non-uniform length and the use of a target cost, (Sagisaka 1988, Sagisaka et al. 1992, Hunt and Black 1996, Black and Taylor 1994, Syrdal et al. 2000).

A third paradigm, **articulatory synthesizers** attempt to synthesize speech by modeling the physics of the vocal tract as an open tube. Representative models include Stevens et al. (1953), Flanagan et al. (1975), and Fant (1986). See Klatt (1975) and Flanagan (1972) for more details.

Most early TTS systems used phonemes as input; development of the text analysis components of TTS came somewhat later, drawing on NLP. Indeed the first true text-to-speech system seems to have been the system of Umeda and Teranishi (Umeda et al. 1968, Teranishi and Umeda 1968, Umeda 1976), which included a parser that assigned prosodic boundaries, as well as accent and stress.

**Exercises**

16.1 Analyze each of the errors in the incorrectly recognized transcription of “um the phone is I left the...” on page 352. For each one, give your best guess as to whether you think it is caused by a problem in signal processing, pronunciation modeling, lexicon size, language model, or pruning in the decoding search.
Part III

ANNOTATING LINGUISTIC STRUCTURE

In the final part of the book we discuss the task of detecting linguistic structure. In the early history of NLP these structures were an intermediate step toward deeper language processing. In modern NLP, we don’t generally make explicit use of parse or other structures inside the neural language models we introduced in Part I, or directly in applications like those we discussed in Part II.

Instead linguistic structure plays a number of new roles. One of the most important roles is to provide a useful interpretive lens on neural networks. Knowing that a particular layer or neuron may be computing something related to a particular kind of structure can help us break open the ‘black box’ and understand what the components of our language models are doing. A second important role for linguistic structure is as as a practical tool for social scientific studies of text: knowing which adjective modifies which noun, or whether a particular implicit metaphor is being used, can be important for measuring attitudes toward groups or individuals. Detailed semantic structure can be helpful, for example in finding particular clauses that have particular meanings in legal contracts. Word sense labels can help keep any corpus study from measuring facts about the wrong word sense. Relation structures can be used to help build knowledge bases from text. Finally, linguistic structure can be important to answer questions about language itself. To answer linguistic questions about how language changes over time or across individuals we’ll need to be able, for example, to parse entire documents from different time periods.

In our study of linguistic structure, we begin with one of the oldest tasks in computational linguistics: the extraction of syntactic structure, and give two sets of algorithms for parsing: extracting syntactic structure, including constituency parsing and dependency parsing. We then introduce model-theoretic semantics and give algorithms for semantic parsing. We then introduce a variety of structures related to meaning, including semantic roles, word senses, entity relations, and events. We conclude with linguistic structures that tend to be related to discourse and meaning over larger texts, including coreference, and discourse coherence. In each case we’ll give algorithms for automatically annotating the relevant structure.
The study of grammar has an ancient pedigree. The grammar of Sanskrit was described by the Indian grammarian Pāṇini sometime between the 7th and 4th centuries BCE, in his famous treatise the Astādhyāyī (‘8 books’). And our word syntax comes from the Greek σύνταξις, meaning “setting out together or arrangement”, and refers to the way words are arranged together. We have seen syntactic notions in previous chapters like the use of part-of-speech categories (Chapter 8). In this chapter and the next one we introduce formal models for capturing more sophisticated notions of grammatical structure, and algorithms for parsing these structures.

Our focus in this chapter is context-free grammars and the CKY algorithm for parsing them. Context-free grammars are the backbone of many formal models of the syntax of natural language (and, for that matter, of computer languages). Syntactic parsing is the task of assigning a syntactic structure to a sentence. Parse trees (whether for context-free grammars or for the dependency or CCG formalisms we introduce in following chapters) can be used in applications such as grammar checking: sentence that cannot be parsed may have grammatical errors (or at least be hard to read). Parse trees can be an intermediate stage of representation for the formal semantic analysis of Chapter 20. And parsers and the grammatical structure they assign a sentence are a useful text analysis tool for text data science applications that require modeling the relationship of elements in sentences.

In this chapter we introduce context-free grammars, give a small sample grammar of English, introduce more formal definitions of context-free grammars and grammar normal form, and talk about treebanks: corpora that have been annotated with syntactic structure. We then discuss parse ambiguity and the problems it presents, and turn to parsing itself, giving the famous Cocke-Kasami-Younger (CKY) algorithm (Kasami 1965, Younger 1967), the standard dynamic programming approach to syntactic parsing. The CKY algorithm returns an efficient representation of the set of parse trees for a sentence, but doesn’t tell us which parse tree is the right one. For that, we need to augment CKY with scores for each possible constituent. We’ll see how to do this with neural span-based parsers. Finally, we’ll introduce the standard set of metrics for evaluating parser accuracy.
17.1 Constituency

Syntactic constituency is the idea that groups of words can behave as single units, or constituents. Part of developing a grammar involves building an inventory of the constituents in the language. How do words group together in English? Consider the noun phrase, a sequence of words surrounding at least one noun. Here are some examples of noun phrases (thanks to Damon Runyon):

Harry the Horse  a high-class spot such as Mindy’s
the Broadway coppers  the reason he comes into the Hot Box
they  three parties from Brooklyn

What evidence do we have that these words group together (or “form constituents”)? One piece of evidence is that they can all appear in similar syntactic environments, for example, before a verb.

three parties from Brooklyn arrive... a high-class spot such as Mindy’s attracts...
the Broadway coppers love...
they sit

But while the whole noun phrase can occur before a verb, this is not true of each of the individual words that make up a noun phrase. The following are not grammatical sentences of English (recall that we use an asterisk (*) to mark fragments that are not grammatical English sentences):

*from arrive... *as attracts...
*the is... *spot sat...

Thus, to correctly describe facts about the ordering of these words in English, we must be able to say things like “Noun Phrases can occur before verbs”. Let’s now see how to do this in a more formal way!

17.2 Context-Free Grammars

A widely used formal system for modeling constituent structure in natural language is the context-free grammar, or CFG. Context-free grammars are also called phrase-structure grammars, and the formalism is equivalent to Backus-Naur form, or BNF. The idea of basing a grammar on constituent structure dates back to the psychologist Wilhelm Wundt (1900) but was not formalized until Chomsky (1956) and, independently, Backus (1959).

A context-free grammar consists of a set of rules or productions, each of which expresses the ways that symbols of the language can be grouped and ordered together, and a lexicon of words and symbols. For example, the following productions express that an NP (or noun phrase) can be composed of either a ProperNoun or a determiner (Det) followed by a Nominal; a Nominal in turn can consist of one or
more *Nouns*.\(^1\)

\[
\begin{align*}
NP & \rightarrow \text{Det Nominal} \\
NP & \rightarrow \text{ProperNoun} \\
\text{Nominal} & \rightarrow \text{Noun} \mid \text{Nominal Noun}
\end{align*}
\]

Context-free rules can be hierarchically embedded, so we can combine the previous rules with others, like the following, that express facts about the lexicon:

\[
\begin{align*}
\text{Det} & \rightarrow a \\
\text{Det} & \rightarrow \text{the} \\
\text{Noun} & \rightarrow \text{flight}
\end{align*}
\]

The symbols that are used in a CFG are divided into two classes. The symbols that correspond to words in the language (“the”, “nightclub”) are called *terminal* symbols; the lexicon is the set of rules that introduce these terminal symbols. The symbols that express abstractions over these terminals are called *non-terminals*. In each context-free rule, the item to the right of the arrow (\(\rightarrow\)) is an ordered list of one or more terminals and non-terminals; to the left of the arrow is a single non-terminal symbol expressing some cluster or generalization. The non-terminal associated with each word in the lexicon is its lexical category, or part of speech.

A CFG can be thought of in two ways: as a device for generating sentences and as a device for assigning a structure to a given sentence. Viewing a CFG as a generator, we can read the \(\rightarrow\) arrow as “rewrite the symbol on the left with the string of symbols on the right”.

So starting from the symbol: \(NP\)

we can use our first rule to rewrite \(NP\) as: \(\text{Det Nominal}\)

and then rewrite \(\text{Nominal}\) as: \(\text{Noun}\)

and finally rewrite these parts-of-speech as: \(a \text{ flight}\)

We say the string *a flight* can be derived from the non-terminal \(NP\). Thus, a CFG can be used to generate a set of strings. This sequence of rule expansions is called a *derivation* of the string of words. It is common to represent a derivation by a *parse tree* (commonly shown inverted with the root at the top). Figure 17.1 shows the tree representation of this derivation.

![Parse tree for “a flight”](attachment:parse_tree.png)

In the parse tree shown in Fig. 17.1, we can say that the node \(NP\) *dominates* all the nodes in the tree (\(\text{Det, Nom, Noun, a, flight}\)). We can say further that it immediately dominates the nodes \(\text{Det}\) and \(\text{Nom}\).

The formal language defined by a CFG is the set of strings that are derivable from the designated *start symbol*. Each grammar must have one designated start

---

\(^1\) When talking about these rules we can pronounce the rightarrow \(\rightarrow\) as “goes to”, and so we might read the first rule above as “NP goes to Det Nominal.”
symbol, which is often called $S$. Since context-free grammars are often used to define sentences, $S$ is usually interpreted as the “sentence” node, and the set of strings that are derivable from $S$ is the set of sentences in some simplified version of English.

Let’s add a few additional rules to our inventory. The following rule expresses the fact that a sentence can consist of a noun phrase followed by a verb phrase:

$$ S \rightarrow NP \ VP \quad \text{I prefer a morning flight} $$

A verb phrase in English consists of a verb followed by assorted other things; for example, one kind of verb phrase consists of a verb followed by a noun phrase:

$$ VP \rightarrow \text{Verb} \ NP \quad \text{prefer a morning flight} $$

Or the verb may be followed by a noun phrase and a prepositional phrase:

$$ VP \rightarrow \text{Verb} \ NP \ PP \quad \text{leave Boston in the morning} $$

Or the verb phrase may have a verb followed by a prepositional phrase alone:

$$ VP \rightarrow \text{Verb} \ PP \quad \text{leaving on Thursday} $$

A prepositional phrase generally has a preposition followed by a noun phrase. For example, a common type of prepositional phrase in the ATIS corpus is used to indicate location or direction:

$$ PP \rightarrow \text{Preposition} \ NP \quad \text{from Los Angeles} $$

The $NP$ inside a $PP$ need not be a location; $PP$s are often used with times and dates, and with other nouns as well; they can be arbitrarily complex. Here are ten examples from the ATIS corpus:

| to Seattle | on these flights |
| in Minneapolis | about the ground transportation in Chicago |
| on Wednesday | of the round trip flight on United Airlines |
| in the evening | of the AP fifty seven flight |
| on the ninth of July | with a stopover in Nashville |

Figure 17.2 gives a sample lexicon, and Fig. 17.3 summarizes the grammar rules we’ve seen so far, which we’ll call $L_0$. Note that we can use the or-symbol | to indicate that a non-terminal has alternate possible expansions.

<table>
<thead>
<tr>
<th>Noun</th>
<th>flights</th>
<th>flight</th>
<th>breeze</th>
<th>trip</th>
<th>morning</th>
</tr>
</thead>
<tbody>
<tr>
<td>Verb</td>
<td>is</td>
<td>prefer</td>
<td>like</td>
<td>need</td>
<td>want</td>
</tr>
<tr>
<td>Adjective</td>
<td>cheapest</td>
<td>non-stop</td>
<td>first</td>
<td>latest</td>
<td></td>
</tr>
<tr>
<td>Pronoun</td>
<td>me</td>
<td>I</td>
<td>you</td>
<td>it</td>
<td></td>
</tr>
<tr>
<td>Proper-Noun</td>
<td>Alaska</td>
<td>Baltimore</td>
<td>Los Angeles</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Chicago</td>
<td>United</td>
<td>American</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Determiner</td>
<td>the</td>
<td>a</td>
<td>an</td>
<td>this</td>
<td>these</td>
</tr>
<tr>
<td>Preposition</td>
<td>from</td>
<td>to</td>
<td>on</td>
<td>near</td>
<td>in</td>
</tr>
<tr>
<td>Conjunction</td>
<td>and</td>
<td>or</td>
<td>but</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 17.2 The lexicon for $L_0$.

We can use this grammar to generate sentences of this “ATIS-language”. We start with $S$, expand it to $NP \ VP$, then choose a random expansion of $NP$ (let’s say, to
17.2 • Context-Free Grammars

<table>
<thead>
<tr>
<th>Grammar Rules</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S \to NP \ VP )</td>
<td>I want a morning flight</td>
</tr>
<tr>
<td>( NP \to Pronoun )</td>
<td>I</td>
</tr>
<tr>
<td>( \mid Proper-Noun )</td>
<td>Los Angeles</td>
</tr>
<tr>
<td>( \mid Det \ Nominal )</td>
<td>a flight</td>
</tr>
<tr>
<td>( Nominal \to Nominal \ Noun )</td>
<td>morning + flight</td>
</tr>
<tr>
<td>( \mid Noun )</td>
<td>flights</td>
</tr>
<tr>
<td>( VP \to Verb )</td>
<td>do</td>
</tr>
<tr>
<td>( \mid Verb \ NP )</td>
<td>want + a flight</td>
</tr>
<tr>
<td>( \mid Verb \ NP \ PP )</td>
<td>leave + Boston + in the morning</td>
</tr>
<tr>
<td>( \mid Verb \ PP )</td>
<td>leaving + on Thursday</td>
</tr>
<tr>
<td>( PP \to Preposition \ NP )</td>
<td>from + Los Angeles</td>
</tr>
</tbody>
</table>

**Figure 17.3** The grammar for \( L_0 \), with example phrases for each rule.

\[
(17.1) \quad [S[NP[I[I[VP[Verb[I[NP[Det[a[Nom[Nom[flight]]]]]]]]]]]]]
\]

We can also represent a parse tree in a more compact format called **bracketed notation**; here is the bracketed representation of the parse tree of Fig. 17.4:

A CFG like that of \( L_0 \) defines a formal language. Sentences (strings of words) that can be derived by a grammar are in the formal language defined by that grammar, and are called **grammatical** sentences. Sentences that cannot be derived by a given formal grammar are not in the language defined by that grammar and are referred to as **ungrammatical**. This hard line between "in" and "out" characterizes all formal languages but is only a very simplified model of how natural languages really work. This is because determining whether a given sentence is part of a given natural language (say, English) often depends on the context. In linguistics, the use of formal languages to model natural languages is called **generative grammar** since the language is defined by the set of possible sentences "generated" by the grammar. (Note that this is a different sense of the word ‘generate’ than we in the use of
language models to generate text.)

17.2.1 Formal Definition of Context-Free Grammar

We conclude this section with a quick, formal description of a context-free grammar and the language it generates. A context-free grammar $G$ is defined by four parameters: $N, \Sigma, R, S$ (technically it is a “4-tuple”).

- $N$ a set of non-terminal symbols (or variables)
- $\Sigma$ a set of terminal symbols (disjoint from $N$)
- $R$ a set of rules or productions, each of the form $A \rightarrow \beta$, where $A$ is a non-terminal, $\beta$ is a string of symbols from the infinite set of strings $(\Sigma \cup N)^*$
- $S$ a designated start symbol and a member of $N$

For the remainder of the book we adhere to the following conventions when discussing the formal properties of context-free grammars (as opposed to explaining particular facts about English or other languages).

- Capital letters like $A$, $B$, and $S$ are non-terminals
- Lower-case Greek letters like $\alpha$, $\beta$, and $\gamma$ are strings drawn from $(\Sigma \cup N)^*$
- Lower-case Roman letters like $u$, $v$, and $w$ are strings of terminals

A language is defined through the concept of derivation. One string derives another one if it can be rewritten as the second one by some series of rule applications. More formally, following Hopcroft and Ullman (1979),

if $A \rightarrow \beta$ is a production of $R$ and $\alpha$ and $\gamma$ are any strings in the set $(\Sigma \cup N)^*$, then we say that $\alpha A \gamma$ directly derives $\alpha \beta \gamma$, or $\alpha A \gamma \Rightarrow \alpha \beta \gamma$.

Derivation is then a generalization of direct derivation:

Let $\alpha_1, \alpha_2, \ldots, \alpha_m$ be strings in $(\Sigma \cup N)^*, m \geq 1$, such that

$\alpha_1 \Rightarrow \alpha_2, \alpha_2 \Rightarrow \alpha_3, \ldots, \alpha_{m-1} \Rightarrow \alpha_m$

We say that $\alpha_1$ derives $\alpha_m$, or $\alpha_1 \Rightarrow^* \alpha_m$.

We can then formally define the language $L_G$ generated by a grammar $G$ as the set of strings composed of terminal symbols that can be derived from the designated start symbol $S$.

$L_G = \{ w | w \text{ is in } \Sigma^* \text{ and } S \Rightarrow^* w \}$

The problem of mapping from a string of words to its parse tree is called syntactic parsing, as we’ll see in Section 17.6.

17.3 Treebanks

A corpus in which every sentence is annotated with a parse tree is called a treebank.
Treebanks play an important role in parsing as well as in linguistic investigations of syntactic phenomena.

Treebanks are generally made by running a parser over each sentence and then having the resulting parse hand-corrected by human linguists. Figure 17.5 shows sentences from the Penn Treebank project, which includes various treebanks in English, Arabic, and Chinese. The Penn Treebank part-of-speech tagset was defined in Chapter 8, but we’ll see minor formatting differences across treebanks. The use of LISP-style parenthesized notation for trees is extremely common and resembles the bracketed notation we saw earlier in (17.1). For those who are not familiar with it we show a standard node-and-line tree representation in Fig. 17.6.

![Fig. 17.5](image)

**Figure 17.5** Parses from the LDC Treebank3 for (a) Brown and (b) ATIS sentences.

![Fig. 17.6](image)

**Figure 17.6** The tree corresponding to the Brown corpus sentence in the previous figure.

The sentences in a treebank implicitly constitute a grammar of the language. For example, from the parsed sentences in Fig. 17.5 we can extract the CFG rules shown in Fig. 17.7 (with rule suffixes (-SBJ) stripped for simplicity). The grammar used to parse the Penn Treebank is very flat, resulting in very many rules. For example,
among the approximately 4,500 different rules for expanding VPs are separate rules for PP sequences of any length and every possible arrangement of verb arguments:

- $\text{VP} \rightarrow \text{VBD PP}$
- $\text{VP} \rightarrow \text{VBD PP PP}$
- $\text{VP} \rightarrow \text{VBD PP PP PP}$
- $\text{VP} \rightarrow \text{VB ADJP}$
- $\text{VP} \rightarrow \text{MD VP}$
- $\text{VP} \rightarrow \text{MD VP}$
- $\text{VP} \rightarrow \text{MD VP}$
- $\text{VP} \rightarrow \text{ADVP VB PP}$
- $\text{VP} \rightarrow \text{ADVP VB PP}$
- $\text{VP} \rightarrow \text{ADVP VB PP}$

17.4 Grammar Equivalence and Normal Form

A formal language is defined as a (possibly infinite) set of strings of words. This suggests that we could ask if two grammars are equivalent by asking if they generate the same set of strings. In fact, it is possible to have two distinct context-free grammars generate the same language. We say that two grammars are **strongly equivalent** if they generate the same set of strings and if they assign the same phrase structure to each sentence (allowing merely for renaming of the non-terminal symbols). Two grammars are **weakly equivalent** if they generate the same set of strings but do not assign the same phrase structure to each sentence.

It is sometimes useful to have a **normal form** for grammars, in which each of the productions takes a particular form. For example, a context-free grammar is in **Chomsky normal form** (CNF) (Chomsky, 1963) if it is $\epsilon$-free and if in addition each production is either of the form $A \rightarrow B \ C$ or $A \rightarrow a$. That is, the right-hand side of each rule either has two non-terminal symbols or one terminal symbol. Chomsky normal form grammars are **binary branching**, that is they have binary trees (down to the prelexical nodes). We make use of this binary branching property in the CKY parsing algorithm in Chapter 17.

Any context-free grammar can be converted into a weakly equivalent Chomsky normal form grammar. For example, a rule of the form

$$A \rightarrow B \ C \ D$$

can be converted into the following two CNF rules (Exercise 17.1 asks the reader to
formulate the complete algorithm):

\[ A \rightarrow B \ X \]

\[ X \rightarrow C \ D \]

Sometimes using binary branching can actually produce smaller grammars. For example, the sentences that might be characterized as

\[ VP \rightarrow \text{VBD NP PP}^* \]

are represented in the Penn Treebank by this series of rules:

\[ VP \rightarrow \text{VBD NP PP} \]
\[ VP \rightarrow \text{VBD NP PP PP} \]
\[ VP \rightarrow \text{VBD NP PP PP PP} \]
\[ VP \rightarrow \text{VBD NP PP PP PP PP} \]
... but could also be generated by the following two-rule grammar:

\[ VP \rightarrow \text{VBD NP PP} \]
\[ VP \rightarrow \text{VP PP} \]

The generation of a symbol A with a potentially infinite sequence of symbols B with a rule of the form \( A \rightarrow A \ B \) is known as Chomsky-adjunction.

### 17.5 Ambiguity

Ambiguity is the most serious problem faced by syntactic parsers. Chapter 8 introduced the notions of part-of-speech ambiguity and part-of-speech disambiguation. Here, we introduce a new kind of ambiguity, called structural ambiguity, illustrated with a new toy grammar \( \mathcal{L}_1 \), shown in Figure 17.8, which adds a few rules to the \( \mathcal{L}_0 \) grammar from the last chapter.

Structural ambiguity occurs when the grammar can assign more than one parse to a sentence. Groucho Marx’s well-known line as Captain Spaulding in Animal
Crackers is ambiguous because the phrase *in my pajamas* can be part of the *NP* headed by *elephant* or a part of the verb phrase headed by *shot*. Figure 17.9 illustrates these two analyses of Marx’s line using rules from $\mathcal{L}_1$.

Structural ambiguity, appropriately enough, comes in many forms. Two common kinds of ambiguity are attachment ambiguity and coordination ambiguity. A sentence has an attachment ambiguity if a particular constituent can be attached to the parse tree at more than one place. The Groucho Marx sentence is an example of PP-attachment ambiguity: the preposition phrase can be attached either as part of the NP or as part of the VP. Various kinds of adverbial phrases are also subject to this kind of ambiguity. For instance, in the following example the gerundive-VP *flying to Paris* can be part of a gerundive sentence whose subject is *the Eiffel Tower* or it can be an adjunct modifying the VP headed by *saw*:

(17.2) We saw the Eiffel Tower flying to Paris.

In coordination ambiguity phrases can be conjoined by a conjunction like *and*. For example, the phrase *old men and women* can be bracketed as [*old [men and women]*], referring to *old men* and *old women*, or as [*old men*] and [*women*], in which case it is only the men who are old. These ambiguities combine in complex ways in real sentences, like the following news sentence from the Brown corpus:

(17.3) President Kennedy today pushed aside other White House business to devote all his time and attention to working on the Berlin crisis address he will deliver tomorrow night to the American people over nationwide television and radio.

This sentence has a number of ambiguities, although since they are semantically unreasonable, it requires a careful reading to see them. The last noun phrase could be parsed [*nationwide [television and radio]*] or [*[nationwide television] and radio*]. The direct object of *pushed aside* should be *other White House business* but could also be the bizarre phrase [*other White House business to devote all his time and attention to working*] (i.e., a structure like *Kennedy affirmed [his intention to propose a new budget to address the deficit]*)}. Then the phrase on the Berlin crisis address he
will deliver tomorrow night to the American people could be an adjunct modifying the verb pushed. A PP like over nationwide television and radio could be attached to any of the higher VPs or NPs (e.g., it could modify people or night).

The fact that there are many grammatically correct but semantically unreasonable parses for naturally occurring sentences is an irksome problem that affects all parsers. Fortunately, the CKY algorithm below is designed to efficiently handle structural ambiguities. And as we’ll see in the following section, we can augment CKY with neural methods to choose a single correct parse by syntactic disambiguation.

17.6 CKY Parsing: A Dynamic Programming Approach

Dynamic programming provides a powerful framework for addressing the problems caused by ambiguity in grammars. Recall that a dynamic programming approach systematically fills in a table of solutions to subproblems. The complete table has the solution to all the subproblems needed to solve the problem as a whole. In the case of syntactic parsing, these subproblems represent parse trees for all the constituents detected in the input.

The dynamic programming advantage arises from the context-free nature of our grammar rules—once a constituent has been discovered in a segment of the input we can record its presence and make it available for use in any subsequent derivation that might require it. This provides both time and storage efficiencies since subtrees can be looked up in a table, not reanalyzed. This section presents the Cocke-Kasami-Younger (CKY) algorithm, the most widely used dynamic-programming based approach to parsing. Chart parsing (Kaplan 1973, Kay 1982) is a related approach, and dynamic programming methods are often referred to as chart parsing methods.

17.6.1 Conversion to Chomsky Normal Form

The CKY algorithm requires grammars to first be in Chomsky Normal Form (CNF). Recall from Section 17.4 that grammars in CNF are restricted to rules of the form $A \rightarrow BC$ or $A \rightarrow w$. That is, the right-hand side of each rule must expand either to two non-terminals or to a single terminal. Restricting a grammar to CNF does not lead to any loss in expressiveness, since any context-free grammar can be converted into a corresponding CNF grammar that accepts exactly the same set of strings as the original grammar.

Let’s start with the process of converting a generic CFG into one represented in CNF. Assuming we’re dealing with an $\epsilon$-free grammar, there are three situations we need to address in any generic grammar: rules that mix terminals with non-terminals on the right-hand side, rules that have a single non-terminal on the right-hand side, and rules in which the length of the right-hand side is greater than 2.

The remedy for rules that mix terminals and non-terminals is to simply introduce a new dummy non-terminal that covers only the original terminal. For example, a rule for an infinitive verb phrase such as $\text{INF-VP} \rightarrow \text{to VP}$ would be replaced by the two rules $\text{INF-VP} \rightarrow \text{TO VP}$ and $\text{TO} \rightarrow \text{to}$.

Rules with a single non-terminal on the right are called unit productions. We can eliminate unit productions by rewriting the right-hand side of the original rules with the right-hand side of all the non-unit production rules that they ultimately lead to. More formally, if $A \rightarrow B$ by a chain of one or more unit productions and $B \rightarrow \gamma$
is a non-unit production in our grammar, then we add $A \rightarrow \gamma$ for each such rule in the grammar and discard all the intervening unit productions. As we demonstrate with our toy grammar, this can lead to a substantial flattening of the grammar and a consequent promotion of terminals to fairly high levels in the resulting trees.

Rules with right-hand sides longer than 2 are normalized through the introduction of new non-terminals that spread the longer sequences over several new rules. Formally, if we have a rule like

$$A \rightarrow BC\gamma$$

we replace the leftmost pair of non-terminals with a new non-terminal and introduce a new production, resulting in the following new rules:

$$A \rightarrow XI\gamma$$
$$XI \rightarrow BC$$

In the case of longer right-hand sides, we simply iterate this process until the offending rule has been replaced by rules of length 2. The choice of replacing the leftmost pair of non-terminals is purely arbitrary; any systematic scheme that results in binary rules would suffice.

In our current grammar, the rule $S \rightarrow Aux\ NP\ VP$ would be replaced by the two rules $S \rightarrow XI\ VP$ and $XI \rightarrow Aux\ NP$.

The entire conversion process can be summarized as follows:

1. Copy all conforming rules to the new grammar unchanged.
2. Convert terminals within rules to dummy non-terminals.
3. Convert unit productions.
4. Make all rules binary and add them to new grammar.

Figure 17.10 shows the results of applying this entire conversion procedure to the $L_1$ grammar introduced earlier on page 375. Note that this figure doesn’t show the original lexical rules; since these original lexical rules are already in CNF, they all carry over unchanged to the new grammar. Figure 17.10 does, however, show the various places where the process of eliminating unit productions has, in effect, created new lexical rules. For example, all the original verbs have been promoted to both VPs and to Ss in the converted grammar.

### 17.6.2 CKY Recognition

With our grammar now in CNF, each non-terminal node above the part-of-speech level in a parse tree will have exactly two daughters. A two-dimensional matrix can be used to encode the structure of an entire tree. For a sentence of length $n$, we will work with the upper-triangular portion of an $(n+1) \times (n+1)$ matrix. Each cell $[i,j]$ in this matrix contains the set of non-terminals that represent all the constituents that span positions $i$ through $j$ of the input. Since our indexing scheme begins with 0, it’s natural to think of the indexes as pointing at the gaps between the input words (as in 0 Book 1 that 2 flight 3). These gaps are often called fenceposts, on the metaphor of the posts between segments of fencing. It follows then that the cell that represents the entire input resides in position $[0,n]$ in the matrix.

Since each non-terminal entry in our table has two daughters in the parse, it follows that for each constituent represented by an entry $[i,j]$, there must be a position in the input, $k$, where it can be split into two parts such that $i < k < j$. Given such
a position $k$, the first constituent $[i,k]$ must lie to the left of entry $[i,j]$ somewhere along row $i$, and the second entry $[k,j]$ must lie beneath it, along column $j$.

To make this more concrete, consider the following example with its completed parse matrix, shown in Fig. 17.11.

(17.4) Book the flight through Houston.

The superdiagonal row in the matrix contains the parts of speech for each word in the input. The subsequent diagonals above that superdiagonal contain constituents that cover all the spans of increasing length in the input.

Given this setup, CKY recognition consists of filling the parse table in the right way. To do this, we’ll proceed in a bottom-up fashion so that at the point where we are filling any cell $[i,j]$, the cells containing the parts that could contribute to this entry (i.e., the cells to the left and the cells below) have already been filled. The algorithm given in Fig. 17.12 fills the upper-triangular matrix a column at a time working from left to right, with each column filled from bottom to top, as the right side of Fig. 17.11 illustrates. This scheme guarantees that at each point in time we have all the information we need (to the left, since all the columns to the left have already been filled, and below since we’re filling bottom to top). It also mirrors online processing, since filling the columns from left to right corresponds to processing each word one at a time.

The outermost loop of the algorithm given in Fig. 17.12 iterates over the columns, and the second loop iterates over the rows, from the bottom up. The purpose of the innermost loop is to range over all the places where a substring spanning $i$ to $j$ in the input might be split in two. As $k$ ranges over the places where the string can be split, the pairs of cells we consider move, in lockstep, to the right along row $i$ and down along column $j$. Figure 17.13 illustrates the general case of filling cell $[i,j]$. 

<table>
<thead>
<tr>
<th>$\mathcal{L}_1$ Grammar</th>
<th>$\mathcal{L}_1$ in CNF</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S \rightarrow NP \ VP$</td>
<td>$S \rightarrow NP \ VP$</td>
</tr>
<tr>
<td>$S \rightarrow Aux \ NP \ VP$</td>
<td>$S \rightarrow XI \ VP$</td>
</tr>
<tr>
<td>$S \rightarrow VP$</td>
<td>$XI \rightarrow Aux \ NP$</td>
</tr>
<tr>
<td>$S \rightarrow book</td>
<td>include</td>
</tr>
<tr>
<td>$S \rightarrow Verb \ NP$</td>
<td>$S \rightarrow Verb \ NP$</td>
</tr>
<tr>
<td>$S \rightarrow X2 \ PP$</td>
<td>$S \rightarrow X2 \ PP$</td>
</tr>
<tr>
<td>$S \rightarrow Verb \ PP$</td>
<td>$S \rightarrow Verb \ PP$</td>
</tr>
<tr>
<td>$S \rightarrow VP \ PP$</td>
<td>$S \rightarrow VP \ PP$</td>
</tr>
<tr>
<td>$NP \rightarrow Pronoun$</td>
<td>$NP \rightarrow I</td>
</tr>
<tr>
<td>$NP \rightarrow Proper-Noun$</td>
<td>$NP \rightarrow TWA</td>
</tr>
<tr>
<td>$NP \rightarrow Det \ Nominal$</td>
<td>$NP \rightarrow Det \ Nominal$</td>
</tr>
<tr>
<td>$Nominal \rightarrow Noun$</td>
<td>$Nominal \rightarrow book</td>
</tr>
<tr>
<td>$Nominal \rightarrow Nominal \ Noun$</td>
<td>$Nominal \rightarrow Nominal \ Noun$</td>
</tr>
<tr>
<td>$Nominal \rightarrow Nominal \ PP$</td>
<td>$Nominal \rightarrow Nominal \ PP$</td>
</tr>
<tr>
<td>$VP \rightarrow Verb$</td>
<td>$VP \rightarrow book</td>
</tr>
<tr>
<td>$VP \rightarrow Verb \ NP$</td>
<td>$VP \rightarrow Verb \ NP$</td>
</tr>
<tr>
<td>$VP \rightarrow Verb \ NP \ PP$</td>
<td>$VP \rightarrow X2 \ PP$</td>
</tr>
<tr>
<td>$VP \rightarrow Verb \ PP$</td>
<td>$VP \rightarrow Verb \ PP$</td>
</tr>
<tr>
<td>$VP \rightarrow VP \ PP$</td>
<td>$VP \rightarrow VP \ PP$</td>
</tr>
<tr>
<td>$PP \rightarrow Preposition \ NP$</td>
<td>$PP \rightarrow Preposition \ NP$</td>
</tr>
</tbody>
</table>

Figure 17.10 $\mathcal{L}_1$ Grammar and its conversion to CNF. Note that although they aren’t shown here, all the original lexical entries from $\mathcal{L}_1$ carry over unchanged as well.
function CKY-Parse(words, grammar) returns table

for \( j \leftarrow 1 \) to \( \text{LENGTH(words)} \) do
  for all \( \{A \mid A \rightarrow \text{words}[j] \in \text{grammar}\} \)
    \( \text{table}[j - 1, j] \leftarrow \text{table}[j - 1, j] \cup A \)
  for \( i \leftarrow j - 2 \) down to 0 do
    for \( k \leftarrow i + 1 \) to \( j - 1 \) do
      for all \( \{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\} \)
        \( \text{table}[i, j] \leftarrow \text{table}[i, j] \cup A \)

Figure 17.12  The CKY algorithm.

At each such split, the algorithm considers whether the contents of the two cells can be combined in a way that is sanctioned by a rule in the grammar. If such a rule exists, the non-terminal on its left-hand side is entered into the table.

Figure 17.14 shows how the five cells of column 5 of the table are filled after the word Houston is read. The arrows point out the two spans that are being used to add an entry to the table. Note that the action in cell \([0, 5]\) indicates the presence of three alternative parses for this input, one where the PP modifies the flight, one where it modifies the booking, and one that captures the second argument in the original \(VP \rightarrow \text{Verb NP PP}\) rule, now captured indirectly with the \(VP \rightarrow X2 PP\) rule.

17.6.3 CKY Parsing

The algorithm given in Fig. 17.12 is a recognizer, not a parser. That is, it can tell us whether a valid parse exists for a given sentence based on whether or not if finds an S in cell \([0, n]\), but it can’t provide the derivation, which is the actual job for a parser. To turn it into a parser capable of returning all possible parses for a given input, we can make two simple changes to the algorithm: the first change is to augment the entries in the table so that each non-terminal is paired with pointers to the table entries from which it was derived (more or less as shown in Fig. 17.14), the second change is to permit multiple versions of the same non-terminal to be entered into the table (again as shown in Fig. 17.14). With these changes, the completed table contains all the possible parses for a given input. Returning an arbitrary single
parse consists of choosing an $S$ from cell $[0, n]$ and then recursively retrieving its component constituents from the table. Of course, instead of returning every parse for a sentence, we usually want just the best parse; we’ll see how to do that in the next section.

### 17.6.4 CKY in Practice

Finally, we should note that while the restriction to CNF does not pose a problem theoretically, it does pose some non-trivial problems in practice. The returned CNF trees may not be consistent with the original grammar built by the grammar developers, and will complicate any syntax-driven approach to semantic analysis.

One approach to getting around these problems is to keep enough information around to transform our trees back to the original grammar as a post-processing step of the parse. This is trivial in the case of the transformation used for rules with length greater than 2. Simply deleting the new dummy non-terminals and promoting their daughters restores the original tree.

In the case of unit productions, it turns out to be more convenient to alter the basic CKY algorithm to handle them directly than it is to store the information needed to recover the correct trees. Exercise 17.3 asks you to make this change. Many of the probabilistic parsers presented in Appendix C use the CKY algorithm altered in
Figure 17.14  Filling the cells of column 5 after reading the word Houston.
just this manner.

17.7 Span-Based Neural Constituency Parsing

While the CKY parsing algorithm we’ve seen so far does great at enumerating all the possible parse trees for a sentence, it has a large problem: it doesn’t tell us which parse is the correct one! That is, it doesn’t disambiguate among the possible parses. To solve the disambiguation problem we’ll use a simple neural extension of the CKY algorithm. The intuition of such parsing algorithms (often called span-based constituency parsing, or neural CKY), is to train a neural classifier to assign a score to each constituent, and then use a modified version of CKY to combine these constituent scores to find the best-scoring parse tree.

Here we’ll describe a version of the algorithm from Kitaev et al. (2019). This parser learns to map a span of words to a constituent, and, like CKY, hierarchically combines larger and larger spans to build the parse-tree bottom-up. But unlike classic CKY, this parser doesn’t use the hand-written grammar to constrain what constituents can be combined, instead just relying on the learned neural representations of spans to encode likely combinations.

17.7.1 Computing Scores for a Span

Let’s begin by considering just the constituent (we’ll call it a span) that lies between fencepost positions $i$ and $j$ with non-terminal symbol label $l$. We’ll build a system to assign a score $s(i, j, l)$ to this constituent span.

![Diagram](image)

**Figure 17.15** A simplified outline of computing the span score for the span *the flight* with the label NP.

Fig. 17.15 sketches the architecture. The input word tokens are embedded by
passing them through a pretrained language model like BERT. Because BERT operates on the level of subword (wordpiece) tokens rather than words, we’ll first need to convert the BERT outputs to word representations. One standard way of doing this is to simply use the first subword unit as the representation for the entire word; using the last subword unit, or the sum of all the subword units are also common. The embeddings can then be passed through some postprocessing layers; Kitaev et al. (2019), for example, use 8 Transformer layers.

The resulting word encoder outputs $y_t$ are then used to compute a span score. First, we must map the word encodings (indexed by word positions) to span encodings (indexed by fenceposts). We do this by representing each fencepost with two separate values; the intuition is that a span endpoint to the right of a word represents different information than a span endpoint to the left of a word. We convert each word output $y_t$ into a (leftward-pointing) value for spans ending at this fencepost, $\langle y_t \rangle$, and a (rightward-pointing) value $\langle y_t \rangle$, for spans beginning at this fencepost, by splitting $y_t$ into two halves. Each span then stretches from one double-vector fencepost to another, as in the following representation of the flight, which is span$(1, 3)$:

<table>
<thead>
<tr>
<th>START</th>
<th>Book</th>
<th>the</th>
<th>flight</th>
<th>through</th>
</tr>
</thead>
<tbody>
<tr>
<td>$y_0$</td>
<td>$\langle y_0 \rangle$</td>
<td>$\langle y_1 \rangle$</td>
<td>$\langle y_2 \rangle$</td>
<td>$\langle y_3 \rangle$</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
</tbody>
</table>

span$(1, 3)$

A traditional way to represent a span, developed originally for RNN-based models (Wang and Chang, 2016), but extended also to Transformers, is to take the difference between the embeddings of its start and end, i.e., representing span $(i, j)$ by subtracting the embedding of $i$ from the embedding of $j$. Here we represent a span by concatenating the difference of each of its fencepost components:

$$v(i, j) = [\langle y_j \rangle - \langle y_i \rangle; \langle \frac{y_{j+1} - y_{i+1}}{2} \rangle]$$ (17.5)

The span vector $v$ is then passed through an MLP span classifier, with two fully-connected layers and one ReLU activation function, whose output dimensionality is the number of possible non-terminal labels:

$$s(i, j, \cdot) = W_2 \text{ReLU}(\text{LayerNorm}(W_1 v(i, j)))$$ (17.6)

The MLP then outputs a score for each possible non-terminal.

### 17.7.2 Integrating Span Scores into a Parse

Now we have a score for each labeled constituent span $s(i, j, l)$. But we need a score for an entire parse tree. Formally a tree $T$ is represented as a set of $|T|$ such labeled spans, with the $t^{th}$ span starting at position $i_t$ and ending at position $j_t$, with label $l_t$:

$$T = \{ (i_t, j_t, l_t) : t = 1, \ldots, |T| \}$$ (17.7)

Thus once we have a score for each span, the parser can compute a score for the whole tree $s(T)$ simply by summing over the scores of its constituent spans:

$$s(T) = \sum_{(i,j,l) \in T} s(i, j, l)$$ (17.8)
And we can choose the final parse tree as the tree with the maximum score:

$$\hat{T} = \arg\max_T s(T)$$  \hfill (17.9)

The simplest method to produce the most likely parse is to greedily choose the highest scoring label for each span. This greedy method is not guaranteed to produce a tree, since the best label for a span might not fit into a complete tree. In practice, however, the greedy method tends to find trees; in their experiments Gaddy et al. (2018) finds that 95% of predicted bracketings form valid trees.

Nonetheless it is more common to use a variant of the CKY algorithm to find the full parse. The variant defined in Gaddy et al. (2018) works as follows. Let’s define $s_{\text{best}}(i, j)$ as the score of the best subtree spanning $(i, j)$. For spans of length one, we choose the best label:

$$s_{\text{best}}(i, i+1) = \max_l s(i, i+1, l)$$  \hfill (17.10)

For other spans $(i, j)$, the recursion is:

$$s_{\text{best}}(i, j) = \max_l s(i, j, l)$$

$$+ \max_k \left[ s_{\text{best}}(i, k) + s_{\text{best}}(k, j) \right]$$  \hfill (17.11)

Note that the parser is using the max label for span $(i, j) +$ the max labels for spans $(i, k)$ and $(k, j)$ without worrying about whether those decisions make sense given a grammar. The role of the grammar in classical parsing is to help constrain possible combinations of constituents (NPs like to be followed by VPs). By contrast, the neural model seems to learn these kinds of contextual constraints during its mapping from spans to non-terminals.

For more details on span-based parsing, including the margin-based training algorithm, see Stern et al. (2017), Gaddy et al. (2018), Kitaev and Klein (2018), and Kitaev et al. (2019).

### 17.8 Evaluating Parsers

The standard tool for evaluating parsers that assign a single parse tree to a sentence is the PARSEVAL metrics (Black et al., 1991). The PARSEVAL metric measures how much the constituents in the hypothesis parse tree look like the constituents in a hand-labeled, reference parse. PARSEVAL thus requires a human-labeled reference (or “gold standard”) parse tree for each sentence in the test set; we generally draw these reference parses from a treebank like the Penn Treebank.

A constituent in a hypothesis parse $C_h$ of a sentence $s$ is labeled correct if there is a constituent in the reference parse $C_r$ with the same starting point, ending point, and non-terminal symbol. We can then measure the precision and recall just as for tasks we’ve seen already like named entity tagging:

$labeled \ \text{recall}: = \frac{\# \text{ of correct constituents in hypothesis parse of } s}{\# \text{ of total constituents in reference parse of } s}$

$labeled \ \text{precision}: = \frac{\# \text{ of correct constituents in hypothesis parse of } s}{\# \text{ of total constituents in hypothesis parse of } s}$
As usual, we often report a combination of the two, $F_1$:

$$F_1 = \frac{2PR}{P + R} \quad (17.12)$$

We additionally use a new metric, crossing brackets, for each sentence $s$:

**cross-brackets:** the number of constituents for which the reference parse has a bracketing such as $((A \ B) \ C)$ but the hypothesis parse has a bracketing such as $(A \ (B \ C))$.

For comparing parsers that use different grammars, the PARSEVAL metric includes a canonicalization algorithm for removing information likely to be grammar-specific (auxiliaries, pre-infinitival “to”, etc.) and for computing a simplified score (Black et al., 1991). The canonical implementation of the PARSEVAL metrics is called evalb (Sekine and Collins, 1997).

### 17.9 Heads and Head-Finding

Syntactic constituents can be associated with a lexical **head**: $N$ is the head of an $NP$, $V$ is the head of a $VP$. This idea of a head for each constituent dates back to Bloomfield 1914, and is central to the dependency grammars and dependency parsing we’ll introduce in Chapter 18. Indeed, heads can be used as a way to map between constituency and dependency parses. Heads are also important in probabilistic parsing (Appendix C) and in constituent-based grammar formalisms like Head-Driven Phrase Structure Grammar (Pollard and Sag, 1994).

In one simple model of lexical heads, each context-free rule is associated with a head (Charniak 1997, Collins 1999). The head is the word in the phrase that is grammatically the most important. Heads are passed up the parse tree; thus, each non-terminal in a parse tree is annotated with a single word, which is its lexical head. Figure 17.16 shows an example of such a tree from Collins (1999), in which each non-terminal is annotated with its head.

For the generation of such a tree, each CFG rule must be augmented to identify one right-side constituent to be the head child. The headword for a node is then set to the headword of its head child. Choosing these head children is simple for textbook examples ($NN$ is the head of $NP$) but is complicated and indeed controversial for...
most phrases. (Should the complementizer to or the verb be the head of an infinite verb phrase?) Modern linguistic theories of syntax generally include a component that defines heads (see, e.g., (Pollard and Sag, 1994)).

An alternative approach to finding a head is used in most practical computational systems. Instead of specifying head rules in the grammar itself, heads are identified dynamically in the context of trees for specific sentences. In other words, once a sentence is parsed, the resulting tree is walked to decorate each node with the appropriate head. Most current systems rely on a simple set of handwritten rules, such as a practical one for Penn Treebank grammars given in Collins (1999) but developed originally by Magerman (1995). For example, the rule for finding the head of an NP is as follows (Collins, 1999, p. 238):

- If the last word is tagged POS, return last-word.
- Else search from right to left for the first child which is an NN, NNP, NNPS, NX, POS, or JJR.
- Else search from left to right for the first child which is an NP.
- Else search from right to left for the first child which is a $, ADJP, or PRN.
- Else search from right to left for the first child which is a CD.
- Else search from right to left for the first child which is a JJ, JJS, RB or QP.
- Else return the last word

Selected other rules from this set are shown in Fig. 17.17. For example, for VP rules of the form $VP → Y_1 \cdots Y_n$, the algorithm would start from the left of $Y_1 \cdots Y_n$ looking for the first $Y_i$ of type TO; if no TOs are found, it would search for the first $Y_i$ of type VBD; if no VBDs are found, it would search for a VBN, and so on. See Collins (1999) for more details.

<table>
<thead>
<tr>
<th>Parent</th>
<th>Direction</th>
<th>Priority List</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADJP</td>
<td>Left</td>
<td>NNS QP NN $ ADVP JJ VBN VBG ADJP JJR NP JJS DT FW RBR RBS SBAR RB</td>
</tr>
<tr>
<td>ADVP</td>
<td>Right</td>
<td>RB RBR RBS FW ADVP TO CD JJR JJ IN NP JJS NN</td>
</tr>
<tr>
<td>PRN</td>
<td>Left</td>
<td>$ IN NNS NN JJ RB DT CD NCD QP JJR JJS</td>
</tr>
<tr>
<td>PRT</td>
<td>Right</td>
<td>RP</td>
</tr>
<tr>
<td>QP</td>
<td>Left</td>
<td>TO IN VP S SBAR ADJP UCP NP</td>
</tr>
<tr>
<td>SBAR</td>
<td>Left</td>
<td>WHNP WHPP WHADVP WHADJP IN DT S SQ SINV SBAR FRAG</td>
</tr>
<tr>
<td>VP</td>
<td>Left</td>
<td>TO VBD VBN MD VBZ VB VBG VBP VP ADJP NN NNS NP</td>
</tr>
</tbody>
</table>

Figure 17.17 Some head rules from Collins (1999). The head rules are also called a head percolation table.

17.10 Summary

This chapter introduced constituency parsing. Here’s a summary of the main points:

- In many languages, groups of consecutive words act as a group or a constituent, which can be modeled by context-free grammars (which are also known as phrase-structure grammars).
- A context-free grammar consists of a set of rules or productions, expressed over a set of non-terminal symbols and a set of terminal symbols. Formally, a particular context-free language is the set of strings that can be derived from a particular context-free grammar.
• Structural ambiguity is a significant problem for parsers. Common sources of structural ambiguity include PP-attachment and coordination ambiguity.

• Dynamic programming parsing algorithms, such as CKY, use a table of partial parses to efficiently parse ambiguous sentences.

• CKY restricts the form of the grammar to Chomsky normal form (CNF).

• The basic CKY algorithm compactly represents all possible parses of the sentence but doesn’t choose a single best parse.

• Choosing a single parse from all possible parses (disambiguation) can be done by neural constituency parsers.

• Span-based neural constituency parses train a neural classifier to assign a score to each constituent, and then use a modified version of CKY to combine these constituent scores to find the best-scoring parse tree.

• Parsers are evaluated with three metrics: labeled recall, labeled precision, and cross-brackets.

• Partial parsing and chunking are methods for identifying shallow syntactic constituents in a text. They are solved by sequence models trained on syntactically-annotated data.

Bibliographical and Historical Notes

According to Percival (1976), the idea of breaking up a sentence into a hierarchy of constituents appeared in the Völkerpsychologie of the groundbreaking psychologist Wilhelm Wundt (Wundt, 1900):

...den sprachlichen Ausdruck für die willkürliche Gliederung einer Gesamtvorstellung in ihre in logische Beziehung zueinander gesetzten Bestandteile

[the linguistic expression for the arbitrary division of a total idea into its constituent parts placed in logical relations to one another]

Wundt’s idea of constituency was taken up into linguistics by Leonard Bloomfield in his early book An Introduction to the Study of Language (Bloomfield, 1914). By the time of his later book, Language (Bloomfield, 1933), what was then called “immediate-constituent analysis” was a well-established method of syntactic study in the United States. By contrast, traditional European grammar, dating from the Classical period, defined relations between words rather than constituents, and European syntacticians retained this emphasis on such dependency grammars, the subject of Chapter 18. (And indeed, both dependency and constituency grammars have been in vogue in computational linguistics at different times).

American Structuralism saw a number of specific definitions of the immediate constituent, couched in terms of their search for a “discovery procedure”: a methodological algorithm for describing the syntax of a language. In general, these attempt to capture the intuition that “The primary criterion of the immediate constituent is the degree in which combinations behave as simple units” (Bazell, 1952/1966, p. 284). The most well known of the specific definitions is Harris’ idea of distributional similarity to individual units, with the substitutability test. Essentially, the method proceeded by breaking up a construction into constituents by attempting to substitute simple structures for possible constituents—if a substitution of a simple form, say,
man, was substitutable in a construction for a more complex set (like intense young man), then the form intense young man was probably a constituent. Harris’s test was the beginning of the intuition that a constituent is a kind of equivalence class.

The context-free grammar was a formalization of this idea of hierarchical constituency defined in Chomsky (1956) and further expanded upon (and argued against) in Chomsky (1957) and Chomsky (1956/1975). Shortly after Chomsky’s initial work, the context-free grammar was reinvented by Backus (1959) and independently by Naur et al. (1960) in their descriptions of the ALGOL programming language; Backus (1996) noted that he was influenced by the productions of Emil Post and that Naur’s work was independent of his (Backus’) own. After this early work, a great number of computational models of natural language processing were based on context-free grammars because of the early development of efficient parsing algorithms.

Dynamic programming parsing has a history of independent discovery. According to the late Martin Kay (personal communication), a dynamic programming parser containing the roots of the CKY algorithm was first implemented by John Cocke in 1960. Later work extended and formalized the algorithm, as well as proving its time complexity (Kay 1967, Younger 1967, Kasami 1965). The related well-formed substring table (WFST) seems to have been independently proposed by Kuno (1965) as a data structure that stores the results of all previous computations in the course of the parse. Based on a generalization of Cocke’s work, a similar data structure had been independently described in Kay (1967) (and Kay 1973). The top-down application of dynamic programming to parsing was described in Earley’s Ph.D. dissertation (Earley 1968, Earley 1970). Sheil (1976) showed the equivalence of the WFST and the Earley algorithm. Norvig (1991) shows that the efficiency offered by dynamic programming can be captured in any language with a memoization function (such as in LISP) simply by wrapping the memoization operation around a simple top-down parser.

The earliest disambiguation algorithms for parsing were based on probabilistic context-free grammars, first worked out by Booth (1969) and Salomaa (1969); see Appendix C for more history. Neural methods were first applied to parsing at around the same time as statistical parsing methods were developed (Henderson, 1994). In the earliest work neural networks were used to estimate some of the probabilities for statistical constituency parsers (Henderson, 2003, 2004; Emami and Jelinek, 2005). The next decades saw a wide variety of neural parsing algorithms, including recursive neural architectures (Socher et al., 2011, 2013), encoder-decoder models (Vinyals et al., 2015; Choe and Charniak, 2016), and the idea of focusing on spans (Cross and Huang, 2016). For more on the span-based self-attention approach we describe in this chapter see Stern et al. (2017), Gaddy et al. (2018), Kitaev and Klein (2018), and Kitaev et al. (2019). See Chapter 18 for the parallel history of neural dependency parsing.

The classic reference for parsing algorithms is Aho and Ullman (1972); although the focus of that book is on computer languages, most of the algorithms have been applied to natural language.

Exercises

17.1 Implement the algorithm to convert arbitrary context-free grammars to CNF.
Apply your program to the $L_1$ grammar.

17.2 Implement the CKY algorithm and test it with your converted $L_1$ grammar.

17.3 Rewrite the CKY algorithm given in Fig. 17.12 on page 380 so that it can accept grammars that contain unit productions.

17.4 Discuss how to augment a parser to deal with input that may be incorrect, for example, containing spelling errors or mistakes arising from automatic speech recognition.

17.5 Implement the PARSEVAL metrics described in Section 17.8. Next, use a parser and a treebank, compare your metrics against a standard implementation. Analyze the errors in your approach.
The focus of the last chapter was on context-free grammars and constituent-based representations. Here we present another important family of grammar formalisms called dependency grammars. In dependency formalisms, phrasal constituents and phrase-structure rules do not play a direct role. Instead, the syntactic structure of a sentence is described solely in terms of directed binary grammatical relations between the words, as in the following dependency parse:

```
I prefer the morning flight through Denver
```

Relations among the words are illustrated above the sentence with directed, labeled arcs from heads to dependents. We call this a typed dependency structure because the labels are drawn from a fixed inventory of grammatical relations. A root node explicitly marks the root of the tree, the head of the entire structure.

Figure 18.1 on the next page shows the dependency analysis from (18.1) but visualized as a tree, alongside its corresponding phrase-structure analysis of the kind given in the prior chapter. Note the absence of nodes corresponding to phrasal constituents or lexical categories in the dependency parse; the internal structure of the dependency parse consists solely of directed relations between words. These head-dependent relationships directly encode important information that is often buried in the more complex phrase-structure parses. For example, the arguments to the verb prefer are directly linked to it in the dependency structure, while their connection to the main verb is more distant in the phrase-structure tree. Similarly, morning and Denver, modifiers of flight, are linked to it directly in the dependency structure. This fact that the head-dependent relations are a good proxy for the semantic relationship between predicates and their arguments is an important reason why dependency grammars are currently more common than constituency grammars in natural language processing.

Another major advantage of dependency grammars is their ability to deal with languages that have a relatively free word order. For example, word order in Czech can be much more flexible than in English; a grammatical object might occur before or after a location adverbial. A phrase-structure grammar would need a separate rule
for each possible place in the parse tree where such an adverbial phrase could occur. A dependency-based approach can have just one link type representing this particular adverbial relation; dependency grammar approaches can thus abstract away a bit more from word order information.

In the following sections, we’ll give an inventory of relations used in dependency parsing, discuss two families of parsing algorithms (transition-based, and graph-based), and discuss evaluation.

18.1 Dependency Relations

The traditional linguistic notion of grammatical relation provides the basis for the binary relations that comprise these dependency structures. The arguments to these relations consist of a head and a dependent. The head plays the role of the central organizing word, and the dependent as a kind of modifier. The head-dependent relationship is made explicit by directly linking heads to the words that are immediately dependent on them.

In addition to specifying the head-dependent pairs, dependency grammars allow us to classify the kinds of grammatical relations, or grammatical function that the dependent plays with respect to its head. These include familiar notions such as subject, direct object and indirect object. In English these notions strongly correlate with, but by no means determine, both position in a sentence and constituent type and are therefore somewhat redundant with the kind of information found in phrase-structure trees. However, in languages with more flexible word order, the information encoded directly in these grammatical relations is critical since phrase-based constituent syntax provides little help.

Linguists have developed taxonomies of relations that go well beyond the familiar notions of subject and object. While there is considerable variation from theory
to theory, there is enough commonality that cross-linguistic standards have been
developed. The Universal Dependencies (UD) project (de Marneffe et al., 2021),
an open community effort to annotate dependencies and other aspects of grammar
across more than 100 languages, provides an inventory of 37 dependency relations.
Fig. 18.2 shows a subset of the UD relations and Fig. 18.3 provides some examples.
The motivation for all of the relations in the Universal Dependency scheme is
beyond the scope of this chapter, but the core set of frequently used relations can be
broken into two sets: clausal relations that describe syntactic roles with respect to a
predicate (often a verb), and modifier relations that categorize the ways that words
can modify their heads.

Consider, for example, the following sentence:

United canceled the morning flights to Houston.

Here the clausal relations NSUBJ and DOBJ identify the subject and direct object of
the predicate cancel, while the NMOD, DET, and CASE relations denote modifiers of
the nouns flights and Houston.

18.1.1 Dependency Formalisms

A dependency structure can be represented as a directed graph $G = (V, A)$, consisting
of a set of vertices $V$, and a set of ordered pairs of vertices $A$, which we’ll call arcs.
For the most part we will assume that the set of vertices, $V$, corresponds exactly
to the set of words in a given sentence. However, they might also correspond to
punctuation, or when dealing with morphologically complex languages the set of
vertices might consist of stems and affixes. The set of arcs, $A$, captures the head-
dependent and grammatical function relationships between the elements in $V$.

Different grammatical theories or formalisms may place further constraints on
these dependency structures. Among the more frequent restrictions are that the
structures must be connected, have a designated root node, and be acyclic or planar. Of
most relevance to the parsing approaches discussed in this chapter is the common,
Relation | Examples with head and dependent
---|---
NSUBJ | United canceled the flight.
OBJ | United diverted the flight to Reno.
We booked her the first flight to Miami.
IOBJ | We booked her the flight to Miami.
COMPOUND | We took the morning flight.
NMOD | flight to Houston.
AMOD | Book the cheapest flight.
APPOS | United, a unit of UAL, matched the fares.
DET | The flight was canceled.
Which flight was delayed?
CONJ | We flew to Denver and drove to Steamboat.
CC | We flew to Denver and drove to Steamboat.
CASE | Book the flight through Houston.

Figure 18.3 Examples of some Universal Dependency relations.

dependency tree

computationally-motivated, restriction to rooted trees. That is, a dependency tree is a directed graph that satisfies the following constraints:

1. There is a single designated root node that has no incoming arcs.
2. With the exception of the root node, each vertex has exactly one incoming arc.
3. There is a unique path from the root node to each vertex in V.

Taken together, these constraints ensure that each word has a single head, that the dependency structure is connected, and that there is a single root node from which one can follow a unique directed path to each of the words in the sentence.

18.1.2 Projectivity

The notion of projectivity imposes an additional constraint that is derived from the order of the words in the input. An arc from a head to a dependent is said to be projective if there is a path from the head to every word that lies between the head and the dependent in the sentence. A dependency tree is then said to be projective if all the arcs that make it up are projective. All the dependency trees we’ve seen thus far have been projective. There are, however, many valid constructions which lead to non-projective trees, particularly in languages with relatively flexible word order.

Consider the following example.

JetBlue canceled our flight this morning which was already late

(18.3)

In this example, the arc from flight to its modifier late is non-projective since there is no path from flight to the intervening words this and morning. As we can see from this diagram, projectivity (and non-projectivity) can be detected in the way we’ve been drawing our trees. A dependency tree is projective if it can be drawn with no crossing edges. Here there is no way to link flight to its dependent late without crossing the arc that links morning to its head.
Our concern with projectivity arises from two related issues. First, the most widely used English dependency treebanks were automatically derived from phrase-structure treebanks through the use of head-finding rules. The trees generated in such a fashion will always be projective, and hence will be incorrect when non-projective examples like this one are encountered.

Second, there are computational limitations to the most widely used families of parsing algorithms. The transition-based approaches discussed in Section 18.2 can only produce projective trees, hence any sentences with non-projective structures will necessarily contain some errors. This limitation is one of the motivations for the more flexible graph-based parsing approach described in Section 18.3.

18.1.3 Dependency Treebanks

Treebanks play a critical role in the development and evaluation of dependency parsers. They are used for training parsers, they act as the gold labels for evaluating parsers, and they also provide useful information for corpus linguistics studies.

Dependency treebanks are created by having human annotators directly generate dependency structures for a given corpus, or by hand-correcting the output of an automatic parser. A few early treebanks were also based on using a deterministic process to translate existing constituent-based treebanks into dependency trees.

The largest open community project for building dependency trees is the Universal Dependencies project at https://universaldependencies.org/ introduced above, which currently has almost 200 dependency treebanks in more than 100 languages (de Marneffe et al., 2021). Here are a few UD examples showing dependency trees for sentences in Spanish, Basque, and Mandarin Chinese:

[Spanish] Subiremos al tren a las cinco. “We will be boarding the train at five.”

[Basque] Ekaitzak itsasontzia hondoratu du. “The storm has sunk the ship.”
18.2 Transition-Based Dependency Parsing

Our first approach to dependency parsing is called **transition-based** parsing. This architecture draws on **shift-reduce parsing**, a paradigm originally developed for analyzing programming languages (Aho and Ullman, 1972). In transition-based parsing we’ll have a **stack** on which we build the parse, a **buffer** of tokens to be parsed, and a parser which takes actions on the parse via a predictor called an **oracle**, as illustrated in Fig. 18.4.

The parser walks through the sentence left-to-right, successively shifting items from the buffer onto the stack. At each time point we examine the top two elements on the stack, and the oracle makes a decision about what **transition** to apply to build the parse. The possible transitions correspond to the intuitive actions one might take in creating a dependency tree by examining the words in a single pass over the input from left to right (Covington, 2001):

- Assign the current word as the head of some previously seen word,
- Assign some previously seen word as the head of the current word,
- Postpone dealing with the current word, storing it for later processing.

We’ll formalize this intuition with the following three transition operators that will operate on the top two elements of the stack:

- **LEFTARC**: Assert a head-dependent relation between the word at the top of the stack and the second word; remove the second word from the stack.
- **RIGHTARC**: Assert a head-dependent relation between the second word on the stack and the word at the top; remove the top word from the stack;
18.2 • Transition-Based Dependency Parsing

• **SHIFT**: Remove the word from the front of the input buffer and push it onto
  the stack.

We’ll sometimes call operations like **LEFTARC** and **RIGHTARC reduce** operations,
based on a metaphor from shift-reduce parsing, in which reducing means combin-
ing elements on the stack. There are some preconditions for using operators. The
**LEFTARC** operator cannot be applied when **ROOT** is the second element of the stack
(since by definition the **ROOT** node cannot have any incoming arcs). And both the
**LEFTARC** and **RIGHTARC** operators require two elements to be on the stack to be
applied.

This particular set of operators implements what is known as the **arc standard**
approach to transition-based parsing (Covington 2001, Nivre 2003). In arc standard
parsing the transition operators only assert relations between elements at the top of
the stack, and once an element has been assigned its head it is removed from the
stack and is not available for further processing. As we’ll see, there are alternative
transition systems which demonstrate different parsing behaviors, but the arc
standard approach is quite effective and is simple to implement.

The specification of a transition-based parser is quite simple, based on repre-
senting the current state of the parse as a **configuration**: the stack, an input buffer
of words or tokens, and a set of relations representing a dependency tree. Parsing
means making a sequence of transitions through the space of possible configura-
tions. We start with an initial configuration in which the stack contains the **ROOT
node**, the buffer has the tokens in the sentence, and an empty set of relations repre-
sents the parse. In the final goal state, the stack and the word list should be empty,
and the set of relations will represent the final parse. Fig. 18.5 gives the algorithm.

```plaintext
function DEPENDENCYPARSE(words) returns dependency tree
    state ← { [root], [words], [] }; initial configuration
    while state not final
        t ← ORACLE(state); choose a transition operator to apply
        state ← APPLY(t, state); apply it, creating a new state
    return state
```

**Figure 18.5** A generic transition-based dependency parser

At each step, the parser consults an oracle (we’ll come back to this shortly) that
provides the correct transition operator to use given the current configuration. It then
applies that operator to the current configuration, producing a new configuration.
The process ends when all the words in the sentence have been consumed and the
**ROOT** node is the only element remaining on the stack.

The efficiency of transition-based parsers should be apparent from the algorithm.
The complexity is linear in the length of the sentence since it is based on a single
left to right pass through the words in the sentence. (Each word must first be shifted
onto the stack and then later reduced.)

Note that unlike the dynamic programming and search-based approaches dis-
cussed in Chapter 17, this approach is a straightforward greedy algorithm—the or-
acle provides a single choice at each step and the parser proceeds with that choice,
no other options are explored, no backtracking is employed, and a single parse is
returned in the end.

Figure 18.6 illustrates the operation of the parser with the sequence of transitions
leading to a parse for the following example.

![Diagram](18.7)

Let’s consider the state of the configuration at Step 2, after the word *me* has been pushed onto the stack.

<table>
<thead>
<tr>
<th>Stack</th>
<th>Word List</th>
<th>Relations</th>
</tr>
</thead>
<tbody>
<tr>
<td>[root, book, me]</td>
<td>[the, morning, flight]</td>
<td></td>
</tr>
</tbody>
</table>

The correct operator to apply here is **RIGHTARC** which assigns *book* as the head of *me* and pops *me* from the stack resulting in the following configuration.

<table>
<thead>
<tr>
<th>Stack</th>
<th>Word List</th>
<th>Relations</th>
</tr>
</thead>
<tbody>
<tr>
<td>[root, book]</td>
<td>[the, morning, flight]</td>
<td>(book → me)</td>
</tr>
</tbody>
</table>

After several subsequent applications of the **SHIFT** and **LEFTARC** operators, the configuration in Step 6 looks like the following:

<table>
<thead>
<tr>
<th>Stack</th>
<th>Word List</th>
<th>Relations</th>
</tr>
</thead>
<tbody>
<tr>
<td>[root, book, the, morning, flight]</td>
<td>[]</td>
<td>(book → me)</td>
</tr>
</tbody>
</table>

Here, all the remaining words have been passed onto the stack and all that is left to do is to apply the appropriate reduce operators. In the current configuration, we employ the **LEFTARC** operator resulting in the following state.

<table>
<thead>
<tr>
<th>Stack</th>
<th>Word List</th>
<th>Relations</th>
</tr>
</thead>
<tbody>
<tr>
<td>[root, book, the, flight]</td>
<td>[]</td>
<td>(book → me)</td>
</tr>
</tbody>
</table>

At this point, the parse for this sentence consists of the following structure.

![Diagram](18.8)

There are several important things to note when examining sequences such as the one in Figure 18.6. First, the sequence given is not the only one that might lead to a reasonable parse. In general, there may be more than one path that leads to the same result, and due to ambiguity, there may be other transition sequences that lead to different equally valid parses.

Second, we are assuming that the oracle always provides the correct operator at each point in the parse—an assumption that is unlikely to be true in practice. As a result, given the greedy nature of this algorithm, incorrect choices will lead to incorrect parses since the parser has no opportunity to go back and pursue alternative choices. Section 18.2.4 will introduce several techniques that allow transition-based approaches to explore the search space more fully.
Finally, for simplicity, we have illustrated this example without the labels on the dependency relations. To produce labeled trees, we can parameterize the LEFT-ARC and RIGHT-ARC operators with dependency labels, as in LEFT-ARC(NSUBJ) or RIGHT-ARC(OBJ). This is equivalent to expanding the set of transition operators from our original set of three to a set that includes LEFT-ARC and RIGHT-ARC operators for each relation in the set of dependency relations being used, plus an additional one for the SHIFT operator. This, of course, makes the job of the oracle more difficult since it now has a much larger set of operators from which to choose.

### 18.2.1 Creating an Oracle

The oracle for greedily selecting the appropriate transition is trained by supervised machine learning. As with all supervised machine learning methods, we will need training data: configurations annotated with the correct transition to take. We can draw these from dependency trees. And we need to extract features of the configuration. We’ll introduce neural classifiers that represent the configuration via embeddings, as well as classic systems that use hand-designed features.

**Generating Training Data**

The oracle from the algorithm in Fig. 18.5 takes as input a configuration and returns a transition operator. Therefore, to train a classifier, we will need configurations paired with transition operators (i.e., LEFT-ARC, RIGHT-ARC, or SHIFT). Unfortunately, treebanks pair entire sentences with their corresponding trees, not configurations with transitions.

To generate the required training data, we employ the oracle-based parsing algorithm in a clever way. We supply our oracle with the training sentences to be parsed along with their corresponding reference parses from the treebank. To produce training instances, we then simulate the operation of the parser by running the algorithm and relying on a new training oracle to give us correct transition operators for each successive configuration.

To see how this works, let’s first review the operation of our parser. It begins with a default initial configuration where the stack contains the ROOT, the input list is just the list of words, and the set of relations is empty. The LEFT-ARC and RIGHT-ARC operators each add relations between the words at the top of the stack to the set of relations being accumulated for a given sentence. Since we have a gold-standard reference parse for each training sentence, we know which dependency relations are valid for a given sentence. Therefore, we can use the reference parse to guide the
selection of operators as the parser steps through a sequence of configurations.

To be more precise, given a reference parse and a configuration, the training oracle proceeds as follows:

- Choose \texttt{LEFTARC} if it produces a correct head-dependent relation given the reference parse and the current configuration,
- Otherwise, choose \texttt{RIGHTARC} if (1) it produces a correct head-dependent relation given the reference parse and (2) all of the dependents of the word at the top of the stack have already been assigned,
- Otherwise, choose \texttt{SHIFT}.

The restriction on selecting the \texttt{RIGHTARC} operator is needed to ensure that a word is not popped from the stack, and thus lost to further processing, before all its dependents have been assigned to it.

More formally, during training the oracle has access to the following:

- A current configuration with a stack \( S \) and a set of dependency relations \( R_c \)
- A reference parse consisting of a set of vertices \( V \) and a set of dependency relations \( R_p \)

Given this information, the oracle chooses transitions as follows:

\begin{align*}
\texttt{LEFTARC}(r): & \text{ if } (S_1 \ r \ S_2) \in R_p \\
\texttt{RIGHTARC}(r): & \text{ if } (S_2 \ r \ S_1) \in R_p \text{ and } \forall r', w \ s.t. (S_1 \ r' \ w) \in R_p \text{ then } (S_1 \ r' \ w) \in R_c \\
\text{SHIFT}: & \text{ otherwise}
\end{align*}

Let’s walk through the processing of the following example as shown in Fig. 18.7.

![Diagram](image)

At Step 1, \texttt{LEFTARC} is not applicable in the initial configuration since it asserts a relation, (root \( \leftarrow \) book), not in the reference answer; \texttt{RIGHTARC} does assert a relation contained in the final answer (root \( \rightarrow \) book), however \textit{book} has not been attached to any of its dependents yet, so we have to defer, leaving \texttt{SHIFT} as the only
possible action. The same conditions hold in the next two steps. In step 3, \textsc{leftarc} is selected to link \textit{the} to its head.

Now consider the situation in Step 4.

\begin{tabular}{|c|c|c|}
\hline
Stack & Word buffer & Relations \\
\hline
[root, book, flight] & [through, Houston] & (the ← flight) \\
\hline
\end{tabular}

Here, we might be tempted to add a dependency relation between \textit{book} and \textit{flight}, which is present in the reference parse. But doing so now would prevent the later attachment of \textit{Houston} since \textit{flight} would have been removed from the stack. Fortunately, the precondition on choosing \textsc{rightarc} prevents this choice and we're again left with \textsc{shift} as the only viable option. The remaining choices complete the set of operators needed for this example.

To recap, we derive appropriate training instances consisting of configuration-transition pairs from a treebank by simulating the operation of a parser in the context of a reference dependency tree. We can deterministically record correct parser actions at each step as we progress through each training example, thereby creating the training set we require.

### 18.2.2 A feature-based classifier

We’ll now introduce two classifiers for choosing transitions, here a classic feature-based algorithm and in the next section a neural classifier using embedding features.

Feature-based classifiers generally use the same features we’ve seen with part-of-speech tagging and partial parsing: Word forms, lemmas, parts of speech, the head, and the dependency relation to the head. Other features may be relevant for some languages, for example morphosyntactic features like case marking on subjects or objects. The features are extracted from the training configurations, which consist of the stack, the buffer and the current set of relations. Most useful are features referencing the top levels of the stack, the words near the front of the buffer, and the dependency relations already associated with any of those elements.

We’ll use a \textit{feature template} as we did for sentiment analysis and part-of-speech tagging. Feature templates allow us to automatically generate large numbers of specific features from a training set. For example, consider the following feature templates that are based on single positions in a configuration.

\begin{equation}
\langle s_1.w, op \rangle, \langle s_2.w, op \rangle \langle s_1.t, op \rangle, \langle s_2.t, op \rangle
\end{equation}

\begin{equation}
\langle b_1.w, op \rangle, \langle b_1.t, op \rangle \langle s_1.w.t, op \rangle
\end{equation}

Here features are denoted as \textit{location.property}, where \(s = \text{stack}, b = \text{the word buffer}, w = \text{word forms}, t = \text{part-of-speech}, \text{and } op = \text{operator. Thus the feature for the word form at the top of the stack would be } s_1.w, \text{the part of speech tag at the front of the buffer } b_1.t, \text{and the concatenated feature } s_1.wt \text{ represents the word form concatenated with the part of speech of the word at the top of the stack. Consider applying these templates to the following intermediate configuration derived from a training oracle for (18.2).}

\begin{tabular}{|c|c|c|}
\hline
Stack & Word buffer & Relations \\
\hline
[root, canceled, flights] & [to Houston] & (canceled → United) \\
& & (flights → morning) \\
& & (flights → the) \\
\hline
\end{tabular}
The correct transition here is \textit{shift} (you should convince yourself of this before proceeding). The application of our set of feature templates to this configuration would result in the following set of instantiated features.

\begin{equation}
\langle s_1.w = \text{flights}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle s_2.w = \text{canceled}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle s_1.t = \text{NNS}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle s_2.t = \text{VBD}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle b_1.w = \text{to}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle b_1.t = \text{TO}, op = \text{shift} \rangle
\end{equation}

\begin{equation}
\langle s_1.wt = \text{flightsNNS}, op = \text{shift} \rangle
\end{equation}

Given that the left and right arc transitions operate on the top two elements of the stack, features that \textit{combine} properties from these positions are even more useful. For example, a feature like \(s_1.t \circ s_2.t\) concatenates the part of speech tag of the word at the top of the stack with the tag of the word beneath it.

\begin{equation}
\langle s_1.t \circ s_2.t = \text{NNSVBD}, op = \text{shift} \rangle
\end{equation}

Given the training data and features, any classifier, like multinomial logistic regression or support vector machines, can be used.

### 18.2.3 A neural classifier

The oracle can also be implemented by a neural classifier. A standard architecture is simply to pass the sentence through an encoder, then take the presentation of the top 2 words on the stack and the first word of the buffer, concatenate them, and present to a feedforward network that predicts the transition to take (Kiperwasser and Goldberg, 2016; Kulmizev et al., 2019). Fig. 18.8 sketches this model. Learning can be done with cross-entropy loss.
18.2.4 Advanced Methods in Transition-Based Parsing

The basic transition-based approach can be elaborated in a number of ways to improve performance by addressing some of the most obvious flaws in the approach.

Alternative Transition Systems

The arc-standard transition system described above is only one of many possible systems. A frequently used alternative is the arc eager transition system. The arc eager approach gets its name from its ability to assert rightward relations much sooner than in the arc standard approach. To see this, let’s revisit the arc standard trace of Example 18.9, repeated here.

Consider the dependency relation between *book* and *flight* in this analysis. As is shown in Fig. 18.7, an arc-standard approach would assert this relation at Step 8, despite the fact that *book* and *flight* first come together on the stack much earlier at Step 4. The reason this relation can’t be captured at this point is due to the presence of the postnominal modifier *through Houston*. In an arc-standard approach, dependents are removed from the stack as soon as they are assigned their heads. If *flight* had been assigned *book* as its head in Step 4, it would no longer be available to serve as the head of *Houston*.

While this delay doesn’t cause any issues in this example, in general the longer a word has to wait to get assigned its head the more opportunities there are for something to go awry. The arc-eager system addresses this issue by allowing words to be attached to their heads as early as possible, before all the subsequent words dependent on them have been seen. This is accomplished through minor changes to the LEFTARC and RIGHTARC operators and the addition of a new REDUCE operator.

- **LEFTARC**: Assert a head-dependent relation between the word at the front of the input buffer and the word at the top of the stack; pop the stack.
- **RIGHTARC**: Assert a head-dependent relation between the word on the top of the stack and the word at the front of the input buffer; shift the word at the front of the input buffer to the stack.
- **SHIFT**: Remove the word from the front of the input buffer and push it onto the stack.
- **REDUCE**: Pop the stack.

The LEFTARC and RIGHTARC operators are applied to the top of the stack and the front of the input buffer, instead of the top two elements of the stack as in the arc-standard approach. The RIGHTARC operator now moves the dependent to the stack from the buffer rather than removing it, thus making it available to serve as the head of following words. The new REDUCE operator removes the top element from the stack. Together these changes permit a word to be eagerly assigned its head and still allow it to serve as the head for later dependents. The trace shown in Fig. 18.9 illustrates the new decision sequence for this example.

In addition to demonstrating the arc-eager transition system, this example demonstrates the power and flexibility of the overall transition-based approach. We were able to swap in a new transition system without having to make any changes to the
underlying parsing algorithm. This flexibility has led to the development of a diverse set of transition systems that address different aspects of syntax and semantics including: assigning part of speech tags (Choi and Palmer, 2011a), allowing the generation of non-projective dependency structures (Nivre, 2009), assigning semantic roles (Choi and Palmer, 2011b), and parsing texts containing multiple languages (Bhat et al., 2017).

### Beam Search

The computational efficiency of the transition-based approach discussed earlier derives from the fact that it makes a single pass through the sentence, greedily making decisions without considering alternatives. Of course, this is also a weakness – once a decision has been made it can not be undone, even in the face of overwhelming evidence arriving later in a sentence. We can use **beam search** to explore alternative decision sequences. Recall from Chapter 10 that beam search uses a breadth-first search strategy with a heuristic filter that prunes the search frontier to stay within a fixed-size **beam width**.

In applying beam search to transition-based parsing, we’ll elaborate on the algorithm given in Fig. 18.5. Instead of choosing the single best transition operator at each iteration, we’ll apply all applicable operators to each state on an agenda and then score the resulting configurations. We then add each of these new configurations to the frontier, subject to the constraint that there has to be room within the beam. As long as the size of the agenda is within the specified beam width, we can add new configurations to the agenda. Once the agenda reaches the limit, we only add new configurations that are better than the worst configuration on the agenda (removing the worst element so that we stay within the limit). Finally, to insure that we retrieve the best possible state on the agenda, the while loop continues as long as there are non-final states on the agenda.

The beam search approach requires a more elaborate notion of scoring than we used with the greedy algorithm. There, we assumed that the oracle would be a supervised classifier that chose the best transition operator based on features of the current configuration. This choice can be viewed as assigning a score to all the possible transitions and picking the best one.

\[ T(c) = \arg\max_{t} \text{Score}(t, c) \]

With beam search we are now searching through the space of decision sequences, so it makes sense to base the score for a configuration on its entire history. So we can define the score for a new configuration as the score of its predecessor plus the

<table>
<thead>
<tr>
<th>Step</th>
<th>Stack</th>
<th>Word List</th>
<th>Action</th>
<th>Relation Added</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>[root]</td>
<td>[book, the, flight, through, houston]</td>
<td>RIGHTARC</td>
<td>(root → book)</td>
</tr>
<tr>
<td>1</td>
<td>[root, book]</td>
<td>[the, flight, through, houston]</td>
<td>SHIFT</td>
<td>(the ← flight)</td>
</tr>
<tr>
<td>2</td>
<td>[root, book, the]</td>
<td>[flight, through, houston]</td>
<td>LEFTARC</td>
<td>(book → flight)</td>
</tr>
<tr>
<td>3</td>
<td>[root, book]</td>
<td>[flight, through, houston]</td>
<td>RIGHTARC</td>
<td>(through ← flight)</td>
</tr>
<tr>
<td>4</td>
<td>[root, book, flight]</td>
<td>[through, houston]</td>
<td>SHIFT</td>
<td>(flight → houston)</td>
</tr>
<tr>
<td>5</td>
<td>[root, book, flight, through]</td>
<td>[houston]</td>
<td>REDUCE</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>[root, book, flight]</td>
<td>[houston]</td>
<td>REDUCE</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>[root, book, flight, houston]</td>
<td>[]</td>
<td>REDUCE</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>[root, book, flight]</td>
<td>[]</td>
<td>REDUCE</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>[root, book]</td>
<td>[]</td>
<td>REDUCE</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>[root]</td>
<td>[]</td>
<td>REDUCE</td>
<td>Done</td>
</tr>
</tbody>
</table>

**Figure 18.9** A processing trace of *Book the flight through Houston* using the arc-eager transition operators.
18.3 Graph-Based Dependency Parsing

Graph-based methods are the second important family of dependency parsing algorithms. Graph-based parsers are more accurate than transition-based parsers, especially on long sentences; transition-based methods have trouble when the heads are very far from the dependents (McDonald and Nivre, 2011). Graph-based methods avoid this difficulty by scoring entire trees, rather than relying on greedy local decisions. Furthermore, unlike transition-based approaches, graph-based parsers can produce non-projective trees. Although projectivity is not a significant issue for English, it is definitely a problem for many of the world’s languages.

Graph-based dependency parsers search through the space of possible trees for a given sentence for a tree (or trees) that maximize some score. These methods encode the search space as directed graphs and employ methods drawn from graph theory to search the space for optimal solutions. More formally, given a sentence $S$ we’re looking for the best dependency tree in $\mathcal{G}_S$, the space of all possible trees for that sentence, that maximizes some score.

$$\hat{T}(S) = \arg\max_{t \in \mathcal{G}_S} \text{Score}(t, S)$$
We’ll make the simplifying assumption that this score can be edge-factored, meaning that the overall score for a tree is the sum of the scores of each of the scores of the edges that comprise the tree.

\[ \text{Score}(t, S) = \sum_{e \in t} \text{Score}(e) \]

Graph-based algorithms have to solve two problems: (1) assigning a score to each edge, and (2) finding the best parse tree given the scores of all potential edges. In the next few sections we’ll introduce solutions to these two problems, beginning with the second problem of finding trees, and then giving a feature-based and a neural algorithm for solving the first problem of assigning scores.

### 18.3.1 Parsing via finding the maximum spanning tree

In graph-based parsing, given a sentence \( S \) we start by creating a graph \( G \) which is a fully-connected, weighted, directed graph where the vertices are the input words and the directed edges represent all possible head-dependent assignments. We’ll include an additional \textsc{root} node with outgoing edges directed at all of the other vertices. The weights of each edge in \( G \) reflect the score for each possible head-dependent relation assigned by some scoring algorithm.

It turns out that finding the best dependency parse for \( S \) is equivalent to finding the maximum spanning tree over \( G \). A spanning tree over a graph \( G \) is a subset of \( G \) that is a tree and covers all the vertices in \( G \); a spanning tree over \( G \) that starts from the \textsc{root} is a valid parse of \( S \). A maximum spanning tree is the spanning tree with the highest score. Thus a maximum spanning tree of \( G \) emanating from the \textsc{root} is the optimal dependency parse for the sentence.

A directed graph for the example \textit{Book that flight} is shown in Fig. 18.11, with the maximum spanning tree corresponding to the desired parse shown in blue. For ease of exposition, we’ll describe here the algorithm for \textit{unlabeled} dependency parsing.

Before describing the algorithm it’s useful to consider two intuitions about directed graphs and their spanning trees. The first intuition begins with the fact that every vertex in a spanning tree has exactly one incoming edge. It follows from this that every connected component of a spanning tree (i.e., every set of vertices that are linked to each other by paths over edges) will also have one incoming edge. The second intuition is that the absolute values of the edge scores are not critical to determining its maximum spanning tree. Instead, it is the relative weights of the edges entering each vertex that matters. If we were to subtract a constant amount from each edge entering a given vertex it would have no impact on the choice of
the maximum spanning tree since every possible spanning tree would decrease by exactly the same amount.

The first step of the algorithm itself is quite straightforward. For each vertex in the graph, an incoming edge (representing a possible head assignment) with the highest score is chosen. If the resulting set of edges produces a spanning tree then we’re done. More formally, given the original fully-connected graph $G = (V, E)$, a subgraph $T = (V, F)$ is a spanning tree if it has no cycles and each vertex (other than the root) has exactly one edge entering it. If the greedy selection process produces such a tree then it is the best possible one.

Unfortunately, this approach doesn’t always lead to a tree since the set of edges selected may contain cycles. Fortunately, in yet another case of multiple discovery, there is a straightforward way to eliminate cycles generated during the greedy selection phase. Chu and Liu (1965) and Edmonds (1967) independently developed an approach that begins with greedy selection and follows with an elegant recursive cleanup phase that eliminates cycles.

The cleanup phase begins by adjusting all the weights in the graph by subtracting the score of the maximum edge entering each vertex from the score of all the edges entering that vertex. This is where the intuitions mentioned earlier come into play. We have scaled the values of the edges so that the weights of the edges in the cycle have no bearing on the weight of any of the possible spanning trees. Subtracting the value of the edge with maximum weight from each edge entering a vertex results in a weight of zero for all of the edges selected during the greedy selection phase, including all of the edges involved in the cycle.

Having adjusted the weights, the algorithm creates a new graph by selecting a cycle and collapsing it into a single new node. Edges that enter or leave the cycle are altered so that they now enter or leave the newly collapsed node. Edges that do not touch the cycle are included and edges within the cycle are dropped.

Now, if we knew the maximum spanning tree of this new graph, we would have what we need to eliminate the cycle. The edge of the maximum spanning tree directed towards the vertex representing the collapsed cycle tells us which edge to delete in order to eliminate the cycle. How do we find the maximum spanning tree of this new graph? We recursively apply the algorithm to the new graph. This will either result in a spanning tree or a graph with a cycle. The recursions can continue as long as cycles are encountered. When each recursion completes we expand the collapsed vertex, restoring all the vertices and edges from the cycle with the exception of the single edge to be deleted.

Putting all this together, the maximum spanning tree algorithm consists of greedy edge selection, re-scoring of edge costs and a recursive cleanup phase when needed. The full algorithm is shown in Fig. 18.12.

Fig. 18.13 steps through the algorithm with our *Book that flight* example. The first row of the figure illustrates greedy edge selection with the edges chosen shown in blue (corresponding to the set $F$ in the algorithm). This results in a cycle between *that* and *flight*. The scaled weights using the maximum value entering each node are shown in the graph to the right.

Collapsing the cycle between *that* and *flight* to a single node (labelled *tf*) and recursing with the newly scaled costs is shown in the second row. The greedy selection step in this recursion yields a spanning tree that links *root* to *book*, as well as an edge that links *book* to the contracted node. Expanding the contracted node, we can see that this edge corresponds to the edge from *book* to *flight* in the original graph. This in turn tells us which edge to drop to eliminate the cycle.
function MaxSpanningTree(G=(V,E), root, score) returns spanning tree

F ← []
T' ← []
score' ← []
for each v ∈ V do
    bestInEdge ← argmax e=(u,v)∈ E score[e]
    F ← F ∪ bestInEdge
    for each e=(u,v) ∈ E do
        score'[e] ← score[e] − score[bestInEdge]
if T=(V,F) is a spanning tree then return it
else
    C ← a cycle in F
    G' ← CONTRACT(G, C)
    T' ← MaxSpanningTree(G', root, score')
    T ← EXPAND(T', C)
    return T

function CONTRACT(G, C) returns contracted graph

function EXPAND(T, C) returns expanded graph

Figure 18.12 The Chu-Liu Edmonds algorithm for finding a maximum spanning tree in a weighted directed graph.

On arbitrary directed graphs, this version of the CLE algorithm runs in \( O(mn) \) time, where \( m \) is the number of edges and \( n \) is the number of nodes. Since this particular application of the algorithm begins by constructing a fully connected graph \( m = n^2 \) yielding a running time of \( O(n^3) \). Gabow et al. (1986) present a more efficient implementation with a running time of \( O(m + n \log n) \).

18.3.2 A feature-based algorithm for assigning scores

Recall that given a sentence, \( S \), and a candidate tree, \( T \), edge-factored parsing models make the simplification that the score for the tree is the sum of the scores of the edges that comprise the tree:

\[
\text{score} (S, T) = \sum_{e \in T} \text{score} (S, e)
\]

In a feature-based algorithm we compute the edge score as a weighted sum of features extracted from it:

\[
\text{score} (S, e) = \sum_{i=1}^{N} w_i f_i (S, e)
\]

Or more succinctly,

\[
\text{score} (S, e) = w \cdot f
\]

Given this formulation, we need to identify relevant features and train the weights.

The features (and feature combinations) used to train edge-factored models mirror those used in training transition-based parsers, such as
Figure 18.13 Chu-Liu-Edmonds graph-based example for Book that flight

- Wordforms, lemmas, and parts of speech of the headword and its dependent.
- Corresponding features from the contexts before, after and between the words.
- Word embeddings.
- The dependency relation itself.
- The direction of the relation (to the right or left).
- The distance from the head to the dependent.

Given a set of features, our next problem is to learn a set of weights corresponding to each. Unlike many of the learning problems discussed in earlier chapters, here we are not training a model to associate training items with class labels, or parser actions. Instead, we seek to train a model that assigns higher scores to correct trees than to incorrect ones. An effective framework for problems like this is to use inference-based learning combined with the perceptron learning rule. In this framework, we parse a sentence (i.e., perform inference) from the training set using some initially random set of initial weights. If the resulting parse matches the corresponding tree in the training data, we do nothing to the weights. Otherwise, we find those features in the incorrect parse that are not present in the reference parse and we lower their weights by a small amount based on the learning rate. We do this incrementally for each sentence in our training data until the weights converge.
18.3.3 A neural algorithm for assigning scores

State-of-the-art graph-based multilingual parsers are based on neural networks. Instead of extracting hand-designed features to represent each edge between words $w_i$ and $w_j$, these parsers run the sentence through an encoder, and then pass the encoded representation of the two words $w_i$ and $w_j$ through a network that estimates a score for the edge $i \rightarrow j$.

Here we’ll sketch the biaffine algorithm of Dozat and Manning (2017) and Dozat et al. (2017) shown in Fig. 18.14, drawing on the work of Grünewald et al. (2021) who tested many versions of the algorithm via their STEPS system. The algorithm first runs the sentence $X = x_1, \ldots, x_n$ through an encoder to produce a contextual embedding representation for each token $R = r_1, \ldots, r_n$. The embedding for each token is now passed through two separate feedforward networks, one to produce a representation of this token as a head, and one to produce a representation of this token as a dependent:

$$h_{\text{head}}^i = \text{FFN}_{\text{head}}(r_i) \quad (18.13)$$

$$h_{\text{dep}}^i = \text{FFN}_{\text{dep}}(r_i) \quad (18.14)$$

Now to assign a score to the directed edge $i \rightarrow j$, ($w_i$ is the head and $w_j$ is the dependent), we feed the head representation of $i$, $h_{\text{head}}^i$, and the dependent representation of $j$, $h_{\text{dep}}^j$, into a biaffine scoring function:

$$\text{Score}(i \rightarrow j) = \text{Biaff}(h_{\text{head}}^i, h_{\text{dep}}^j) \quad (18.15)$$

$$\text{Biaff}(x, y) = x^\top U y + W(x \oplus y) + b \quad (18.16)$$

![Figure 18.14](image-url)
where $U$, $W$, and $b$ are weights learned by the model. The idea of using a biaffine function is to allow the system to learn multiplicative interactions between the vectors $x$ and $y$.

If we pass $\text{Score}(i \rightarrow j)$ through a softmax, we end up with a probability distribution, for each token $j$, over potential heads $i$ (all other tokens in the sentence):

$$p(i \rightarrow j) = \text{softmax}([\text{Score}(k \rightarrow j); \forall k \neq j, 1 \leq k \leq n])$$  \hspace{1cm} (18.17)

This probability can then be passed to the maximum spanning tree algorithm of Section 18.3.1 to find the best tree.

This $p(i \rightarrow j)$ classifier is trained by optimizing the cross-entropy loss.

Note that the algorithm as we’ve described it is unlabeled. To make this into a labeled algorithm, the Dozat and Manning (2017) algorithm actually trains two classifiers. The first classifier, the edge-scorer, the one we described above, assigns a probability $p(i \rightarrow j)$ to each word $w_i$ and $w_j$. Then the Maximum Spanning Tree algorithm is run to get a single best dependency parse tree for the second. We then apply a second classifier, the label-scorer, whose job is to find the maximum probability label for each edge in this parse. This second classifier has the same form as (18.15-18.17), but instead of being trained to predict with binary softmax the probability of an edge existing between two words, it is trained with a softmax over dependency labels to predict the dependency label between the words.

**18.4 Evaluation**

As with phrase structure-based parsing, the evaluation of dependency parsers proceeds by measuring how well they work on a test set. An obvious metric would be exact match (EM)—how many sentences are parsed correctly. This metric is quite pessimistic, with most sentences being marked wrong. Such measures are not fine-grained enough to guide the development process. Our metrics need to be sensitive enough to tell if actual improvements are being made.

For these reasons, the most common method for evaluating dependency parsers are labeled and unlabeled attachment accuracy. Labeled attachment refers to the proper assignment of a word to its head along with the correct dependency relation. Unlabeled attachment simply looks at the correctness of the assigned head, ignoring the dependency relation. Given a system output and a corresponding reference parse, accuracy is simply the percentage of words in an input that are assigned the correct head with the correct relation. These metrics are usually referred to as the labeled attachment score (LAS) and unlabeled attachment score (UAS). Finally, we can make use of a label accuracy score (LS), the percentage of tokens with correct labels, ignoring where the relations are coming from.

As an example, consider the reference parse and system parse for the following example shown in Fig. 18.15.

(18.18) Book me the flight through Houston.

The system correctly finds 4 of the 6 dependency relations present in the reference parse and receives an LAS of 2/3. However, one of the 2 incorrect relations found by the system holds between book and flight, which are in a head-dependent relation in the reference parse; the system therefore achieves a UAS of 5/6.

Beyond attachment scores, we may also be interested in how well a system is performing on a particular kind of dependency relation, for example $\text{NSUBJ}$, across
Figure 18.15  Reference and system parses for Book me the flight through Houston, resulting in an LAS of 2/3 and an UAS of 5/6.

a development corpus. Here we can make use of the notions of precision and recall introduced in Chapter 8, measuring the percentage of relations labeled NSUBJ by the system that were correct (precision), and the percentage of the NSUBJ relations present in the development set that were in fact discovered by the system (recall). We can employ a confusion matrix to keep track of how often each dependency type was confused for another.

18.5 Summary

This chapter has introduced the concept of dependency grammars and dependency parsing. Here’s a summary of the main points that we covered:

- In dependency-based approaches to syntax, the structure of a sentence is described in terms of a set of binary relations that hold between the words in a sentence. Larger notions of constituency are not directly encoded in dependency analyses.
- The relations in a dependency structure capture the head-dependent relationship among the words in a sentence.
- Dependency-based analysis provides information directly useful in further language processing tasks including information extraction, semantic parsing and question answering.
- Transition-based parsing systems employ a greedy stack-based algorithm to create dependency structures.
- Graph-based methods for creating dependency structures are based on the use of maximum spanning tree methods from graph theory.
- Both transition-based and graph-based approaches are developed using supervised machine learning techniques.
- Treebanks provide the data needed to train these systems. Dependency treebanks can be created directly by human annotators or via automatic transformation from phrase-structure treebanks.
- Evaluation of dependency parsers is based on labeled and unlabeled accuracy scores as measured against withheld development and test corpora.
Bibliographical and Historical Notes

The dependency-based approach to grammar is much older than the relatively recent phrase-structure or constituency grammars, which date only to the 20th century. Dependency grammar dates back to the Indian grammarian Pāṇini sometime between the 7th and 4th centuries BCE, as well as the ancient Greek linguistic traditions. Contemporary theories of dependency grammar all draw heavily on the 20th century work of Tesnière (1959).

Automatic parsing using dependency grammars was first introduced into computational linguistics by early work on machine translation at the RAND Corporation led by David Hays. This work on dependency parsing closely paralleled work on constituent parsing and made explicit use of grammars to guide the parsing process. After this early period, computational work on dependency parsing remained intermittent over the following decades. Notable implementations of dependency parsers for English during this period include Link Grammar (Sleator and Temperley, 1993), Constraint Grammar (Karlsson et al., 1995), and MINIPAR (Lin, 2003).

Dependency parsing saw a major resurgence in the late 1990’s with the appearance of large dependency-based treebanks and the associated advent of data driven approaches described in this chapter. Eisner (1996) developed an efficient dynamic programming approach to dependency parsing based on bilexical grammars derived from the Penn Treebank. Covington (2001) introduced the deterministic word by word approach underlying current transition-based approaches. Yamada and Matsumoto (2003) and Kudo and Matsumoto (2002) introduced both the shift-reduce paradigm and the use of supervised machine learning in the form of support vector machines to dependency parsing.

Transition-based parsing is based on the shift-reduce parsing algorithm originally developed for analyzing programming languages (Aho and Ullman, 1972). Shift-reduce parsing also makes use of a context-free grammar. Input tokens are successively shifted onto the stack and the top two elements of the stack are matched against the right-hand side of the rules in the grammar; when a match is found the matched elements are replaced on the stack (reduced) by the non-terminal from the left-hand side of the rule being matched. In transition-based dependency parsing we skip the grammar, and alter the reduce operation to add a dependency relation between a word and its head.


The graph-based maximum spanning tree approach to dependency parsing was introduced by McDonald et al. 2005a, McDonald et al. 2005b. The neural classifier was introduced by (Kiperwasser and Goldberg, 2016).

The long-running Prague Dependency Treebank project (Hajič, 1998) is the most significant effort to directly annotate a corpus with multiple layers of morphological, syntactic and semantic information. PDT 3.0 contains over 1.5 M tokens (Bejček et al., 2013).

Universal Dependencies (UD) (de Marneffe et al., 2021) is an open community
project to create a framework for dependency treebank annotation, with nearly 200
treebanks in over 100 languages. The UD annotation scheme evolved out of several
distinct efforts including Stanford dependencies (de Marneffe et al. 2006, de Marneffe
and Manning 2008, de Marneffe et al. 2014), Google’s universal part-of-speech
tags (Petrov et al., 2012), and the Interset interlingua for morphosyntactic tagsets
(Zeman, 2008).

The Conference on Natural Language Learning (CoNLL) has conducted an in-
fluential series of shared tasks related to dependency parsing over the years (Buch-
More recent evaluations have focused on parser robustness with respect to morpho-
logically rich languages (Seddah et al., 2013), and non-canonical language forms
such as social media, texts, and spoken language (Petrov and McDonald, 2012).
Choi et al. (2015) presents a performance analysis of 10 dependency parsers across
a range of metrics, as well as DEPENDABLE, a robust parser evaluation tool.

Exercises
Imagine that you are an analyst with an investment firm that tracks airline stocks. You’re given the task of determining the relationship (if any) between airline announcements of fare increases and the behavior of their stocks the next day. Historical data about stock prices is easy to come by, but what about the airline announcements? You will need to know at least the name of the airline, the nature of the proposed fare hike, the dates of the announcement, and possibly the response of other airlines. Fortunately, these can be all found in news articles like this one:

Citing high fuel prices, United Airlines said Friday it has increased fares by $6 per round trip on flights to some cities also served by lower-cost carriers. American Airlines, a unit of AMR Corp., immediately matched the move, spokesman Tim Wagner said. United, a unit of UAL Corp., said the increase took effect Thursday and applies to most routes where it competes against discount carriers, such as Chicago to Dallas and Denver to San Francisco.

This chapter presents techniques for extracting limited kinds of semantic content from text. This process of information extraction (IE) turns the unstructured information embedded in texts into structured data, for example for populating a relational database to enable further processing.

We begin with the task of relation extraction: finding and classifying semantic relations among entities mentioned in a text, like child-of (X is the child-of Y), or part-whole or geospatial relations. Relation extraction has close links to populating a relational database, and knowledge graphs, datasets of structured relational knowledge, are a useful way for search engines to present information to users.

Next, we discuss event extraction, the task of finding events in which these entities participate, like, in our sample text, the fare increases by United and American and the reporting events said and cite. Events are also situated in time, occurring at a particular date or time, and events can be related temporally, happening before or after or simultaneously with each other. We’ll need to recognize temporal expressions like Friday, Thursday or two days from now and times such as 3:30 P.M., and normalize them onto specific calendar dates or times. We’ll need to link Friday to the time of United’s announcement, Thursday to the previous day’s fare increase, and we’ll need to produce a timeline in which United’s announcement follows the fare increase and American’s announcement follows both of those events.

The related task of template filling is to find recurring stereotypical events or situations in documents and fill in the template slots. These slot-fillers may consist of text segments extracted directly from the text, or concepts like times, amounts, or ontology entities that have been inferred through additional processing. Our airline
text presents such a stereotypical situation since airlines often raise fares and then wait to see if competitors follow along. Here we can identify United as a lead airline that initially raised its fares, $6 as the amount, Thursday as the increase date, and American as an airline that followed along, leading to a filled template like the following:

<table>
<thead>
<tr>
<th>FARE-RAISE ATTEMPT:</th>
<th>LEAD AIRLINE: United Airlines</th>
</tr>
</thead>
<tbody>
<tr>
<td>AMOUNT:</td>
<td>$6</td>
</tr>
<tr>
<td>EFFECTIVE DATE:</td>
<td>2006-10-26</td>
</tr>
<tr>
<td>FOLLOWER:</td>
<td>American Airlines</td>
</tr>
</tbody>
</table>

19.1 Relation Extraction

Let’s assume that we have detected the named entities in our sample text (perhaps using the techniques of Chapter 8), and would like to discern the relationships that exist among the detected entities:

Citing high fuel prices, [ORG United Airlines] said [TIME Friday] it has increased fares by [MONEY $6] per round trip on flights to some cities also served by lower-cost carriers. [ORG American Airlines], a unit of [ORG AMR Corp.], immediately matched the move, spokesman [PER Tim Wagner] said. [ORG United], a unit of [ORG UAL Corp.], said the increase took effect [TIME Thursday] and applies to most routes where it competes against discount carriers, such as [LOC Chicago] to [LOC Dallas] and [LOC Denver] to [LOC San Francisco].

The text tells us, for example, that Tim Wagner is a spokesman for American Airlines, that United is a unit of UAL Corp., and that American is a unit of AMR. These binary relations are instances of more generic relations such as part-of or employs that are fairly frequent in news-style texts. Figure 19.1 lists the 17 relations used in the ACE relation extraction evaluations and Fig. 19.2 shows some sample relations. We might also extract more domain-specific relation such as the notion of an airline route. For example from this text we can conclude that United has routes to Chicago, Dallas, Denver, and San Francisco.
Sets of relations have been defined for many other domains as well. For example UMLS, the Unified Medical Language System from the US National Library of Medicine has a network that defines 134 broad subject categories, entity types, and 54 relations between the entities, such as the following:

<table>
<thead>
<tr>
<th>Entity</th>
<th>Relation</th>
<th>Entity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Injury</td>
<td>disrupts</td>
<td>Physiological Function</td>
</tr>
<tr>
<td>Bodily Location</td>
<td>location-of</td>
<td>Biologic Function</td>
</tr>
<tr>
<td>Anatomical Structure</td>
<td>part-of</td>
<td>Organism</td>
</tr>
<tr>
<td>Pharmacologic Substance</td>
<td>causes</td>
<td>Pathological Function</td>
</tr>
<tr>
<td>Pharmacologic Substance</td>
<td>treats</td>
<td>Pathologic Function</td>
</tr>
</tbody>
</table>

Given a medical sentence like this one:

(19.1) Doppler echocardiography can be used to diagnose left anterior descending artery stenosis in patients with type 2 diabetes

We could thus extract the UMLS relation:

_Echocardiography, Doppler Diagnoses Acquired stenosis_

Wikipedia also offers a large supply of relations, drawn from infoboxes, structured tables associated with certain Wikipedia articles. For example, the Wikipedia infobox for Stanford includes structured facts like state = “California” or president = "Marc Tessier-Lavigne". These facts can be turned into relations like president-of or located-in, or into relations in a metalanguage called RDF (Resource Description Framework). An RDF triple is a tuple of entity-relation-entity, called a subject-predicate-object expression. Here’s a sample RDF triple:

**subject** | **predicate** | **object**
--- | --- | ---
Golden Gate Park | location | San Francisco

For example the crowdsourced DBpedia (Bizer et al., 2009) is an ontology derived from Wikipedia containing over 2 billion RDF triples. Another dataset from Wikipedia infoboxes, Freebase (Bollacker et al., 2008), now part of Wikidata (Vrandečić and Krötzsch, 2014), has relations between people and their nationality, or locations, and other locations they are contained in.

WordNet or other ontologies offer useful ontological relations that express hierarchical relations between words or concepts. For example WordNet has the is-a or hypernym relation between classes,

Giraffe is-a ruminant is-a ungulate is-a mammal is-a vertebrate ...

WordNet also has Instance-of relation between individuals and classes, so that for example San Francisco is in the Instance-of relation with city. Extracting these relations is an important step in extending or building ontologies.

Finally, there are large datasets that contain sentences hand-labeled with their relations, designed for training and testing relation extractors. The TACRED dataset (Zhang et al., 2017) contains 106,264 examples of relation triples about particular people or organizations, labeled in sentences from news and web text drawn from the
annual TAC Knowledge Base Population (TAC KBP) challenges. TACRED contains 41 relation types (like per:city of birth, org:subsidiaries, org:member of, per:spouse), plus a no relation tag; examples are shown in Fig. 19.3. About 80% of all examples are annotated as no relation; having sufficient negative data is important for training supervised classifiers.

<table>
<thead>
<tr>
<th>Example</th>
<th>Entity Types &amp; Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carey will succeed Cathleen P. Black, who held the position for 15 years and will take on a new role as chairwoman of Hearst Magazines, the company said.</td>
<td>PERSON/TITLE Relation: per:title</td>
</tr>
<tr>
<td>Irene Morgan Kirkaldy, who was born and reared in Baltimore, lived on Long Island and ran a child-care center in Queens with her second husband, Stanley Kirkaldy.</td>
<td>PERSON/CITY Relation: per:city_of_birth</td>
</tr>
<tr>
<td>Baldwin declined further comment, and said JetBlue chief executive Dave Barger was unavailable.</td>
<td>Types: PERSON/TITLE Relation: no_relation</td>
</tr>
</tbody>
</table>

Figure 19.3 Example sentences and labels from the TACRED dataset (Zhang et al., 2017).

A standard dataset was also produced for the SemEval 2010 Task 8, detecting relations between nominals (Hendrickx et al., 2009). The dataset has 10,717 examples, each with a pair of nominals (untyped) hand-labeled with one of 9 directed relations like product-producer (a factory manufactures suits) or component-whole (my apartment has a large kitchen).

19.2 Relation Extraction Algorithms

There are five main classes of algorithms for relation extraction: handwritten patterns, supervised machine learning, semi-supervised (via bootstrapping or distant supervision), and unsupervised. We’ll introduce each of these in the next sections.

19.2.1 Using Patterns to Extract Relations

The earliest and still common algorithm for relation extraction is lexico-syntactic patterns, first developed by Hearst (1992a), and therefore often called Hearst patterns. Consider the following sentence:

Agar is a substance prepared from a mixture of red algae, such as Gelidium, for laboratory or industrial use.

Hearst points out that most human readers will not know what Gelidium is, but that they can readily infer that it is a kind of (a hyponym of) red algae, whatever that is. She suggests that the following lexico-syntactic pattern

\[ NP_0 \text{ such as } NP_1 \{, NP_2 \ldots, (and|or) NP_i \}, i \geq 1 \] (19.2)

implies the following semantics

\[ \forall NP_i, i \geq 1, \text{hyponym}(NP_i, NP_0) \] (19.3)

allowing us to infer

\[ \text{hyponym}(\text{Gelidium, red algae}) \] (19.4)
Figure 19.4 shows five patterns Hearst (1992a, 1998) suggested for inferring the hyponym relation; we’ve shown $\text{NP}_H$ as the parent/hyponym. Modern versions of the pattern-based approach extend it by adding named entity constraints. For example if our goal is to answer questions about “Who holds what office in which organization?”, we can use patterns like the following:

**PER, POSITION of ORG:**

George Marshall, Secretary of State of the United States

**PER (named|appointed|chose|etc.) PER Prep? POSITION**

Truman appointed Marshall Secretary of State

**PER [be]? (named|appointed|etc.) Prep? ORG POSITION**

George Marshall was named US Secretary of State

Hand-built patterns have the advantage of high-precision and they can be tailored to specific domains. On the other hand, they are often low-recall, and it’s a lot of work to create them for all possible patterns.

### 19.2.2 Relation Extraction via Supervised Learning

Supervised machine learning approaches to relation extraction follow a scheme that should be familiar by now. A fixed set of relations and entities is chosen, a training corpus is hand-annotated with the relations and entities, and the annotated texts are then used to train classifiers to annotate an unseen test set.

The most straightforward approach, illustrated in Fig. 19.5 is: (1) Find pairs of named entities (usually in the same sentence). (2): Apply a relation-classification on each pair. The classifier can use any supervised technique (logistic regression, RNN, Transformer, random forest, etc.).

An optional intermediate filtering classifier can be used to speed up the processing by making a binary decision on whether a given pair of named entities are related (by any relation). It’s trained on positive examples extracted directly from all relations in the annotated corpus, and negative examples generated from within-sentence entity pairs that are not annotated with a relation.

**Feature-based supervised relation classifiers.** Let’s consider sample features for a feature-based classifier (like logistic regression or random forests), classifying the relationship between *American Airlines* (Mention 1, or M1) and *Tim Wagner* (Mention 2, M2) from this sentence:

\[(19.5)\text{ American Airlines, a unit of AMR, immediately matched the move,}\]
\[
\text{spokesman Tim Wagner said}\]

These include word features (as embeddings, or 1-hot, stemmed or not):

- The headwords of M1 and M2 and their concatenation

  *American Airlines Wagner Airlines-Wagner*
function FINDRELATIONS(words) returns relations

relations ← nil
entities ← FINDENTITIES(words)
forall entity pairs ⟨e1, e2⟩ in entities do
    if RELATED?(e1, e2)
        relations ← relations+CLASSIFYRELATION(e1, e2)

Figure 19.5  Finding and classifying the relations among entities in a text.

• Bag-of-words and bigrams in M1 and M2
  American, Airlines, Tim, Wagner, American Airlines, Tim Wagner

• Words or bigrams in particular positions
  M2: -1 spokesman
  M2: +1 said

• Bag of words or bigrams between M1 and M2:
  a, AMR, of, immediately, matched, move, spokesman, the, unit

Named entity features:

• Named-entity types and their concatenation
  (M1: ORG, M2: PER, M1M2: ORG-PER)

• Entity Level of M1 and M2 (from the set NAME, NOMINAL, PRONOUN)
  M1: NAME [it or he would be PRONOUN]
  M2: NAME [the company would be NOMINAL]

• Number of entities between the arguments (in this case 1, for AMR)

Syntactic structure is a useful signal, often represented as the dependency or constituency syntactic path traversed through the tree between the entities.

• Constituent paths between M1 and M2
  NP ↑ NP ↑ S ↑ S ↓ NP

• Dependency-tree paths
  Airlines ← subj matched ← comp said → subj Wagner

Neural supervised relation classifiers  Neural models for relation extraction similarly treat the task as supervised classification. Let’s consider a typical system applied to the TACRED relation extraction dataset and task (Zhang et al., 2017). In TACRED we are given a sentence and two spans within it: a subject, which is a person or organization, and an object, which is any other entity. The task is to assign a relation from the 42 TAC relations, or no relation.

A typical Transformer-encoder algorithm, shown in Fig. 19.6, simply takes a pretrained encoder like BERT and adds a linear layer on top of the sentence representation (for example the BERT [CLS] token), a linear layer that is finetuned as a 1-of-N classifier to assign one of the 43 labels. The input to the BERT encoder is partially de-lexified; the subject and object entities are replaced in the input by their NER tags. This helps keep the system from overfitting to the individual lexical items (Zhang et al., 2017). When using BERT-type Transformers for relation extraction, it helps to use versions of BERT like RoBERTa (Liu et al., 2019) or spanBERT (Joshi et al., 2020) that don’t have two sequences separated by a [SEP] token, but instead form the input from a single long sequence of sentences.

In general, if the test set is similar enough to the training set, and if there is enough hand-labeled data, supervised relation extraction systems can get high ac-
curacies. But labeling a large training set is extremely expensive and supervised models are brittle: they don’t generalize well to different text genres. For this reason, much research in relation extraction has focused on the semi-supervised and unsupervised approaches we turn to next.

### 19.2.3 Semisupervised Relation Extraction via Bootstrapping

Supervised machine learning assumes that we have lots of labeled data. Unfortunately, this is expensive. But suppose we just have a few high-precision seed patterns, like those in Section 19.2.1, or perhaps a few seed tuples. That’s enough to bootstrap a classifier! **Bootstrapping** proceeds by taking the entities in the seed pair, and then finding sentences (on the web, or whatever dataset we are using) that contain both entities. From all such sentences, we extract and generalize the context around the entities to learn new patterns. Fig. 19.7 sketches a basic algorithm.

```plaintext
function BOOTSTRAP(Relation R) returns new relation tuples
    tuples ← Gather a set of seed tuples that have relation R
    iterate
        sentences ← find sentences that contain entities in tuples
        patterns ← generalize the context between and around entities in sentences
        newpairs ← use patterns to identify more tuples
        newpairs ← newpairs with high confidence
        tuples ← tuples + newpairs
    return tuples
```

Suppose, for example, that we need to create a list of airline/hub pairs, and we know only that Ryanair has a hub at Charleroi. We can use this seed fact to discover new patterns by finding other mentions of this relation in our corpus. We search for the terms **Ryanair**, **Charleroi** and **hub** in some proximity. Perhaps we find the following set of sentences:

(19.6) Budget airline Ryanair, which uses Charleroi as a hub, scrapped all weekend flights out of the airport.

(19.7) All flights in and out of Ryanair’s hub at Charleroi airport were grounded on Friday...

(19.8) A spokesman at Charleroi, a main hub for Ryanair, estimated that 8000 passengers had already been affected.
From these results, we can use the context of words between the entity mentions, the words before mention one, the word after mention two, and the named entity types of the two mentions, and perhaps other features, to extract general patterns such as the following:

- / [ORG], which uses [LOC] as a hub /
- / [ORG]’s hub at [LOC] /
- / [LOC], a main hub for [ORG] /

These new patterns can then be used to search for additional tuples.

Bootstrapping systems also assign confidence values to new tuples to avoid semantic drift. In semantic drift, an erroneous pattern leads to the introduction of erroneous tuples, which, in turn, lead to the creation of problematic patterns and the meaning of the extracted relations ‘drifts’. Consider the following example:

(19.9) Sydney has a ferry hub at Circular Quay.

If accepted as a positive example, this expression could lead to the incorrect introduction of the tuple ⟨Sydney, Circular Quay⟩. Patterns based on this tuple could propagate further errors into the database.

Confidence values for patterns are based on balancing two factors: the pattern’s performance with respect to the current set of tuples and the pattern’s productivity in terms of the number of matches it produces in the document collection. More formally, given a document collection \( D \), a current set of tuples \( T \), and a proposed pattern \( p \), we need to track two factors:

- \( \text{hits}(p) \): the set of tuples in \( T \) that \( p \) matches while looking in \( D \)
- \( \text{finds}(p) \): The total set of tuples that \( p \) finds in \( D \)

The following equation balances these considerations (Riloff and Jones, 1999).

\[
Conf_{\text{RlogF}}(p) = \frac{|\text{hits}(p)|}{|\text{finds}(p)|} \log(|\text{finds}(p)|)
\]  

(19.10)

This metric is generally normalized to produce a probability.

We can assess the confidence in a proposed new tuple by combining the evidence supporting it from all the patterns \( P \) that match that tuple in \( D \) (Agichtein and Gravano, 2000). One way to combine such evidence is the noisy-or technique. Assume that a given tuple is supported by a subset of the patterns in \( P \), each with its own confidence assessed as above. In the noisy-or model, we make two basic assumptions. First, that for a proposed tuple to be false, all of its supporting patterns must have been in error, and second, that the sources of their individual failures are all independent. If we loosely treat our confidence measures as probabilities, then the probability of any individual pattern \( p \) failing is \( 1 - Conf(p) \); the probability of all of the supporting patterns for a tuple being wrong is the product of their individual failure probabilities, leaving us with the following equation for our confidence in a new tuple.

\[
Conf(t) = 1 - \prod_{p \in P} (1 - Conf(p))
\]  

(19.11)

Setting conservative confidence thresholds for the acceptance of new patterns and tuples during the bootstrapping process helps prevent the system from drifting away from the targeted relation.
19.2.4 Distant Supervision for Relation Extraction

Although hand-labeling text with relation labels is expensive to produce, there are ways to find indirect sources of training data. The **distant supervision** method (Mintz et al., 2009) combines the advantages of bootstrapping with supervised learning. Instead of just a handful of seeds, distant supervision uses a large database to acquire a huge number of seed examples, creates lots of noisy pattern features from all these examples and then combines them in a supervised classifier.

For example suppose we are trying to learn the *place-of-birth* relationship between people and their birth cities. In the seed-based approach, we might have only 5 examples to start with. But Wikipedia-based databases like DBPedia or Freebase have tens of thousands of examples of many relations; including over 100,000 examples of *place-of-birth*, *(<Edwin Hubble, Marshfield>, <Albert Einstein, Ulm>, etc...)*. The next step is to run named entity taggers on large amounts of text—Mintz et al. (2009) used 800,000 articles from Wikipedia—and extract all sentences that have two named entities that match the tuple, like the following:

...Hubble was born in Marshfield...
...Einstein, born (1879), Ulm...
...Hubble’s birthplace in Marshfield...

Training instances can now be extracted from this data, one training instance for each identical tuple \(<\text{relation}, \text{entity1}, \text{entity2}>\). Thus there will be one training instance for each of:

\(<\text{born-in, Edwin Hubble, Marshfield}>\>
\(<\text{born-in, Albert Einstein, Ulm}>\>
\(<\text{born-year, Albert Einstein, 1879}>\>

and so on.

We can then apply feature-based or neural classification. For feature-based classification, we can use standard supervised relation extraction features like the named entity labels of the two mentions, the words and dependency paths in between the mentions, and neighboring words. Each tuple will have features collected from many training instances; the feature vector for a single training instance like *(<born-in, Albert Einstein, Ulm>)* will have lexical and syntactic features from many different sentences that mention Einstein and Ulm.

Because distant supervision has very large training sets, it is also able to use very rich features that are conjunctions of these individual features. So we will extract thousands of patterns that conjoin the entity types with the intervening words or dependency paths like these:

PER was born in LOC
PER, born (XXXX), LOC
PER’s birthplace in LOC

To return to our running example, for this sentence:

(19.12) **American Airlines**, a unit of AMR, immediately matched the move, spokesman **Tim Wagner** said

we would learn rich conjunction features like this one:

\(M1 \land ORG \& M2 \land PER \& \text{nextword=“said”} \& \text{path= NP} \uparrow \text{NP} \uparrow \text{S} \uparrow \text{S} \downarrow \text{NP}\)

The result is a supervised classifier that has a huge rich set of features to use in detecting relations. Since not every test sentence will have one of the training...
relations, the classifier will also need to be able to label an example as no-relation. This label is trained by randomly selecting entity pairs that do not appear in any Freebase relation, extracting features for them, and building a feature vector for each such tuple. The final algorithm is sketched in Fig. 19.8.

```
function Distant Supervision(Database D, Text T) returns relation classifier C

foreach relation R
  foreach tuple (e1,e2) of entities with relation R in D
    sentences ← Sentences in T that contain e1 and e2
    f ← Frequent features in sentences
    observations ← observations + new training tuple (e1, e2, f, R)
    C ← Train supervised classifier on observations
  return C
```

Figure 19.8 The distant supervision algorithm for relation extraction. A neural classifier would skip the feature set f.

Distant supervision shares advantages with each of the methods we’ve examined. Like supervised classification, distant supervision uses a classifier with lots of features, and supervised by detailed hand-created knowledge. Like pattern-based classifiers, it can make use of high-precision evidence for the relation between entities. Indeed, distance supervision systems learn patterns just like the hand-built patterns of early relation extractors. For example the is-a or hypernym extraction system of Snow et al. (2005) used hypernym/hyponym NP pairs from WordNet as distant supervision, and then learned new patterns from large amounts of text. Their system induced exactly the original 5 template patterns of Hearst (1992a), but also 70,000 additional patterns including these four:

- NP_H like NP  Many hormones like leptin...
- NP_H called NP  ...using a markup language called XHTML
- NP is a NP_H  Ruby is a programming language...
- NP, a NP_H  IBM, a company with a long...

This ability to use a large number of features simultaneously means that, unlike the iterative expansion of patterns in seed-based systems, there’s no semantic drift. Like unsupervised classification, it doesn’t use a labeled training corpus of texts, so it isn’t sensitive to genre issues in the training corpus, and relies on very large amounts of unlabeled data. Distant supervision also has the advantage that it can create training tuples to be used with neural classifiers, where features are not required.

The main problem with distant supervision is that it tends to produce low-precision results, and so current research focuses on ways to improve precision. Furthermore, distant supervision can only help in extracting relations for which a large enough database already exists. To extract new relations without datasets, or relations for new domains, purely unsupervised methods must be used.

### 19.2.5 Unsupervised Relation Extraction

The goal of unsupervised relation extraction is to extract relations from the web when we have no labeled training data, and not even any list of relations. This task is often called open information extraction or Open IE. In Open IE, the relations
are simply strings of words (usually beginning with a verb).
For example, the ReVerb system (Fader et al., 2011) extracts a relation from a sentence $s$ in 4 steps:

1. Run a part-of-speech tagger and entity chunker over $s$
2. For each verb in $s$, find the longest sequence of words $w$ that start with a verb and satisfy syntactic and lexical constraints, merging adjacent matches.
3. For each phrase $w$, find the nearest noun phrase $x$ to the left which is not a relative pronoun, wh-word or existential “there”. Find the nearest noun phrase $y$ to the right.
4. Assign confidence $c$ to the relation $r = (x, w, y)$ using a confidence classifier and return it.

A relation is only accepted if it meets syntactic and lexical constraints. The syntactic constraints ensure that it is a verb-initial sequence that might also include nouns (relations that begin with light verbs like make, have, or do often express the core of the relation with a noun, like have a hub in):

$$V \mid VP \mid VW*P$$
$$V = \text{verb particle? adv?}$$
$$W = \text{noun | adj | adv | pron | det}$$
$$P = \text{prep | particle | infinitive “to”}$$

The lexical constraints are based on a dictionary $D$ that is used to prune very rare, long relation strings. The intuition is to eliminate candidate relations that don’t occur with sufficient number of distinct argument types and so are likely to be bad examples. The system first runs the above relation extraction algorithm offline on 500 million web sentences and extracts a list of all the relations that occur after normalizing them (removing inflection, auxiliary verbs, adjectives, and adverbs). Each relation $r$ is added to the dictionary if it occurs with at least 20 different arguments. Fader et al. (2011) used a dictionary of 1.7 million normalized relations.

Finally, a confidence value is computed for each relation using a logistic regression classifier. The classifier is trained by taking 1000 random web sentences, running the extractor, and hand labeling each extracted relation as correct or incorrect. A confidence classifier is then trained on this hand-labeled data, using features of the relation and the surrounding words. Fig. 19.9 shows some sample features used in the classification.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(x, r, y)$</td>
<td>covers all words in $s$</td>
</tr>
<tr>
<td>the last preposition in $r$ is for</td>
<td></td>
</tr>
<tr>
<td>the last preposition in $r$ is on</td>
<td></td>
</tr>
<tr>
<td>$\text{len}(s) \leq 10$</td>
<td></td>
</tr>
<tr>
<td>there is a coordinating conjunction to the left of $r$ in $s$</td>
<td></td>
</tr>
<tr>
<td>$r$ matches a lone $V$ in the syntactic constraints</td>
<td></td>
</tr>
<tr>
<td>there is preposition to the left of $x$ in $s$</td>
<td></td>
</tr>
<tr>
<td>there is an NP to the right of $y$ in $s$</td>
<td></td>
</tr>
</tbody>
</table>

Figure 19.9 Features for the classifier that assigns confidence to relations extracted by the Open Information Extraction system REVERB (Fader et al., 2011).

For example the following sentence:

(19.13) United has a hub in Chicago, which is the headquarters of United Continental Holdings.
has the relation phrases has a hub in and is the headquarters of (it also has has and is, but longer phrases are preferred). Step 3 finds United to the left and Chicago to the right of has a hub in, and skips over which to find Chicago to the left of is the headquarters of. The final output is:

r1: <United, has a hub in, Chicago>
r2: <Chicago, is the headquarters of, United Continental Holdings>

The great advantage of unsupervised relation extraction is its ability to handle a huge number of relations without having to specify them in advance. The disadvantage is the need to map all the strings into some canonical form for adding to databases or knowledge graphs. Current methods focus heavily on relations expressed with verbs, and so will miss many relations that are expressed nominally.

### 19.2.6 Evaluation of Relation Extraction

Supervised relation extraction systems are evaluated by using test sets with human-annotated, gold-standard relations and computing precision, recall, and F-measure. Labeled precision and recall require the system to classify the relation correctly, whereas unlabeled methods simply measure a system’s ability to detect entities that are related.

Semi-supervised and unsupervised methods are much more difficult to evaluate, since they extract totally new relations from the web or a large text. Because these methods use very large amounts of text, it is generally not possible to run them solely on a small labeled test set, and as a result it’s not possible to pre-annotate a gold set of correct instances of relations.

For these methods it’s possible to approximate (only) precision by drawing a random sample of relations from the output, and having a human check the accuracy of each of these relations. Usually this approach focuses on the tuples to be extracted from a body of text rather than on the relation mentions; systems need not detect every mention of a relation to be scored correctly. Instead, the evaluation is based on the set of tuples occupying the database when the system is finished. That is, we want to know if the system can discover that Ryanair has a hub at Charleroi; we don’t really care how many times it discovers it. The estimated precision $\hat{P}$ is then

$$\hat{P} = \frac{\# \text{ of correctly extracted relation tuples in the sample}}{\text{total # of extracted relation tuples in the sample}}.$$  \hspace{1cm} (19.14)

Another approach that gives us a little bit of information about recall is to compute precision at different levels of recall. Assuming that our system is able to rank the relations it produces (by probability, or confidence) we can separately compute precision for the top 1000 new relations, the top 10,000 new relations, the top 100,000, and so on. In each case we take a random sample of that set. This will show us how the precision curve behaves as we extract more and more tuples. But there is no way to directly evaluate recall.

### 19.3 Extracting Events

The task of event extraction is to identify mentions of events in texts. For the purposes of this task, an event mention is any expression denoting an event or state that can be assigned to a particular point, or interval, in time. The following markup of the sample text on page 415 shows all the events in this text.
[EVENT Citing] high fuel prices, United Airlines [EVENT said] Friday it has [EVENT increased] fares by $6 per round trip on flights to some cities also served by lower-cost carriers. American Airlines, a unit of AMR Corp., immediately [EVENT matched] [EVENT the move], spokesman Tim Wagner [EVENT said]. United, a unit of UAL Corp., [EVENT said] [EVENT the increase] took effect Thursday and [EVENT applies] to most routes where it [EVENT competes] against discount carriers, such as Chicago to Dallas and Denver to San Francisco.

In English, most event mentions correspond to verbs, and most verbs introduce events. However, as we can see from our example, this is not always the case. Events can be introduced by noun phrases, as in the move and the increase, and some verbs fail to introduce events, as in the phrasal verb took effect, which refers to when the event began rather than to the event itself. Similarly, light verbs such as make, take, and have often fail to denote events. A light verb is a verb that has very little meaning itself, and the associated event is instead expressed by its direct object noun. In light verb examples like took a flight, it’s the word flight that defines the event; these light verbs just provide a syntactic structure for the noun’s arguments.

Various versions of the event extraction task exist, depending on the goal. For example in the TempEval shared tasks (Verhagen et al. 2009) the goal is to extract events and aspects like their aspectual and temporal properties. Events are to be classified as actions, states, reporting events (say, report, tell, explain), perception events, and so on. The aspect, tense, and modality of each event also needs to be extracted. Thus for example the various said events in the sample text would be annotated as (class=REPORTING, tense=PAST, aspect=PERFECTIVE).

Event extraction is generally modeled via supervised learning, detecting events via IOB sequence models and assigning event classes and attributes with multi-class classifiers. The input can be neural models starting from encoders; or classic feature-based models using features like those in Fig. 19.10.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Character affixes</td>
<td>Character-level prefixes and suffixes of target word</td>
</tr>
<tr>
<td>Nominalization suffix</td>
<td>Character-level suffixes for nominalizations (e.g., -tion)</td>
</tr>
<tr>
<td>Part of speech</td>
<td>Part of speech of the target word</td>
</tr>
<tr>
<td>Light verb</td>
<td>Binary feature indicating that the target is governed by a light verb</td>
</tr>
<tr>
<td>Subject syntactic category</td>
<td>Syntactic category of the subject of the sentence</td>
</tr>
<tr>
<td>Morphological stem</td>
<td>Stemmed version of the target word</td>
</tr>
<tr>
<td>Verb root</td>
<td>Root form of the verb basis for a nominalization</td>
</tr>
<tr>
<td>WordNet hypernyms</td>
<td>Hypernym set for the target</td>
</tr>
</tbody>
</table>

**Figure 19.10** Features commonly used in classic feature-based approaches to event detection.

### 19.4 Representing Time

[**temporal logic**] Let’s begin by introducing the basics of temporal logic and how human languages convey temporal information. The most straightforward theory of time holds that it flows inexorably forward and that events are associated with either points or intervals in time, as on a timeline. We can order distinct events by situating them on the timeline; one event precedes another if the flow of time leads from the first event
to the second. Accompanying these notions in most theories is the idea of the current moment in time. Combining this notion with the idea of a temporal ordering relationship yields the familiar notions of past, present, and future.

Various kinds of temporal representation systems can be used to talk about temporal ordering relationship. One of the most commonly used in computational modeling is the interval algebra of Allen (1984). Allen models all events and time expressions as intervals there is no representation for points (although intervals can be very short). In order to deal with intervals without points, he identifies 13 primitive relations that can hold between these temporal intervals. Fig. 19.11 shows these 13 Allen relations.

Allen relations

---

19.4.1 Reichenbach’s reference point

The relation between simple verb tenses and points in time is by no means straightforward. The present tense can be used to refer to a future event, as in this example: (19.15) Ok, we fly from San Francisco to Boston at 10.

Or consider the following examples:

(19.16) Flight 1902 arrived late.

(19.17) Flight 1902 had arrived late.

Although both refer to events in the past, representing them in the same way seems wrong. The second example seems to have another unnamed event lurking in the background (e.g., Flight 1902 had already arrived late when something else happened).
To account for this phenomena, Reichenbach (1947) introduced the notion of a reference point. In our simple temporal scheme, the current moment in time is equated with the time of the utterance and is used as a reference point for when the event occurred (before, at, or after). In Reichenbach's approach, the notion of the reference point is separated from the utterance time and the event time. The following examples illustrate the basics of this approach:

(19.18) When Mary’s flight departed, I ate lunch.
(19.19) When Mary’s flight departed, I had eaten lunch.

In both of these examples, the eating event has happened in the past, that is, prior to the utterance. However, the verb tense in the first example indicates that the eating event began when the flight departed, while the second example indicates that the eating was accomplished prior to the flight’s departure. Therefore, in Reichenbach’s terms the departure event specifies the reference point. These facts can be accommodated by additional constraints relating the eating and departure events. In the first example, the reference point precedes the eating event, and in the second example, the eating precedes the reference point. Figure 19.12 illustrates Reichenbach’s approach with the primary English tenses. Exercise 19.4 asks you to represent these examples in FOL.

Languages have many other ways to convey temporal information besides tense. Most useful for our purposes will be temporal expressions like in the morning or 6:45 or afterwards.

(19.20) I’d like to go at 6:45 in the morning.
(19.21) Somewhere around noon, please.
(19.22) I want to take the train back afterwards.

Incidentally, temporal expressions display a fascinating metaphorical conceptual organization. Temporal expressions in English are frequently expressed in spatial terms, as is illustrated by the various uses of at, in, somewhere, and near in these examples (Lakoff and Johnson 1980, Jackendoff 1983). Metaphorical organizations such as these, in which one domain is systematically expressed in terms of another, are very common in languages of the world.
19.5 Representing Aspect

A related notion to time is **aspect**, which is what we call the way events can be categorized by their internal temporal structure or temporal contour. By this we mean questions like whether events are ongoing or have ended, or whether they are conceptualized as happening at a point in time or over some interval. Such notions of temporal contour have been used to divide event expressions into classes since Aristotle, although the set of four classes we’ll introduce here is due to Vendler (1967) (you may also see the German term *aktionsart* used to refer to these classes).

The most basic aspectual distinction is between **events** (which involve change) and **states** (which do not involve change). **Stative expressions** represent the notion of an event participant being in a **state**, or having a particular property, at a given point in time. Stative expressions capture aspects of the world at a single point in time, and conceptualize the participant as unchanging and continuous. Consider the following ATIS examples.

(19.23) I like express trains.
(19.24) I need the cheapest fare.
(19.25) I want to go first class.

In examples like these, the event participant denoted by the subject can be seen as experiencing something at a specific point in time, and don’t involve any kind of internal change over time (the liking or needing is conceptualized as continuous and unchanging).

Non-states (which we’ll refer to as **events**) are divided into subclasses; we’ll introduce three here. **Activity expressions** describe events undertaken by a participant that occur over a span of time (rather than being conceptualized as a single point in time like stative expressions), and have no particular end point. Of course in practice all things end, but the meaning of the expression doesn’t represent this fact. Consider the following examples:

(19.26) She drove a Mazda.
(19.27) I live in Brooklyn.

These examples both specify that the subject is engaged in, or has engaged in, the activity specified by the verb for some period of time, but doesn’t specify when the driving or living might have stopped.

Two more classes of expressions, **achievement expressions** and **accomplishment expressions**, describe events that take place over time, but also conceptualize the event as having a particular kind of endpoint or goal. The Greek word *telos* means ‘end’ or ‘goal’ and so the events described by these kinds of expressions are often called **telic** events.

**Accomplishment expressions** describe events that have a natural end point and result in a particular state. Consider the following examples:

(19.28) He booked me a reservation.
(19.29) The 7:00 train got me to New York City.

In these examples, an event is seen as occurring over some period of time that ends when the intended state is accomplished (i.e., the state of me having a reservation, or me being in New York City).

The final aspectual class, **achievement expressions**, is only subtly different than accomplishments. Consider the following:
Like accomplishment expressions, achievement expressions result in a state. But unlike accomplishments, achievement events are ‘punctual’: they are thought of as happening in an instant and the verb doesn’t conceptualize the process or activity leading up the state. Thus the events in these examples may in fact have been preceded by extended searching or traveling events, but the verb doesn’t conceptualize these preceding processes, but rather conceptualizes the events corresponding to finding and reaching as points, not intervals.

In summary, a standard way of categorizing event expressions by their temporal contours is via these four general classes:

**Stative:** I know my departure gate.

**Activity:** John is flying.

**Accomplishment:** Sally booked her flight.

**Achievement:** She found her gate.

Before moving on, note that event expressions can easily be shifted from one class to another. Consider the following examples:

(19.32) I flew.
(19.33) I flew to New York.

The first example is a simple activity; it has no natural end point. The second example is clearly an accomplishment event since it has an end point, and results in a particular state. Clearly, the classification of an event is not solely governed by the verb, but by the semantics of the entire expression in context.

## 19.6 Temporally Annotated Datasets: TimeBank

The **TimeBank** corpus consists of American English text annotated with temporal information (Pustejovsky et al., 2003). The annotations use TimeML (Saurí et al., 2006), a markup language for time based on Allen’s interval algebra discussed above (Allen, 1984). There are three types of TimeML objects: an EVENT represent events and states, a TIME represents time expressions like dates, and a LINK represents various relationships between events and times (event-event, event-time, and time-time). The links include temporal links (TLINK) for the 13 Allen relations, aspectual links (ALINK) for aspectual relationships between events and subevents, and SLINKS which mark factuality.

Consider the following sample sentence and its corresponding markup shown in Fig. 19.13, selected from one of the TimeBank documents.

(19.34) Delta Air Lines earnings soared 33% to a record in the fiscal first quarter, bucking the industry trend toward declining profits.

This text has three events and two temporal expressions (including the creation time of the article, which serves as the document time), and four temporal links that capture the using the Allen relations:

- Soaring\(_{e1}\) is **included** in the fiscal first quarter\(_{t58}\)
- Soaring\(_{e1}\) is **before** 1989-10-26\(_{t57}\)
- Soaring\(_{e1}\) is **simultaneous** with the bucking\(_{e3}\)
Delta Air Lines earnings soared 33% to a record in the fiscal first quarter, bucking the industry trend toward declining profits.

Figure 19.13 Example from the TimeBank corpus.

- Declining_e4 includes soaring_e1

We can also visualize the links as a graph. The TimeBank snippet in Eq. 19.35 would be represented with a graph like Fig. 19.14.

$\text{(19.35)}$ Pacific First Financial Corp. shareholders approved its acquisition by Royal Trustco Ltd. of Toronto for $27 a share, or $212 million. The thrift holding company said it expects to obtain regulatory approval and complete the transaction by year-end.

Figure 19.14 A graph of the text in Eq. 19.35, adapted from (Ocal et al., 2022). TLINKS are shown in blue, ALINKS in red, and SLINKS in green.

19.7 Automatic Temporal Analysis

Here we introduce the three common steps used in analyzing time in text:

1. Extracting temporal expressions
2. Normalizing these expressions, by converting them to a standard format.
3. Linking events to times and extracting time graphs and timelines

19.7.1 Extracting Temporal Expressions

Temporal expressions are phrases that refer to absolute points in time, relative times, durations, and sets of these. Absolute temporal expressions are those that can be mapped directly to calendar dates, times of day, or both. Relative temporal expressions map to particular times through some other reference point (as in a week from last Tuesday). Finally, durations denote spans of time at varying levels of granularity (seconds, minutes, days, weeks, centuries, etc.). Figure 19.15 lists some sample temporal expressions in each of these categories.

Temporal expressions are grammatical constructions that often have temporal lexical triggers as their heads, making them easy to find. Lexical triggers might be nouns, proper nouns, adjectives, and adverbs; full temporal expressions consist
of their phrasal projections: noun phrases, adjective phrases, and adverbial phrases (Figure 19.16).

<table>
<thead>
<tr>
<th>Category</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Noun</td>
<td>morning, noon, night, winter, dusk, dawn</td>
</tr>
<tr>
<td>Proper Noun</td>
<td>January, Monday, Ides, Easter, Rosh Hashana, Ramadan, Tet</td>
</tr>
<tr>
<td>Adjective</td>
<td>recent, past, annual, former</td>
</tr>
<tr>
<td>Adverb</td>
<td>hourly, daily, monthly, yearly</td>
</tr>
</tbody>
</table>

The task is to detect temporal expressions in running text, like this examples, shown with TIMEX3 tags (Pustejovsky et al. 2005, Ferro et al. 2005).

A fare increase initiated `<TIMEX3>last week</TIMEX3>` by UAL Corp’s United Airlines was matched by competitors over `<TIMEX3>the weekend</TIMEX3>`, marking the second successful fare increase in `<TIMEX3>two weeks</TIMEX3>`.

**Rule-based** approaches use cascades of regular expressions to recognize larger and larger chunks from previous stages, based on patterns containing parts of speech, trigger words (e.g., *February*) or classes (e.g., *MONTH*) (Chang and Manning, 2012; Strötgen and Gertz, 2013; Chambers, 2013). Here’s a rule from SUTime (Chang and Manning, 2012) for detecting expressions like *3 years old*:

```
/\(\d+\)[-\s]+(\$TEUnits)(s)?([-\s]+old)?\/
```

**Sequence-labeling** approaches use the standard IOB scheme, marking words that are either (I)nside, (O)utside or at the (B)eginning of a temporal expression:

_A fare increase initiated last week by UAL Corp’s..._

```
O O O O B I O O O
```

A statistical sequence labeler is trained, using either embeddings or a fine-tuned encoder, or classic features extracted from the token and context including words, lexical triggers, and POS.

Temporal expression recognizers are evaluated with the usual recall, precision, and *F*-measures. A major difficulty for all of these very lexicalized approaches is avoiding expressions that trigger false positives:

(19.36) _1984 tells the story of Winston Smith..._

(19.37) _...U2’s classic Sunday Bloody Sunday_

### 19.7.2 Temporal Normalization

**Temporal normalization** is the task of mapping a temporal expression to a point in time or to a duration. Points in time correspond to calendar dates, to times of day, or both. Durations primarily consist of lengths of time. Normalized times are represented via the ISO 8601 standard for encoding temporal values (ISO8601, 2004). Fig. 19.17 reproduces our earlier example with these value attributes.
The dateline, or document date, for this text was July 2, 2007. The ISO representation for this kind of expression is YYYY-MM-DD, or in this case, 2007-07-02. The encodings for the temporal expressions in our sample text all follow from this date, and are shown here as values for the VALUE attribute.

The first temporal expression in the text proper refers to a particular week of the year. In the ISO standard, weeks are numbered from 01 to 53, with the first week of the year being the one that has the first Thursday of the year. These weeks are represented with the template YYYY-Wnn. The ISO week for our document date is week 27; thus the value for last week is represented as “2007-W26”.

The next temporal expression is the weekend. ISO weeks begin on Monday; thus, weekends occur at the end of a week and are fully contained within a single week. Weekends are treated as durations, so the value of the VALUE attribute has to be a length. Durations are represented according to the pattern Pnx, where n is an integer denoting the length and x represents the unit, as in P3Y for three years or P2D for two days. In this example, one weekend is captured as P1WE. In this case, there is also sufficient information to anchor this particular weekend as part of a particular week. Such information is encoded in the ANCHOR TIME ID attribute.

Finally, the phrase two weeks also denotes a duration captured as P2W. Figure 19.18 give some more examples, but there is a lot more to the various temporal annotation standards; consult ISO8601 (2004), Ferro et al. (2005), and Pustejovsky et al. (2005) for more details.

Most current approaches to temporal normalization are rule-based (Chang and Manning 2012, Strögen and Gertz 2013). Patterns that match temporal expressions are associated with semantic analysis procedures. For example, the pattern above for recognizing phrases like 3 years old can be associated with the predicate Duration that takes two arguments, the length and the unit of time:

pattern: /\(\d+\)[-\s]\($\text{TEUnits}\)(s)?([-\s]old)?/  
result: Duration($1, $2)

The task is difficult because fully qualified temporal expressions are fairly rare in real texts. Most temporal expressions in news articles are incomplete and are only implicitly anchored, often with respect to the dateline of the article, which we refer to as the document’s temporal anchor. The values of temporal expressions such as today, yesterday, or tomorrow can all be computed with respect to this temporal anchor.
anchor. The semantic procedure for today simply assigns the anchor, and the attachments for tomorrow and yesterday add a day and subtract a day from the anchor, respectively. Of course, given the cyclic nature of our representations for months, weeks, days, and times of day, our temporal arithmetic procedures must use modulo arithmetic appropriate to the time unit being used.

Unfortunately, even simple expressions such as the weekend or Wednesday introduce a fair amount of complexity. In our current example, the weekend clearly refers to the weekend of the week that immediately precedes the document date. But this won’t always be the case, as is illustrated in the following example.

(19.38) Random security checks that began yesterday at Sky Harbor will continue at least through the weekend.

In this case, the expression the weekend refers to the weekend of the week that the anchoring date is part of (i.e., the coming weekend). The information that signals this meaning comes from the tense of continue, the verb governing the weekend.

Relative temporal expressions are handled with temporal arithmetic similar to that used for today and yesterday. The document date indicates that our example article is ISO week 27, so the expression last week normalizes to the current week minus 1. To resolve ambiguous next and last expressions we consider the distance from the anchoring date to the nearest unit. Next Friday can refer either to the immediately next Friday or to the Friday following that, but the closer the document date is to a Friday, the more likely it is that the phrase will skip the nearest one. Such ambiguities are handled by encoding language and domain-specific heuristics into the temporal attachments.

19.7.3 Temporal Ordering of Events

The goal of temporal analysis, is to link times to events and then fit all these events into a complete timeline. This ambitious task is the subject of considerable current research but solving it with a high level of accuracy is beyond the capabilities of current systems. A somewhat simpler, but still useful, task is to impose a partial ordering on the events and temporal expressions mentioned in a text. Such an ordering can provide many of the same benefits as a true timeline. An example of such a partial ordering is the determination that the fare increase by American Airlines came after the fare increase by United in our sample text. Determining such an ordering can be viewed as a binary relation detection and classification task.

Even this partial ordering task assumes that in addition to the detecting and normalizing time expressions steps described above, we have already detected all the events in the text. Indeed, many temporal expressions are anchored to events mentioned in a text and not directly to other temporal expressions. Consider the following example:

(19.39) One week after the storm, JetBlue issued its customer bill of rights.

To determine when JetBlue issued its customer bill of rights we need to determine the time of the storm event, and then we need to modify that time by the temporal expression one week after.

Thus once the events and times have been detected, our goal next is to assert links between all the times and events: i.e. creating event-event, event-time, time-time, DCT-event, and DCT-time TimeML TINKS. This can be done by training time relation classifiers to predict the correct T:INK between each pair of times/events, supervised by the gold labels in the TimeBank corpus with features like words/embeddings, parse paths, tense and aspect. The sieve-based architecture using precision-
ranked sets of classifiers, which we’ll introduce in Chapter 26, is also commonly used.

Systems that perform all 4 tasks (time extraction creation and normalization, event extraction, and time/event linking) include TARSQI (Verhagen et al., 2005) CLEARTK (Bethard, 2013), CAEVO (Chambers et al., 2014), and CATENA (Mirza and Tonelli, 2016).

19.8 Template Filling

Many texts contain reports of events, and possibly sequences of events, that often correspond to fairly common, stereotypical situations in the world. These abstract situations or stories, related to what have been called scripts (Schank and Abelson, 1977), consist of prototypical sequences of sub-events, participants, and their roles. The strong expectations provided by these scripts can facilitate the proper classification of entities, the assignment of entities into roles and relations, and most critically, the drawing of inferences that fill in things that have been left unsaid. In their simplest form, such scripts can be represented as templates consisting of fixed sets of slots that take as values slot-fillers belonging to particular classes. The task of template filling is to find documents that invoke particular scripts and then fill the slots in the associated templates with fillers extracted from the text. These slot-fillers may consist of text segments extracted directly from the text, or they may consist of concepts that have been inferred from text elements through some additional processing.

A filled template from our original airline story might look like the following.

<table>
<thead>
<tr>
<th>FARE-RAISE ATTEMPT:</th>
<th>LEAD AIRLINE: UNITED AIRLINES</th>
</tr>
</thead>
<tbody>
<tr>
<td>AMOUNT:</td>
<td>$6</td>
</tr>
<tr>
<td>EFFECTIVE DATE:</td>
<td>2006-10-26</td>
</tr>
<tr>
<td>FOLLOWER:</td>
<td>AMERICAN AIRLINES</td>
</tr>
</tbody>
</table>

This template has four slots (LEAD AIRLINE, AMOUNT, EFFECTIVE DATE, FOLLOWER). The next section describes a standard sequence-labeling approach to filling slots. Section 19.8.2 then describes an older system based on the use of cascades of finite-state transducers and designed to address a more complex template-filling task that current learning-based systems don’t yet address.

19.8.1 Machine Learning Approaches to Template Filling

In the standard paradigm for template filling, we are given training documents with text spans annotated with predefined templates and their slot fillers. Our goal is to create one template for each event in the input, filling in the slots with text spans.

The task is generally modeled by training two separate supervised systems. The first system decides whether the template is present in a particular sentence. This task is called template recognition or sometimes, in a perhaps confusing bit of terminology, event recognition. Template recognition can be treated as a text classification task, with features extracted from every sequence of words that was labeled in training documents as filling any slot from the template being detected. The usual set of features can be used: tokens, embeddings, word shapes, part-of-speech tags, syntactic chunk tags, and named entity tags.
The second system has the job of **role-filler extraction**. A separate classifier is trained to detect each role (LEAD-AIRLINE, AMOUNT, and so on). This can be a binary classifier that is run on every noun-phrase in the parsed input sentence, or a sequence model run over sequences of words. Each role classifier is trained on the labeled data in the training set. Again, the usual set of features can be used, but now trained only on an individual noun phrase or the fillers of a single slot.

Multiple non-identical text segments might be labeled with the same slot label. For example in our sample text, the strings *United* or *United Airlines* might be labeled as the LEAD AIRLINE. These are not incompatible choices and the coreference resolution techniques introduced in Chapter 26 can provide a path to a solution.

A variety of annotated collections have been used to evaluate this style of approach to template filling, including sets of job announcements, conference calls for papers, restaurant guides, and biological texts. A key open question is extracting templates in cases where there is no training data or even predefined templates, by inducing templates as sets of linked events (Chambers and Jurafsky, 2011).

### 19.8.2 Earlier Finite-State Template-Filling Systems

The templates above are relatively simple. But consider the task of producing a template that contained all the information in a text like this one (Grishman and Sundheim, 1995):

Bridgestone Sports Co. said Friday it has set up a joint venture in Taiwan with a local concern and a Japanese trading house to produce golf clubs to be shipped to Japan. The joint venture, Bridgestone Sports Taiwan Co., capitalized at 20 million new Taiwan dollars, will start production in January 1990 with production of 20,000 iron and “metal wood” clubs a month.

The MUC-5 ‘joint venture’ task (the *Message Understanding Conferences* were a series of U.S. government-organized information-extraction evaluations) was to produce hierarchically linked templates describing joint ventures. Figure 19.19 shows a structure produced by the FASTUS system (Hobbs et al., 1997). Note how the filler of the **ACTIVITY** slot of the TIE-UP template is itself a template with slots.

<table>
<thead>
<tr>
<th>Tie-up-1</th>
<th>Activity-1</th>
</tr>
</thead>
<tbody>
<tr>
<td>RELATIONSHIP</td>
<td>tie-up</td>
</tr>
<tr>
<td>ENTITIES</td>
<td>Bridgestone Sports Co.</td>
</tr>
<tr>
<td></td>
<td>a local concern</td>
</tr>
<tr>
<td></td>
<td>a Japanese trading house</td>
</tr>
<tr>
<td>JOINT VENTURE</td>
<td>Bridgestone Sports Taiwan Co.</td>
</tr>
<tr>
<td>ACTIVITY</td>
<td>Activity-1</td>
</tr>
<tr>
<td>AMOUNT</td>
<td>NTS$20000000</td>
</tr>
</tbody>
</table>

**Figure 19.19** The templates produced by FASTUS given the input text on page 437.

Early systems for dealing with these complex templates were based on cascades of transducers based on handwritten rules, as sketched in Fig. 19.20.

The first four stages use handwritten regular expression and grammar rules to do basic tokenization, chunking, and parsing. Stage 5 then recognizes entities and events with a recognizer based on finite-state transducers (FSTs), and inserts the recognized objects into the appropriate slots in templates. This FST recognizer is based on hand-built regular expressions like the following (NG indicates Noun-Group and VG Verb-Group), which matches the first sentence of the news story above.
Figure 19.20 Levels of processing in FASTUS (Hobbs et al., 1997). Each level extracts a specific type of information which is then passed on to the next higher level.

NG(Company/ies) VG(Set-up) NG(Joint-Venture) with NG(Company/ies)
VG(Produce) NG(Product)

The result of processing these two sentences is the five draft templates (Fig. 19.21) that must then be merged into the single hierarchical structure shown in Fig. 19.19. The merging algorithm, after performing coreference resolution, merges two activities that are likely to be describing the same events.

<table>
<thead>
<tr>
<th>No.</th>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Tokens</td>
<td>Tokenize input stream of characters</td>
</tr>
<tr>
<td>2</td>
<td>Complex Words</td>
<td>Multiword phrases, numbers, and proper names.</td>
</tr>
<tr>
<td>3</td>
<td>Basic phrases</td>
<td>Segment sentences into noun and verb groups</td>
</tr>
<tr>
<td>4</td>
<td>Complex phrases</td>
<td>Identify complex noun groups and verb groups</td>
</tr>
<tr>
<td>5</td>
<td>Semantic Patterns</td>
<td>Identify entities and events, insert into templates.</td>
</tr>
<tr>
<td>6</td>
<td>Merging</td>
<td>Merge references to the same entity or event</td>
</tr>
</tbody>
</table>

Figure 19.21 The five partial templates produced by stage 5 of FASTUS. These templates are merged in stage 6 to produce the final template shown in Fig. 19.19 on page 437.

19.9 Summary

This chapter has explored techniques for extracting limited forms of semantic content from texts.

- **Relations among entities** can be extracted by pattern-based approaches, supervised learning methods when annotated training data is available, lightly supervised bootstrapping methods when small numbers of seed tuples or seed patterns are available, distant supervision when a database of relations is available, and unsupervised or Open IE methods.
- Reasoning about time can be facilitated by detection and normalization of temporal expressions.
- **Events** can be ordered in time using sequence models and classifiers trained on temporally- and event-labeled data like the TimeBank corpus.
• **Template-filling** applications can recognize stereotypical situations in texts and assign elements from the text to roles represented as **fixed sets of slots**.

### Bibliographical and Historical Notes

The earliest work on information extraction addressed the template-filling task in the context of the Frump system (DeJong, 1982). Later work was stimulated by the U.S. government-sponsored MUC conferences (Sundheim 1991, Sundheim 1992, Sundheim 1993, Sundheim 1995). Early MUC systems like **CIRCUS** (Lehnert et al., 1991) and **SCISOR** (Jacobs and Rau, 1990) were quite influential and inspired later systems like **FASTUS** (Hobbs et al., 1997). Chinchor et al. (1993) describe the MUC evaluation techniques.

Due to the difficulty of porting systems from one domain to another, attention shifted to machine learning approaches. Early supervised learning approaches to IE (Cardie 1993, Cardie 1994, Riloff 1993, Soderland et al. 1995, Huffman 1996) focused on automating the knowledge acquisition process, mainly for finite-state rule-based systems. Their success, and the earlier success of HMM-based speech recognition, led to the use of sequence labeling (HMMs: Bikel et al. 1997; MEMMs McCallum et al. 2000; CRFs: Lafferty et al. 2001), and a wide exploration of features (Zhou et al., 2005). Neural approaches followed from the pioneering results of Collobert et al. (2011), who applied a CRF on top of a convolutional net.

Progress in this area continues to be stimulated by formal evaluations with shared benchmark datasets, including the Automatic Content Extraction (ACE) evaluations of 2000-2007 on named entity recognition, relation extraction, and temporal expressions\(^1\), the **KBP** (Knowledge Base Population) evaluations (Ji et al. 2010, Surdeanu 2013) of relation extraction tasks like **slot filling** (extracting attributes (‘slots’) like age, birthplace, and spouse for a given entity) and a series of SemEval workshops (Hendrickx et al., 2009).

Semisupervised relation extraction was first proposed by Hearst (1992b), and extended by systems like AutoSlog-TS (Riloff, 1996), DIPRE (Brin, 1998), SNOWBALL (Agichtein and Gravano, 2000), and Jones et al. (1999). The distant supervision algorithm we describe was drawn from Mintz et al. (2009), who first used the term ‘distant supervision’ (which was suggested to them by Chris Manning) but similar ideas had occurred in earlier systems like Craven and Kumlien (1999) and Morgan et al. (2004) under the name **weakly labeled data**, as well as in Snow et al. (2005) and Wu and Weld (2007). Among the many extensions are Wu and Weld (2010), Riedel et al. (2010), and Ritter et al. (2013). Open IE systems include **KNOW IT ALL** Etzioni et al. (2005), TextRunner (Banko et al., 2007), and **REVERB** (Fader et al., 2011). See Riedel et al. (2013) for a universal schema that combines the advantages of distant supervision and Open IE.

### Exercises

**19.1** Acronym expansion, the process of associating a phrase with an acronym, can

\(^1\) [www.nist.gov/speech/tests/ace/](http://www.nist.gov/speech/tests/ace/)
be accomplished by a simple form of relational analysis. Develop a system based on the relation analysis approaches described in this chapter to populate a database of acronym expansions. If you focus on English Three Letter Acronyms (TLAs) you can evaluate your system’s performance by comparing it to Wikipedia’s TLA page.

19.2 Acquire the CMU seminar corpus and develop a template-filling system by using any of the techniques mentioned in Section 19.8. Analyze how well your system performs as compared with state-of-the-art results on this corpus.

19.3 A useful functionality in newer email and calendar applications is the ability to associate temporal expressions connected with events in email (doctor’s appointments, meeting planning, party invitations, etc.) with specific calendar entries. Collect a corpus of email containing temporal expressions related to event planning. How do these expressions compare to the kinds of expressions commonly found in news text that we’ve been discussing in this chapter?

19.4 For the following sentences, give FOL translations that capture the temporal relationships between the events.

1. When Mary’s flight departed, I ate lunch.
2. When Mary’s flight departed, I had eaten lunch.

The seven circumstances, associated with Hermagoras and Aristotle (Sloan, 2010)

Sometime between the 7th and 4th centuries BCE, the Indian grammarian Pāṇini wrote a famous treatise on Sanskrit grammar, the Āṣṭādhyāyī (‘8 books’), a treatise that has been called “one of the greatest monuments of human intelligence” (Bloomfield, 1933, 11). The work describes the linguistics of the Sanskrit language in the form of 3959 sutras, each very efficiently (since it had to be memorized!) expressing part of a formal rule system that brilliantly prefigured modern mechanisms of formal language theory (Penn and Kiparsky, 2012). One set of rules describes the kārakas, semantic relationships between a verb and noun arguments, roles like agent, instrument, or destination. Pāṇini’s work was the earliest we know of that modeled the linguistic realization of events and their participants. This task of understanding how participants relate to events—being able to answer the question “Who did what to whom” (and perhaps also “when and where”)—is a central question of natural language processing.

Let’s move forward 2.5 millennia to the present and consider the very mundane goal of understanding text about a purchase of stock by XYZ Corporation. This purchasing event and its participants can be described by a wide variety of surface forms. The event can be described by a verb (sold, bought) or a noun (purchase), and XYZ Corp can be the syntactic subject (of bought), the indirect object (of sold), or in a genitive or noun compound relation (with the noun purchase) despite having notionally the same role in all of them:

- XYZ corporation bought the stock.
- They sold the stock to XYZ corporation.
- The stock was bought by XYZ corporation.
- The purchase of the stock by XYZ corporation...
- The stock purchase by XYZ corporation...

In this chapter we introduce a level of representation that captures the commonality between these sentences: there was a purchase event, the participants were XYZ Corp and some stock, and XYZ Corp was the buyer. These shallow semantic representations, semantic roles, express the role that arguments of a predicate take in the event, codified in databases like PropBank and FrameNet. We’ll introduce semantic role labeling, the task of assigning roles to spans in sentences, and selectional restrictions, the preferences that predicates express about their arguments, such as the fact that the theme of eat is generally something edible.

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1 Figure shows a birch bark manuscript from Kashmir of the Rupavattra, a grammatical textbook based on the Sanskrit grammar of Panini. Image from the Wellcome Collection.
20.1 Semantic Roles

Consider the meanings of the arguments Sasha, Pat, the window, and the door in these two sentences.

(20.1) Sasha broke the window.
(20.2) Pat opened the door.

The subjects Sasha and Pat, what we might call the breaker of the window-breaking event and the opener of the door-opening event have something in common. They are both volitional actors, often animate, and they have direct causal responsibility for their events.

**Thematic roles** are a way to capture this semantic commonality between breakers and openers. We say that the subjects of both these verbs are agents. Thus, AGENT is the thematic role that represents an abstract idea such as volitional causation. Similarly, the direct objects of both these verbs, the BrokenThing and OpenedThing, are both prototypically inanimate objects that are affected in some way by the action.

The semantic role for these participants is theme.

<table>
<thead>
<tr>
<th>Thematic Role</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>AGENT</td>
<td>The volitional causer of an event</td>
</tr>
<tr>
<td>EXPERIENCER</td>
<td>The experiencer of an event</td>
</tr>
<tr>
<td>FORCE</td>
<td>The non-volitional causer of the event</td>
</tr>
<tr>
<td>THEME</td>
<td>The participant most directly affected by an event</td>
</tr>
<tr>
<td>RESULT</td>
<td>The end product of an event</td>
</tr>
<tr>
<td>CONTENT</td>
<td>The proposition or content of a propositional event</td>
</tr>
<tr>
<td>INSTRUMENT</td>
<td>An instrument used in an event</td>
</tr>
<tr>
<td>BENEFICIARY</td>
<td>The beneficiary of an event</td>
</tr>
<tr>
<td>SOURCE</td>
<td>The origin of the object of a transfer event</td>
</tr>
<tr>
<td>GOAL</td>
<td>The destination of an object of a transfer event</td>
</tr>
</tbody>
</table>

Figure 20.1 Some commonly used thematic roles with their definitions.

Although thematic roles are one of the oldest linguistic models, as we saw above, their modern formulation is due to Fillmore (1968) and Gruber (1965). Although there is no universally agreed-upon set of roles, Figs. 20.1 and 20.2 list some thematic roles that have been used in various computational papers, together with rough definitions and examples. Most thematic role sets have about a dozen roles, but we’ll see sets with smaller numbers of roles with even more abstract meanings, and sets with very large numbers of roles that are specific to situations. We’ll use the general term **semantic roles** for all sets of roles, whether small or large.

20.2 Diathesis Alternations

The main reason computational systems use semantic roles is to act as a shallow meaning representation that can let us make simple inferences that aren’t possible from the pure surface string of words, or even from the parse tree. To extend the earlier examples, if a document says that Company A acquired Company B, we’d like to know that this answers the query Was Company B acquired? despite the fact that the two sentences have very different surface syntax. Similarly, this shallow semantics might act as a useful intermediate language in machine translation.
Thematic Role | Example
--- | ---
AGENT | The waiter spilled the soup.
EXPERIENCER | John has a headache.
FORCE | The wind blows debris from the mall into our yards.
THEME | Only after Benjamin Franklin broke the ice...
RESULT | The city built a regulation-size baseball diamond...
CONTENT | Mona asked “You met Mary Ann at a supermarket?”
INSTRUMENT | He poached catfish, stunning them with a shocking device...
BENEFICIARY | Whenever Ann Callahan makes hotel reservations for her boss...
SOURCE | I flew in from Boston.
GOAL | I drove to Portland.

Figure 20.2 Some prototypical examples of various thematic roles.

Semantic roles thus help generalize over different surface realizations of predicate arguments. For example, while the AGENT is often realized as the subject of the sentence, in other cases the THEME can be the subject. Consider these possible realizations of the thematic arguments of the verb *break*:

(20.3) John broke the window.

(20.4) John broke the window with a rock.

(20.5) The rock broke the window.

(20.6) The window broke.

These examples suggest that *break* has (at least) the possible arguments AGENT, THEME, and INSTRUMENT. The set of thematic role arguments taken by a verb is often called the thematic grid, θ-grid, or case frame. We can see that there are (among others) the following possibilities for the realization of these arguments of *break*:

AGENT/Subject, THEME/Object
AGENT/Subject, THEME/Object, INSTRUMENT/PP with INSTRUMENT/Subject, THEME/Object
THEME/Subject

It turns out that many verbs allow their thematic roles to be realized in various syntactic positions. For example, verbs like *give* can realize the THEME and GOAL arguments in two different ways:

(20.8) a. Doris gave the book to Cary.

b. Doris gave Cary the book.

These multiple argument structure realizations (the fact that *break* can take AGENT, INSTRUMENT, or THEME as subject, and *give* can realize its THEME and GOAL in either order) are called verb alternations or diathesis alternations. The alternation we showed above for *give*, the dative alternation, seems to occur with particular semantic classes of verbs, including “verbs of future having” (advance, allocate, offer,
owe), “send verbs” (forward, hand, mail), “verbs of throwing” (kick, pass, throw), and so on. Levin (1993) lists for 3100 English verbs the semantic classes to which they belong (47 high-level classes, divided into 193 more specific classes) and the various alternations in which they participate. These lists of verb classes have been incorporated into the online resource VerbNet (Kipper et al., 2000), which links each verb to both WordNet and FrameNet entries.

20.3 Semantic Roles: Problems with Thematic Roles

Representing meaning at the thematic role level seems like it should be useful in dealing with complications like diathesis alternations. Yet it has proved quite difficult to come up with a standard set of roles, and equally difficult to produce a formal definition of roles like AGENT, THEME, or INSTRUMENT.

For example, researchers attempting to define role sets often find they need to fragment a role like AGENT or THEME into many specific roles. Levin and Rappaport Hovav (2005) summarize a number of such cases, such as the fact there seem to be at least two kinds of INSTRUMENTS, intermediary instruments that can appear as subjects and enabling instruments that cannot:

(20.9)  
(a) The cook opened the jar with the new gadget.  
(b) The new gadget opened the jar.

(20.10)  
(a) Shelly ate the sliced banana with a fork.  
(b) *The fork ate the sliced banana.

In addition to the fragmentation problem, there are cases in which we’d like to reason about and generalize across semantic roles, but the finite discrete lists of roles don’t let us do this.

Finally, it has proved difficult to formally define the thematic roles. Consider the AGENT role; most cases of AGENTS are animate, volitional, sentient, causal, but any individual noun phrase might not exhibit all of these properties.

These problems have led to alternative semantic role models that use either many fewer or many more roles.

The first of these options is to define generalized semantic roles that abstract over the specific thematic roles. For example, PROTO-AGENT and PROTO-PATIENT are generalized roles that express roughly agent-like and roughly patient-like meanings. These roles are defined, not by necessary and sufficient conditions, but rather by a set of heuristic features that accompany more agent-like or more patient-like meanings. Thus, the more an argument displays agent-like properties (being volitionally involved in the event, causing an event or a change of state in another participant, being sentient or intentionally involved, moving) the greater the likelihood that the argument can be labeled a PROTO-AGENT. The more patient-like the properties (undergoing change of state, causally affected by another participant, stationary relative to other participants, etc.), the greater the likelihood that the argument can be labeled a PROTO-PATIENT.

The second direction is instead to define semantic roles that are specific to a particular verb or a particular group of semantically related verbs or nouns.

In the next two sections we describe two commonly used lexical resources that make use of these alternative versions of semantic roles. PropBank uses both proto-roles and verb-specific semantic roles. FrameNet uses semantic roles that are specific to a general semantic idea called a frame.
20.4 The Proposition Bank

The Proposition Bank, generally referred to as PropBank, is a resource of sentences annotated with semantic roles. The English PropBank labels all the sentences in the Penn TreeBank; the Chinese PropBank labels sentences in the Penn Chinese TreeBank. Because of the difficulty of defining a universal set of thematic roles, the semantic roles in PropBank are defined with respect to an individual verb sense. Each sense of each verb thus has a specific set of roles, which are given only numbers rather than names: Arg0, Arg1, Arg2, and so on. In general, Arg0 represents the PROTO-AGENT, and Arg1, the PROTO-PATIENT. The semantics of the other roles are less consistent, often being defined specifically for each verb. Nonetheless there are some generalization; the Arg2 is often the benefactive, instrument, attribute, or end state, the Arg3 the start point, benefactive, instrument, or attribute, and the Arg4 the end point.

Here are some slightly simplified PropBank entries for one sense each of the verbs agree and fall. Such PropBank entries are called frame files: note that the definitions in the frame file for each role (“Other entity agreeing”, “Extent, amount fallen”) are informal glosses intended to be read by humans, rather than being formal definitions.

(20.11) agree.01
Arg0: Agreer
Arg1: Proposition
Arg2: Other entity agreeing
Ex1: [Arg0 The group] agreed [Arg1 it wouldn’t make an offer].
Ex2: [ArgM-TMP Usually] [Arg0 John] agrees [Arg2 with Mary]
[Arg1 on everything].

(20.12) fall.01
Arg1: Logical subject, patient, thing falling
Arg2: Extent, amount fallen
Arg3: start point
Arg4: end point, end state of arg1
Ex1: [Arg1 Sales] fell [Arg4 to $25 million] [Arg3 from $27 million].
Ex2: [Arg1 The average junk bond] fell [Arg2 by 4.2%].

Note that there is no Arg0 role for fall, because the normal subject of fall is a PROTO-PATIENT.

The PropBank semantic roles can be useful in recovering shallow semantic information about verbal arguments. Consider the verb increase:

(20.13) increase.01 “go up incrementally”
Arg0: causer of increase
Arg1: thing increasing
Arg2: amount increased by, EXT, or MNR
Arg3: start point
Arg4: end point

A PropBank semantic role labeling would allow us to infer the commonality in the event structures of the following three examples, that is, that in each case Big Fruit Co. is the AGENT and the price of bananas is the THEME, despite the differing surface forms.
(20.14) \([\text{Arg}_0 \text{ Big Fruit Co.}] \text{ increased [Arg}_1 \text{ the price of bananas}].\)

(20.15) \([\text{Arg}_1 \text{ The price of bananas was increased again [Arg}_0 \text{ by Big Fruit Co.}].\)

(20.16) \([\text{Arg}_1 \text{ The price of bananas increased [Arg}_2 \text{ 5%}.] \)

PropBank also has a number of non-numbered arguments called \textbf{ArgMs}, (ArgM-TMP, ArgM-LOC, etc.) which represent modification or adjunct meanings. These are relatively stable across predicates, so aren’t listed with each frame file. Data labeled with these modifiers can be helpful in training systems to detect temporal, location, or directional modification across predicates. Some of the ArgM’s include:

- **TMP** when? yesterday evening, now
- **LOC** where? at the museum, in San Francisco
- **DIR** where to/from? down, to Bangkok
- **MNR** how? clearly, with much enthusiasm
- **PRP/CAU** why? because ..., in response to the ruling
- **REC** themselves, each other
- **ADV** miscellaneous
- **PRD** secondary predication ...ate the meat raw

While PropBank focuses on verbs, a related project, \textbf{NomBank} (Meyers et al., 2004) adds annotations to noun predicates. For example the noun \textit{agreement} in Apple’s \textit{agreement with IBM} would be labeled with Apple as the Arg0 and IBM as the Arg2. This allows semantic role labelers to assign labels to arguments of both verbal and nominal predicates.

### 20.5 FrameNet

While making inferences about the semantic commonalities across different sentences with \textit{increase} is useful, it would be even more useful if we could make such inferences in many more situations, across different verbs, and also between verbs and nouns. For example, we’d like to extract the similarity among these three sentences:

(20.17) \([\text{Arg}_1 \text{ The price of bananas increased [Arg}_2 \text{ 5%}.] \)

(20.18) \([\text{Arg}_1 \text{ The price of bananas rose [Arg}_2 \text{ 5%}.] \)

(20.19) There has been a \([\text{Arg}_2 \text{ 5%}] \text{ rise [Arg}_1 \text{ in the price of bananas}].\)

Note that the second example uses the different verb \textit{rise}, and the third example uses the noun rather than the verb \textit{rise}. We’d like a system to recognize that the \textit{price of bananas} is what went up, and that \textit{5%} is the amount it went up, no matter whether the \textit{5%} appears as the object of the verb \textit{increased} or as a nominal modifier of the noun \textit{rise}.

The \textbf{FrameNet} project is another semantic-role-labeling project that attempts to address just these kinds of problems (Baker et al. 1998, Fillmore et al. 2003, Fillmore and Baker 2009, Ruppenhofer et al. 2016). Whereas roles in the PropBank project are specific to an individual verb, roles in the FrameNet project are specific to a frame.

What is a frame? Consider the following set of words:

- \textit{reservation, flight, travel, buy, price, cost, fare, rates, meal, plane}

There are many individual lexical relations of hyponymy, synonymy, and so on between many of the words in this list. The resulting set of relations does not,
However, add up to a complete account of how these words are related. They are clearly all defined with respect to a coherent chunk of common-sense background information concerning air travel.

We call the holistic background knowledge that unites these words a frame (Fillmore, 1985). The idea that groups of words are defined with respect to some background information is widespread in artificial intelligence and cognitive science, where besides frame we see related works like a model (Johnson-Laird, 1983), or even script (Schank and Abelson, 1977).

A frame in FrameNet is a background knowledge structure that defines a set of frame-specific semantic roles, called frame elements, and includes a set of predicates that use these roles. Each word evokes a frame and profiles some aspect of the frame and its elements. The FrameNet dataset includes a set of frames and frame elements, the lexical units associated with each frame, and a set of labeled example sentences. For example, the change_position_on_a_scale frame is defined as follows:

This frame consists of words that indicate the change of an Item’s position on a scale (the Attribute) from a starting point (Initial_value) to an end point (Final_value).

Some of the semantic roles (frame elements) in the frame are defined as in Fig. 20.3. Note that these are separated into core roles, which are frame specific, and non-core roles, which are more like the Arg-M arguments in PropBank, expressing more general properties of time, location, and so on.

<table>
<thead>
<tr>
<th>Core Roles</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ATTRIBUTE</td>
<td>The ATTRIBUTE is a scalar property that the ITEM possesses.</td>
</tr>
<tr>
<td>DIFFERENCE</td>
<td>The distance by which an ITEM changes its position on the scale.</td>
</tr>
<tr>
<td>FINAL_STATE</td>
<td>A description that presents the ITEM’s state after the change in the ATTRIBUTE’s value as an independent predication.</td>
</tr>
<tr>
<td>FINAL_VALUE</td>
<td>The position on the scale where the ITEM ends up.</td>
</tr>
<tr>
<td>INITIAL_STATE</td>
<td>A description that presents the ITEM’s state before the change in the ATTRIBUTE’s value as an independent predication.</td>
</tr>
<tr>
<td>INITIAL_VALUE</td>
<td>The initial position on the scale from which the ITEM moves away.</td>
</tr>
<tr>
<td>ITEM</td>
<td>The entity that has a position on the scale.</td>
</tr>
<tr>
<td>VALUE_RANGE</td>
<td>A portion of the scale, typically identified by its end points, along which the values of the ATTRIBUTE fluctuate.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Some Non-Core Roles</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>DURATION</td>
<td>The length of time over which the change takes place.</td>
</tr>
<tr>
<td>SPEED</td>
<td>The rate of change of the VALUE.</td>
</tr>
<tr>
<td>GROUP</td>
<td>The GROUP in which an ITEM changes the value of an ATTRIBUTE in a specified way.</td>
</tr>
</tbody>
</table>

Figure 20.3 The frame elements in the change_position_on_a_scale frame from the FrameNet Labelers Guide (Ruppenhofer et al., 2016).

Here are some example sentences:

(20.20) [ITEM Oil] rose [ATTRIBUTE in price] [DIFFERENCE by 2%].
(20.21) [ITEM It] has increased [FINAL_STATE to having them 1 day a month].
(20.22) [ITEM Microsoft shares] fell [FINAL_VALUE to 7 5/8].
(20.23) [ITEM Colon cancer incidence] fell [DIFFERENCE by 50%] [GROUP among men].
(20.24) a steady *increase* \[\text{INITIAL\_VALUE} \text{from 9.5} \] \[\text{FINAL\_VALUE} \text{to 14.3} \] \[\text{ITEM in dividends}\]

(20.25) a \[\text{DIFFERENCE 5\%} \] \[\text{ITEM dividend} \] *increase...*

Note from these example sentences that the frame includes target words like *rise*, *fall*, and *increase*. In fact, the complete frame consists of the following words:

**VERBS:** dwindled, move, soar, escalation, shift

**ADVERBS:** decrease, fluctuate, triple, growth, hop

**NOUNS:** hike, double, slide, increase

FrameNet also codes relationships between frames, allowing frames to inherit from each other, or representing relations between frames like causation (and generalizations among frame elements in different frames can be represented by inheritance as well). Thus, there is a *Cause* change of position on a scale frame that is linked to the *Change of position on a scale* frame by the *cause* relation, but that adds an AGENT role and is used for causative examples such as the following:

(20.26) [AGENT They] raised [ITEM the price of their soda] [DIFFERENCE by 2\%].

Together, these two frames would allow an understanding system to extract the common event semantics of all the verbal and nominal causative and non-causative usages.

FrameNets have also been developed for many other languages including Spanish, German, Japanese, Portuguese, Italian, and Chinese.

## 20.6 Semantic Role Labeling

**Semantic role labeling** (sometimes shortened as SRL) is the task of automatically finding the **semantic roles** of each argument of each predicate in a sentence. Current approaches to semantic role labeling are based on supervised machine learning, often using the FrameNet and PropBank resources to specify what counts as a predicate, define the set of roles used in the task, and provide training and test sets.

Recall that the difference between these two models of semantic roles is that FrameNet (20.27) employs many frame-specific frame elements as roles, while PropBank (20.28) uses a smaller number of numbered argument labels that can be interpreted as verb-specific labels, along with the more general ARGM labels. Some examples:

(20.27) [You] can’t [blame] [the program] [for being unable to identify it]

(20.28) [The San Francisco Examiner] issued [a special edition] [yesterday]

### 20.6.1 A Feature-based Algorithm for Semantic Role Labeling

A simplified feature-based semantic role labeling algorithm is sketched in Fig. 20.4. Feature-based algorithms—from the very earliest systems like (Simmons, 1973)—begin by parsing, using broad-coverage parsers to assign a parse to the input string.
Figure 20.5 shows a parse of (20.28) above. The parse is then traversed to find all words that are predicates.

For each of these predicates, the algorithm examines each node in the parse tree and uses supervised classification to decide the semantic role (if any) it plays for this predicate. Given a labeled training set such as PropBank or FrameNet, a feature vector is extracted for each node, using feature templates described in the next subsection. A 1-of-N classifier is then trained to predict a semantic role for each constituent given these features, where N is the number of potential semantic roles plus an extra NONE role for non-role constituents. Any standard classification algorithms can be used. Finally, for each test sentence to be labeled, the classifier is run on each relevant constituent.

```plaintext
function SEMANTICROLELABEL(words) returns labeled tree
    parse ← PARSE(words)
    for each predicate in parse do
        for each node in parse do
            featurevector ← EXTRACTFEATURES(node, predicate, parse)
            CLASSIFYNODE(node, featurevector, parse)
```

Figure 20.4 A generic semantic-role-labeling algorithm. CLASSIFYNODE is a 1-of-N classifier that assigns a semantic role (or NONE for non-role constituents), trained on labeled data such as FrameNet or PropBank.

Figure 20.5 Parse tree for a PropBank sentence, showing the PropBank argument labels. The dotted line shows the path feature NP↑S↓VP↓VBD for ARG0, the NP-SBJ constituent The San Francisco Examiner.

Instead of training a single-stage classifier as in Fig. 20.5, the node-level classification task can be broken down into multiple steps:

1. **Pruning:** Since only a small number of the constituents in a sentence are arguments of any given predicate, many systems use simple heuristics to prune unlikely constituents.
2. **Identification:** a binary classification of each node as an argument to be labeled or a NONE.
3. **Classification:** a 1-of-N classification of all the constituents that were labeled as arguments by the previous stage.
The separation of identification and classification may lead to better use of features (different features may be useful for the two tasks) or to computational efficiency.

**Global Optimization**

The classification algorithm of Fig. 20.5 classifies each argument separately (‘locally’), making the simplifying assumption that each argument of a predicate can be labeled independently. This assumption is false; there are interactions between arguments that require a more ‘global’ assignment of labels to constituents. For example, constituents in FrameNet and PropBank are required to be non-overlapping. More significantly, the semantic roles of constituents are not independent. For example PropBank does not allow multiple identical arguments; two constituents of the same verb cannot both be labeled ARG0.

Role labeling systems thus often add a fourth step to deal with global consistency across the labels in a sentence. For example, the local classifiers can return a list of possible labels associated with probabilities for each constituent, and a second-pass Viterbi decoding or re-ranking approach can be used to choose the best consensus label. Integer linear programming (ILP) is another common way to choose a solution that conforms best to multiple constraints.

**Features for Semantic Role Labeling**

Most systems use some generalization of the core set of features introduced by Gildea and Jurafsky (2000). Common basic features templates (demonstrated on the NP-SBJ constituent *The San Francisco Examiner* in Fig. 20.5) include:

- The governing **predicate**, in this case the verb *issued*. The predicate is a crucial feature since labels are defined only with respect to a particular predicate.
- The **phrase type** of the constituent, in this case, *NP* (or *NP-SBJ*). Some semantic roles tend to appear as *NPs*, others as *S* or *PP*, and so on.
- The **headword** of the constituent, *Examiner*. The headword of a constituent can be computed with standard head rules, such as those given in Appendix D in Fig. 17.17. Certain headwords (e.g., pronouns) place strong constraints on the possible semantic roles they are likely to fill.
- The **headword part of speech** of the constituent, *NNP*.
- The **path** in the parse tree from the constituent to the predicate. This path is marked by the dotted line in Fig. 20.5. Following Gildea and Jurafsky (2000), we can use a simple linear representation of the path, *NP↓S↓VP↓VBD*. ↑ and ↓ represent upward and downward movement in the tree, respectively. The path is very useful as a compact representation of many kinds of grammatical function relationships between the constituent and the predicate.
- The **voice** of the clause in which the constituent appears, in this case, *active* (as contrasted with passive). Passive sentences tend to have strongly different linkings of semantic roles to surface form than do active ones.
- The binary **linear position** of the constituent with respect to the predicate, either *before* or *after*.
- The **subcategory** of the predicate, the set of expected arguments that appear in the verb phrase. We can extract this information by using the phrase-structure rule that expands the immediate parent of the predicate; *VP → VBD NP PP* for the predicate in Fig. 20.5.
- The named entity type of the constituent.
The first words and the last word of the constituent.

The following feature vector thus represents the first NP in our example (recall that most observations will have the value NONE rather than, for example, ARG0, since most constituents in the parse tree will not bear a semantic role):

ARG0: [issued, NP, Examiner, NNP, NP, VP, VBD, active, before, VP, NP, PP, ORG, The, Examiner]

Other features are often used in addition, such as sets of n-grams inside the constituent, or more complex versions of the path features (the upward or downward halves, or whether particular nodes occur in the path).

It’s also possible to use dependency parses instead of constituency parses as the basis of features, for example using dependency parse paths instead of constituency paths.

### 20.6.2 A Neural Algorithm for Semantic Role Labeling

A simple neural approach to SRL is to treat it as a sequence labeling task like named-entity recognition, using the BIO approach. Let’s assume that we are given the predicate and the task is just detecting and labeling spans. Recall that with BIO tagging, we have a begin and end tag for each possible role (B-ARG0, I-ARG0; B-ARG1, I-ARG1, and so on), plus an outside tag O.

As with all the taggers, the goal is to compute the highest probability tag sequence $\hat{y}$, given the input sequence of words $w$:

$$\hat{y} = \arg \max_{y \in \mathcal{T}} P(y|w)$$

Fig. 20.6 shows a sketch of a standard algorithm from He et al. (2017). Here each input word is mapped to pretrained embeddings, and then each token is concatenated with the predicate embedding and then passed through a feedforward network with a softmax which outputs a distribution over each SRL label. For decoding, a CRF layer can be used instead of the MLP layer on top of the biLSTM output to do global inference, but in practice this doesn’t seem to provide much benefit.
20.6.3 Evaluation of Semantic Role Labeling

The standard evaluation for semantic role labeling is to require that each argument label must be assigned to the exactly correct word sequence or parse constituent, and then compute precision, recall, and F-measure. Identification and classification can also be evaluated separately. Two common datasets used for evaluation are CoNLL-2005 (Carreras and Màrquez, 2005) and CoNLL-2012 (Pradhan et al., 2013).

20.7 Selectional Restrictions

We turn in this section to another way to represent facts about the relationship between predicates and arguments. A selectional restriction is a semantic type constraint that a verb imposes on the kind of concepts that are allowed to fill its argument roles. Consider the two meanings associated with the following example:

(20.29) I want to eat someplace nearby.

There are two possible parses and semantic interpretations for this sentence. In the sensible interpretation, *eat* is intransitive and the phrase *someplace nearby* is an adjunct that gives the location of the eating event. In the nonsensical *speaker-as-Godzilla* interpretation, *eat* is transitive and the phrase *someplace nearby* is the direct object and the THEME of the eating, like the NP *Malaysian food* in the following sentences:

(20.30) I want to eat Malaysian food.

How do we know that *someplace nearby* isn’t the direct object in this sentence? One useful cue is the semantic fact that the THEME of EATING events tends to be something that is *edible*. This restriction placed by the verb *eat* on the filler of its THEME argument is a selectional restriction.

Selectional restrictions are associated with senses, not entire lexemes. We can see this in the following examples of the lexeme *serve*:

(20.31) The restaurant serves green-lipped mussels.

(20.32) Which airlines serve Denver?

Example (20.31) illustrates the offering-food sense of *serve*, which ordinarily restricts its THEME to be some kind of food. Example (20.32) illustrates the provides a commercial service to sense of *serve*, which constrains its THEME to be some type of appropriate location.

Selectional restrictions vary widely in their specificity. The verb *imagine*, for example, imposes strict requirements on its AGENT role (restricting it to humans and other animate entities) but places very few semantic requirements on its THEME role. A verb like *diagonalize*, on the other hand, places a very specific constraint on the filler of its THEME role: it has to be a matrix, while the arguments of the adjective *odorless* are restricted to concepts that could possess an odor:

(20.33) In rehearsal, I often ask the musicians to *imagine* a tennis game.

(20.34) Radon is an *odorless* gas that can’t be detected by human senses.

(20.35) To *diagonalize* a matrix is to find its eigenvalues.

These examples illustrate that the set of concepts we need to represent selectional restrictions (being a matrix, being able to possess an odor, etc) is quite open ended. This distinguishes selectional restrictions from other features for representing lexical knowledge, like parts-of-speech, which are quite limited in number.
20.7.1 Representing Selectional Restrictions

One way to capture the semantics of selectional restrictions is to use and extend the event representation of Chapter 19. Recall that the neo-Davidsonian representation of an event consists of a single variable that stands for the event, a predicate denoting the kind of event, and variables and relations for the event roles. Ignoring the issue of the \( \lambda \)-structures and using thematic roles rather than deep event roles, the semantic contribution of a verb like eat might look like the following:

\[
\exists e, x, y \text{Eating}(e) \land \text{Agent}(e, x) \land \text{Theme}(e, y)
\]

With this representation, all we know about \( y \), the filler of the Theme role, is that it is associated with an Eating event through the Theme relation. To stipulate the selectional restriction that \( y \) must be something edible, we simply add a new term to that effect:

\[
\exists e, x, y \text{Eating}(e) \land \text{Agent}(e, x) \land \text{Theme}(e, y) \land \text{EdibleThing}(y)
\]

When a phrase like ate a hamburger is encountered, a semantic analyzer can form the following kind of representation:

\[
\exists e, x, y \text{Eating}(e) \land \text{Eater}(e, x) \land \text{Theme}(e, y) \land \text{EdibleThing}(y) \land \text{Hamburger}(y)
\]

This representation is perfectly reasonable since the membership of \( y \) in the category Hamburger is consistent with its membership in the category EdibleThing, assuming a reasonable set of facts in the knowledge base. Correspondingly, the representation for a phrase such as ate a takeoff would be ill-formed because membership in an event-like category such as Takeoff would be inconsistent with membership in the category EdibleThing.

While this approach adequately captures the semantics of selectional restrictions, there are two problems with its direct use. First, using FOL to perform the simple task of enforcing selectional restrictions is overkill. Other, far simpler, formalisms can do the job with far less computational cost. The second problem is that this approach presupposes a large, logical knowledge base of facts about the concepts that make up selectional restrictions. Unfortunately, although such common-sense knowledge bases are being developed, none currently have the kind of coverage necessary to the task.

A more practical approach is to state selectional restrictions in terms of WordNet synsets rather than as logical concepts. Each predicate simply specifies a WordNet synset as the selectional restriction on each of its arguments. A meaning representation is well-formed if the role filler word is a hyponym (subordinate) of this synset.

For our ate a hamburger example, for instance, we could set the selectional restriction on the Theme role of the verb eat to the synset \{food, nutrient\}, glossed as any substance that can be metabolized by an animal to give energy and build tissue. Luckily, the chain of hypernyms for hamburger shown in Fig. 20.7 reveals that hamburgers are indeed food. Again, the filler of a role need not match the restriction synset exactly; it just needs to have the synset as one of its superordinates.

We can apply this approach to the Theme roles of the verbs imagine, lift, and diagonalize, discussed earlier. Let us restrict imagine’s Theme to the synset \{entity\}, lift’s Theme to \{physical entity\}, and diagonalize to \{matrix\}. This arrangement correctly permits imagine a hamburger and lift a hamburger, while also correctly ruling out diagonalize a hamburger.
### Sense 1
hamburger, beefburger --
(a fried cake of minced beef served on a bun)

- sandwich
- snack food
- dish
  - nutriment, nourishment, nutrition...
  - food, nutrient
  - substance
    - matter
  - physical entity
  - entity

**Figure 20.7** Evidence from WordNet that hamburgers are edible.

#### 20.7.2 Selectional Preferences

In the earliest implementations, selectional restrictions were considered strict constraints on the kind of arguments a predicate could take (Katz and Fodor 1963, Hirst 1987). For example, the verb *eat* might require that its THEME argument be [+FOOD]. Early word sense disambiguation systems used this idea to rule out senses that violated the selectional restrictions of their governing predicates.

Very quickly, however, it became clear that these selectional restrictions were better represented as preferences rather than strict constraints (Wilks 1975b, Wilks 1975a). For example, selectional restriction violations (like inedible arguments of *eat*) often occur in well-formed sentences, for example because they are negated (20.36), or because selectional restrictions are overstated (20.37):

(20.36) But it fell apart in 1931, perhaps because people realized you can’t eat gold for lunch if you’re hungry.

(20.37) In his two championship trials, Mr. Kulkarni ate glass on an empty stomach, accompanied only by water and tea.

Modern systems for selectional preferences therefore specify the relation between a predicate and its possible arguments with soft constraints of some kind.

### Selectional Association

One of the most influential has been the selectional association model of Resnik (1993). Resnik defines the idea of **selectional preference strength** as the general amount of information that a predicate tells us about the semantic class of its arguments. For example, the verb *eat* tells us a lot about the semantic class of its direct objects, since they tend to be edible. The verb *be*, by contrast, tells us less about its direct objects. The selectional preference strength can be defined by the difference in information between two distributions: the distribution of expected semantic classes $P(c)$ (how likely is it that a direct object will fall into class $c$) and the distribution of expected semantic classes for the particular verb $P(c|v)$ (how likely is it that the direct object of the specific verb $v$ will fall into semantic class $c$). The greater the difference between these distributions, the more information the verb is giving us about possible objects. The difference between these two distributions can be quantified by **relative entropy**, or the Kullback-Leibler divergence (Kullback and Leibler, 1951). The Kullback-Leibler or **KL divergence** $D(P||Q)$ expresses the...
difference between two probability distributions $P$ and $Q$

$$D(P||Q) = \sum_x P(x) \log \frac{P(x)}{Q(x)} \quad (20.38)$$

The selectional preference $S_R(v)$ uses the KL divergence to express how much information, in bits, the verb $v$ expresses about the possible semantic class of its argument.

$$S_R(v) = D(P(c|v)||P(c)) = \sum_c P(c|v) \log \frac{P(c|v)}{P(c)} \quad (20.39)$$

Resnik then defines the selectional association of a particular class and verb as the relative contribution of that class to the general selectional preference of the verb:

$$A_R(v,c) = \frac{1}{S_R(v)} P(c|v) \log \frac{P(c|v)}{P(c)} \quad (20.40)$$

The selectional association is thus a probabilistic measure of the strength of association between a predicate and a class dominating the argument to the predicate. Resnik estimates the probabilities for these associations by parsing a corpus, counting all the times each predicate occurs with each argument word, and assuming that each word is a partial observation of all the WordNet concepts containing the word. The following table from Resnik (1996) shows some sample high and low selectional associations for verbs and some WordNet semantic classes of their direct objects.

<table>
<thead>
<tr>
<th>Verb</th>
<th>Direct Object</th>
<th>Semantic Class</th>
<th>Assoc</th>
<th>Direct Object</th>
<th>Semantic Class</th>
<th>Assoc</th>
</tr>
</thead>
<tbody>
<tr>
<td>read</td>
<td>WRITING</td>
<td>6.80</td>
<td>ACTIVITY</td>
<td>-0.20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>write</td>
<td>WRITING</td>
<td>7.26</td>
<td>COMMERCE</td>
<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>see</td>
<td>ENTITY</td>
<td>5.79</td>
<td>METHOD</td>
<td>-0.01</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Selectional Preference via Conditional Probability

An alternative to using selectional association between a verb and the WordNet class of its arguments is to use the conditional probability of an argument word given a predicate verb, directly modeling the strength of association of one verb (predicate) with one noun (argument).

The conditional probability model can be computed by parsing a very large corpus (billions of words), and computing co-occurrence counts: how often a given verb occurs with a given noun in a given relation. The conditional probability of an argument noun given a verb for a particular relation $P(n|v,r)$ can then be used as a selectional preference metric for that pair of words (Brockmann and Lapata 2003, Keller and Lapata 2003):

$$P(n|v,r) = \begin{cases} \frac{C(n,v,r)}{C(v,r)} & \text{if } C(n,v,r) > 0 \\ 0 & \text{otherwise} \end{cases}$$

The inverse probability $P(v|n,r)$ was found to have better performance in some cases (Brockmann and Lapata, 2003):

$$P(v|n,r) = \begin{cases} \frac{C(n,v,r)}{C(n,r)} & \text{if } C(n,v,r) > 0 \\ 0 & \text{otherwise} \end{cases}$$
An even simpler approach is to use the simple log co-occurrence frequency of the predicate with the argument log \( \text{count}(v,n,r) \) instead of conditional probability; this seems to do better for extracting preferences for syntactic subjects rather than objects (Brockmann and Lapata, 2003).

### Evaluating Selectional Preferences

One way to evaluate models of selectional preferences is to use **pseudowords** (Gale et al. 1992b, Schütze 1992a). A pseudoword is an artificial word created by concatenating a test word in some context (say banana) with a confounder word (say door) to create banana-door. The task of the system is to identify which of the two words is the original word. To evaluate a selectional preference model (for example on the relationship between a verb and a direct object) we take a test corpus and select all verb tokens. For each verb token (say drive) we select the direct object (e.g., car), concatenated with a confounder word that is its nearest neighbor, the noun with the frequency closest to the original (say house), to make car/house. We then use the selectional preference model to choose which of car and house are more preferred objects of drive, and compute how often the model chooses the correct original object (e.g., car) (Chambers and Jurafsky, 2010).

Another evaluation metric is to get human preferences for a test set of verb-argument pairs, and have them rate their degree of plausibility. This is usually done by using magnitude estimation, a technique from psychophysics, in which subjects rate the plausibility of an argument proportional to a modulus item. A selectional preference model can then be evaluated by its correlation with the human preferences (Keller and Lapata, 2003).

### 20.8 Primitive Decomposition of Predicates

One way of thinking about the semantic roles we have discussed through the chapter is that they help us define the roles that arguments play in a decompositional way, based on finite lists of thematic roles (agent, patient, instrument, proto-agent, proto-patient, etc.). This idea of decomposing meaning into sets of primitive semantic elements or features, called **primitive decomposition** or **componential analysis**, has been taken even further, and focused particularly on predicates.

Consider these examples of the verb kill:

\[(20.41) \text{Jim killed his philodendron.}\]
\[(20.42) \text{Jim did something to cause his philodendron to become not alive.}\]

There is a truth-conditional (‘propositional semantics’) perspective from which these two sentences have the same meaning. Assuming this equivalence, we could represent the meaning of kill as:

\[(20.43) \text{KILL}(x,y) \iff \text{CAUSE}(x, \text{BECOME}(\text{NOT}(\text{ALIVE}(y))))\]

thus using semantic primitives like do, cause, become not, and alive.

Indeed, one such set of potential semantic primitives has been used to account for some of the verbal alternations discussed in Section 20.2 (Lakoff 1965, Dowty 1979). Consider the following examples.

\[(20.44) \text{John opened the door.} \implies \text{CAUSE}(\text{John, BECOME(OPEN(door))})\]
\[(20.45) \text{The door opened.} \implies \text{BECOME(OPEN(door))}\]
The door is open. ⇒ OPEN(door)

The decompositional approach asserts that a single state-like predicate associated with open underlies all of these examples. The differences among the meanings of these examples arises from the combination of this single predicate with the primitives CAUSE and BECOME.

While this approach to primitive decomposition can explain the similarity between states and actions or causative and non-causative predicates, it still relies on having a large number of predicates like open. More radical approaches choose to break down these predicates as well. One such approach to verbal predicate decomposition that played a role in early natural language systems is conceptual dependency (CD), a set of ten primitive predicates, shown in Fig. 20.8.

<table>
<thead>
<tr>
<th>Primitive</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>ATTRANS</td>
<td>The abstract transfer of possession or control from one entity to another</td>
</tr>
<tr>
<td>PTRANS</td>
<td>The physical transfer of an object from one location to another</td>
</tr>
<tr>
<td>MTRANS</td>
<td>The transfer of mental concepts between entities or within an entity</td>
</tr>
<tr>
<td>MBUILD</td>
<td>The creation of new information within an entity</td>
</tr>
<tr>
<td>PROPEL</td>
<td>The application of physical force to move an object</td>
</tr>
<tr>
<td>MOVE</td>
<td>The integral movement of a body part by an animal</td>
</tr>
<tr>
<td>INGEST</td>
<td>The taking in of a substance by an animal</td>
</tr>
<tr>
<td>EXPEL</td>
<td>The expulsion of something from an animal</td>
</tr>
<tr>
<td>SPEAK</td>
<td>The action of producing a sound</td>
</tr>
<tr>
<td>ATTEND</td>
<td>The action of focusing a sense organ</td>
</tr>
</tbody>
</table>

Below is an example sentence along with its CD representation. The verb brought is translated into the two primitives ATTRANS and PTRANS to indicate that the waiter both physically conveyed the check to Mary and passed control of it to her. Note that CD also associates a fixed set of thematic roles with each primitive to represent the various participants in the action.

(20.47) The waiter brought Mary the check.

∃x,y ATTRANS(x) ∧ Actor(x, Waiter) ∧ Object(x, Check) ∧ To(x, Mary) ∧ PTRANS(y) ∧ Actor(y, Waiter) ∧ Object(y, Check) ∧ To(y, Mary)

20.9 Summary

- **Semantic roles** are abstract models of the role an argument plays in the event described by the predicate.
- **Thematic roles** are a model of semantic roles based on a single finite list of roles. Other semantic role models include per-verb semantic role lists and proto-agent/proto-patient, both of which are implemented in PropBank, and per-frame role lists, implemented in FrameNet.
• **Semantic role labeling** is the task of assigning semantic role labels to the constituents of a sentence. The task is generally treated as a supervised machine learning task, with models trained on PropBank or FrameNet. Algorithms generally start by parsing a sentence and then automatically tag each parse tree node with a semantic role. Neural models map straight from words end-to-end.

• Semantic **selectional restrictions** allow words (particularly predicates) to post constraints on the semantic properties of their argument words. **Selectional preference** models (like **selectional association** or simple conditional probability) allow a weight or probability to be assigned to the association between a predicate and an argument word or class.

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**Bibliographical and Historical Notes**

Although the idea of semantic roles dates back to Pāṇini, they were re-introduced into modern linguistics by Gruber (1965), Fillmore (1966) and Fillmore (1968). Fillmore had become interested in argument structure by studying Lucien Tesnière’s groundbreaking *Éléments de Syntaxe Structurale* (Tesnière, 1959) in which the term ‘dependency’ was introduced and the foundations were laid for dependency grammar. Following Tesnière’s terminology, Fillmore first referred to argument roles as **actants** (Fillmore, 1966) but quickly switched to the term **case**, (see Fillmore (2003)) and proposed a universal list of semantic roles or cases (Agent, Patient, Instrument, etc.), that could be taken on by the arguments of predicates. Verbs would be listed in the lexicon with their **case frame**, the list of obligatory (or optional) case arguments.

The idea that semantic roles could provide an intermediate level of semantic representation that could help map from syntactic parse structures to deeper, more fully-specified representations of meaning was quickly adopted in natural language processing, and systems for extracting case frames were created for machine translation (Wilks, 1973), question-answering (Hendrix et al., 1973), spoken-language processing (Nash-Webber, 1975), and dialogue systems (Bobrow et al., 1977). General-purpose semantic role labelers were developed. The earliest ones (Simmons, 1973) first parsed a sentence by means of an ATN (Augmented Transition Network) parser. Each verb then had a set of rules specifying how the parse should be mapped to semantic roles. These rules mainly made reference to grammatical functions (subject, object, complement of specific prepositions) but also checked constituent internal features such as the animacy of head nouns. Later systems assigned roles from pre-built parse trees, again by using dictionaries with verb-specific case frames (Levin 1977, Marcus 1980).

By 1977 case representation was widely used and taught in AI and NLP courses, and was described as a standard of natural language processing in the first edition of Winston’s 1977 textbook *Artificial Intelligence*.

In the 1980s Fillmore proposed his model of **frame semantics**, later describing the intuition as follows:

“The idea behind frame semantics is that speakers are aware of possibly quite complex situation types, packages of connected expectations, that go by various names—frames, schemas, scenarios, scripts, cultural narratives, memes—and the words in our language are understood with such frames as their presupposed background.” (Fillmore, 2012, p. 712)
The word *frame* seemed to be in the air for a suite of related notions proposed at about the same time by Minsky (1974), Hymes (1974), and Goffman (1974), as well as related notions with other names like *scripts* (Schank and Abelson, 1975) and *schemata* (Bobrow and Norman, 1975) (see Tannen (1979) for a comparison). Fillmore was also influenced by the semantic field theorists and by a visit to the Yale AI lab where he took notice of the lists of slots and fillers used by early information extraction systems like DeJong (1982) and Schank and Abelson (1977). In the 1990s Fillmore drew on these insights to begin the FrameNet corpus annotation project.

At the same time, Beth Levin drew on her early case frame dictionaries (Levin, 1977) to develop her book which summarized sets of verb classes defined by shared argument realizations (Levin, 1993). The VerbNet project built on this work (Kipper et al., 2000), leading soon afterwards to the PropBank semantic-role-labeled corpus created by Martha Palmer and colleagues (Palmer et al., 2005).

The combination of rich linguistic annotation and corpus-based approach instantiated in FrameNet and PropBank led to a revival of automatic approaches to semantic role labeling, first on FrameNet (Gildea and Jurafsky, 2000) and then on PropBank data (Gildea and Palmer, 2002, inter alia). The problem first addressed in the 1970s by handwritten rules was thus now generally recast as one of supervised machine learning enabled by large and consistent databases. Many popular features used for role labeling are defined in Gildea and Jurafsky (2002), Surdeanu et al. (2003), Xue and Palmer (2004), Pradhan et al. (2005), Che et al. (2009), and Zhao et al. (2009). The use of dependency rather than constituency parses was introduced in the CoNLL-2008 shared task (Surdeanu et al., 2008). For surveys see Palmer et al. (2010) and Marquez et al. (2008).

The use of neural approaches to semantic role labeling was pioneered by Colbert et al. (2011), who applied a CRF on top of a convolutional net. Early work like Foland, Jr. and Martin (2015) focused on using dependency features. Later work eschewed syntactic features altogether; Zhou and Xu (2015b) introduced the use of a stacked (6-8 layer) biLSTM architecture, and (He et al., 2017) showed how to augment the biLSTM architecture with highway networks and also replace the CRF with A* decoding that make it possible to apply a wide variety of global constraints in SRL decoding.

Most semantic role labeling schemes only work within a single sentence, focusing on the object of the verbal (or nominal, in the case of NomBank) predicate. However, in many cases, a verbal or nominal predicate may have an implicit argument: one that appears only in a contextual sentence, or perhaps not at all and must be inferred. In the two sentences *This house has a new owner. The sale was finalized 10 days ago.* the *sale* in the second sentence has no ARG1, but a reasonable reader would infer that the Arg1 should be the *house* mentioned in the prior sentence. Finding these arguments, implicit argument detection (sometimes shortened as iSRL) was introduced by Gerber and Chai (2010) and Ruppenhofer et al. (2010). See Do et al. (2017) for more recent neural models.

To avoid the need for huge labeled training sets, unsupervised approaches for semantic role labeling attempt to induce the set of semantic roles by clustering over arguments. The task was pioneered by Riloff and Schmelzenbach (1998) and Swier and Stevenson (2004); see Grenager and Manning (2006), Titov and Klementiev (2012), Lang and Lapata (2014), Woodsend and Lapata (2015), and Titov and Khoddam (2014).

Recent innovations in frame labeling include *connotation frames*, which mark richer information about the argument of predicates. Connotation frames mark the
sentiment of the writer or reader toward the arguments (for example using the verb *survive* in *he survived a bombing* expresses the writer’s sympathy toward the subject *he* and negative sentiment toward the bombing. See Chapter 25 for more details.

Selectional preference has been widely studied beyond the selectional association models of Resnik (1993) and Resnik (1996). Methods have included clustering (Rooth et al., 1999), discriminative learning (Bergsma et al., 2008a), and topic models (Séaghdha 2010, Ritter et al. 2010b), and constraints can be expressed at the level of words or classes (Agirre and Martinez, 2001). Selectional preferences have also been successfully integrated into semantic role labeling (Erk 2007, Zapirain et al. 2013, Do et al. 2017).

Exercises
In this chapter we turn to tools for interpreting affective meaning, extending our study of sentiment analysis in Chapter 4. We use the word ‘affective’, following the tradition in affective computing (Picard, 1995) to mean emotion, sentiment, personality, mood, and attitudes. Affective meaning is closely related to subjectivity, the study of a speaker or writer’s evaluations, opinions, emotions, and speculations (Wiebe et al., 1999).

How should affective meaning be defined? One influential typology of affective states comes from Scherer (2000), who defines each class of affective states by factors like its cognitive realization and time course (Fig. 21.1).

**Emotion:** Relatively brief episode of response to the evaluation of an external or internal event as being of major significance. (angry, sad, joyful, fearful, ashamed, proud, elated, desperate)

**Mood:** Diffuse affect state, most pronounced as change in subjective feeling, of low intensity but relatively long duration, often without apparent cause. (cheerful, gloomy, irritable, listless, depressed, buoyant)

**Interpersonal stance:** Affective stance taken toward another person in a specific interaction, coloring the interpersonal exchange in that situation. (distant, cold, warm, supportive, contemptuous, friendly)

**Attitude:** Relatively enduring, affectively colored beliefs, preferences, and predispositions towards objects or persons. (liking, loving, hating, valuing, desiring)

**Personality traits:** Emotionally laden, stable personality dispositions and behavior tendencies, typical for a person. (nervous, anxious, reckless, morose, hostile, jealous)

Figure 21.1 The Scherer typology of affective states (Scherer, 2000).

We can design extractors for each of these kinds of affective states. Chapter 4 already introduced sentiment analysis, the task of extracting the positive or negative orientation that a writer expresses in a text. This corresponds in Scherer’s typology to the extraction of attitudes: figuring out what people like or dislike, from affect-rich texts like consumer reviews of books or movies, newspaper editorials, or public sentiment in blogs or tweets.

Detecting emotion and moods is useful for detecting whether a student is confused, engaged, or certain when interacting with a tutorial system, whether a caller to a help line is frustrated, whether someone’s blog posts or tweets indicated depression. Detecting emotions like fear in novels, for example, could help us trace what groups or situations are feared and how that changes over time.
Detecting different interpersonal stances can be useful when extracting information from human-human conversations. The goal here is to detect stances like friendliness or awkwardness in interviews or friendly conversations, for example for summarizing meetings or finding parts of a conversation where people are especially excited or engaged, conversational hot spots that can help in meeting summarization. Detecting the personality of a user—such as whether the user is an extrovert or the extent to which they are open to experience—can help improve conversational agents, which seem to work better if they match users’ personality expectations (Mairesse and Walker, 2008). And affect is important for generation as well as recognition; synthesizing affect is important for conversational agents in various domains, including literacy tutors such as children’s storybooks, or computer games.

In Chapter 4 we introduced the use of naive Bayes classification to classify a document’s sentiment. Various classifiers have been successfully applied to many of these tasks, using all the words in the training set as input to a classifier which then determines the affect status of the text.

In this chapter we focus on an alternative model, in which instead of using every word as a feature, we focus only on certain words, ones that carry particularly strong cues to affect or sentiment. We call these lists of words affective lexicons or sentiment lexicons. These lexicons presuppose a fact about semantics: that words have affective meanings or connotations. The word connotation has different meanings in different fields, but here we use it to mean the aspects of a word’s meaning that are related to a writer or reader’s emotions, sentiment, opinions, or evaluations. In addition to their ability to help determine the affective status of a text, connotation lexicons can be useful features for other kinds of affective tasks, and for computational social science analysis.

In the next sections we introduce basic theories of emotion, show how sentiment lexicons are a special case of emotion lexicons, and mention some useful lexicons. We then survey three ways for building lexicons: human labeling, semi-supervised, and supervised. Finally, we talk about how to detect affect toward a particular entity, and introduce connotation frames.

21.1 Defining Emotion

One of the most important affective classes is emotion, which Scherer (2000) defines as a “relatively brief episode of response to the evaluation of an external or internal event as being of major significance”.

Detecting emotion has the potential to improve a number of language processing tasks. Emotion recognition could help dialogue systems like tutoring systems detect that a student was unhappy, bored, hesitant, confident, and so on. Automatically detecting emotions in reviews or customer responses (anger, dissatisfaction, trust) could help businesses recognize specific problem areas or ones that are going well. Emotion can play a role in medical NLP tasks like helping diagnose depression or suicidal intent. Detecting emotions expressed toward characters in novels might play a role in understanding how different social groups were viewed by society at different times.

Computational models of emotion in NLP have mainly been based on two families of theories of emotion (out of the many studied in the field of affective science). In one of these families, emotions are viewed as fixed atomic units, limited in number, and from which others are generated, often called basic emotions (Tomkins
a model dating back to Darwin. Perhaps the most well-known of this family of theories are the 6 emotions proposed by Ekman (e.g., Ekman 1999) to be universally present in all cultures: *surprise, happiness, anger, fear, disgust, sadness*. Another atomic theory is the Plutchik (1980) wheel of emotion, consisting of 8 basic emotions in four opposing pairs: *joy–sadness, anger–fear, trust–disgust,* and *anticipation–surprise*, together with the emotions derived from them, shown in Fig. 21.2.

![Figure 21.2 Plutchik wheel of emotion.](image)

The second class of emotion theories widely used in NLP views emotion as a space in 2 or 3 dimensions (Russell, 1980). Most models include the two dimensions *valence* and *arousal*, and many add a third, *dominance*. These can be defined as:

- **valence**: the pleasantness of the stimulus
- **arousal**: the level of alertness, activeness, or energy provoked by the stimulus
- **dominance**: the degree of control or dominance exerted by the stimulus or the emotion

Sentiment can be viewed as a special case of this second view of emotions as points in space. In particular, the *valence* dimension, measuring how pleasant or unpleasant a word is, is often used directly as a measure of sentiment.

In these lexicon-based models of affect, the affective meaning of a word is generally fixed, irrespective of the linguistic context in which a word is used, or the dialect or culture of the speaker. By contrast, other models in affective science represent emotions as much richer processes involving cognition (Barrett et al., 2007). In *appraisal theory*, for example, emotions are complex processes, in which a person considers how an event is congruent with their goals, taking into account variables like the agency, certainty, urgency, novelty and control associated with the event (Moors et al., 2013). Computational models in NLP taking into account these richer theories of emotion will likely play an important role in future work.
21.2 Available Sentiment and Affect Lexicons

A wide variety of affect lexicons have been created and released. The most basic lexicons label words along one dimension of semantic variability, generally called “sentiment” or “valence”.

In the simplest lexicons this dimension is represented in a binary fashion, with a wordlist for positive words and a wordlist for negative words. The oldest is the General Inquirer (Stone et al., 1966), which drew on content analysis and on early work in the cognitive psychology of word meaning (Osgood et al., 1957). The General Inquirer has a lexicon of 1915 positive words and a lexicon of 2291 negative words (as well as other lexicons discussed below). The MPQA Subjectivity lexicon (Wilson et al., 2005) has 2718 positive and 4912 negative words drawn from prior lexicons plus a bootstrapped list of subjective words and phrases (Riloff and Wiebe, 2003). Each entry in the lexicon is hand-labeled for sentiment and also labeled for reliability (strongly subjective or weakly subjective). The polarity lexicon of Hu and Liu (2004b) gives 2006 positive and 4783 negative words, drawn from product reviews, labeled using a bootstrapping method from WordNet.

| Positive | admire, amazing, assure, celebration, charm, eager, enthusiastic, excellent, fancy, fantastic, frolic, graceful, happy, joy, luck, majesty, mercy, nice, patience, perfect, proud, rejoice, relief, respect, satisfactorily, sensational, super, terrific, thank, vivid, wise, wonderful, zest |
| Negative | abominable, anger, anxious, bad, catastrophe, cheap, complaint, condescending, deceit, defective, disappointment, embarrass, fake, fear, filthy, fool, guilt, hate, idiot, inflict, lazy, miserable, mourn, nervous, objection, pest, plot, reject, scream, silly, terrible, unfriendly, vile, wicked |

The NRC Valence, Arousal, and Dominance (VAD) lexicon (Mohammad, 2018a) assigns valence, arousal, and dominance scores to 20,000 words. Some examples are shown in Fig. 21.4.

<table>
<thead>
<tr>
<th>Valence</th>
<th>Arousal</th>
<th>Dominance</th>
</tr>
</thead>
<tbody>
<tr>
<td>vacation</td>
<td>.840</td>
<td>enraged</td>
</tr>
<tr>
<td>delightful</td>
<td>.918</td>
<td>party</td>
</tr>
<tr>
<td>whistle</td>
<td>.653</td>
<td>organized</td>
</tr>
<tr>
<td>consolation</td>
<td>.408</td>
<td>effortless</td>
</tr>
<tr>
<td>torture</td>
<td>.115</td>
<td>napping</td>
</tr>
</tbody>
</table>

The NRC Word-Emotion Association Lexicon, also called EmoLex (Mohammad and Turney, 2013), uses the Plutchik (1980) 8 basic emotions defined above. The lexicon includes around 14,000 words including words from prior lexicons as well as frequent nouns, verbs, adverbs and adjectives. Values from the lexicon for some sample words:
21.3 Creating Affect Lexicons by Human Labeling

For a smaller set of 5,814 words, the NRC Emotion/Affect Intensity Lexicon (Mohammad, 2018b) contains real-valued scores of association for anger, fear, joy, and sadness; Fig. 21.5 shows examples.

<table>
<thead>
<tr>
<th>Word</th>
<th>Anger</th>
<th>Fear</th>
<th>Joy</th>
<th>Sadness</th>
<th>Surprise</th>
<th>Trust</th>
<th>Positive</th>
<th>Negative</th>
</tr>
</thead>
<tbody>
<tr>
<td>reward</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>worry</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>tenderness</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>sweetheart</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>suddenly</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>thirst</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>garbage</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure 21.5 Sample emotional intensities for words for anger, fear, joy, and sadness from Mohammad (2018b).

LIWC, Linguistic Inquiry and Word Count, is a widely used set of 73 lexicons containing over 2300 words (Pennebaker et al., 2007), designed to capture aspects of lexical meaning relevant for social psychological tasks. In addition to sentiment-related lexicons like ones for negative emotion (bad, weird, hate, problem, tough) and positive emotion (love, nice, sweet), LIWC includes lexicons for categories like anger, sadness, cognitive mechanisms, perception, tentative, and inhibition, shown in Fig. 21.6.

There are various other hand-built affective lexicons. The General Inquirer includes additional lexicons for dimensions like strong vs. weak, active vs. passive, overstated vs. understated, as well as lexicons for categories like pleasure, pain, virtue, vice, motivation, and cognitive orientation.

Another useful feature for various tasks is the distinction between concrete words like banana or bathrobe and abstract words like belief and although. The lexicon in Brysbaert et al. (2014) used crowdsourcing to assign a rating from 1 to 5 of the concreteness of 40,000 words, thus assigning banana, bathrobe, and bagel 5, belief 1.19, although 1.07, and in between words like brisk a 2.5.

21.3 Creating Affect Lexicons by Human Labeling

The earliest method used to build affect lexicons, and still in common use, is to have humans label each word. This is now most commonly done via crowdsourcing: breaking the task into small pieces and distributing them to a large number of anno-
## Lexicons for Sentiment, Affect, and Connotation

### Figure 21.6
Samples from 5 of the 73 lexical categories in LIWC (Pennebaker et al., 2007).
The * means the previous letters are a word prefix and all words with that prefix are included in the category.

<table>
<thead>
<tr>
<th>Positive Emotion</th>
<th>Negative Emotion</th>
<th>Insight</th>
<th>Inhibition</th>
<th>Family</th>
<th>Negate</th>
</tr>
</thead>
<tbody>
<tr>
<td>appreciat*</td>
<td>anger*</td>
<td>aware*</td>
<td>avoid*</td>
<td>brother*</td>
<td>aren’t</td>
</tr>
<tr>
<td>comfort*</td>
<td>bore*</td>
<td>believe</td>
<td>careful*</td>
<td>cousin*</td>
<td>cannot</td>
</tr>
<tr>
<td>great</td>
<td>cry</td>
<td>decid*</td>
<td>hesitat*</td>
<td>daughter*</td>
<td>didn’t</td>
</tr>
<tr>
<td>happy</td>
<td>despair*</td>
<td>feel</td>
<td>limit*</td>
<td>family</td>
<td>neither</td>
</tr>
<tr>
<td>interest</td>
<td>fail*</td>
<td>figur*</td>
<td>oppos*</td>
<td>father*</td>
<td>never</td>
</tr>
<tr>
<td>joy*</td>
<td>fear</td>
<td>know</td>
<td>prevent*</td>
<td>grandf*</td>
<td>no</td>
</tr>
<tr>
<td>perfect*</td>
<td>griev*</td>
<td>knew</td>
<td>relucan*</td>
<td>grandm*</td>
<td>nobod*</td>
</tr>
<tr>
<td>please*</td>
<td>hate*</td>
<td>means</td>
<td>safe*</td>
<td>husband</td>
<td>none</td>
</tr>
<tr>
<td>safe*</td>
<td>panic*</td>
<td>notice*</td>
<td>stop</td>
<td>mom</td>
<td>nor</td>
</tr>
<tr>
<td>terrific</td>
<td>suffers</td>
<td>recogni*</td>
<td>stubborn*</td>
<td>mother</td>
<td>nothing</td>
</tr>
<tr>
<td>value</td>
<td>terrify</td>
<td>sense</td>
<td>wait</td>
<td>niece*</td>
<td>nowhere</td>
</tr>
<tr>
<td>wow*</td>
<td>violent*</td>
<td>think</td>
<td>wary</td>
<td>wife</td>
<td>without</td>
</tr>
</tbody>
</table>

### -tators. Let's take a look at some of the methodological choices for two crowdsourced emotion lexicons.

The NRC Emotion Lexicon (EmoLex) (Mohammad and Turney, 2013), labeled emotions in two steps. To ensure that the annotators were judging the correct sense of the word, they first answered a multiple-choice synonym question that primed the correct sense of the word (without requiring the annotator to read a potentially confusing sense definition). These were created automatically using the headwords associated with the thesaurus category of the sense in question in the Macquarie dictionary and the headwords of 3 random distractor categories. An example:

Which word is closest in meaning (most related) to startle?

- automobile
- shake
- honesty
- entertain

For each word (e.g. startle), the annotator was then asked to rate how associated that word is with each of the 8 emotions (joy, fear, anger, etc.). The associations were rated on a scale of not, weakly, moderately, and strongly associated. Outlier ratings were removed, and then each term was assigned the class chosen by the majority of the annotators, with ties broken by choosing the stronger intensity, and then the 4 levels were mapped into a binary label for each word (no and weak mapped to 0, moderate and strong mapped to 1).

The NRC VAD Lexicon (Mohammad, 2018a) was built by selecting words and emoticons from prior lexicons and annotating them with crowd-sourcing using **best-worst scaling** (Louviere et al. 2015, Kiritchenko and Mohammad 2017). In best-worst scaling, annotators are given N items (usually 4) and are asked which item is the best (highest) and which is the worst (lowest) in terms of some property. The set of words used to describe the ends of the scales are taken from prior literature. For valence, for example, the raters were asked:

Q1. Which of the four words below is associated with the MOST happiness / pleasure / positiveness / satisfaction / contentedness / hopefulness OR LEAST unhappiness / annoyance / negativeness / dissatisfaction /
21.4 • Semi-supervised Induction of Affect Lexicons

Another common way to learn sentiment lexicons is to start from a set of seed words that define two poles of a semantic axis (words like good or bad), and then find ways to label each word \( w \) by its similarity to the two seed sets. Here we summarize two families of seed-based semi-supervised lexicon induction algorithms, axis-based and graph-based.

### 21.4.1 Semantic Axis Methods

One of the most well-known lexicon induction methods, the Turney and Littman (2003) algorithm, is given seed words like good or bad, and then for each word \( w \) to be labeled, measures both how similar it is to good and how different it is from bad. Here we describe a slight extension of the algorithm due to An et al. (2018), which is based on computing a semantic axis.

In the first step, we choose seed words by hand. There are two methods for dealing with the fact that the affect of a word is different in different contexts: (1) start with a single large seed lexicon and rely on the induction algorithm to fine-tune it to the domain, or (2) choose different seed words for different genres. Hellrich et al. (2019) suggests that for modeling affect across different historical time periods, starting with a large modern affect dictionary is better than small seedsets tuned to be stable across time. As an example of the second approach, Hamilton et al. (2016a) define one set of seed words for general sentiment analysis, a different set for Twitter, and yet another set for sentiment in financial text:

<table>
<thead>
<tr>
<th>Domain</th>
<th>Positive seeds</th>
<th>Negative seeds</th>
</tr>
</thead>
<tbody>
<tr>
<td>General</td>
<td>good, lovely, excellent, fortunate, pleasant, delightful, perfect, loved, love, happy</td>
<td>bad, horrible, poor, unfortunate, unpleasant, disgusting, evil, hated, hate, unhappy</td>
</tr>
<tr>
<td>Twitter</td>
<td>love, loved, loves, awesome, nice, amazing, best, fantastic, correct, happy</td>
<td>hate, hated, hates, terrible, nasty, awful, worst, horrible, wrong, sad</td>
</tr>
<tr>
<td>Finance</td>
<td>successful, excellent, profit, beneficial, improving, improved, success, gains, positive</td>
<td>negligent, loss, volatile, wrong, losses, damages, bad, litigation, failure, down, negative</td>
</tr>
</tbody>
</table>

In the second step, we compute embeddings for each of the pole words. These embeddings can be off-the-shelf word2vec embeddings, or can be computed directly
on a specific corpus (for example using a financial corpus if a finance lexicon is the goal), or we can fine-tune off-the-shelf embeddings to a corpus. Fine-tuning is especially important if we have a very specific genre of text but don’t have enough data to train good embeddings. In fine-tuning, we begin with off-the-shelf embeddings like word2vec, and continue training them on the small target corpus.

Once we have embeddings for each pole word, we create an embedding that represents each pole by taking the centroid of the embeddings of each of the seed words; recall that the centroid is the multidimensional version of the mean. Given a set of embeddings for the positive seed words \( S^+ = \{E(w^+_1), E(w^+_2), ..., E(w^+_n)\} \), and embeddings for the negative seed words \( S^- = \{E(w^-_1), E(w^-_2), ..., E(w^-_m)\} \), the pole centroids are:

\[
V^+ = \frac{1}{n} \sum_{i=1}^{n} E(w^+_i) \\
V^- = \frac{1}{m} \sum_{i=1}^{m} E(w^-_i) 
\] (21.1)

The semantic axis defined by the poles is computed just by subtracting the two vectors:

\[
V_{\text{axis}} = V^+ - V^- 
\] (21.2)

\( V_{\text{axis}} \), the semantic axis, is a vector in the direction of positive sentiment. Finally, we compute (via cosine similarity) the angle between the vector in the direction of positive sentiment and the direction of \( w \)'s embedding. A higher cosine means that \( w \) is more aligned with \( S^+ \) than \( S^- \).

\[
\text{score}(w) = \cos(E(w), V_{\text{axis}}) = \frac{E(w) \cdot V_{\text{axis}}}{\|E(w)\| \|V_{\text{axis}}\|} 
\] (21.3)

If a dictionary of words with sentiment scores is sufficient, we’re done! Or if we need to group words into a positive and a negative lexicon, we can use a threshold or other method to give us discrete lexicons.

### 21.4.2 Label Propagation

An alternative family of methods defines lexicons by propagating sentiment labels on graphs, an idea suggested in early work by Hatzivassiloglou and McKeown (1997). We’ll describe the simple SentProp (Sentiment Propagation) algorithm of Hamilton et al. (2016a), which has four steps:

1. **Define a graph:** Given word embeddings, build a weighted lexical graph by connecting each word with its \( k \) nearest neighbors (according to cosine similarity). The weights of the edge between words \( w_i \) and \( w_j \) are set as:
   
   \[
   E_{i,j} = \arccos \left( -\frac{w_i^\top w_j}{\|w_i\| \|w_j\|} \right) .  
   \] (21.4)

2. **Define a seed set:** Choose positive and negative seed words.

3. **Propagate polarities from the seed set:** Now we perform a random walk on this graph, starting at the seed set. In a random walk, we start at a node and
then choose a node to move to with probability proportional to the edge probability. A word’s polarity score for a seed set is proportional to the probability of a random walk from the seed set landing on that word (Fig. 21.7).

4. Create word scores: We walk from both positive and negative seed sets, resulting in positive (`\text{rawscore}^+(w_i)`) and negative (`\text{rawscore}^-(w_i)`) raw label scores. We then combine these values into a positive-polarity score as:

\[
\text{score}^+(w_i) = \frac{\text{rawscore}^+(w_i)}{\text{rawscore}^+(w_i) + \text{rawscore}^-(w_i)}
\] (21.5)

It’s often helpful to standardize the scores to have zero mean and unit variance within a corpus.

5. Assign confidence to each score: Because sentiment scores are influenced by the seed set, we’d like to know how much the score of a word would change if a different seed set is used. We can use bootstrap sampling to get confidence regions, by computing the propagation `B` times over random subsets of the positive and negative seed sets (for example using `B = 50` and choosing 7 of the 10 seed words each time). The standard deviation of the bootstrap sampled polarity scores gives a confidence measure.

![Figure 21.7](image)

**Figure 21.7** Intuition of the SENTPROP algorithm. (a) Run random walks from the seed words. (b) Assign polarity scores (shown here as colors green or red) based on the frequency of random walk visits.

### 21.4.3 Other Methods

The core of semisupervised algorithms is the metric for measuring similarity with the seed words. The Turney and Littman (2003) and Hamilton et al. (2016a) approaches above used embedding cosine as the distance metric: words were labeled as positive basically if their embeddings had high cosines with positive seeds and low cosines with negative seeds. Other methods have chosen other kinds of distance metrics besides embedding cosine.

For example the Hatzivassiloglou and McKeown (1997) algorithm uses syntactic cues; two adjectives are considered similar if they were frequently conjoined by `and` and rarely conjoined by `but`. This is based on the intuition that adjectives conjoined by the words `and` tend to have the same polarity; positive adjectives are generally coordinated with positive, negative with negative:

- fair and legitimate, corrupt and brutal

but less often positive adjectives coordinated with negative:

*fair and brutal, *corrupt and legitimate

By contrast, adjectives conjoined by `but` are likely to be of opposite polarity:
fair but brutal

Another cue to opposite polarity comes from morphological negation (un-, im-, -less). Adjectives with the same root but differing in a morphological negative (adequate/inadequate, thoughtful/thoughtless) tend to be of opposite polarity.

Yet another method for finding words that have a similar polarity to seed words is to make use of a thesaurus like WordNet (Kim and Hovy 2004, Hu and Liu 2004b). A word’s synonyms presumably share its polarity while a word’s antonyms probably have the opposite polarity. After a seed lexicon is built, each lexicon is updated as follows, possibly iterated.

Lex+: Add synonyms of positive words (well) and antonyms (like fine) of negative words
Lex−: Add synonyms of negative words (awful) and antonyms (like evil) of positive words

An extension of this algorithm assigns polarity to WordNet senses, called SentiWordNet (Baccianella et al., 2010). Fig. 21.8 shows some examples.

<table>
<thead>
<tr>
<th>Synset</th>
<th>Pos</th>
<th>Neg</th>
<th>Obj</th>
</tr>
</thead>
<tbody>
<tr>
<td>good#6 ‘agreeable or pleasing’</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>respectable#2 honorable#4 good#4 estimable#2 ‘deserving of esteem’</td>
<td>0.75</td>
<td>0</td>
<td>0.25</td>
</tr>
<tr>
<td>estimable#3 computable#1 ‘may be computed or estimated’</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>sting#1 burn#4 bite#2 ‘cause a sharp or stinging pain’</td>
<td>0</td>
<td>0.875</td>
<td>.125</td>
</tr>
<tr>
<td>acute#6 ‘of critical importance and consequence’</td>
<td>0.625</td>
<td>0.125</td>
<td>.250</td>
</tr>
<tr>
<td>acute#4 ‘of an angle; less than 90 degrees’</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>acute#1 ‘having or experiencing a rapid onset and short but severe course’</td>
<td>0</td>
<td>0.5</td>
<td>0.5</td>
</tr>
</tbody>
</table>

In this algorithm, polarity is assigned to entire synsets rather than words. A positive lexicon is built from all the synsets associated with 7 positive words, and a negative lexicon from synsets associated with 7 negative words. A classifier is then trained from this data to take a WordNet gloss and decide if the sense being defined is positive, negative or neutral. A further step (involving a random-walk algorithm) assigns a score to each WordNet synset for its degree of positivity, negativity, and neutrality.

In summary, semisupervised algorithms use a human-defined set of seed words for the two poles of a dimension, and use similarity metrics like embedding cosine, coordination, morphology, or thesaurus structure to score words by how similar they are to the positive seeds and how dissimilar to the negative seeds.

21.5 Supervised Learning of Word Sentiment

Semi-supervised methods require only minimal human supervision (in the form of seed sets). But sometimes a supervision signal exists in the world and can be made use of. One such signal is the scores associated with online reviews.

The web contains an enormous number of online reviews for restaurants, movies, books, or other products, each of which have the text of the review along with an
Movie review excerpts (IMDb)

10 A great movie. This film is just a wonderful experience. It’s surreal, zany, witty and slapstick all at the same time. And terrific performances too.

1 This was probably the worst movie I have ever seen. The story went nowhere even though they could have done some interesting stuff with it.

Restaurant review excerpts (Yelp)

5 The service was impeccable. The food was cooked and seasoned perfectly... The watermelon was perfectly square ... The grilled octopus was ... mouthwatering...

2 ...it took a while to get our waters, we got our entree before our starter, and we never received silverware or napkins until we requested them...

Book review excerpts (GoodReads)

1 I am going to try and stop being deceived by eye-catching titles. I so wanted to like this book and was so disappointed by it.

5 This book is hilarious. I would recommend it to anyone looking for a satirical read with a romantic twist and a narrator that keeps butting in

Product review excerpts (Amazon)

5 The lid on this blender though is probably what I like the best about it... enables you to pour into something without even taking the lid off! ... the perfect pitcher! ... works fantastic.

1 I hate this blender... It is nearly impossible to get frozen fruit and ice to turn into a smoothie... You have to add a TON of liquid. I also wish it had a spout ...

Figure 21.9 Excerpts from some reviews from various review websites, all on a scale of 1 to 5 stars except IMDb, which is on a scale of 1 to 10 stars.

associated review score: a value that may range from 1 star to 5 stars, or scoring 1 to 10. Fig. 21.9 shows samples extracted from restaurant, book, and movie reviews.

We can use this review score as supervision: positive words are more likely to appear in 5-star reviews; negative words in 1-star reviews. And instead of just a binary polarity, this kind of supervision allows us to assign a word a more complex representation of its polarity: its distribution over stars (or other scores).

Thus in a ten-star system we could represent the sentiment of each word as a 10-tuple, each number a score representing the word’s association with that polarity level. This association can be a raw count, or a likelihood $P(w|c)$, or some other function of the count, for each class $c$ from 1 to 10.

For example, we could compute the IMDb likelihood of a word like disappointing occurring in a 1 star review by dividing the number of times disappointing occurs in 1-star reviews in the IMDb dataset (8,557) by the total number of words occurring in 1-star reviews (25,395,214), so the IMDb estimate of $P(\text{disappointing}|1)$ is .0003.

A slight modification of this weighting, the normalized likelihood, can be used as an illuminating visualization (Potts, 2011)\(^1\)

$$P(w|c) = \frac{\text{count}(w,c)}{\sum_{w\in c}\text{count}(w,c)}$$

$$\text{PottsScore}(w) = \frac{P(w|c)}{\sum_c P(w|c)} \quad (21.6)$$

Dividing the IMDb estimate $P(\text{disappointing}|1)$ of .0003 by the sum of the likelihood $P(w|c)$ over all categories gives a Potts score of 0.10. The word disappointing thus is associated with the vector [.10, .12, .14, .14, .13, .11, .08, .06, .06, .05]. The

\(^1\) Each element of the Potts score of a word $w$ and category $c$ can be shown to be a variant of the pointwise mutual information $\text{pmi}(w,c)$ without the log term; see Exercise 25.1.
Potts diagram (Potts, 2011) is a visualization of these word scores, representing the prior sentiment of a word as a distribution over the rating categories.

Fig. 21.10 shows the Potts diagrams for 3 positive and 3 negative scalar adjectives. Note that the curve for strongly positive scalars have the shape of the letter J, while strongly negative scalars look like a reverse J. By contrast, weakly positive and negative scalars have a hump-shape, with the maximum either below the mean (weakly negative words like disappointing) or above the mean (weakly positive words like good). These shapes offer an illuminating typology of affective meaning.

Fig. 21.10 Potts diagrams (Potts, 2011) for positive and negative scalar adjectives, showing the J-shape and reverse J-shape for strongly positive and negative adjectives, and the hump-shape for more weakly polarized adjectives.

Fig. 21.11 shows the Potts diagrams for emphasizing and attenuating adverbs. Note that emphatics tend to have a J-shape (most likely to occur in the most positive reviews) or a U-shape (most likely to occur in the strongly positive and negative). Attenuators all have the hump-shape, emphasizing the middle of the scale and downplaying both extremes. The diagrams can be used both as a typology of lexical sentiment, and also play a role in modeling sentiment compositionality.

In addition to functions like posterior $P(c|w)$, likelihood $P(w|c)$, or normalized likelihood (Eq. 21.6) many other functions of the count of a word occurring with a sentiment label have been used. We’ll introduce some of these on page 476, including ideas like normalizing the counts per writer in Eq. 21.14.

21.5.1 Log Odds Ratio Informative Dirichlet Prior

One thing we often want to do with word polarity is to distinguish between words that are more likely to be used in one category of texts than in another. We may, for example, want to know the words most associated with 1 star reviews versus those associated with 5 star reviews. These differences may not be just related to sentiment. We might want to find words used more often by Democratic than Republican members of Congress, or words used more often in menus of expensive restaurants
Instead, let’s compute the number of words in corpus $i$ if using word to be.

Another large corpus to get a prior estimate of what we expect the frequency of each one particular category of texts compared to another. It’s based on the idea of using a particularly useful method for finding words that are statistically overrepresented in “log odds ratio informative Dirichlet prior” method of Monroe et al. (2008) that is a different since all counts are large.

Counts there may be statistical fluctuations, or even zero occurrences in one corpus. Rare words will seem to occur very differently in the two corpora since with tiny counts there may be statistical fluctuations, or even zero occurrences in one corpus compared to non-zero occurrences in the other. Very frequent words will also seem different since all counts are large.

In this section we walk through the details of one solution to this problem: the “log odds ratio informative Dirichlet prior” method of Monroe et al. (2008) that is a particularly useful method for finding words that are statistically overrepresented in one particular category of texts compared to another. It’s based on the idea of using another large corpus to get a prior estimate of what we expect the frequency of each word to be.

Let’s start with the goal: assume we want to know whether the word horrible occurs more in corpus $i$ or corpus $j$. We could compute the log likelihood ratio, using $f^i(w)$ to mean the frequency of word $w$ in corpus $i$, and $n^i$ to mean the total number of words in corpus $i$:

$$ \text{llr}(\text{horrible}) = \log \frac{P^i(\text{horrible})}{P^j(\text{horrible})} $$
$$ = \log f^i(\text{horrible}) - \log P^j(\text{horrible}) $$
$$ = \log \frac{f^i(\text{horrible})}{n^i} - \log \frac{f^j(\text{horrible})}{n^j} \quad (21.7) $$

Instead, let’s compute the log odds ratio: does horrible have higher odds in $i$ or in
$j$:  
\[
\text{lor}(\text{horrible}) = \log \left( \frac{P^i(\text{horrible})}{1 - P^i(\text{horrible})} \right) - \log \left( \frac{P^j(\text{horrible})}{1 - P^j(\text{horrible})} \right)
\]
\[
= \log \left( \frac{\tilde{f}(\text{horrible})}{n^i} \right) - \log \left( \frac{\tilde{f}(\text{horrible})}{n^j} \right)
\]
\[
= \log \left( \frac{\tilde{f}(\text{horrible})}{n^i - \tilde{f}(\text{horrible})} \right) - \log \left( \frac{\tilde{f}(\text{horrible})}{n^j - \tilde{f}(\text{horrible})} \right)
\]
(21.8)

The Dirichlet intuition is to use a large background corpus to get a prior estimate of what we expect the frequency of each word $w$ to be. We’ll do this very simply by adding the counts from that corpus to the numerator and denominator, so that we’re essentially shrinking the counts toward that prior. It’s like asking how large are the differences between $i$ and $j$ given what we would expect given their frequencies in a well-estimated large background corpus.

The method estimates the difference between the frequency of word $w$ in two corpora $i$ and $j$ via the prior-modified log odds ratio for $w$, $\delta_w^{(i-j)}$, which is estimated as:

\[
\delta_w^{(i-j)} = \log \left( \frac{f_w^i + \alpha_w}{n^i + \alpha_w} \right) - \log \left( \frac{f_w^j + \alpha_w}{n^j + \alpha_w} \right)
\]
(21.9)

(where $n^i$ is the size of corpus $i$, $n^j$ is the size of corpus $j$, $f_w^i$ is the count of word $w$ in corpus $i$, $f_w^j$ is the count of word $w$ in corpus $j$, $\alpha_0$ is the scaled size of the background corpus, and $\alpha_w$ is the scaled count of word $w$ in the background corpus.)

In addition, Monroe et al. (2008) make use of an estimate for the variance of the log–odds–ratio:

\[
\sigma^2(\delta_w^{(i-j)}) \approx \frac{1}{f_w^i + \alpha_w} + \frac{1}{f_w^j + \alpha_w}
\]
(21.10)

The final statistic for a word is then the $z$–score of its log–odds–ratio:

\[
\frac{\delta_w^{(i-j)}}{\sqrt{\sigma^2(\delta_w^{(i-j)})}}
\]
(21.11)

The Monroe et al. (2008) method thus modifies the commonly used log odds ratio in two ways: it uses the $z$-scores of the log odds ratio, which controls for the amount of variance in a word’s frequency, and it uses counts from a background corpus to provide a prior count for words.

Fig. 21.12 shows the method applied to a dataset of restaurant reviews from Yelp, comparing the words used in 1-star reviews to the words used in 5-star reviews (Jurafsky et al., 2014). The largest difference is in obvious sentiment words, with the 1-star reviews using negative sentiment words like worse, bad, awful and the 5-star reviews using positive sentiment words like great, best, amazing. But there are other illuminating differences. 1-star reviews use logical negation (no, not), while 5-star reviews use emphatics and emphasize universality (very, highly, every, always). 1-star reviews use first person plurals (we, us, our) while 5 star reviews use the second person. 1-star reviews talk about people (manager, waiter, customer) while 5-star reviews talk about dessert and properties of expensive restaurants like courses and atmosphere. See Jurafsky et al. (2014) for more details.
### Sentiment Recognition

**Figure 21.12** The top 50 words associated with one-star and five-star restaurant reviews in a Yelp dataset of 900,000 reviews, using the Monroe et al. (2008) method (Jurafsky et al., 2014).

#### 21.6 Using Lexicons for Sentiment Recognition

In Chapter 4 we introduced the naive Bayes algorithm for sentiment analysis. The lexicons we have focused on throughout the chapter so far can be used in a number of ways to improve sentiment detection.

In the simplest case, lexicons can be used when we don’t have sufficient training data to build a supervised sentiment analyzer; it can often be expensive to have a human assign sentiment to each document to train the supervised classifier.

In such situations, lexicons can be used in a rule-based algorithm for classification. The simplest version is just to use the ratio of positive to negative words: if a document has more positive than negative words (using the lexicon to decide the polarity of each word in the document), it is classified as positive. Often a threshold \( \lambda \) is used, in which a document is classified as positive only if the ratio is greater than \( \lambda \). If the sentiment lexicon includes positive and negative weights for each word, \( \theta^+_w \) and \( \theta^-_w \), these can be used as well. Here’s a simple such sentiment algorithm:

\[
\begin{align*}
    f^+ &= \sum_{w \text{ s.t. } w \in \text{positivelexicon}} \theta^+_w \cdot \text{count}(w) \\
    f^- &= \sum_{w \text{ s.t. } w \in \text{negativelexicon}} \theta^-_w \cdot \text{count}(w) \\
    \text{sentiment} &= \begin{cases} 
    + & \text{if } \frac{f^+}{f^-} > \lambda \\
    - & \text{if } \frac{f^-}{f^+} > \lambda \\
    0 & \text{otherwise.}
    \end{cases}
\end{align*}
\]

(21.12)

If supervised training data is available, these counts computed from sentiment lexicons, sometimes weighted or normalized in various ways, can also be used as features in a classifier along with other lexical or non-lexical features. We return to such algorithms in Section 21.7.
21.7 Using Lexicons for Affect Recognition

Detection of emotion (and the other kinds of affective meaning described by Scherer (2000)) can be done by generalizing the algorithms described above for detecting sentiment.

The most common algorithms involve supervised classification: a training set is labeled for the affective meaning to be detected, and a classifier is built using features extracted from the training set. As with sentiment analysis, if the training set is large enough, and the test set is sufficiently similar to the training set, simply using all the words or all the bigrams as features in a powerful classifier like SVM or logistic regression, as described in Fig. 4.2 in Chapter 4, is an excellent algorithm whose performance is hard to beat. Thus we can treat affective meaning classification of a text sample as simple document classification.

Some modifications are nonetheless often necessary for very large datasets. For example, the Schwartz et al. (2013) study of personality, gender, and age using 700 million words of Facebook posts used only a subset of the n-grams of lengths 1-3. Only words and phrases used by at least 1% of the subjects were included as features, and 2-grams and 3-grams were only kept if they had sufficiently high PMI (PMI greater than $2 \times$ length, where length is the number of words):

$$pmi(phrase) = \log \frac{p(phrase)}{\prod_{w \in phrase} p(w)}$$  \hspace{1cm} (21.13)

Various weights can be used for the features, including the raw count in the training set, or some normalized probability or log probability. Schwartz et al. (2013), for example, turn feature counts into phrase likelihoods by normalizing them by each subject’s total word use.

$$p(phrase|subject) = \frac{freq(phrase, subject)}{\sum_{phrase' \in vocab(subject)} freq(phrase', subject)}$$ \hspace{1cm} (21.14)

If the training data is sparser, or not as similar to the test set, any of the lexicons we’ve discussed can play a helpful role, either alone or in combination with all the words and n-grams.

Many possible values can be used for lexicon features. The simplest is just an indicator function, in which the value of a feature $f_L$ takes the value 1 if a particular text has any word from the relevant lexicon $L$. Using the notation of Chapter 4, in which a feature value is defined for a particular output class $c$ and document $x$.

$$f_L(c, x) = \begin{cases} 1 & \text{if } \exists w : w \in L \& w \in x \& \text{class} = c \\ 0 & \text{otherwise} \end{cases}$$

Alternatively the value of a feature $f_L$ for a particular lexicon $L$ can be the total number of word tokens in the document that occur in $L$:

$$f_L = \sum_{w \in L} count(w)$$

For lexica in which each word is associated with a score or weight, the count can be multiplied by a weight $\theta_w^L$:

$$f_L = \sum_{w \in L} \theta_w^L count(w)$$
Counts can alternatively be logged or normalized per writer as in Eq. 21.14. However they are defined, these lexicon features are then used in a supervised classifier to predict the desired affective category for the text or document. Once a classifier is trained, we can examine which lexicon features are associated with which classes. For a classifier like logistic regression the feature weight gives an indication of how associated the feature is with the class.

### 21.8 Lexicon-based methods for Entity-Centric Affect

What if we want to get an affect score not for an entire document, but for a particular entity in the text? The entity-centric method of Field and Tsvetkov (2019) combines affect lexicons with contextual embeddings to assign an affect score to an entity in text. In the context of affect about people, they relabel the Valence/Arousal/Dominance dimension as Sentiment/Agency/Power. The algorithm first trains classifiers to map embeddings to scores:

1. For each word \( w \) in the training corpus:
   a. Use off-the-shelf pretrained encoders (like BERT) to extract a contextual embedding \( e \) for each instance of the word. No additional fine-tuning is done.
   b. Average over the \( e \) embeddings of each instance of \( w \) to obtain a single embedding vector for one training point \( w \).
   c. Use the NRC VAD Lexicon to get S, A, and P scores for \( w \).
2. Train (three) regression models on all words \( w \) to predict V, A, D scores from a word’s average embedding.

Now given an entity mention \( m \) in a text, we assign affect scores as follows:

1. Use the same pretrained LM to get contextual embeddings for \( m \) in context.
2. Feed this embedding through the 3 regression models to get S, A, P scores for the entity.

This results in a (S,A,P) tuple for a given entity mention; To get scores for the representation of an entity in a complete document, we can run coreference resolution and average the (S,A,P) scores for all the mentions. Fig. 21.13 shows the scores from their algorithm for characters from the movie *The Dark Knight* when run on Wikipedia plot summary texts with gold coreference.

### 21.9 Connotation Frames

The lexicons we’ve described so far define a word as a point in affective space. A connotation frame, by contrast, is a lexicon that incorporates a richer kind of grammatical structure, by combining affective lexicons with the frame semantic lexicons of Chapter 24. The basic insight of connotation frame lexicons is that a predicate like a verb expresses connotations about the verb’s arguments (Rashkin et al. 2016, Rashkin et al. 2017).

Consider sentences like:

(21.15) Country A violated the sovereignty of Country B
Role1 is the sympathetic antagonist. Role2 is a victim.

Connotation Frame for "Role1 violates Role2"

By using the verb violate in (21.15), the author is expressing their sympathies with Country B, portraying Country B as a victim, and expressing antagonism toward the agent Country A. By contrast, in using the verb survive, the author of (21.16) is expressing that the bombing is a negative experience, and the subject of the sentence, the teenager, is a sympathetic character. These aspects of connotation are inherent in the meaning of the verbs violate and survive, as shown in Fig. 21.14.

The connotation frame lexicons of Rashkin et al. (2016) and Rashkin et al. (2017) also express other connotative aspects of the predicate toward each argument, including the effect (something bad happened to x) value: (x is valuable), and mental state: (x is distressed by the event). Connotation frames can also mark the power differential between the arguments (using the verb implore means that the theme argument has greater power than the agent), and the agency of each argument (waited is low agency). Fig. 21.15 shows a visualization from Sap et al. (2017).

Connotation frames can be built by hand (Sap et al., 2017), or they can be learned by supervised learning (Rashkin et al., 2016), for example using hand-labeled train-
21.10 Summary

- Many kinds of affective states can be distinguished, including emotions, moods, attitudes (which include sentiment), interpersonal stance, and personality.

- Emotion can be represented by fixed atomic units often called basic emotions, or as points in space defined by dimensions like valence and arousal.

- Words have connotational aspects related to these affective states, and this connotational aspect of word meaning can be represented in lexicons.

- Affective lexicons can be built by hand, using crowd sourcing to label the affective content of each word.

- Lexicons can be built with semi-supervised, bootstrapping from seed words using similarity metrics like embedding cosine.

- Lexicons can be learned in a fully supervised manner, when a convenient training signal can be found in the world, such as ratings assigned by users on a review site.

- Words can be assigned weights in a lexicon by using various functions of word counts in training texts, and ratio metrics like log odds ratio informative Dirichlet prior.

- Affect can be detected, just like sentiment, by using standard supervised text classification techniques, using all the words or bigrams in a text as features. Additional features can be drawn from counts of words in lexicons.

- Lexicons can also be used to detect affect in a rule-based classifier by picking the simple majority sentiment based on counts of words in each lexicon.

- Connotation frames express richer relations of affective meaning that a predicate encodes about its arguments.
Bibliographical and Historical Notes

The idea of formally representing the subjective meaning of words began with Osgood et al. (1957), the same pioneering study that first proposed the vector space model of meaning described in Chapter 6. Osgood et al. (1957) had participants rate words on various scales, and ran factor analysis on the ratings. The most significant factor they uncovered was the evaluative dimension, which distinguished between pairs like good/bad, valuable/worthless, pleasant/unpleasant. This work influenced the development of early dictionaries of sentiment and affective meaning in the field of content analysis (Stone et al., 1966).

Wiebe (1994) began an influential line of work on detecting subjectivity in text, beginning with the task of identifying subjective sentences and the subjective characters who are described in the text as holding private states, beliefs or attitudes. Learned sentiment lexicons such as the polarity lexicons of Hatzivassiloglou and McKeown (1997) were shown to be a useful feature in subjectivity detection (Hatzivassiloglou and Wiebe 2000, Wiebe 2000).

The term sentiment seems to have been introduced in 2001 by Das and Chen (2001), to describe the task of measuring market sentiment by looking at the words in stock trading message boards. In the same paper Das and Chen (2001) also proposed the use of a sentiment lexicon. The list of words in the lexicon was created by hand, but each word was assigned weights according to how much it discriminated a particular class (say buy versus sell) by maximizing across-class variation and minimizing within-class variation. The term sentiment, and the use of lexicons, caught on quite quickly (e.g., inter alia, Turney 2002). Pang et al. (2002) first showed the power of using all the words without a sentiment lexicon; see also Wang and Manning (2012).

Most of the semi-supervised methods we describe for extending sentiment dictionaries drew on the early idea that synonyms and antonyms tend to co-occur in the same sentence (Miller and Charles 1991, Justeson and Katz 1991, Riloff and Shepherd 1997). Other semi-supervised methods for learning cues to affective meaning rely on information extraction techniques, like the AutoSlog pattern extractors (Riloff and Wiebe, 2003). Graph based algorithms for sentiment were first suggested by Hatzivassiloglou and McKeown (1997), and graph propagation became a standard method (Zhu and Ghahramani 2002, Zhu et al. 2003, Zhou et al. 2004a, Velikovich et al. 2010). Crowdsourcing can also be used to improve precision by filtering the result of semi-supervised lexicon learning (Riloff and Shepherd 1997, Fast et al. 2016).

Much recent work focuses on ways to learn embeddings that directly encode sentiment or other properties, such as the DENSIFIER algorithm of Rothe et al. (2016) that learns to transform the embedding space to focus on sentiment (or other) information.

Exercises

21.1 Show that the relationship between a word $w$ and a category $c$ in the Potts Score in Eq. 21.6 is a variant of the pointwise mutual information $\text{pmi}(w,c)$ without the log term.
An important component of language processing is knowing who is being talked about in a text. Consider the following passage:

(22.1) Victoria Chen, CFO of Megabucks Banking, saw her pay jump to $2.3 million, as the 38-year-old became the company’s president. It is widely known that she came to Megabucks from rival Lotsabucks.

Each of the underlined phrases in this passage is used by the writer to refer to a person named Victoria Chen. We call linguistic expressions like her or Victoria Chen mentions or referring expressions, and the discourse entity that is referred to (Victoria Chen) the referent. (To distinguish between referring expressions and their referents, we italicize the former.)¹ Two or more referring expressions that are used to refer to the same discourse entity are said to corefer; thus, Victoria Chen and she corefer in (22.1).

Coreference is an important component of natural language processing. A dialogue system that has just told the user “There is a 2pm flight on United and a 4pm one on Cathay Pacific” must know which flight the user means by “I’ll take the second one”. A question answering system that uses Wikipedia to answer a question about Marie Curie must know who she was in the sentence “She was born in Warsaw”. And a machine translation system translating from a language like Spanish, in which pronouns can be dropped, must use coreference from the previous sentence to decide whether the Spanish sentence “Me encanta el conocimiento”, dice.” should be translated as “I love knowledge”, he says”, or “I love knowledge”, she says”. Indeed, this example comes from an actual news article in El País about a female professor and was mistranslated as “he” in machine translation because of inaccurate coreference resolution (Schiebinger, 2013).

Natural language processing systems (and humans) interpret linguistic expressions with respect to a discourse model (Karttunen, 1969). A discourse model (Fig. 22.1) is a mental model that the understander builds incrementally when interpreting a text, containing representations of the entities referred to in the text, as well as properties of the entities and relations among them. When a referent is first mentioned in a discourse, we say that a representation for it is evoked into the model. Upon subsequent mention, this representation is accessed from the model.

¹ As a convenient shorthand, we sometimes speak of a referring expression referring to a referent, e.g., saying that she refers to Victoria Chen. However, the reader should keep in mind that what we really mean is that the speaker is performing the act of referring to Victoria Chen by uttering she.
Reference in a text to an entity that has been previously introduced into the discourse is called **anaphora**, and the referring expression used is said to be an **anaphor**, or anaphoric. In passage (22.1), the pronouns *she* and *her* and the definite NP *the 38-year-old* are therefore anaphoric. The anaphor corefers with a prior mention (in this case *Victoria Chen*) that is called the **antecedent**. Not every referring expression is an antecedent. An entity that has only a single mention in a text (like Lotsabucks in (22.1)) is called a **singleton**.

In this chapter we focus on the task of **coreference resolution**. Coreference resolution is the task of determining whether two mentions **corefer**, by which we mean they refer to the same entity in the discourse model (the same **discourse entity**). The set of coreferring expressions is often called a **coreference chain** or a **cluster**. For example, in processing (22.1), a coreference resolution algorithm would need to find at least four coreference chains, corresponding to the four entities in the discourse model in Fig. 22.1.

1. \{Victoria Chen, her, the 38-year-old, She\}
2. \{Megabucks Banking, the company, Megabucks\}
3. \{her pay\}
4. \{Lotsabucks\}

Note that mentions can be nested; for example the mention *her* is syntactically part of another mention, *her pay*, referring to a completely different discourse entity.

Coreference resolution thus comprises two tasks (although they are often performed jointly): (1) identifying the mentions, and (2) clustering them into coreference chains/discourse entities.

We said that two mentions corefered if they are associated with the same **discourse entity**. But often we’d like to go further, deciding which real world entity is associated with this discourse entity. For example, the mention *Washington* might refer to the US state, or the capital city, or the person George Washington; the interpretation of the sentence will of course be very different for each of these. The task of **entity linking** (Ji and Grishman, 2011) or **entity resolution** is the task of mapping a discourse entity to some real-world individual. We usually operationalize entity

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2 We will follow the common NLP usage of *anaphor* to mean any mention that has an antecedent, rather than the more narrow usage to mean only mentions (like pronouns) whose interpretation depends on the antecedent (under the narrower interpretation, repeated names are not anaphors).

3 Computational linguistics/NLP thus differs in its use of the term *reference* from the field of formal semantics, which uses the words *reference* and *coreference* to describe the relation between a mention and a real-world entity. By contrast, we follow the functional linguistics tradition in which a mention refers to a discourse entity (Webber, 1978) and the relation between a discourse entity and the real world individual requires an additional step of linking.
linking or resolution by mapping to an ontology: a list of entities in the world, like a gazeteer (Chapter 19). Perhaps the most common ontology used for this task is Wikipedia; each Wikipedia page acts as the unique id for a particular entity. Thus the entity linking task of *wikification* (Mihalcea and Csomai, 2007) is the task of deciding which Wikipedia page corresponding to an individual is being referred to by a mention. But entity linking can be done with any ontology; for example if we have an ontology of genes, we can link mentions of genes in text to the disambiguated gene name in the ontology.

In the next sections we introduce the task of coreference resolution in more detail, and survey a variety of architectures for resolution. We also introduce two architectures for the task of entity linking.

Before turning to algorithms, however, we mention some important tasks we will only touch on briefly at the end of this chapter. First are the famous Winograd Schema problems (so-called because they were first pointed out by Terry Winograd in his dissertation). These entity coreference resolution problems are designed to be too difficult to be solved by the resolution methods we describe in this chapter, and the kind of real-world knowledge they require has made them a kind of challenge task for natural language processing. For example, consider the task of determining the correct antecedent of the pronoun *they* in the following example:

(22.2) The city council denied the demonstrators a permit because
   a. they feared violence.
   b. they advocated violence.

Determining the correct antecedent for the pronoun *they* requires understanding that the second clause is intended as an explanation of the first clause, and also that city councils are perhaps more likely than demonstrators to fear violence and that demonstrators might be more likely to advocate violence. Solving Winograd Schema problems requires finding way to represent or discover the necessary real world knowledge.

A problem we won’t discuss in this chapter is the related task of *event coreference*, deciding whether two event mentions (such as the *buy* and the *acquisition* in these two sentences from the ECB+ corpus) refer to the same event:

(22.3) AMD agreed to *[buy]* Markham, Ontario-based ATI for around $5.4 billion in cash and stock, the companies announced Monday.

(22.4) The *[acquisition]* would turn AMD into one of the world’s largest providers of graphics chips.

Event mentions are much harder to detect than entity mentions, since they can be verbal as well as nominal. Once detected, the same mention-pair and mention-ranking models used for entities are often applied to events.

An even more complex kind of coreference is *discourse deixis* (Webber, 1988), in which an anaphor refers back to a discourse segment, which can be quite hard to delimit or categorize, like the examples in (22.5) adapted from Webber (1991):

(22.5) According to Soleil, Beau just opened a restaurant
   a. But *that* turned out to be a lie.
   b. But *that* was false.
   c. *That* struck me as a funny way to describe the situation.

The referent of *that* is a speech act (see Chapter 15) in (22.5a), a proposition in (22.5b), and a manner of description in (22.5c). We don’t give algorithms in this chapter for these difficult types of *non-nominal antecedents*, but see Kolhatkar et al. (2018) for a survey.
22.1 Coreference Phenomena: Linguistic Background

We now offer some linguistic background on reference phenomena. We introduce the four types of referring expressions (definite and indefinite NPs, pronouns, and names), describe how these are used to evoke and access entities in the discourse model, and talk about linguistic features of the anaphor/antecedent relation (like number/gender agreement, or properties of verb semantics).

22.1.1 Types of Referring Expressions

Indefinite Noun Phrases: The most common form of indefinite reference in English is marked with the determiner *a* (or *an*), but it can also be marked by a quantifier such as *some* or even the determiner *this*. Indefinite reference generally introduces into the discourse context entities that are new to the hearer.

(22.6)  

a. Mrs. Martin was so very kind as to send Mrs. Goddard *a beautiful goose*.  
b. He had gone round one day to bring her *some walnuts*.  
c. I saw *this beautiful cauliflower* today.

Definite Noun Phrases: Definite reference, such as via NPs that use the English article *the*, refers to an entity that is identifiable to the hearer. An entity can be identifiable to the hearer because it has been mentioned previously in the text and thus is already represented in the discourse model:

(22.7)  

It concerns a white stallion which I have sold to an officer. But the pedigree of *the white stallion* was not fully established.

Alternatively, an entity can be identifiable because it is contained in the hearer’s set of beliefs about the world, or the uniqueness of the object is implied by the description itself, in which case it evokes a representation of the referent into the discourse model, as in (22.9):

(22.8)  

I read about it in the *New York Times*.

(22.9)  

Have you seen the car keys?

These last uses are quite common; more than half of definite NPs in newswire texts are non-anaphoric, often because they are the first time an entity is mentioned (Poesio and Vieira 1998, Bean and Riloff 1999).

Pronouns: Another form of definite reference is pronominalization, used for entities that are extremely salient in the discourse, (as we discuss below):

(22.10)  

Emma smiled and chatted as cheerfully as *she* could.

Pronouns can also participate in cataphora, in which they are mentioned before their referents are, as in (22.11).

(22.11)  

Even before *she saw it*, Dorothy had been thinking about the Emerald City every day.

Here, the pronouns *she and it* both occur before their referents are introduced.

Pronouns also appear in quantified contexts in which they are considered to be bound, as in (22.12).

(22.12)  

Every dancer brought *her* left arm forward.

Under the relevant reading, *her* does not refer to some woman in context, but instead behaves like a variable bound to the quantified expression *every dancer*. We are not concerned with the bound interpretation of pronouns in this chapter.
In some languages, pronouns can appear as clitics attached to a word, like *lo* (‘it’) in this Spanish example from AnCora (Recasens and Martí, 2010):

(22.13) La intención es reconocer el gran prestigio que tiene la maratón y unirlo con esta gran carrera.

‘The aim is to recognize the great prestige that the Marathon has and join it with this great race.’

**Demonstrative Pronouns:** Demonstrative pronouns *this* and *that* can appear either alone or as determiners, for instance, *this ingredient*, *that spice*:

(22.14) I just bought a copy of Thoreau’s *Walden*. I had bought one five years ago. *That one* had been very tattered; *this one* was in much better condition.

Note that *this NP* is ambiguous; in colloquial spoken English, it can be indefinite, as in (22.6), or definite, as in (22.14).

**Zero Anaphora:** Instead of using a pronoun, in some languages (including Chinese, Japanese, and Italian) it is possible to have an anaphor that has no lexical realization at all, called a zero anaphor or zero pronoun, as in the following Italian and Japanese examples from Poesio et al. (2016):

(22.15) EN [John]i went to visit some friends. On the way [he]i bought some wine.

IT [Giovanni]i andò a far visita a degli amici. Per via φi comprò del vino.

JA [John]-wa yujin-o houmon-sita. Tochu-de φi wain-o ka-tta.

or this Chinese example:

(22.16) [我] 前一会精神上太紧张。[0] 现在比较平静了

[I] was too nervous a while ago. … [0] am now calmer.

Zero anaphors complicate the task of mention detection in these languages.

**Names:** Names (such as of people, locations, or organizations) can be used to refer to both new and old entities in the discourse:

(22.17) a. *Miss Woodhouse* certainly had not done him justice.

b. *International Business Machines* sought patent compensation from Amazon; *IBM* had previously sued other companies.

### 22.1.2 Information Status

The way referring expressions are used to evoke new referents into the discourse (introducing new information), or access old entities from the model (old information), is called their information status or information structure. Entities can be discourse-new or discourse-old, and indeed it is common to distinguish at least three kinds of entities informationally (Prince, 1981):

**new NPs:**

- brand new NPs: these introduce entities that are discourse-new and hearer-new like *a fruit* or *some walnuts*.

**unused NPs:** these introduce entities that are discourse-new but hearer-old (like *Hong Kong*, *Marie Curie*, or *the New York Times*).

**old NPs:** also called evoked NPs, these introduce entities that already in the discourse model, hence are both discourse-old and hearer-old, like *it* in “*I went to a new restaurant. It was...*.”
inferrables: these introduce entities that are neither hearer-old nor discourse-old, but the hearer can infer their existence by reasoning based on other entities that are in the discourse. Consider the following examples:

(22.18) I went to a superb restaurant yesterday. The chef had just opened it.
(22.19) Mix flour, butter and water. Knead the dough until shiny.

Neither the chef nor the dough were in the discourse model based on the first sentence of either example, but the reader can make a bridging inference that these entities should be added to the discourse model and associated with the restaurant and the ingredients, based on world knowledge that restaurants have chefs and dough is the result of mixing flour and liquid (Haviland and Clark 1974, Webber and Baldwin 1992, Nissim et al. 2004, Hou et al. 2018).

The form of an NP gives strong clues to its information status. We often talk about an entity’s position on the given-new dimension, the extent to which the referent is given (salient in the discourse, easier for the hearer to call to mind, predictable by the hearer), versus new (non-salient in the discourse, unpredictable) (Chafe 1976, Prince 1981, Gundel et al. 1993). A referent that is very accessible (Ariel, 2001) i.e., very salient in the hearer’s mind or easy to call to mind, can be referred to with less linguistic material. For example pronouns are used only when the referent has a high degree of activation or salience in the discourse model. By contrast, less salient entities, like a new referent being introduced to the discourse, will need to be introduced with a longer and more explicit referring expression to help the hearer recover the referent.

Thus when an entity is first introduced into a discourse its mentions are likely to have full names, titles or roles, or appositive or restrictive relative clauses, as in the introduction of our protagonist in (22.1): Victoria Chen, CFO of Megabucks Banking. As an entity is discussed over a discourse, it becomes more salient to the hearer and its mentions on average typically becomes shorter and less informative, for example with a shortened name (for example Ms. Chen), a definite description (the 38-year-old), or a pronoun (she or her) (Hawkins 1978). However, this change in length is not monotonic, and is sensitive to discourse structure (Grosz 1977b, Reichman 1985, Fox 1993).

22.1.3 Complications: Non-Referring Expressions

Many noun phrases or other nominals are not referring expressions, although they may bear a confusing superficial resemblance. For example in some of the earliest computational work on reference resolution, Karttunen (1969) pointed out that the NP a car in the following example does not create a discourse referent:

(22.20) Janet doesn’t have a car.

and cannot be referred back to by anaphoric it or the car:

(22.21) *It is a Toyota.
(22.22) *The car is red.

We summarize here four common types of structures that are not counted as mentions in coreference tasks and hence complicate the task of mention-detection:

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4 Pronouns also usually (but not always) refer to entities that were introduced no further than one or two sentences back in the ongoing discourse, whereas definite noun phrases can often refer further back.
Appositives: An appositional structure is a noun phrase that appears next to a head noun phrase, describing the head. In English they often appear in commas, like “a unit of UAL” appearing in apposition to the NP United, or CFO of Megabucks Banking in apposition to Victoria Chen.

(22.23) Victoria Chen, CFO of Megabucks Banking, saw ...
(22.24) United, a unit of UAL, matched the fares.

Appositional NPs are not referring expressions, instead functioning as a kind of supplementary parenthetical description of the head NP. Nonetheless, sometimes it is useful to link these phrases to an entity they describe, and so some datasets like OntoNotes mark appositional relationships.

Predicative and Prenominal NPs: Predicative or attributive NPs describe properties of the head noun. In United is a unit of UAL, the NP a unit of UAL describes a property of United, rather than referring to a distinct entity. Thus they are not marked as mentions in coreference tasks; in our example the NPs $2.3 million and the company’s president, are attributive, describing properties of her pay and the 38-year-old; Example (22.27) shows a Chinese example in which the predicate NP (中国最大的城市; China’s biggest city) is not a mention.

(22.25) her pay jumped to $2.3 million
(22.26) the 38-year-old became the company’s president
(22.27) 上海是[中国最大的城市] [Shanghai is China’s biggest city]

Expletives: Many uses of pronouns like it in English and corresponding pronouns in other languages are not referential. Such expletive or pleonastic cases include it is raining, in idioms like hit it off, or in particular syntactic situations like clefts (22.28a) or extraposition (22.28b):

(22.28) a. It was Emma Goldman who founded Mother Earth
     b. It surprised me that there was a herring hanging on her wall.

Generics: Another kind of expression that does not refer back to an entity explicitly evoked in the text is generic reference. Consider (22.29).

(22.29) I love mangos. They are very tasty.

Here, they refers, not to a particular mango or set of mangos, but instead to the class of mangos in general. The pronoun you can also be used generically:

(22.30) In July in San Francisco you have to wear a jacket.

22.1.4 Linguistic Properties of the Coreference Relation

Now that we have seen the linguistic properties of individual referring expressions we turn to properties of the antecedent/anaphor pair. Understanding these properties is helpful both in designing novel features and performing error analyses.

Number Agreement: Referring expressions and their referents must generally agree in number; English she/her/he/him/his/it are singular, we/us/they/them are plural, and you is unspecified for number. So a plural antecedent like the chefs cannot generally corefer with a singular anaphor like she. However, algorithms cannot enforce number agreement too strictly. First, semantically plural entities can be referred to by either it or they:

(22.31) IBM announced a new machine translation product yesterday. They have been working on it for 20 years.
Second, **singular they** has become much more common, in which *they* is used to describe singular individuals, often useful because *they* is gender neutral. Although recently increasing, singular *they* is quite old, part of English for many centuries.\(^5\)

**Person Agreement:** English distinguishes between first, second, and third person, and a pronoun’s antecedent must agree with the pronoun in person. Thus a third person pronoun (*he, she, they, him, her, them, his, her, their*) must have a third person antecedent (one of the above or any other noun phrase). However, phenomena like quotation can cause exceptions; in this example *I, my,* and *she* are coreferent:

(22.32) “I voted for Nader because he was most aligned with my values,” she said.

**Gender or Noun Class Agreement:** In many languages, all nouns have grammatical gender or noun class\(^6\) and pronouns generally agree with the grammatical gender of their antecedent. In English this occurs only with third-person singular pronouns, which distinguish between *male* (*he, him, his*), *female* (*she, her*), and *nonpersonal* (*it*) grammatical genders. Non-binary pronouns like *ze* or *hir* may also occur in more recent texts. Knowing which gender to associate with a name in text can be complex, and may require world knowledge about the individual. Some examples:

(22.33) Maryam has a theorem. She is exciting. (*she=Maryam, not the theorem*)

(22.34) Maryam has a theorem. It is exciting. (*it=the theorem, not Maryam*)

**Binding Theory Constraints:** The *binding theory* is a name for syntactic constraints on the relations between a mention and an antecedent in the same sentence (Chomsky, 1981). Oversimplifying a bit, **reflexive** pronouns like *himself* and *herself* corefer with the subject of the most immediate clause that contains them (22.35), whereas nonreflexives cannot corefer with this subject (22.36).

(22.35) Janet bought **herself** a bottle of fish sauce. [*herself=Janet*]

(22.36) Janet bought **her** a bottle of fish sauce. [*her ≠ Janet*]

**Recency:** Entities introduced in recent utterances tend to be more salient than those introduced from utterances further back. Thus, in (22.37), the pronoun *it* is more likely to refer to Jim’s map than the doctor’s map.

(22.37) The doctor found an old map in the captain’s chest. Jim found an even older map hidden on the shelf. It described an island.

**Grammatical Role:** Entities mentioned in subject position are more salient than those in object position, which are in turn more salient than those mentioned in oblique positions. Thus although the first sentence in (22.38) and (22.39) expresses roughly the same propositional content, the preferred referent for the pronoun *he* varies with the subject—John in (22.38) and Bill in (22.39).

(22.38) Billy Bones went to the bar with Jim Hawkins. He called for a glass of rum. [*he = Billy*]

(22.39) Jim Hawkins went to the bar with Billy Bones. He called for a glass of rum. [*he = Jim*]

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5 Here’s a bound pronoun example from Shakespeare’s *Comedy of Errors*: *There’s not a man I meet but doth salute me As if I were their well-acquainted friend*

6 The word “gender” is generally only used for languages with 2 or 3 noun classes, like most Indo-European languages; many languages, like the Bantu languages or Chinese, have a much larger number of noun classes.
Verb Semantics: Some verbs semantically emphasize one of their arguments, biasing the interpretation of subsequent pronouns. Compare (22.40) and (22.41).

(22.40) John telephoned Bill. He lost the laptop.
(22.41) John criticized Bill. He lost the laptop.

These examples differ only in the verb used in the first sentence, yet “he” in (22.40) is typically resolved to John, whereas “he” in (22.41) is resolved to Bill. This may be partly due to the link between implicit causality and saliency: the implicit cause of a “criticizing” event is its object, whereas the implicit cause of a “telephoning” event is its subject. In such verbs, the entity which is the implicit cause may be more salient.

Selectional Restrictions: Many other kinds of semantic knowledge can play a role in referent preference. For example, the selectional restrictions that a verb places on its arguments (Chapter 24) can help eliminate referents, as in (22.42).

(22.42) I ate the soup in my new bowl after cooking it for hours.

There are two possible referents for it, the soup and the bowl. The verb eat, however, requires that its direct object denote something edible, and this constraint can rule out bowl as a possible referent.

22.2 Coreference Tasks and Datasets

We can formulate the task of coreference resolution as follows: Given a text $T$, find all entities and the coreference links between them. We evaluate our task by comparing the links our system creates with those in human-created gold coreference annotations on $T$.

Let’s return to our coreference example, now using superscript numbers for each coreference chain (cluster), and subscript letters for individual mentions in the cluster:

(22.43) [Victoria Chen]$^1_a$, CFO of [Megabucks Banking]$^2_a$, saw [[her]$^1_b$ pay]$^3_a$ jump to $2.3$ million, as [the 38-year-old]$^1_c$ also became [[the company]$^2_b$’s president. It is widely known that [she]$^1_d$ came to [Megabucks]$^2_b$ from rival [Lotsabucks]$^4_a$.

Assuming example (22.43) was the entirety of the article, the chains for her pay and Lotsabucks are singleton mentions:

1. {Victoria Chen, her, the 38-year-old, She}
2. {Megabucks Banking, the company, Megabucks}
3. {her pay}
4. {Lotsabucks}

For most coreference evaluation campaigns, the input to the system is the raw text of articles, and systems must detect mentions and then link them into clusters. Solving this task requires dealing with pronominal anaphora (figuring out that her refers to Victoria Chen), filtering out non-referential pronouns like the pleonastic It in It has been ten years), dealing with definite noun phrases to figure out that the 38-year-old is coreferent with Victoria Chen, and that the company is the same as Megabucks. And we need to deal with names, to realize that Megabucks is the same as Megabucks Banking.
Exactly what counts as a mention and what links are annotated differs from task to task and dataset to dataset. For example some coreference datasets do not label singletons, making the task much simpler. Resolvers can achieve much higher scores on corpora without singletons, since singletons constitute the majority of mentions in running text, and they are often hard to distinguish from non-referential NPs. Some tasks use gold mention-detection (i.e. the system is given human-labeled mention boundaries and the task is just to cluster these gold mentions), which eliminates the need to detect and segment mentions from running text.

Coreference is usually evaluated by the CoNLL F1 score, which combines three metrics: MUC, B3, and CEAFe; Section 22.8 gives the details.

Let’s mention a few characteristics of one popular coreference dataset, OntoNotes (Pradhan et al. 2007c, Pradhan et al. 2007a), and the CoNLL 2012 Shared Task based on it (Pradhan et al., 2012a). OntoNotes contains hand-annotated Chinese and English coreference datasets of roughly one million words each, consisting of newswire, magazine articles, broadcast news, broadcast conversations, web data and conversational speech data, as well as about 300,000 words of annotated Arabic newswire. The most important distinguishing characteristic of OntoNotes is that it does not label singletons, simplifying the coreference task, since singletons represent 60%-70% of all entities. In other ways, it is similar to other coreference datasets. Referring expression NPs that are coreferent are marked as mentions, but generics and pleonastic pronouns are not marked. Appositive clauses are not marked as separate mentions, but they are included in the mention. Thus in the NP, “Richard Godown, president of the Industrial Biotechnology Association” the mention is the entire phrase. Prenominal modifiers are annotated as separate entities only if they are proper nouns. Thus wheat is not an entity in wheat fields, but UN is an entity in UN policy (but not adjectives like American in American policy).

A number of corpora mark richer discourse phenomena. The ISNotes corpus annotates a portion of OntoNotes for information status, include bridging examples (Hou et al., 2018). The LitBank coreference corpus (Bamman et al., 2020) contains coreference annotations for 210,532 tokens from 100 different literary novels, including singletons and quantified and negated noun phrases. The AnCora-CO coreference corpus (Recasens and Martí, 2010) contains 400,000 words each of Spanish (AnCora-CO-Es) and Catalan (AnCora-CO-Ca) news data, and includes labels for complex phenomena like discourse deixis in both languages. The ARRAU corpus (Uryupina et al., 2020) contains 350,000 words of English marking all NPs, which means singleton clusters are available. ARRAU includes diverse genres like dialog (the TRAINS data) and fiction (the Pear Stories), and has labels for bridging references, discourse deixis, generics, and ambiguous anaphoric relations.

### 22.3 Mention Detection

The first stage of coreference is **mention detection**: finding the spans of text that constitute each mention. Mention detection algorithms are usually very liberal in proposing candidate mentions (i.e., emphasizing recall), and only filtering later. For example many systems run parsers and named entity taggers on the text and extract every span that is either an NP, a possessive pronoun, or a named entity.

Doing so from our sample text repeated in (22.44):

(22.44) Victoria Chen, CFO of Megabucks Banking, saw her pay jump to $2.3
million, as the 38-year-old also became the company’s president. It is widely known that she came to Megabucks from rival Lotsabucks.

might result in the following list of 13 potential mentions:

<table>
<thead>
<tr>
<th>Name</th>
<th>Role</th>
<th>Quantity</th>
<th>Company</th>
</tr>
</thead>
<tbody>
<tr>
<td>Victoria Chen</td>
<td>CFO of Megabucks</td>
<td>$2.3 million</td>
<td>she</td>
</tr>
<tr>
<td></td>
<td>Banking</td>
<td></td>
<td>Megabucks</td>
</tr>
<tr>
<td>her</td>
<td>the 38-year-old</td>
<td></td>
<td>Lotsabucks</td>
</tr>
<tr>
<td>her pay</td>
<td>the company’s president</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

More recent mention detection systems are even more generous; the span-based algorithm we will describe in Section 22.6 first extracts literally all n-gram spans of words up to N=10. Of course recall from Section 22.1.3 that many NPs—and the overwhelming majority of random n-gram spans—are not referring expressions. Therefore all such mention detection systems need to eventually filter out pleonastic/expletive pronouns like *It* above, appositives like *CFO of Megabucks Banking Inc* or predicate nominals like *the company’s president* or *$2.3 million*.

Some of this filtering can be done by rules. Early rule-based systems designed regular expressions to deal with pleonastic *it*, like the following rules from *Lappin and Leass* (1994) that use dictionaries of cognitive verbs (e.g., *believe, know, anticipate*) to capture pleonastic *it* in “It is thought that ketchup...”, or modal adjectives (e.g., *necessary, possible, certain, important*), for, e.g., “It is likely that I...”. Such rules are sometimes used as part of modern systems:

- It is Modaladjective that S
- It is Modaladjective (for NP) to VP
- It is Cogn-ed that S
- It seems/appears/means/follows (that) S

Mention-detection rules are sometimes designed specifically for particular evaluation campaigns. For OntoNotes, for example, mentions are not embedded within larger mentions, and while numeric quantities are annotated, they are rarely coreferential. Thus for OntoNotes tasks like CoNLL 2012 (Pradhan et al., 2012a), a common first pass rule-based mention detection algorithm (Lee et al., 2013) is:

1. Take all NPs, possessive pronouns, and named entities.
2. Remove numeric quantities (100 dollars, 8%), mentions embedded in larger mentions, adjectival forms of nations, and stop words (like *there*).
3. Remove pleonastic *it* based on regular expression patterns.

Rule-based systems, however, are generally insufficient to deal with mention-detection, and so modern systems incorporate some sort of learned mention detection component, such as a referentiality classifier, an anaphoricity classifier—detecting whether an NP is an anaphor—or a discourse-new classifier—detecting whether a mention is discourse-new and a potential antecedent for a future anaphor.

An anaphoricity detector, for example, can draw its positive training examples from any span that is labeled as an anaphoric referring expression in hand-labeled datasets like OntoNotes, ARRAU, or AnCora. Any other NP or named entity can be marked as a negative training example. Anaphoricity classifiers use features of the candidate mention such as its head word, surrounding words, definiteness, animacy, length, position in the sentence/discourse, many of which were first proposed in early work by *Ng and Cardie* (2002a); see Section 22.5 for more on features.
Referentiality or anaphoricity detectors can be run as filters, in which only mentions that are classified as anaphoric or referential are passed on to the coreference system. The end result of such a filtering mention detection system on our example above might be the following filtered set of 9 potential mentions:

<table>
<thead>
<tr>
<th>Mention</th>
<th>Anaphoric</th>
<th>Coreferential</th>
</tr>
</thead>
<tbody>
<tr>
<td>Victoria Chen</td>
<td></td>
<td></td>
</tr>
<tr>
<td>her pay</td>
<td></td>
<td></td>
</tr>
<tr>
<td>she</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Megabucks Bank</td>
<td></td>
<td></td>
</tr>
<tr>
<td>the 38-year-old</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Megabucks</td>
<td></td>
<td></td>
</tr>
<tr>
<td>her</td>
<td></td>
<td></td>
</tr>
<tr>
<td>the company</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Lotsabucks</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

It turns out, however, that hard filtering of mentions based on an anaphoricity or referentiality classifier leads to poor performance. If the anaphoricity classifier threshold is set too high, too many mentions are filtered out and recall suffers. If the classifier threshold is set too low, too many pleonastic or non-referential mentions are included and precision suffers.

The modern approach is instead to perform mention detection, anaphoricity, and coreference jointly in a single end-to-end model (Ng 2005b, Denis and Baldridge 2007, Rahman and Ng 2009). For example mention detection in the Lee et al. (2017b,2018) system is based on a single end-to-end neural network that computes a score for each mention being referential, a score for two mentions being coreference, and combines them to make a decision, training all these scores with a single end-to-end loss. We’ll describe this method in detail in Section 22.6. ⁷

Despite these advances, correctly detecting referential mentions seems to still be an unsolved problem, since systems incorrectly marking pleonastic pronouns like *it* and other non-referential NPs as coreferent is a large source of errors of modern coreference resolution systems (Kummerfeld and Klein 2013, Martschat and Strube 2014, Martschat and Strube 2015, Wiseman et al. 2015, Lee et al. 2017a).

Mention, referentiality, or anaphoricity detection is thus an important open area of investigation. Other sources of knowledge may turn out to be helpful, especially in combination with unsupervised and semisupervised algorithms, which also mitigate the expense of labeled datasets. In early work, for example Bean and Riloff (1999) learned patterns for characterizing anaphoric or non-anaphoric NPs; (by extracting and generalizing over the first NPs in a text, which are guaranteed to be non-anaphoric). Chang et al. (2012) look for head nouns that appear frequently in the training data but never appear as gold mentions to help find non-referential NPs. Bergsma et al. (2008b) use web counts as a semisupervised way to augment standard features for anaphoricity detection for English *it*, an important task because *it* is both common and ambiguous; between a quarter and half *it* examples are non-anaphoric. Consider the following two examples:

(22.45) You can make *it* in advance. [anaphoric]
(22.46) You can make *it* in Hollywood. [non-anaphoric]

The *it* in make *it* is non-anaphoric, part of the idiom *make it*. Bergsma et al. (2008b) turn the context around each example into patterns, like “*make * in advance” from (22.45), and “*make * in Hollywood” from (22.46). They then use Google n-grams to enumerate all the words that can replace *it* in the patterns. Non-anaphoric contexts tend to only have *it* in the wildcard positions, while anaphoric contexts occur with many other NPs (for example *make them in advance* is just as frequent in their data

⁷ Some systems try to avoid mention detection or anaphoricity detection altogether. For datasets like OntoNotes which don’t label singletons, an alternative to filtering out non-referential mentions is to run coreference resolution, and then simply delete any candidate mentions which were not corefered with another mention. This likely doesn’t work as well as explicitly modeling referentiality, and cannot solve the problem of detecting singletons, which is important for tasks like entity linking.
22.4 Architectures for Coreference Algorithms

Modern systems for coreference are based on supervised neural machine learning, supervised from hand-labeled datasets like OntoNotes. In this section we overview the various architecture of modern systems, using the categorization of Ng (2010), which distinguishes algorithms based on whether they make each coreference decision in a way that is entity-based—representing each entity in the discourse model—or only mention-based—considering each mention independently, and whether they use ranking models to directly compare potential antecedents. Afterwards, we go into more detail on one state-of-the-art algorithm in Section 22.6.

22.4.1 The Mention-Pair Architecture

We begin with the mention-pair architecture, the simplest and most influential coreference architecture, which introduces many of the features of more complex algorithms, even though other architectures perform better. The mention-pair architecture is based around a classifier that—as its name suggests—is given a pair of mentions, a candidate anaphor and a candidate antecedent, and makes a binary classification decision: coreferring or not.

Let’s consider the task of this classifier for the pronoun *she* in our example, and assume the slightly simplified set of potential antecedents in Fig. 22.2.

For each prior mention (Victoria Chen, Megabucks Banking, *her*, etc.), the binary classifier computes a probability: whether or not the mention is the antecedent of *she*. We want this probability to be high for actual antecedents (Victoria Chen, *her*, the 38-year-old) and low for non-antecedents (Megabucks Banking, *her pay*).

For training, we need a heuristic for selecting training samples; since most pairs of mentions in a document are not coreferent, selecting every pair would lead to a massive overabundance of negative samples. The most common heuristic, from (Soon et al., 2001), is to choose the closest antecedent as a positive example, and all pairs in between as the negative examples. More formally, for each anaphor mention \( m_i \) we create

- one positive instance \( (m_i, m_j) \) where \( m_j \) is the closest antecedent to \( m_i \), and
• a negative instance \((m_i, m_k)\) for each \(m_k\) between \(m_i\) and \(m_l\)

Thus for the anaphor \(she\), we would choose \((she, her)\) as the positive example and no negative examples. Similarly, for the anaphor \(the\ company\) we would choose \((the\ company, Megabucks)\) as the positive example and \((the\ company, she)\) \((the\ company, the\ 38-year-old)\) \((the\ company, her\ pay)\) and \((the\ company, her)\) as negative examples.

Once the classifier is trained, it is applied to each test sentence in a clustering step. For each mention \(i\) in a document, the classifier considers each of the prior \(i - 1\) mentions. In closest-first clustering (Soon et al., 2001), the classifier is run right to left (from mention \(i - 1\) down to mention 1) and the first antecedent with probability \(> 0.5\) is linked to \(i\). If no antecedent has probably \(> 0.5\), no antecedent is selected for \(i\). In best-first clustering, the classifier is run on all \(i - 1\) antecedents and the most probable preceding mention is chosen as the antecedent for \(i\). The transitive closure of the pairwise relation is taken as the cluster.

While the mention-pair model has the advantage of simplicity, it has two main problems. First, the classifier doesn’t directly compare candidate antecedents to each other, so it’s not trained to decide, between two likely antecedents, which one is in fact better. Second, it ignores the discourse model, looking only at mentions, not entities. Each classifier decision is made completely locally to the pair, without being able to take into account other mentions of the same entity. The next two models each address one of these two flaws.

### 22.4.2 The Mention-Rank Architecture

The mention ranking model directly compares candidate antecedents to each other, choosing the highest-scoring antecedent for each anaphor.

In early formulations, for mention \(i\), the classifier decides which of the \(\{1, \ldots, i - 1\}\) prior mentions is the antecedent (Denis and Baldridge, 2008). But suppose \(i\) is in fact not anaphoric, and none of the antecedents should be chosen? Such a model would need to run a separate anaphoricity classifier on \(i\). Instead, it turns out to be better to jointly learn anaphoricity detection and coreference together with a single loss (Rahman and Ng, 2009).

So in modern mention-ranking systems, for the \(i\)th mention (anaphor), we have an associated random variable \(y_i\) ranging over the values \(Y(i) = \{1, \ldots, i - 1, \epsilon\}\). The value \(\epsilon\) is a special dummy mention meaning that \(i\) does not have an antecedent (i.e., is either discourse-new and starts a new coref chain, or is non-anaphoric).

![Figure 22.3](image)

For each candidate anaphoric mention (like \(she\)), the mention-ranking system assigns a probability distribution over all previous mentions plus the special dummy mention \(\epsilon\).

At test time, for a given mention \(i\) the model computes one softmax over all the antecedents (plus \(\epsilon\)) giving a probability for each candidate antecedent (or none).
Fig. 22.3 shows an example of the computation for the single candidate anaphor she.

Once the antecedent is classified for each anaphor, transitive closure can be run over the pairwise decisions to get a complete clustering.

Training is trickier in the mention-ranking model than the mention-pair model, because for each anaphor we don’t know which of all the possible gold antecedents to use for training. Instead, the best antecedent for each mention is latent; that is, for each mention we have a whole cluster of legal gold antecedents to choose from. Early work used heuristics to choose an antecedent, for example choosing the closest antecedent as the gold antecedent and all non-antecedents in a window of two sentences as the negative examples (Denis and Baldridge, 2008). Various kinds of ways to model latent antecedents exist (Fernandes et al. 2012, Chang et al. 2013, Durrett and Klein 2013). The simplest way is to give credit to any legal antecedent by summing over all of them, with a loss function that optimizes the likelihood of all correct antecedents from the gold clustering (Lee et al., 2017b). We’ll see the details in Section 22.6.

Mention-ranking models can be implemented with hand-build features or with neural representation learning (which might also incorporate some hand-built features). we’ll explore both directions in Section 22.5 and Section 22.6.

### 22.4.3 Entity-based Models

Both the mention-pair and mention-ranking models make their decisions about mentions. By contrast, entity-based models link each mention not to a previous mention but to a previous discourse entity (cluster of mentions).

A mention-ranking model can be turned into an entity-ranking model simply by having the classifier make its decisions over clusters of mentions rather than individual mentions (Rahman and Ng, 2009).

For traditional feature-based models, this can be done by extracting features over clusters. The size of a cluster is a useful feature, as is its ‘shape’, which is the list of types of the mentions in the cluster i.e., sequences of the tokens (P)roper, (D)efinite, (I)ndefinite, (P)r(onoun), so that a cluster composed of {Victoria, her, the 38-year-old} would have the shape P-Pr-D (Björkelund and Kuhn, 2014). An entity-based model that includes a mention-pair classifier can use as features aggregates of mention-pair probabilities, for example computing the average probability of coreference over all mention-pairs in the two clusters (Clark and Manning 2015).

Neural models can learn representations of clusters automatically, for example by using an RNN over the sequence of cluster mentions to encode a state corresponding to a cluster representation (Wiseman et al., 2016), or by learning distributed representations for pairs of clusters by pooling over learned representations of mention pairs (Clark and Manning, 2016b).

However, although entity-based models are more expressive, the use of cluster-level information in practice has not led to large gains in performance, so mention-ranking models are still more commonly used.

### 22.5 Classifiers using hand-built features

Feature-based classifiers, use hand-designed features in logistic regression, SVM, or random forest classifiers for coreference resolution. These classifiers don’t per-
form as well as neural ones. Nonetheless, they are still sometimes useful to build lightweight systems when compute or data are sparse, and the features themselves are useful for error analysis even in neural systems.

Given an anaphor mention and a potential antecedent mention, feature based classifiers make use of three types of features: (i) features of the anaphor, (ii) features of the candidate antecedent, and (iii) features of the relationship between the pair. Entity-based models can make additional use of two additional classes: (iv) feature of all mentions from the antecedent’s entity cluster, and (v) features of the relation between the anaphor and the mentions in the antecedent entity cluster.

<table>
<thead>
<tr>
<th>Features of the Anaphor or Antecedent Mention</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>First (last) word</strong></td>
</tr>
<tr>
<td>Victoria/she</td>
</tr>
<tr>
<td><strong>Head word</strong></td>
</tr>
<tr>
<td>Victoria/she</td>
</tr>
<tr>
<td><strong>Attributes</strong></td>
</tr>
<tr>
<td>Sg-F-A-3-PER</td>
</tr>
<tr>
<td>Sg-F-A-3-PER</td>
</tr>
<tr>
<td><strong>Length</strong></td>
</tr>
<tr>
<td>2/1</td>
</tr>
<tr>
<td><strong>Mention type</strong></td>
</tr>
<tr>
<td>P/Pr</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Features of the Antecedent Entity</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Entity shape</strong></td>
</tr>
<tr>
<td>P-Pr-D</td>
</tr>
<tr>
<td><strong>Entity attributes</strong></td>
</tr>
<tr>
<td>Sg-F-A-3-PER</td>
</tr>
<tr>
<td><strong>Ant. cluster size</strong></td>
</tr>
<tr>
<td>3</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Features of the Pair of Mentions</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Sentence distance</strong></td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td><strong>Mention distance</strong></td>
</tr>
<tr>
<td>4</td>
</tr>
<tr>
<td><strong>i-within-i</strong></td>
</tr>
<tr>
<td>F</td>
</tr>
<tr>
<td><strong>Cosine</strong></td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Features of the Pair of Entities</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Exact String Match</strong></td>
</tr>
<tr>
<td>F</td>
</tr>
<tr>
<td><strong>Head Word Match</strong></td>
</tr>
<tr>
<td>F</td>
</tr>
<tr>
<td><strong>Word Inclusion</strong></td>
</tr>
<tr>
<td>F</td>
</tr>
</tbody>
</table>

| Figure 22.4 Feature-based coreference: sample feature values for anaphor “she” and potential antecedent     |
|                                                                                                              |
|                                                                                                              |
|                                                                                                              |
|                                                                                                              |
| “Victoria Chen”                                                                                             |

Figure 22.4 shows a selection of commonly used features, and shows the value that would be computed for the potential anaphor “she” and potential antecedent “Victoria Chen” in our example sentence, repeated below:

(22.47) **Victoria Chen**, CFO of Megabucks Banking, saw her pay jump to $2.3 million, as the 38-year-old also became the company’s president. It is widely known that she came to Megabucks from rival Lotsabucks.

Features that prior work has found to be particularly useful are exact string match, entity headword agreement, mention distance, as well as (for pronouns) exact attribute match and i-within-i, and (for nominals and proper names) word inclusion and cosine. For lexical features (like head words) it is common to only use words that appear enough times (>20 times).
22.6 A neural mention-ranking algorithm

It is crucial in feature-based systems to use conjunctions of features; one experiment suggested that moving from individual features in a classifier to conjunctions of multiple features increased F1 by 4 points (Lee et al., 2017a). Specific conjunctions can be designed by hand (Durrett and Klein, 2013), all pairs of features can be conjoined (Bengtson and Roth, 2008), or feature conjunctions can be learned using decision tree or random forest classifiers (Ng and Cardie 2002a, Lee et al. 2017a).

Features can also be used in neural models as well. Neural systems use contextual word embeddings so don’t benefit from shallow features like string match or mention types. However features like mention length, distance between mentions, or genre can complement neural contextual embedding models.

22.6 A neural mention-ranking algorithm

In this section we describe the neural e2e-coref algorithms of Lee et al. (2017b) (simplified and extended a bit, drawing on Joshi et al. (2019) and others). This is a mention-ranking algorithm that considers all possible spans of text in the document, assigns a mention-score to each span, prunes the mentions based on this score, then assigns coreference links to the remaining mentions.

More formally, given a document $D$ with $T$ words, the model considers all of the $T(T+1)/2$ text spans in $D$ (unigrams, bigrams, trigrams, 4-grams, etc; in practice we only consider spans up a maximum length around 10). The task is to assign to each span $i$ an antecedent $y_i$, a random variable ranging over the values $Y(i) = \{1, ..., i-1, \epsilon\}$; each previous span and a special dummy token $\epsilon$. Choosing the dummy token means that $i$ does not have an antecedent, either because $i$ is discourse-new and starts a new coreference chain, or because $i$ is non-anaphoric.

For each pair of spans $i$ and $j$, the system assigns a score $s(i, j)$ for the coreference link between span $i$ and span $j$. The system then learns a distribution $P(y_i)$ over the antecedents for span $i$:

$$P(y_i) = \frac{\exp(s(i, y_i))}{\sum_{y' \in Y(i)} \exp(s(i, y'))}$$  \hspace{1cm} (22.48)

This score $s(i, j)$ includes three factors that we’ll define below: $m(i)$; whether span $i$ is a mention; $m(j)$; whether span $j$ is a mention; and $c(i, j)$; whether $j$ is the antecedent of $i$:

$$s(i, j) = m(i) + m(j) + c(i, j)$$  \hspace{1cm} (22.49)

For the dummy antecedent $\epsilon$, the score $s(i, \epsilon)$ is fixed to 0. This way if any non-dummy scores are positive, the model predicts the highest-scoring antecedent, but if all the scores are negative it abstains.

22.6.1 Computing span representations

To compute the two functions $m(i)$ and $c(i, j)$ which score a span $i$ or a pair of spans $(i, j)$, we’ll need a way to represent a span. The e2e-coref family of algorithms represents each span by trying to capture 3 words/tokens: the first word, the last word, and the most important word. We first run each paragraph or subdocument through an encoder (like BERT) to generate embeddings $h_i$ for each token $i$. The span $i$ is then represented by a vector $g_i$ that is a concatenation of the encoder output
embedding for the first (start) token of the span, the encoder output for the last (end) token of the span, and a third vector which is an attention-based representation:

\[ g_i = [h_{\text{START}(i)}, h_{\text{END}(i)}, h_{\text{ATT}(i)}] \]  

(22.50)

The goal of the attention vector is to represent which word/token is the likely syntactic head-word of the span; we saw in the prior section that head-words are a useful feature; a matching head-word is a good indicator of coreference. The attention representation is computed as usual; the system learns a weight vector \( \mathbf{w}_\alpha \), and computes its dot product with the hidden state \( \mathbf{h}_t \) transformed by a FFN:

\[ \alpha_t = \mathbf{w}_\alpha \cdot \text{FFN}_\alpha(h_t) \]  

(22.51)

The attention score is normalized into a distribution via a softmax:

\[ a_{i,t} = \frac{\exp(\alpha_t)}{\sum_{k=\text{START}(i)}^{\text{END}(i)} \exp(\alpha_k)} \]  

(22.52)

And then the attention distribution is used to create a vector \( h_{\text{ATT}(i)} \) which is an attention-weighted sum of the embeddings \( \mathbf{e}_t \) of each of the words in span \( i \):

\[ h_{\text{ATT}(i)} = \sum_{t=\text{START}(i)}^{\text{END}(i)} a_{i,t} \cdot \mathbf{e}_t \]  

(22.53)

Fig. 22.5 shows the computation of the span representation and the mention score.

22.6.2 Computing the mention and antecedent scores \( m \) and \( c \)

Now that we know how to compute the vector \( g_i \) for representing span \( i \), we can see the details of the two scoring functions \( m(i) \) and \( c(i,j) \). Both are computed by feedforward networks:

\[ m(i) = w_m \cdot \text{FFN}_m(g_i) \]  

(22.54)

\[ c(i,j) = w_c \cdot \text{FFN}_c([g_i, g_j, g_i \circ g_j]) \]  

(22.55)

At inference time, this mention score \( m \) is used as a filter to keep only the best few mentions.
We then compute the antecedent score for high-scoring mentions. The antecedent score \( c(i, j) \) takes as input a representation of the spans \( i \) and \( j \), but also the element-wise similarity of the two spans to each other \( g_i \circ g_j \) (here \( \circ \) is element-wise multiplication). Fig. 22.6 shows the computation of the score \( s \) for the three possible antecedents of the \emph{company} in the example sentence from Fig. 22.5.

![Figure 22.6](image)

**Figure 22.6** The computation of the score \( s \) for the three possible antecedents of the company in the example sentence from Fig. 22.5. Figure after Lee et al. (2017b).

Given the set of mentions, the joint distribution of antecedents for each document is computed in a forward pass, and we can then do transitive closure on the antecedents to create a final clustering for the document.

Fig. 22.7 shows example predictions from the model, showing the attention weights, which Lee et al. (2017b) find correlate with traditional semantic heads. Note that the model gets the second example wrong, presumably because \emph{attendants} and \emph{pilot} likely have nearby word embeddings.

![Figure 22.7](image)

**Figure 22.7** Sample predictions from the Lee et al. (2017b) model, with one cluster per example, showing one correct example and one mistake. Bold, parenthesized spans are mentions in the predicted cluster. The amount of red color on a word indicates the head-finding attention weight \( a_{it} \) in (22.52). Figure adapted from Lee et al. (2017b).

### 22.6.3 Learning

For training, we don’t have a single gold antecedent for each mention; instead the coreference labeling only gives us each entire cluster of coreferent mentions; so a mention only has a latent antecedent. We therefore use a loss function that maximizes the sum of the coreference probability of any of the legal antecedents. For a given mention \( i \) with possible antecedents \( Y(i) \), let \( \text{GOLD}(i) \) be the set of mentions in the gold cluster containing \( i \). Since the set of mentions occurring before \( i \) is \( Y(i) \), the set of mentions in that gold cluster that also occur before \( i \) is \( Y(i) \cap \text{GOLD}(i) \). We
therefore want to maximize:

\[
\sum_{\hat{y} \in Y(i) \cap \text{GOLD}(i)} P(\hat{y})
\]  

(22.56)

If a mention \(i\) is not in a gold cluster \(\text{GOLD}(i) = \epsilon\).

To turn this probability into a loss function, we’ll use the cross-entropy loss function we defined in Eq. 5.23 in Chapter 5, by taking the \(-\log\) of the probability. If we then sum over all mentions, we get the final loss function for training:

\[
L = \sum_{i=2}^{N} - \log \sum_{\hat{y} \in Y(i) \cap \text{GOLD}(i)} P(\hat{y})
\]  

(22.57)

### 22.7 Entity Linking

**Entity linking** is the task of associating a mention in text with the representation of some real-world entity in an ontology or knowledge base (Ji and Grishman, 2011). It is the natural follow-on to coreference resolution; coreference resolution is the task of associating textual mentions that corefer to the same entity. Entity linking takes the further step of identifying who that entity is. It is especially important for any NLP task that links to a knowledge base.

While there are all sorts of potential knowledge-bases, we’ll focus in this section on Wikipedia, since it’s widely used as an ontology for NLP tasks. In this usage, each unique Wikipedia page acts as the unique id for a particular entity. This task of deciding which Wikipedia page corresponding to an individual is being referred to by a text mention has its own name: **wikification** (Mihalcea and Csomai, 2007).

Since the earliest systems (Mihalcea and Csomai 2007, Cucerzan 2007, Milne and Witten 2008), entity linking is done in (roughly) two stages: **mention detection** and mention disambiguation. We’ll give two algorithms, one simple classic baseline that uses **anchor dictionaries** and information from the Wikipedia graph structure (Ferragina and Scaiella, 2011) and one modern neural algorithm (Li et al., 2020). We’ll focus here mainly on the application of entity linking to questions, since a lot of the literature has been in that context.

#### 22.7.1 Linking based on Anchor Dictionaries and Web Graph

As a simple baseline we introduce the **TAGME linker** (Ferragina and Scaiella, 2011) for Wikipedia, which itself draws on earlier algorithms (Mihalcea and Csomai 2007, Cucerzan 2007, Milne and Witten 2008). Wikification algorithms define the set of entities as the set of Wikipedia pages, so we’ll refer to each Wikipedia page as a unique entity \(e\). **TAGME** first creates a catalog of all entities (i.e. all Wikipedia pages, removing some disambiguation and other meta-pages) and indexes them in a standard IR engine like Lucene. For each page \(e\), the algorithm computes an **in-link count in** \((e)\): the total number of in-links from other Wikipedia pages that point to \(e\). These counts can be derived from Wikipedia dumps.

Finally, the algorithm requires an **anchor dictionary**. An anchor dictionary lists for each Wikipedia page, its **anchor texts**: the hyperlinked spans of text on other pages that point to it. For example, the web page for Stanford University, [http://www.stanford.edu](http://www.stanford.edu), might be pointed to from another page using anchor texts like **Stanford** or **Stanford University**.
We compute a Wikipedia anchor dictionary by including, for each Wikipedia page \( e \), \( e \)’s title as well as all the anchor texts from all Wikipedia pages that point to \( e \). For each anchor string \( a \) we’ll also compute its total frequency \( \text{freq}(a) \) in Wikipedia (including non-anchor uses), the number of times \( a \) occurs as a link (which we’ll call \( \text{link}(a) \)), and its link probability \( \text{linkprob}(a) = \frac{\text{link}(a)}{\text{freq}(a)} \). Some cleanup of the final anchor dictionary is required, for example removing anchor strings composed only of numbers or single characters, that are very rare, or that are very unlikely to be useful entities because they have a very low linkprob.

**Mention Detection**  Given a question (or other text we are trying to link), TAGME detects mentions by querying the anchor dictionary for each token sequence up to 6 words. This large set of sequences is pruned with some simple heuristics (for example pruning substrings if they have small linkprobs). The question:

*What Chinese Dynasty came before the Yuan?*

might give rise to the anchor *Ada Lovelace* and possibly *Ada*, but substrings spans like *Lovelace* might be pruned as having too low a linkprob, and but spans like *born* have such a low linkprob that they would not be in the anchor dictionary at all.

**Mention Disambiguation**  If a mention span is unambiguous (points to only one entity/Wikipedia page), we are done with entity linking! However, many spans are ambiguous, matching anchors for multiple Wikipedia entities/pages. The TAGME algorithm uses two factors for disambiguating ambiguous spans, which have been referred to as prior probability and relatedness/coherence. The first factor is \( p(e|a) \), the probability with which the span refers to a particular entity. For each page \( e \in \mathcal{E}(a) \), the probability \( p(e|a) \) that anchor \( a \) points to \( e \), is the ratio of the number of links into \( e \) with anchor text \( a \) to the total number of occurrences of \( a \) as an anchor:

\[
\text{prior}(a \to e) = p(e|a) = \frac{\text{count}(a \to e)}{\text{link}(a)}
\]

Let’s see how that factor works in linking entities in the following question:

*What Chinese Dynasty came before the Yuan?*

The most common association for the span *Yuan* in the anchor dictionary is the name of the Chinese currency, i.e., the probability \( p(\text{Yuan_currency}| \text{yuan}) \) is very high. Rarer Wikipedia associations for *Yuan* include the common Chinese last name, a language spoken in Thailand, and the correct entity in this case, the name of the Chinese dynasty. So if we chose based only on \( p(e|a) \), we would make the wrong disambiguation and miss the correct link, *Yuan_dynasty*.

To help in just this sort of case, TAGME uses a second factor, the relatedness of this entity to other entities in the input question. In our example, the fact that the question also contains the span *Chinese Dynasty*, which has a high probability link to the page *Dynasties_in_Chinese_history*, ought to help match *Yuan_dynasty*.

Let’s see how this works. Given a question \( q \), for each candidate anchors span \( a \) detected in \( q \), we assign a relatedness score to each possible entity \( e \in \mathcal{E}(a) \) of \( a \). The relatedness score of the link \( a \to e \) is the weighted average relatedness between \( e \) and all other entities in \( q \). Two entities are considered related to the extent their Wikipedia pages share many in-links. More formally, the relatedness between two entities \( A \) and \( B \) is computed as

\[
\text{rel}(A,B) = \frac{\log(\max(|\text{in}(A)|,|\text{in}(B)|)) - \log(|\text{in}(A) \cap \text{in}(B)|)}{\log(|W|) - \log(\min(|\text{in}(A)|,|\text{in}(B)|))}
\]
where \( \text{in}(x) \) is the set of Wikipedia pages pointing to \( x \) and \( W \) is the set of all Wikipedia pages in the collection.

The vote given by anchor \( b \) to the candidate annotation \( a \rightarrow X \) is the average, over all the possible entities of \( b \), of their relatedness to \( X \), weighted by their prior probability:

\[
\text{vote}(b, X) = \frac{1}{|E(b)|} \sum_{Y \in E(b)} \text{rel}(X, Y) p(Y|b)
\]

(22.60)

The total relatedness score for \( a \rightarrow X \) is the sum of the votes of all the other anchors detected in \( q \):

\[
\text{relatedness}(a \rightarrow X) = \sum_{b \in X \setminus a} \text{vote}(b, X)
\]

(22.61)

To score \( a \rightarrow X \), we combine relatedness and prior by choosing the entity \( X \) that has the highest relatedness \( \text{relatedness}(a \rightarrow X) \), finding other entities within a small \( \epsilon \) of this value, and from this set, choosing the entity with the highest prior \( P(X|a) \). The result of this step is a single entity assigned to each span in \( q \).

The TAGME algorithm has one further step of pruning spurious anchor/entity pairs, assigning a score averaging link probability with the coherence.

\[
\text{coherence}(a \rightarrow X) = \frac{1}{|S| - 1} \sum_{B \in S \setminus X} \text{rel}(B, X)
\]

\[
\text{score}(a \rightarrow X) = \frac{\text{coherence}(a \rightarrow X) + \text{linkprob}(a)}{2}
\]

(22.62)

Finally, pairs are pruned if \( \text{score}(a \rightarrow X) < \lambda \), where the threshold \( \lambda \) is set on a held-out set.

### 22.7.2 Neural Graph-based linking

More recent entity linking models are based on **bi-encoders**, encoding a candidate mention span, encoding an entity, and computing the dot product between the encodings. This allows embeddings for all the entities in the knowledge base to be precomputed and cached (Wu et al., 2020). Let’s sketch the ELQ linking algorithm of Li et al. (2020), which is given a question \( q \) and a set of candidate entities from Wikipedia with associated Wikipedia text, and outputs tuples \((e, m_s, m_e)\) of entity id, mention start, and mention end. As Fig. 22.8 shows, it does this by encoding each Wikipedia entity using text from Wikipedia, encoding each mention span using text from the question, and computing their similarity, as we describe below.

**Entity Mention Detection** To get an \( h \)-dimensional embedding for each question token, the algorithm runs the question through BERT in the normal way:

\[
[q_1: \cdots: q_n] = \text{BERT}([\text{CLS}] q_1: \cdots: q_n [\text{SEP}])
\]

(22.63)

It then computes the likelihood of each span \([i, j]\) in \( q \) being an entity mention, in a way similar to the span-based algorithm we saw for the reader above. First we compute the score for \( i/j \) being the start/end of a mention:

\[
s_{\text{start}}(i) = w_{\text{start}} \cdot q_i, \quad s_{\text{end}}(j) = w_{\text{end}} \cdot q_j,
\]

(22.64)
where \( \mathbf{w}_{\text{start}} \) and \( \mathbf{w}_{\text{end}} \) are vectors learned during training. Next, another trainable embedding, \( \mathbf{w}_{\text{mention}} \) is used to compute a score for each token being part of a mention:

\[
    s_{\text{mention}}(t) = \mathbf{w}_{\text{mention}} \cdot \mathbf{q}_t
\]

(22.65)

Mention probabilities are then computed by combining these three scores:

\[
    p([i, j]) = \sigma \left( s_{\text{start}}(i) + s_{\text{end}}(j) + \sum_{t=i}^{j} s_{\text{mention}}(t) \right)
\]

(22.66)

**Entity Linking**  
To link mentions to entities, we next compute embeddings for each entity in the set \( \mathcal{E} = e_1, \ldots, e_i, \ldots, e_w \) of all Wikipedia entities. For each entity \( e_i \) we’ll get text from the entity’s Wikipedia page, the title \( t(e_i) \) and the first 128 tokens of the Wikipedia page which we’ll call the description \( d(e_i) \). This is again run through BERT, taking the output of the CLS token BERT[CLS] as the entity representation:

\[
    \mathbf{x}_{e_i} = \text{BERT}[\text{CLS}](t(e_i)[\text{ENT}]d(e_i)[\text{SEP}])
\]

(22.67)

Mention spans can be linked to entities by computing, for each entity \( e \) and span \([i, j] \), the dot product similarity between the span encoding (the average of the token embeddings) and the entity encoding.

\[
    \mathbf{y}_{i,j} = \frac{1}{(j-i+1)} \sum_{t=i}^{j} \mathbf{q}_t
\]

\[
    s(e, [i, j]) = \mathbf{x}_{e} \cdot \mathbf{y}_{i,j}
\]

(22.68)

Finally, we take a softmax to get a distribution over entities for each span:

\[
    p(e|[i, j]) = \frac{\exp(s(e, [i, j]))}{\sum_{e'\in \mathcal{E}} \exp(s(e', [i, j]))}
\]

(22.69)

**Training**  
The ELQ mention detection and entity linking algorithm is fully supervised. This means, unlike the anchor dictionary algorithms from Section 22.7.1,
it requires datasets with entity boundaries marked and linked. Two such labeled
datasets are WebQuestionsSP (Yih et al., 2016), an extension of the WebQuestions
(Berant et al., 2013) dataset derived from Google search questions, and GraphQues-
tions (Su et al., 2016). Both have had entity spans in the questions marked and
linked (Sorokin and Gurevych 2018, Li et al. 2020) resulting in entity-labeled ver-
sions WebQSP\(_\text{EL}\) and GraphQ\(_\text{EL}\) (Li et al., 2020).

Given a training set, the ELQ mention detection and entity linking phases are
trained jointly, optimizing the sum of their losses. The mention detection loss is
a binary cross-entropy loss, with \(L\) the length of the passage and \(N\) the number of
candidates:

\[
\mathcal{L}_{MD} = -\frac{1}{N} \sum_{1 \leq i \leq f \leq \min(i+L-1,n)} (y_{[i,j]} \log p([i,j]) + (1 - y_{[i,j]}) \log(1 - p([i,j])))
\]

with \(y_{[i,j]} = 1\) if \([i,j]\) is a gold mention span, else 0. The entity linking loss is:

\[
\mathcal{L}_{ED} = -\log p(e_{[i,j]})
\]

where \(e_{[i,j]}\) is the gold entity for mention \([i,j]\).

### 22.8 Evaluation of Coreference Resolution

We evaluate coreference algorithms model-theoretically, comparing a set of hypothesis chains or clusters \(H\) produced by the system against a set of gold or reference chains or clusters \(R\) from a human labeling, and reporting precision and recall.

However, there are a wide variety of methods for doing this comparison. In fact, there are 5 common metrics used to evaluate coreference algorithms: the link based MUC (Vilain et al., 1995) and BLANC (Recasens and Hovy 2011, Luo et al. 2014) metrics, the mention based \(B^3\) metric (Bagga and Baldwin, 1998), the entity based CEA\(F\) metric (Luo, 2005), and the link based \texttt{entity} aware \texttt{LEA} metric (Moosavi and Strube, 2016).

Let’s just explore two of the metrics. The MUC \textbf{F-measure} (Vilain et al., 1995) is based on the number of coreference links (pairs of mentions) common to \(H\) and \(R\). Precision is the number of common links divided by the number of links in \(H\). Recall is the number of common links divided by the number of links in \(R\); This makes MUC biased toward systems that produce large chains (and fewer entities), and it ignores singletons, since they don’t involve links.

\(B^3\) is mention-based rather than link-based. For each mention in the reference chain, we compute a precision and recall, and then we take a weighted sum over all \(N\) mentions in the document to compute a precision and recall for the entire task. For a given mention \(i\), let \(R\) be the reference chain that includes \(i\), and \(H\) the hypothesis chain that has \(i\). The set of correct mentions in \(H\) is \(H \cap R\). Precision for mention \(i\) is thus \(\frac{|H \cap R|}{|H|}\), and recall for mention \(i\) thus \(\frac{|H \cap R|}{|R|}\). The total precision is the weighted sum of the precision for mention \(i\), weighted by a weight \(w_i\). The total recall is the weighted sum of the recall for mention \(i\), weighted by a weight \(w_i\). Equivalently:

\[
\text{Precision} = \sum_{i=1}^{N} w_i \frac{\# \text{ of correct mentions in hypothesis chain containing entity}_i}{\# \text{ of mentions in hypothesis chain containing entity}_i}
\]

\[
\text{Recall} = \sum_{i=1}^{N} w_i \frac{\# \text{ of correct mentions in hypothesis chain containing entity}_i}{\# \text{ of mentions in reference chain containing entity}_i}
\]
The weight $w_i$ for each entity can be set to different values to produce different versions of the algorithm.

Following a proposal from Denis and Baldridge (2009), the CoNLL coreference competitions were scored based on the average of MUC, CEAF-e, and $B^3$ (Pradhan et al. 2011, Pradhan et al. 2012), and so it is common in many evaluation campaigns to report an average of these 3 metrics. See Luo and Pradhan (2016) for a detailed description of the entire set of metrics; reference implementations of these should be used rather than attempting to reimplement from scratch (Pradhan et al., 2014).

Alternative metrics have been proposed that deal with particular coreference domains or tasks. For example, consider the task of resolving mentions to named entities (persons, organizations, geopolitical entities), which might be useful for information extraction or knowledge base completion. A hypothesis chain that correctly contains all the pronouns referring to an entity, but has no version of the name itself, or is linked with a wrong name, is not useful for this task. We might instead want a metric that weights each mention by how informative it is (with names being most informative) (Chen and Ng, 2013) or a metric that considers a hypothesis to match a gold chain only if it contains at least one variant of a name (the NEC F1 metric of Agarwal et al. (2019)).

### 22.9 Winograd Schema problems

From early on in the field, researchers have noted that some cases of coreference are quite difficult, seeming to require world knowledge or sophisticated reasoning to solve. The problem was most famously pointed out by Winograd (1972) with the following example:

(22.72) The city council denied the demonstrators a permit because

a. they feared violence.

b. they advocated violence.

Winograd noticed that the antecedent that most readers preferred for the pronoun they in continuation (a) was the city council, but in (b) was the demonstrators. He suggested that this requires understanding that the second clause is intended as an explanation of the first clause, and also that our cultural frames suggest that city councils are perhaps more likely than demonstrators to fear violence and that demonstrators might be more likely to advocate violence.

In an attempt to get the field of NLP to focus more on methods involving world knowledge and common-sense reasoning, Levesque (2011) proposed a challenge task called the Winograd Schema Challenge. The problems in the challenge task are coreference problems designed to be easily disambiguated by the human reader, but hopefully not solvable by simple techniques such as selectional restrictions, or other basic word association methods.

The problems are framed as a pair of statements that differ in a single word or phrase, and a coreference question:

(22.73) The trophy didn’t fit into the suitcase because it was too large.

Question: What was too large? Answer: The trophy

8 Levesque’s call was quickly followed up by Levesque et al. (2012) and Rahman and Ng (2012), a competition at the IJCAI conference (Davis et al., 2017), and a natural language inference version of the problem called WNLI (Wang et al., 2018a).
(22.74) The trophy didn’t fit into the suitcase because it was too **small**.
Question: What was too **small**? Answer: The suitcase

The problems have the following characteristics:
1. The problems each have two parties
2. A pronoun preferentially refers to one of the parties, but could grammatically also refer to the other
3. A question asks which party the pronoun refers to
4. If one word in the question is changed, the human-preferred answer changes to the other party

The kind of world knowledge that might be needed to solve the problems can vary. In the trophy/suitcase example, it is knowledge about the physical world; that a bigger object cannot fit into a smaller object. In the original Winograd sentence, it is stereotypes about social actors like politicians and protesters. In examples like the following, it is knowledge about human actions like turn-taking or thanking.

(22.75) Bill passed the gameboy to John because his turn was [over/next]. Whose turn was [over/next]? Answers: Bill/John

(22.76) Joan made sure to thank Susan for all the help she had [given/received]. Who had [given/received] help? Answers: Susan/Joan.

Although the Winograd Schema was designed to require common-sense reasoning, a large percentage of the original set of problem can be solved by pre-trained language models, fine-tuned on Winograd Schema sentences (Kocijan et al., 2019). Large pretrained language models encode an enormous amount of world or common-sense knowledge! The current trend is therefore to propose new datasets with increasingly difficult Winograd-like coreference resolution problems like KNOWREF (Emami et al., 2019), with examples like:

(22.77) Marcus is undoubtedly faster than Jarrett right now but in [his] prime the gap wasn’t all that big.

In the end, it seems likely that some combination of language modeling and knowledge will prove fruitful; indeed, it seems that knowledge-based models overfit less to lexical idiosyncracies in Winograd Schema training sets (Trichelair et al., 2018).

### 22.10 Gender Bias in Coreference

As with other aspects of language processing, coreference models exhibit gender and other biases (Zhao et al. 2018a, Rudinger et al. 2018, Webster et al. 2018). For example the WinoBias dataset (Zhao et al., 2018a) uses a variant of the Winograd Schema paradigm to test the extent to which coreference algorithms are biased toward linking gendered pronouns with antecedents consistent with cultural stereotypes. As we summarized in Chapter 6, embeddings replicate societal biases in their training test, such as associating men with historically stereotypical male occupations like doctors, and women with stereotypical female occupations like secretaries (Caliskan et al. 2017, Garg et al. 2018).

A WinoBias sentence contain two mentions corresponding to stereotypically-male and stereotypically-female occupations and a gendered pronoun that must be linked to one of them. The sentence cannot be disambiguated by the gender of the pronoun, but a biased model might be distracted by this cue. Here is an example sentence:
The secretary called the physician and told him about a new patient [pro-stereotypical]

The secretary called the physician and told her about a new patient [anti-stereotypical]

Zhao et al. (2018a) consider a coreference system to be biased if it is more accurate at linking pronouns consistent with gender stereotypical occupations (e.g., him with physician in (22.78)) than linking pronouns inconsistent with gender-stereotypical occupations (e.g., her with physician in (22.79)). They show that coreference systems of all architectures (rule-based, feature-based machine learned, and end-to-end-neural) all show significant bias, performing on average 21 F₁ points worse in the anti-stereotypical cases.

One possible source of this bias is that female entities are significantly underrepresented in the OntoNotes dataset, used to train most coreference systems. Zhao et al. (2018a) propose a way to overcome this bias: they generate a second gender-swapped dataset in which all male entities in OntoNotes are replaced with female ones and vice versa, and retrain coreference systems on the combined original and swapped OntoNotes data, also using debiased GloVE embeddings (Bolukbasi et al., 2016). The resulting coreference systems no longer exhibit bias on the WinoBias dataset, without significantly impacting OntoNotes coreference accuracy.

In a follow-up paper, Zhao et al. (2019) show that the same biases exist in ELMo contextualized word vector representations and coref systems that use them. They showed that retraining ELMo with data augmentation again reduces or removes bias in coreference systems on WinoBias.

Webster et al. (2018) introduces another dataset, GAP, and the task of Gendered Pronoun Resolution as a tool for developing improved coreference algorithms for gendered pronouns. GAP is a gender-balanced labeled corpus of 4,454 sentences with gendered ambiguous pronouns (by contrast, only 20% of the gendered pronouns in the English OntoNotes training data are feminine). The examples were created by drawing on naturally occurring sentences from Wikipedia pages to create hard to resolve cases with two named entities of the same gender and an ambiguous pronoun that may refer to either person (or neither), like the following:

In May, Fujisawa joined Mari Motohashi’s rink as the team’s skip, moving back from Karuizawa to Kitami where she had spent her junior days.

Webster et al. (2018) show that modern coreference algorithms perform significantly worse on resolving feminine pronouns than masculine pronouns in GAP. Kurita et al. (2019) shows that a system based on BERT contextualized word representations shows similar bias.

22.11 Summary

This chapter introduced the task of coreference resolution.

- This is the task of linking together mentions in text which corefer, i.e. refer to the same discourse entity in the discourse model, resulting in a set of coreference chains (also called clusters or entities).
- Mentions can be definite NPs or indefinite NPs, pronouns (including zero pronouns) or names.
• The surface form of an entity mention is linked to its information status (new, old, or inferrable), and how accessible or salient the entity is.
• Some NPs are not referring expressions, such as pleonastic it in *It is raining*.
• Many corpora have human-labeled coreference annotations that can be used for supervised learning, including OntoNotes for English, Chinese, and Arabic, ARRAU for English, and AnCora for Spanish and Catalan.
• Mention detection can start with all nouns and named entities and then use anaphoricity classifiers or referentiality classifiers to filter out non-mentions.
• Three common architectures for coreference are mention-pair, mention-rank, and entity-based, each of which can make use of feature-based or neural classifiers.
• Modern coreference systems tend to be end-to-end, performing mention detection and coreference in a single end-to-end architecture.
• Algorithms learn representations for text spans and heads, and learn to compare anaphor spans with candidate antecedent spans.
• Entity linking is the task of associating a mention in text with the representation of some real-world entity in an ontology.
• Coreference systems are evaluated by comparing with gold entity labels using precision/recall metrics like MUC, B3, CEAF, BLANC, or LEA.
• The Winograd Schema Challenge problems are difficult coreference problems that seem to require world knowledge or sophisticated reasoning to solve.
• Coreference systems exhibit gender bias which can be evaluated using datasets like Winobias and GAP.

Bibliographical and Historical Notes

Coreference has been part of natural language processing since the 1970s (Woods et al. 1972, Winograd 1972). The discourse model and the entity-centric foundation of coreference was formulated by Karttunen (1969) (at the 3rd COLING conference), playing a role also in linguistic semantics (Heim 1982, Kamp 1981). But it was Bonnie Webber’s 1978 dissertation and following work (Webber 1983) that explored the model’s computational aspects, providing fundamental insights into how entities are represented in the discourse model and the ways in which they can license subsequent reference. Many of the examples she provided continue to challenge theories of reference to this day.

The Hobbs algorithm⁹ is a tree-search algorithm that was the first in a long series of syntax-based methods for identifying reference robustly in naturally occurring text. The input to the Hobbs algorithm is a pronoun to be resolved, together with a syntactic (constituency) parse of the sentences up to and including the current sentence. The details of the algorithm depend on the grammar used, but can be understood from a simplified version due to Kehler et al. (2004) that just searches through the list of NPs in the current and prior sentences. This simplified Hobbs algorithm searches NPs in the following order: “(i) in the current sentence from right-to-left, starting with the first NP to the left of the pronoun, (ii) in the previous sentence from left-to-right, (iii) in two sentences prior from left-to-right, and (iv) in

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⁹ The simpler of two algorithms presented originally in Hobbs (1978).
the current sentence from left-to-right, starting with the first noun group to the right of the pronoun (for cataphora). The first noun group that agrees with the pronoun with respect to number, gender, and person is chosen as the antecedent” (Kehler et al., 2004).

Lappin and Leass (1994) was an influential entity-based system that used weights to combine syntactic and other features, extended soon after by Kennedy and Boguraev (1996) whose system avoids the need for full syntactic parses.


Coreference competitions as part of the US DARPA-sponsored MUC conferences provided early labeled coreference datasets (the 1995 MUC-6 and 1998 MUC-7 corpora), and set the tone for much later work, choosing to focus exclusively on the simplest cases of identity coreference (ignoring difficult cases like bridging, metonymy, and part-whole) and drawing the community toward supervised machine learning and metrics like the MUC metric (Vilain et al., 1995). The later ACE evaluations produced labeled coreference corpora in English, Chinese, and Arabic that were widely used for model training and evaluation.

This DARPA work influenced the community toward supervised learning beginning in the mid-90s (Connolly et al. 1994, Aone and Bennett 1995, McCarthy and Lehnert 1995). Soon et al. (2001) laid out a set of basic features, extended by Ng and Cardie (2002b), and a series of machine learning models followed over the next 15 years. These often focused separately on pronominal anaphora resolution (Kehler et al. 2004, Bergsma and Lin 2006), full NP coreference (Cardie and Wagstaff 1999, Ng and Cardie 2002b, Ng 2005a) and definite NP reference (Poesio and Vieira 1998, Vieira and Poesio 2000), as well as separate anaphoricity detection (Bean and Riloff 1999, Bean and Riloff 2004, Ng and Cardie 2002a, Ng 2004), or singleton detection (de Marneffe et al., 2015).

The move from mention-pair to mention-ranking approaches was pioneered by Yang et al. (2003) and Iida et al. (2003) who proposed pairwise ranking methods, then extended by Denis and Baldridge (2008) who proposed to do ranking via a softmax over all prior mentions. The idea of doing mention detection, anaphoricity, and coreference jointly in a single end-to-end model grew out of the early proposal of Ng (2005b) to use a dummy antecedent for mention-ranking, allowing 'non-referential' to be a choice for coreference classifiers, Denis and Baldridge’s 2007 joint system combining anaphoricy classifier probabilities with coreference probabilities, the Denis and Baldridge (2008) ranking model, and the Rahman and Ng (2009) proposal to train the two models jointly with a single objective.

Simple rule-based systems for coreference returned to prominence in the 2010s, partly because of their ability to encode entity-based features in a high-precision way (Zhou et al. 2004b, Haghhighi and Klein 2009, Raghunathan et al. 2010, Lee et al. 2011, Lee et al. 2013, Hajishirzi et al. 2013) but in the end they suffered from an inability to deal with the semantics necessary to correctly handle cases of common noun coreference.

A return to supervised learning led to a number of advances in mention-ranking models which were also extended into neural architectures, for example using re-
inforcement learning to directly optimize coreference evaluation models Clark and Manning (2016a), doing end-to-end coreference all the way from span extraction (Lee et al. 2017b, Zhang et al. 2018). Neural models also were designed to take advantage of global entity-level information (Clark and Manning 2016b, Wiseman et al. 2016, Lee et al. 2018).

Coreference is also related to the task of entity linking discussed in Chapter 14. Coreference can help entity linking by giving more possible surface forms to help link to the right Wikipedia page, and conversely entity linking can help improve coreference resolution. Consider this example from Hajishirzi et al. (2013):


Integrating entity linking into coreference can help draw encyclopedic knowledge (like the fact that Donald Tsang is a president) to help disambiguate the mention the President. Ponzetto and Strube (2006) 2007 and Ratinov and Roth (2012) showed that such attributes extracted from Wikipedia pages could be used to build richer models of entity mentions in coreference. More recent research shows how to do linking and coreference jointly (Hajishirzi et al. 2013, Zheng et al. 2013) or even jointly with named entity tagging as well (Durrett and Klein 2014).

The coreference task as we introduced it involves a simplifying assumption that the relationship between an anaphor and its antecedent is one of identity: the two coreferring mentions refer to the identical discourse referent. In real texts, the relationship can be more complex, where different aspects of a discourse referent can be neutralized or refocused. For example (22.82) (Recasens et al., 2011) shows an example of metonymy, in which the capital city Washington is used metonymically to refer to the US. (22.83-22.84) show other examples (Recasens et al., 2011):

(22.82) a strict interpretation of a policy requires The U.S. to notify foreign dictators of certain coup plots ... Washington rejected the bid ...

(22.83) I once crossed that border into Ashgh-Abad on Nowruz, the Persian New Year. In the South, everyone was celebrating New Year; to the North, it was a regular day.

(22.84) In France, the president is elected for a term of seven years, while in the United States he is elected for a term of four years.

For further linguistic discussions of these complications of coreference see Pustejovsky (1991), van Deemter and Kibble (2000), Poesio et al. (2006), Fauconnier and Turner (2008), Versley (2008), and Barker (2010).


Andy Kehler wrote the Discourse chapter for the 2000 first edition of this textbook, which we used as the starting point for the second-edition chapter, and there are some remnants of Andy’s lovely prose still in this third-edition coreference chapter.

**Exercises**
CHAPTER 23

Discourse Coherence

And even in our wildest and most wandering reveries, nay in our very dreams, we shall find, if we reflect, that the imagination ran not altogether at adventures, but that there was still a connection upheld among the different ideas, which succeeded each other. Were the loosest and freest conversation to be transcribed, there would immediately be transcribed, there would immediately be observed something which connected it in all its transitions.

David Hume, *An enquiry concerning human understanding*, 1748

Orson Welles’ movie *Citizen Kane* was groundbreaking in many ways, perhaps most notably in its structure. The story of the life of fictional media magnate Charles Foster Kane, the movie does not proceed in chronological order through Kane’s life. Instead, the film begins with Kane’s death (famously murmuring “Rosebud”) and is structured around flashbacks to his life inserted among scenes of a reporter investigating his death. The novel idea that the structure of a movie does not have to linearly follow the structure of the real timeline made apparent for 20th century cinematography the infinite possibilities and impact of different kinds of coherent narrative structures.

But coherent structure is not just a fact about movies or works of art. Like movies, language does not normally consist of isolated, unrelated sentences, but instead of collocated, structured, coherent groups of sentences. We refer to such a coherent structured group of sentences as a discourse, and we use the word coherence to refer to the relationship between sentences that makes real discourses different than just random assemblages of sentences. The chapter you are now reading is an example of a discourse, as is a news article, a conversation, a thread on social media, a Wikipedia page, and your favorite novel.

What makes a discourse coherent? If you created a text by taking random sentences each from many different sources and pasted them together, would that be a coherent discourse? Almost certainly not. Real discourses exhibit both local coherence and global coherence. Let’s consider three ways in which real discourses are locally coherent:

First, sentences or clauses in real discourses are related to nearby sentences in systematic ways. Consider this example from Hobbs (1979):

(23.1) John took a train from Paris to Istanbul. He likes spinach.

This sequence is incoherent because it is unclear to a reader why the second sentence follows the first; what does liking spinach have to do with train trips? In fact, a reader might go to some effort to try to figure out how the discourse could be coherent; perhaps there is a French spinach shortage? The very fact that hearers try to identify such connections suggests that human discourse comprehension involves the need to establish this kind of coherence.

By contrast, in the following coherent example:

(23.2) Jane took a train from Paris to Istanbul. She had to attend a conference.
the second sentence gives a **reason** for Jane’s action in the first sentence. Structured relationships like **reason** that hold between text units are called **coherence relations**, and coherent discourses are structured by many such coherence relations. Coherence relations are introduced in Section 23.1.

A second way a discourse can be locally coherent is by virtue of being “about” someone or something. In a coherent discourse some entities are **salient**, and the discourse focuses on them and doesn’t go back and forth between multiple entities. This is called **entity-based coherence**. Consider the following incoherent passage, in which the salient entity seems to wildly swing from John to Jenny to the piano store to the living room, back to Jenny, then the piano again:

\[(23.3)\] John wanted to buy a piano for his living room.
Jenny also wanted to buy a piano.
He went to the piano store.
It was nearby.
The living room was on the second floor.
She didn’t find anything she liked.
The piano he bought was hard to get up to that floor.

Entity-based coherence models measure this kind of coherence by tracking salient entities across a discourse. For example **Centering Theory** (Grosz et al., 1995), the most influential theory of entity-based coherence, keeps track of which entities in the discourse model are salient at any point (salient entities are more likely to be pronominalized or to appear in prominent syntactic positions like subject or object). In Centering Theory, transitions between sentences that maintain the same salient entity are considered more coherent than ones that repeatedly shift between entities.

The **entity grid** model of coherence (Barzilay and Lapata, 2008) is a commonly used model that realizes some of the intuitions of the Centering Theory framework. Entity-based coherence is introduced in Section 23.3.

Finally, discourses can be locally coherent by being **topically coherent**: nearby sentences are generally about the same topic and use the same or similar vocabulary to discuss these topics. Because topically coherent discourses draw from a single semantic field or topic, they tend to exhibit the surface property known as **lexical cohesion** (Halliday and Hasan, 1976): the sharing of identical or semantically related words in nearby sentences. For example, the fact that the words *house*, *chimney*, *garret*, *closet*, and *window*— all of which belong to the same semantic field— appear in the two sentences in (23.4), or that they share the identical word *shingled*, is a cue that the two are tied together as a discourse:

\[(23.4)\] Before winter I built a chimney, and shingled the sides of my house...
I have thus a tight shingled and plastered house... with a garret and a closet, a large window on each side....

In addition to the local coherence between adjacent or nearby sentences, discourses also exhibit **global coherence**. Many genres of text are associated with particular conventional discourse structures. Academic articles might have sections describing the Methodology or Results. Stories might follow conventional plotlines or motifs. Persuasive essays have a particular claim they are trying to argue for, and an essay might express this claim together with a structured set of premises that support the argument and demolish potential counterarguments. We’ll introduce versions of each of these kinds of global coherence.

Why do we care about the local or global coherence of a discourse? Since coherence is a property of a well-written text, coherence detection plays a part in any
task that requires measuring the quality of a text. For example coherence can help in pedagogical tasks like essay grading or essay quality measurement that are trying to grade how well-written a human essay is (Somasundaran et al. 2014, Feng et al. 2014, Lai and Tetreault 2018). Coherence can also help for summarization; knowing the coherence relationship between sentences can help know how to select information from them. Finally, detecting incoherent text may even play a role in mental health tasks like measuring symptoms of schizophrenia or other kinds of disordered language (Ditman and Kuperberg 2010, Elvevåg et al. 2007, Bedi et al. 2015, Iter et al. 2018).

23.1 Coherence Relations

Recall from the introduction the difference between passages (23.5) and (23.6).

(23.5) Jane took a train from Paris to Istanbul. She likes spinach.
(23.6) Jane took a train from Paris to Istanbul. She had to attend a conference.

The reason (23.6) is more coherent is that the reader can form a connection between the two sentences, in which the second sentence provides a potential reason for the first sentences. This link is harder to form for (23.5). These connections between text spans in a discourse can be specified as a set of coherence relations. The next two sections describe two commonly used models of coherence relations and associated corpora: Rhetorical Structure Theory (RST), and the Penn Discourse TreeBank (PDTB).

23.1.1 Rhetorical Structure Theory

The most commonly used model of discourse organization is Rhetorical Structure Theory (RST) (Mann and Thompson, 1987). In RST relations are defined between two spans of text, generally a nucleus and a satellite. The nucleus is the unit that is more central to the writer’s purpose and that is interpretable independently; the satellite is less central and generally is only interpretable with respect to the nucleus. Some symmetric relations, however, hold between two nuclei.

Below are a few examples of RST coherence relations, with definitions adapted from the RST Treebank Manual (Carlson and Marcu, 2001).

**Reason:** The nucleus is an action carried out by an animate agent and the satellite is the reason for the nucleus.

(23.7) [\texttt{NUC} Jane took a train from Paris to Istanbul.] [\texttt{SAT} She had to attend a conference.]

**Elaboration:** The satellite gives additional information or detail about the situation presented in the nucleus.

(23.8) [\texttt{NUC} Dorothy was from Kansas.] [\texttt{SAT} She lived in the midst of the great Kansas prairies.]

**Evidence:** The satellite gives additional information or detail about the situation presented in the nucleus. The information is presented with the goal of convince the reader to accept the information presented in the nucleus.

(23.9) [\texttt{NUC} Kevin must be here.] [\texttt{SAT} His car is parked outside.]
**Attribution:** The satellite gives the source of attribution for an instance of reported speech in the nucleus.

(23.10) [SAT Analysts estimated] [NUC that sales at U.S. stores declined in the quarter, too]

**List:** In this multinuclear relation, a series of nuclei is given, without contrast or explicit comparison:

(23.11) [NUC Billy Bones was the mate;] [NUC Long John, he was quartermaster]

RST relations are traditionally represented graphically; the asymmetric Nucleus-Satellite relation is represented with an arrow from the satellite to the nucleus:

We can also talk about the coherence of a larger text by considering the hierarchical structure between coherence relations. Figure 23.1 shows the rhetorical structure of a paragraph from Marcu (2000a) for the text in (23.12) from the *Scientific American* magazine.

(23.12) With its distant orbit--50 percent farther from the sun than Earth--and slim atmospheric blanket, Mars experiences frigid weather conditions. Surface temperatures typically average about -60 degrees Celsius (-76 degrees Fahrenheit) at the equator and can dip to -123 degrees C near the poles. Only the midday sun at tropical latitudes is warm enough to thaw ice on occasion, but any liquid water formed in this way would evaporate almost instantly because of the low atmospheric pressure.

![Figure 23.1](image-url) A discourse tree for the *Scientific American* text in (23.12), from Marcu (2000a). Note that asymmetric relations are represented with a curved arrow from the satellite to the nucleus.

The leaves in the Fig. 23.1 tree correspond to text spans of a sentence, clause or phrase that are called **elementary discourse units** or EDUs in RST; these units can also be referred to as **discourse segments**. Because these units may correspond to arbitrary spans of text, determining the boundaries of an EDU is an important task for extracting coherence relations. Roughly speaking, one can think of discourse
segments as being analogous to constituents in sentence syntax, and indeed as we’ll see in Section 23.2 we generally draw on parsing algorithms to infer discourse structure.

There are corpora for many discourse coherence models; the RST Discourse TreeBank (Carlson et al., 2001) is the largest available discourse corpus. It consists of 385 English language documents selected from the Penn Treebank, with full RST parses for each one, using a large set of 78 distinct relations, grouped into 16 classes. RST treebanks exist also for Spanish, German, Basque, Dutch and Brazilian Portuguese (Braud et al., 2017).

Now that we’ve seen examples of coherence, we can see more clearly how a coherence relation can play a role in summarization or information extraction. For example, the nuclei of a text presumably express more important information than the satellites, which might be dropped in a summary.

### 23.1.2 Penn Discourse TreeBank (PDTB)

The Penn Discourse TreeBank (PDTB) is a second commonly used dataset that embodies another model of coherence relations (Miltsakaki et al. 2004, Prasad et al. 2008, Prasad et al. 2014). PDTB labeling is lexically grounded. Instead of asking annotators to directly tag the coherence relation between text spans, they were given a list of discourse connectives, words that signal discourse relations, like because, although, when, since, or as a result. In a part of a text where these words marked a coherence relation between two text spans, the connective and the spans were then annotated, as in Fig. 23.13, where the phrase as a result signals a causal relationship between what PDTB calls Arg1 (the first two sentences, here in italics) and Arg2 (the third sentence, here in bold).

(23.13) Jewelry displays in department stores were often cluttered and uninspired. And the merchandise was, well, fake. As a result, marketers of faux gems steadily lost space in department stores to more fashionable rivals—cosmetics makers.

(23.14) In July, the Environmental Protection Agency imposed a gradual ban on virtually all uses of asbestos. (implicit=as a result) By 1997, almost all remaining uses of cancer-causing asbestos will be outlawed.

Not all coherence relations are marked by an explicit discourse connective, and so the PDTB also annotates pairs of neighboring sentences with no explicit signal, like (23.14). The annotator first chooses the word or phrase that could have been its signal (in this case as a result), and then labels its sense. For example for the ambiguous discourse connective since annotators marked whether it is using a CAUSAL or a TEMPORAL sense.

The final dataset contains roughly 18,000 explicit relations and 16,000 implicit relations. Fig. 23.2 shows examples from each of the 4 major semantic classes, while Fig. 23.3 shows the full tagset.

Unlike the RST Discourse Treebank, which integrates these pairwise coherence relations into a global tree structure spanning an entire discourse, the PDTB does not annotate anything above the span-pair level, making no commitment with respect to higher-level discourse structure.

There are also treebanks using similar methods for other languages; (23.15) shows an example from the Chinese Discourse TreeBank (Zhou and Xue, 2015). Because Chinese has a smaller percentage of explicit discourse connectives than English (only 22% of all discourse relations are marked with explicit connectives,
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<table>
<thead>
<tr>
<th>Class</th>
<th>Type</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>TEMPORAL</td>
<td>SYNCHRONOUS</td>
<td>The parishioners of St. Michael and All Angels stop to chat at the church door, as members here always have. (Implicit while) In the tower, five men and women pull rhythmically on ropes attached to the same five bells that first sounded here in 1614.</td>
</tr>
<tr>
<td>CONTINGENCY</td>
<td>REASON</td>
<td>Also unlike Mr. Ruder, Mr. Breeden appears to be in a position to get somewhere with his agenda. (implicit=because) As a former White House aide who worked closely with Congress, he is savvy in the ways of Washington.</td>
</tr>
<tr>
<td>COMPARISON</td>
<td>CONTRAST</td>
<td>The U.S. wants the removal of what it perceives as barriers to investment; Japan denies there are real barriers.</td>
</tr>
<tr>
<td>EXPANSION</td>
<td>CONJUNCTION</td>
<td>Not only do the actors stand outside their characters and make it clear they are at odds with them, but they often literally stand on their heads.</td>
</tr>
</tbody>
</table>

Figure 23.2 The four high-level semantic distinctions in the PDTB sense hierarchy

Figure 23.3 The PDTB sense hierarchy. There are four top-level classes, 16 types, and 23 subtypes (not all types have subtypes). 11 of the 16 types are commonly used for implicit argument classification; the 5 types in italics are too rare in implicit labeling to be used.

compared to 47% in English), annotators labeled this corpus by directly mapping pairs of sentences to 11 sense tags, without starting with a lexical discourse connector.

(23.15) [Conn 为] [Arg2 推动图们江地区开发]. [Arg1 韩国捐款一百万美元设立了图们江发展基金]

“In order to” [Arg2 promote the development of the Tumen River region], [Arg1 South Korea donated one million dollars to establish the Tumen River Development Fund].”

These discourse treebanks have been used for shared tasks on multilingual discourse parsing (Xue et al., 2016).

23.2 Discourse Structure Parsing

Given a sequence of sentences, how can we automatically determine the coherence relations between them? This task is often called discourse parsing (even though for PDTB we are only assigning labels to leaf spans and not building a full parse
23.2.1 EDU segmentation for RST parsing

RST parsing is generally done in two stages. The first stage, EDU segmentation, extracts the start and end of each EDU. The output of this stage would be a labeling like the following:

(23.16) [Mr. Rambo says]_e1 [that a 3.2-acre property]_e2 [overlooking the San Fernando Valley]_e3 [is priced at $4 million]_e4 [because the late actor Erroll Flynn once lived there.]_e5

Since EDUs roughly correspond to clauses, early models of EDU segmentation first ran a syntactic parser, and then post-processed the output. Modern systems generally use neural sequence models supervised by the gold EDU segmentation in datasets like the RST Discourse Treebank. Fig. 23.4 shows an example architecture simplified from the algorithm of Lukasik et al. (2020) that predicts for each token whether or not it is a break. Here the input sentence is passed through an encoder and then passed through a linear layer and a softmax to produce a sequence of 0s and 1, where 1 indicates the start of an EDU.

23.2.2 RST parsing

Tools for building RST coherence structure for a discourse have long been based on syntactic parsing algorithms like shift-reduce parsing (Marcu, 1999). Many modern RST parsers since Ji and Eisenstein (2014) draw on the neural syntactic parsers we saw in Chapter 18, using representation learning to build representations for each span, and training a parser to choose the correct shift and reduce actions based on the gold parses in the training set.

We’ll describe the shift-reduce parser of Yu et al. (2018). The parser state consists of a stack and a queue, and produces this structure by taking a series of actions on the states. Actions include:

- **shift**: pushes the first EDU in the queue onto the stack creating a single-node subtree.
- **reduce**(l,d): merges the top two subtrees on the stack, where l is the coherence relation label, and d is the nuclearity direction, \( d \in \{NN,NS,SN\} \).

As well as the **pop root** operation, to remove the final tree from the stack.

Fig. 23.6 shows the actions the parser takes to build the structure in Fig. 23.5.
tions, whose key point is a transition system. A transition system consists of two parts: states and actions.

### 2.1 The Transition-based System

The transition-based framework converts a structural learning problem into a sequence of action predictions. Thirdly, we present our proposed dynamic oracle used in a number of NLP tasks (Zhu et al., 2013; Dyer et al., 2015; Zhang et al., 2016). In addition, a

### 2.2 Encoder-Decoder

Given an input sequence of EDUs

\[ e_1, e_2, e_3, e_4 \]

transition actions, where each line includes a state and next step action referring to the tree. Enhance the transition-based model with dynamic oracle. Based on the proposed model, we study the
effectiveness of our proposed implicit syntax features. We conduct experiments on a standard RST discourse parsing.

### 2.2.1 Encoder

A transition-based neural model for RST discourse parsing, which follows an encoder-decoder process in detail. By this way, we naturally convert RST discourse parsing into predicting a sequence of

### SH, RD

The problem could be extremely serious when inputs of discourse parsing have different feeding them into neural network models (Braud et al., 2016; Braud et al., 2017).

### Figure 23.5

Example RST discourse tree, showing four EDUs. Figure from Yu et al. (2018).

<table>
<thead>
<tr>
<th>Step</th>
<th>Stack</th>
<th>Queue</th>
<th>Action</th>
<th>Relation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\emptyset$</td>
<td>$e_1, e_2, e_3, e_4$</td>
<td>SH</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>2</td>
<td>$e_1$</td>
<td>$e_2, e_3, e_4$</td>
<td>SH</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>3</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>RD (attr, SN)</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>4</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>SH</td>
<td>$e_1 e_2$</td>
</tr>
<tr>
<td>5</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>SH</td>
<td>$e_1 e_2$</td>
</tr>
<tr>
<td>6</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>$\emptyset$</td>
<td>RD (elab, NS)</td>
</tr>
<tr>
<td>7</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>$\emptyset$</td>
<td>RD (elab, SN)</td>
</tr>
<tr>
<td>8</td>
<td>$e_1, e_2$</td>
<td>$e_3, e_4$</td>
<td>PR</td>
<td>$e_1 e_2, e_3 e_4$</td>
</tr>
</tbody>
</table>

### Figure 23.6

Parsing the example of Fig. 23.5 using a shift-reduce parser. Figure from Yu et al. (2018).

The Yu et al. (2018) uses an encoder-decoder architecture, where the encoder represents the input span of words and EDUs using a hierarchical biLSTM. The first biLSTM layer represents the words inside an EDU, and the second represents the EDU sequence. Given an input sentence $w_1, w_2, ..., w_m$, the words can be represented as usual (by static embeddings, combinations with character embeddings or tags, or contextual embeddings) resulting in an input word representation sequence $x_1^w, x_2^w, ..., x_m^w$. The result of the word-level biLSTM is then a sequence of $h^w$ values:

\[
    h_1^w, h_2^w, ..., h_m^w = \text{biLSTM}(x_1^w, x_2^w, ..., x_m^w) 
\]

An EDU of span $w_s, w_{s+1}, ..., w_t$ then has biLSTM output representation $h_s^w, h_{s+1}^w, ..., h_t^w$, and is represented by average pooling:

\[
    x^e = \frac{1}{t-s+1} \sum_{k=s}^{t} h_k^w 
\]

The second layer uses this input to compute a final representation of the sequence of EDU representations $h^e$:

\[
    h_1^e, h_2^e, ..., h_n^e = \text{biLSTM}(x_1^e, x_2^e, ..., x_n^e) 
\]

The decoder is then a feedforward network $W$ that outputs an action $o$ based on a concatenation of the top three subtrees on the stack $(s_0, s_1, s_2)$ plus the first EDU in the queue ($q_0$):

\[
    o = W(h_0^t, h_1^t, h_1^e, h_{q_0}) 
\]

where the representation of the EDU on the queue $h_{q_0}^e$ comes directly from the encoder, and the three hidden vectors representing partial trees are computed by average pooling over the encoder output for the EDUs in those trees:

\[
    h_S^i = \frac{1}{j-i+1} \sum_{k=i}^{j} h_k^e 
\]
Training first maps each RST gold parse tree into a sequence of oracle actions, and then uses the standard cross-entropy loss (with $l_2$ regularization) to train the system to take such actions. Give a state $S$ and oracle action $a$, we first compute the decoder output using Eq. 23.20, apply a softmax to get probabilities:

$$p_a = \frac{\exp(o_a)}{\sum_{a' \in A} \exp(o_{a'})}$$  \hspace{1cm} (23.22)

and then computing the cross-entropy loss:

$$L_{CE}() = -\log(p_a) + \frac{\lambda}{2} ||\Theta||^2$$  \hspace{1cm} (23.23)

RST discourse parsers are evaluated on the test section of the RST Discourse Treebank, either with gold EDUs or end-to-end, using the RST-Pareval metrics (Marcu, 2000b). It is standard to first transform the gold RST trees into right-branching binary trees, and to report four metrics: trees with no labels (S for Span), labeled with nuclei (N), with relations (R), or both (F for Full), for each metric computing micro-averaged $F_1$ over all spans from all documents (Marcu 2000b, Morey et al. 2017).

### 23.2.3 PDTB discourse parsing

PDTB discourse parsing, the task of detecting PDTB coherence relations between spans, is sometimes called shallow discourse parsing because the task just involves flat relationships between text spans, rather than the full trees of RST parsing.

The set of four subtasks for PDTB discourse parsing was laid out by Lin et al. (2014) in the first complete system, with separate tasks for explicit (tasks 1-3) and implicit (task 4) connectives:

1. Find the discourse connectives (disambiguating them from non-discourse uses)
2. Find the two spans for each connective
3. Label the relationship between these spans
4. Assign a relation between every adjacent pair of sentences

Many systems have been proposed for Task 4: taking a pair of adjacent sentences as input and assign a coherence relation sense label as output. The setup often follows Lin et al. (2009) in assuming gold sentence span boundaries and assigning each adjacent span one of the 11 second-level PDTB tags or none (removing the 5 very rare tags of the 16 shown in italics in Fig. 23.3).

A simple but very strong algorithm for Task 4 is to represent each of the two spans by BERT embeddings and take the last layer hidden state corresponding to the position of the [CLS] token, pass this through a single layer tanh feedforward network and then a softmax for sense classification (Nie et al., 2019).

Each of the other tasks also have been addressed. Task 1 is to disambiguating discourse connectives from their non-discourse use. For example as Pitler and Nenkova (2009) point out, the word and is a discourse connective linking the two clauses by an elaboration/expansion relation in (23.24) while it’s a non-discourse NP conjunction in (23.25):

(23.24) Selling picked up as previous buyers bailed out of their positions and aggressive short sellers—anticipating further declines—moved in.

(23.25) My favorite colors are blue and green.
Similarly, *once* is a discourse connective indicating a temporal relation in (23.26), but simply a non-discourse adverb meaning ‘formerly’ and modifying *used* in (23.27):

(23.26) The asbestos fiber, crocidolite, is unusually resilient once it enters the lungs, with even brief exposures to it causing symptoms that show up decades later, researchers said.

(23.27) A form of asbestos *once* used to make Kent cigarette filters has caused a high percentage of cancer deaths among a group of workers exposed to it more than 30 years ago, researchers reported.

Determining whether a word is a discourse connective is thus a special case of word sense disambiguation. Early work on disambiguation showed that the 4 PDTB high-level sense classes could be disambiguated with high (94%) accuracy used syntactic features from gold parse trees (Pitler and Nenkova, 2009). Recent work performs the task end-to-end from word inputs using a biLSTM-CRF with BIO outputs (B-CONN, I-CONN, O) (Yu et al., 2019).

For task 2, PDTB spans can be identified with the same sequence models used to find RST EDUs: a biLSTM sequence model with pretrained contextual embedding (BERT) inputs (Muller et al., 2019). Simple heuristics also do pretty well as a baseline at finding spans, since 93% of relations are either completely within a single sentence or span two adjacent sentences, with one argument in each sentence (Biran and McKeown, 2015).

### 23.3 Centering and Entity-Based Coherence

A second way a discourse can be coherent is by virtue of being “about” some entity. This idea that at each point in the discourse some entity is salient, and a discourse is coherent by continuing to discuss the same entity, appears early in functional linguistics and the psychology of discourse (Chafe 1976, Kintsch and Van Dijk 1978), and soon made its way to computational models. In this section we introduce two models of this kind of entity-based coherence: Centering Theory (Grosz et al., 1995), and the entity grid model of Barzilay and Lapata (2008).

#### 23.3.1 Centering

Centering Theory (Grosz et al., 1995) is a theory of both discourse salience and discourse coherence. As a model of discourse salience, Centering proposes that at any given point in the discourse one of the entities in the discourse model is salient: it is being “centered” on. As a model of discourse coherence, Centering proposes that discourses in which adjacent sentences continue to maintain the same salient entity are more coherent than those which shift back and forth between multiple entities (we will see that continue and shift are technical terms in the theory).

The following two texts from Grosz et al. (1995) which have exactly the same propositional content but different saliences, can help in understanding the main Centering intuition.

(23.28) a. John went to his favorite music store to buy a piano.
    b. He had frequented the store for many years.
    c. He was excited that he could finally buy a piano.
    d. He arrived just as the store was closing for the day.
(23.29)  
a. John went to his favorite music store to buy a piano.
b. It was a store John had frequented for many years.
c. He was excited that he could finally buy a piano.
d. It was closing just as John arrived.

While these two texts differ only in how the two entities (John and the store) are realized in the sentences, the discourse in (23.28) is intuitively more coherent than the one in (23.29). As Grosz et al. (1995) point out, this is because the discourse in (23.28) is clearly about one individual, John, describing his actions and feelings. The discourse in (23.29), by contrast, focuses first on John, then the store, then back to John, then to the store again. It lacks the “aboutness” of the first discourse.

Centering Theory realizes this intuition by maintaining two representations for each utterance $U_n$. The backward-looking center of $U_n$, denoted as $C_b(U_n)$, represents the current salient entity, the one being focused on in the discourse after $U_n$ is interpreted. The forward-looking centers of $U_n$, denoted as $C_f(U_n)$, are a set of potential future salient entities, the discourse entities evoked by $U_n$ any of which could serve as $C_b$ (the salient entity) of the following utterance, i.e. $C_b(U_{n+1})$.

The set of forward-looking centers $C_f(U_n)$ are ranked according to factors like discourse salience and grammatical role (for example subjects are ranked higher than objects, which are higher ranked than all other grammatical roles). We call the highest-ranked forward-looking center $C_p$ (for “preferred center”). $C_p$ is a kind of prediction about what entity will be talked about next. Sometimes the next utterance indeed talks about this entity, but sometimes another entity becomes salient instead.

We’ll use here the algorithm for centering presented in Brennan et al. (1987), which defines four intersentential relationships between a pair of utterances $U_n$ and $U_{n+1}$ that depend on the relationship between $C_b(U_{n+1})$, $C_b(U_n)$, and $C_p(U_{n+1})$; these are shown in Fig. 23.7.

<table>
<thead>
<tr>
<th>$C_b(U_{n+1}) = C_b(U_n)$ or undefined $C_b(U_n)$</th>
<th>$C_b(U_{n+1}) \neq C_b(U_n)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_b(U_{n+1}) = C_p(U_{n+1})$</td>
<td>Continue</td>
</tr>
<tr>
<td>$C_b(U_{n+1}) \neq C_p(U_{n+1})$</td>
<td>Smooth-Shift</td>
</tr>
<tr>
<td>$C_b(U_{n+1})$</td>
<td>Retain</td>
</tr>
<tr>
<td>$C_b(U_{n+1}) \neq C_p(U_{n+1})$</td>
<td>Rough-Shift</td>
</tr>
</tbody>
</table>

The following rules are used by the algorithm:

**Rule 1:** If any element of $C_f(U_n)$ is realized by a pronoun in utterance $U_{n+1}$, then $C_b(U_{n+1})$ must be realized as a pronoun also.

**Rule 2:** Transition states are ordered. Continue is preferred to Retain is preferred to Smooth-Shift is preferred to Rough-Shift.

Rule 1 captures the intuition that pronominalization (including zero-anaphora) is a common way to mark discourse salience. If there are multiple pronouns in an utterance realizing entities from the previous utterance, one of these pronouns must realize the backward center $C_b$; if there is only one pronoun, it must be $C_b$.

Rule 2 captures the intuition that discourses that continue to center the same entity are more coherent than ones that repeatedly shift to other centers. The transition table is based on two factors: whether the backward-looking center $C_b$ is the same from $U_n$ to $U_{n+1}$ and whether this discourse entity is the one that is preferred ($C_p$) in the new utterance $U_{n+1}$. If both of these hold, a **CONTINUE** relation, the speaker has been talking about the same entity and is going to continue talking about that
entity. In a RETAIN relation, the speaker intends to SHIFT to a new entity in a future utterance and meanwhile places the current entity in a lower rank \( C_f \). In a SHIFT relation, the speaker is shifting to a new salient entity.

Let’s walk through the start of (23.28) again, repeated as (23.30), showing the representations after each utterance is processed.

(23.30) John went to his favorite music store to buy a piano. \( (U_1) \)
He was excited that he could finally buy a piano. \( (U_2) \)
He arrived just as the store was closing for the day. \( (U_3) \)
It was closing just as John arrived \( (U_4) \)

Using the grammatical role hierarchy to order the \( C_f \), for sentence \( U_1 \) we get:

\[
C_f(U_1): \{ \text{John, music store, piano} \}
\]
\[
C_p(U_1): \text{John}
\]
\[
C_b(U_1): \text{undefined}
\]

and then for sentence \( U_2 \):

\[
C_f(U_2): \{ \text{John, piano} \}
\]
\[
C_p(U_2): \text{John}
\]
\[
C_b(U_2): \text{John}
\]

Result: Continue \( (C_p(U_2) = C_b(U_2); C_b(U_1) \text{ undefined}) \)

The transition from \( U_1 \) to \( U_2 \) is thus a CONTINUE. Completing this example is left as exercise (1) for the reader.

### 23.3.2 Entity Grid model

Centering embodies a particular theory of how entity mentioning leads to coherence: that salient entities appear in subject position or are pronominalized, and that discourses are salient by means of continuing to mention the same entity in such ways.

The entity grid model of Barzilay and Lapata (2008) is an alternative way to capture entity-based coherence: instead of having a top-down theory, the entity-grid model using machine learning to induce the patterns of entity mentioning that make a discourse more coherent.

The model is based around an entity grid, a two-dimensional array that represents the distribution of entity mentions across sentences. The rows represent sentences, and the columns represent discourse entities (most versions of the entity grid model focus just on nominal mentions). Each cell represents the possible appearance of an entity in a sentence, and the values represent whether the entity appears and its grammatical role. Grammatical roles are subject (S), object (O), neither (X), or absent (–); in the implementation of Barzilay and Lapata (2008), subjects of passives are represented with O, leading to a representation with some of the characteristics of thematic roles.

Fig. 23.8 from Barzilay and Lapata (2008) shows a grid for the text shown in Fig. 23.9. There is one row for each of the six sentences. The second column, for the entity ‘trial’, is \( O = X \), showing that the trial appears in the first sentence as direct object, in the last sentence as an oblique, and does not appear in the middle sentences. The third column, for the entity Microsoft, shows that it appears as subject in sentence 1 (it also appears as the object of the preposition against, but entities that appear multiple times are recorded with their highest-ranked grammatical function). Computing the entity grids requires extracting entities and doing coreference
resolution to cluster them into discourse entities (Chapter 26) as well as parsing the sentences to get grammatical roles.

In the resulting grid, columns that are dense (like the column for Microsoft) indicate entities that are mentioned often in the texts; sparse columns (like the column for earnings) indicate entities that are mentioned rarely.

In the entity grid model, coherence is measured by patterns of **local entity transition**. For example, Department is a subject in sentence 1, and then not mentioned in sentence 2; this is the transition [S –]. The transitions are thus sequences \{S,O,X,–\}^n which can be extracted as continuous cells from each column. Each transition has a probability; the probability of [S –] in the grid from Fig. 23.8 is 0.08 (it occurs 6 times out of the 75 total transitions of length two). Fig. 23.10 shows the distribution over transitions of length 2 for the text of Fig. 23.9 (shown as the first row \textit{d}_1), and 2 other documents.

![Figure 23.8](image)

**Figure 23.8** Part of the entity grid for the text in Fig. 23.9. Entities are listed by their head noun; each cell represents whether an entity appears as subject (S), object (O), neither (X), or is absent (–). Figure from Barzilay and Lapata (2008).

![Figure 23.9](image)

**Figure 23.9** A discourse with the entities marked and annotated with grammatical functions. Figure from Barzilay and Lapata (2008).

The transitions and their probabilities can then be used as features for a machine learning model. This model can be a text classifier trained to produce human-labeled coherence scores (for example from humans labeling each text as coherent or incoherent). But such data is expensive to gather. Barzilay and Lapata (2005) introduced a simplifying innovation: coherence models can be trained by **self-supervision**: trained to distinguish the natural original order of sentences in a discourse from

![Figure 23.10](image)

**Figure 23.10** A feature vector for representing documents using all transitions of length 2. Document \textit{d}_1 is the text in Fig. 23.9. Figure from Barzilay and Lapata (2008).
23.3.3 Evaluating Neural and Entity-based coherence

Entity-based coherence models, as well as the neural models we introduce in the next section, are generally evaluated in one of two ways.

First, we can have humans rate the coherence of a document and train a classifier to predict these human ratings, which can be categorial (high/low, or high/mid/low) or continuous. This is the best evaluation to use if we have some end task in mind, like essay grading, where human raters are the correct definition of the final label.

Alternatively, since it’s very expensive to get human labels, and we might not yet have an end-task in mind, we can use natural texts to do self-supervision. In self-supervision we pair up a natural discourse with a pseudo-document created by changing the ordering. Since naturally-ordered discourses are more coherent than random permutation (Lin et al., 2011), a successful coherence algorithm should prefer the original ordering.

Self-supervision has been implemented in 3 ways. In the sentence order discrimination task (Barzilay and Lapata, 2005), we compare a document to a random permutation of its sentence. A model is considered correct for an (original, permuted) test pair if it ranks the original document higher. Given \( k \) documents, we can compute \( n \) permutations, resulting in \( kn \) pairs each with one original document and one permutation, to use in training and testing.

In the sentence insertion task (Chen et al., 2007) we take a document, remove one of the \( n \) sentences \( s \), and create \( n - 1 \) copies of the document with \( s \) inserted into each position. The task is to decide which of the \( n \) documents is the one with the original ordering, distinguishing the original position for \( s \) from all other positions. Insertion is harder than discrimination since we are comparing documents that differ by only one sentence.

Finally, in the sentence order reconstruction task (Lapata, 2003), we take a document, randomize the sentences, and train the model to put them back in the correct order. Again given \( k \) documents, we can compute \( n \) permutations, resulting in \( kn \) pairs each with one original document and one permutation, to use in training and testing. Reordering is of course a much harder task than simple classification.

23.4 Representation learning models for local coherence

The third kind of local coherence is topical or semantic field coherence. Discourses cohere by talking about the same topics and subtopics, and drawing on the same semantic fields in doing so.

The field was pioneered by a series of unsupervised models in the 1990s of this kind of coherence that made use of lexical cohesion (Halliday and Hasan, 1976): the sharing of identical or semantically related words in nearby sentences. Morris and Hirst (1991) computed lexical chains of words (like pine, bush trees, trunk) that occurred through a discourse and that were related in Roget’s Thesaurus (by being in the same category, or linked categories). They showed that the number and density of chain correlated with the topic structure. The TextTiling algorithm of Hearst (1997) computed the cosine between neighboring text spans (the normalized dot product of vectors of raw word counts), again showing that sentences or paragraph in
a subtopic have high cosine with each other, but not with sentences in a neighboring subtopic.

A third early model, the LSA Coherence method of Foltz et al. (1998) was the first to use embeddings, modeling the coherence between two sentences as the cosine between their LSA sentence embedding vectors\footnote{See Chapter 6 for more on LSA embeddings; they are computed by applying SVD to the term-document matrix (each cell weighted by log frequency and normalized by entropy), and then the first 300 dimensions are used as the embedding.}, computing embeddings for a sentence $s$ by summing the embeddings of its words $w$:

$$\text{sim}(s,t) = \cos(s,t) = \cos(\sum_{w \in s} w, \sum_{w \in t} w)$$ (23.31)

and defining the overall coherence of a text as the average similarity over all pairs of adjacent sentences $s_i$ and $s_{i+1}$:

$$\text{coherence}(T) = \frac{1}{n-1} \sum_{i=1}^{n-1} \cos(s_i,s_{i+1})$$ (23.32)

Modern neural representation-learning coherence models, beginning with Li et al. (2014), draw on the intuitions of these early unsupervised models for learning sentence representations and measuring how they change between neighboring sentences. But the new models also draw on the idea pioneered by Barzilay and Lapata (2005) of self-supervision. That is, unlike say coherence relation models, which train on hand-labeled representations for RST or PDTB, these models are trained to distinguish natural discourses from unnatural discourses formed by scrambling the order of sentences, thus using representation learning to discover the features that matter for at least the ordering aspect of coherence.

Here we present one such model, the local coherence discriminator (LCD) (Xu et al., 2019). Like early models, LCD computes the coherence of a text as the average of coherence scores between consecutive pairs of sentences. But unlike the early unsupervised models, LCD is a self-supervised model trained to discriminate consecutive sentence pairs $(s_i, s_{i+1})$ in the training documents (assumed to be coherent) from (constructed) incoherent pairs $(s_i, s')$. All consecutive pairs are positive examples, and the negative (incoherent) partner for a sentence $s_i$ is another sentence uniformly sampled from the same document as $s_i$.

Fig. 23.11 describes the architecture of the model $f_\theta$, which takes a sentence pair and returns a score, higher scores for more coherent pairs. Given an input sentence pair $s$ and $t$, the model computes sentence embeddings $s$ and $t$ (using any sentence embeddings algorithm), and then concatenates four features of the pair: (1) the concatenation of the two vectors (2) their difference $s - t$; (3) the absolute value of their difference $|s - t|$; (4) their element-wise product $s \odot t$. These are passed through a one-layer feedforward network to output the coherence score.

The model is trained to make this coherence score higher for real pairs than for negative pairs. More formally, the training objective for a corpus $C$ of documents $d$, each of which consists of a list of sentences $s_i$, is:

$$L_\theta = \sum_{d \in C} \sum_{s_i \in d} \mathbb{E}[L(f_\theta(s_i,s_{i+1}), f_\theta(s_i,s'))]$$ (23.33)

$\mathbb{E}_{p(s'|s_i)}$ is the expectation with respect to the negative sampling distribution conditioned on $s_i$: given a sentence $s_i$ the algorithms samples a negative sentence $s'$
uniformly over the other sentences in the same document. \( L \) is a loss function that takes two scores, one for a positive pair and one for a negative pair, with the goal of encouraging \( f^+ = f_\theta(s_i, s_{i+1}) \) to be high and \( f^- = f_\theta(s_i, s'_i) \) to be low. Fig. 23.11 use the margin loss \( l(f^+, f^-) = \max(0, \eta - f^+ + f^-) \) where \( \eta \) is the margin hyper-parameter.

Xu et al. (2019) also give a useful baseline algorithm that itself has quite high performance in measuring perplexity: train an RNN language model on the data, and compute the log likelihood of sentence \( s_i \) in two ways, once given the preceding context (conditional log likelihood) and once with no context (marginal log likelihood). The difference between these values tells us how much the preceding context improved the predictability of \( s_i \), a predictability measure of coherence.

Training models to predict longer contexts than just consecutive pairs of sentences can result in even stronger discourse representations. For example a Transformer language model trained with a contrastive sentence objective to predict text up to a distance of \( \pm 2 \) sentences improves performance on various discourse coherence tasks (Iter et al., 2020).

Language-model style models are generally evaluated by the methods of Section 23.3.3, although they can also be evaluated on the RST and PDTB coherence relation tasks.

23.5 Global Coherence

A discourse must also cohere globally rather than just at the level of pairs of sentences. Consider stories, for example. The narrative structure of stories is one of the oldest kinds of global coherence to be studied. In his influential *Morphology of the Folktales*, Propp (1968) models the discourse structure of Russian folktales via a kind of plot grammar. His model includes a set of character categories he called *dramatis personae*, like Hero, Villain, Donor, or Helper, and a set of events he called *functions* (like “Villain commits kidnapping”, “Donor tests Hero”, or “Hero is pursued”) that have to occur in particular order, along with other components. Propp shows that the plots of each of the fairy tales he studies can be represented as...
a sequence of these functions, different tales choosing different subsets of functions, but always in the same order. Indeed Lakoff (1972) showed that Propp’s model amounted to a discourse grammar of stories, and in recent computational work Finlayson (2016) demonstrates that some of these Proppian functions could be induced from corpora of folktale texts by detecting events that have similar actions across stories. Bamman et al. (2013) showed that generalizations over dramatis personae could be induced from movie plot summaries on Wikipedia. Their model induced latent personae from features like the actions the character takes (e.g., Villains strangle), the actions done to them (e.g., Villains are foiled and arrested) or the descriptive words used of them (Villains are evil).

In this section we introduce two kinds of such global discourse structure that have been widely studied computationally. The first is the structure of arguments: the way people attempt to convince each other in persuasive essays by offering claims and supporting premises. The second is somewhat related: the structure of scientific papers, and the way authors present their goals, results, and relationship to prior work in their papers.

23.5.1 Argumentation Structure

The first type of global discourse structure is the structure of arguments. Analyzing people’s argumentation computationally is often called argumentation mining.

The study of arguments dates back to Aristotle, who in his Rhetorics described three components of a good argument: pathos (appealing to the emotions of the listener), ethos (appealing to the speaker’s personal character), and logos (the logical structure of the argument).

Most of the discourse structure studies of argumentation have focused on logos, particularly via building and training on annotated datasets of persuasive essays or other arguments (Reed et al. 2008, Stab and Gurevych 2014a, Peldszus and Stede 2016, Habernal and Gurevych 2017, Musi et al. 2018). Such corpora, for example, often include annotations of argumentative components like claims (the central component of the argument that is controversial and needs support) and premises (the reasons given by the author to persuade the reader by supporting or attacking the claim or other premises), as well as the argumentative relations between them like SUPPORT and ATTACK.

Consider the following example of a persuasive essay from Stab and Gurevych (2014b). The first sentence (1) presents a claim (in bold). (2) and (3) present two premises supporting the claim. (4) gives a premise supporting premise (3).

“(1) Museums and art galleries provide a better understanding about arts than Internet. (2) In most museums and art galleries, detailed descriptions in terms of the background, history and author are provided. (3) Seeing an artwork online is not the same as watching it with our own eyes, as (4) the picture online does not show the texture or three-dimensional structure of the art, which is important to study.”

Thus this example has three argumentative relations: SUPPORT(2,1), SUPPORT(3,1) and SUPPORT(4,3). Fig. 23.12 shows the structure of a much more complex argument.

While argumentation mining is clearly related to rhetorical structure and other kinds of coherence relations, arguments tend to be much less local; often a persuasive essay will have only a single main claim, with premises spread throughout the text, without the local coherence we see in coherence relations.
Algorithms for detecting argumentation structure often include classifiers for distinguishing claims, premises, or non-argumentation, together with relation classifiers for deciding if two spans have the SUPPORT, ATTACK, or neither relation (Peldszus and Stede, 2013). While these are the main focus of much computational work, there is also preliminary efforts on annotating and detecting richer semantic relationships (Park and Cardie 2014, Hidey et al. 2017) such as detecting argumentation schemes, larger-scale structures for argument like argument from example, or argument from cause to effect, or argument from consequences (Feng and Hirst, 2011).

Another important line of research is studying how these argument structure (or other features) are associated with the success or persuasiveness of an argument (Habernal and Gurevych 2016, Tan et al. 2016, Hidey et al. 2017. Indeed, while it is Aristotle’s logos that is most related to discourse structure, Aristotle’s ethos and pathos techniques are particularly relevant in the detection of mechanisms of this sort of persuasion. For example scholars have investigated the linguistic realization of features studied by social scientists like reciprocity (people return favors), social proof (people follow others’ choices), authority (people are influenced by those with power), and scarcity (people value things that are scarce), all of which can be brought up in a persuasive argument (Cialdini, 1984). Rosenthal and McKeown (2017) showed that these features could be combined with argumentation structure to predict who influences whom on social media, Althoff et al. (2014) found that linguistic models of reciprocity and authority predicted success in online requests, while the semisupervised model of Yang et al. (2019) detected mentions of scarcity, commitment, and social identity to predict the success of peer-to-peer lending platforms.

See Stede and Schneider (2018) for a comprehensive survey of argument mining.

23.5.2 The structure of scientific discourse

Scientific papers have a very specific global structure: somewhere in the course of the paper the authors must indicate a scientific goal, develop a method for a solution, provide evidence for the solution, and compare to prior work. One popular
annotation scheme for modeling these rhetorical goals is the **argumentative zoning** model of Teufel et al. (1999) and Teufel et al. (2009), which is informed by the idea that each scientific paper tries to make a **knowledge claim** about a new piece of knowledge being added to the repository of the field (Myers, 1992). Sentences in a scientific paper can be assigned one of 15 tags; Fig. 23.13 shows 7 (shortened) examples of labeled sentences.

<table>
<thead>
<tr>
<th>Category</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>AIM</td>
<td>Statement of specific research goal, or hypothesis of current paper</td>
<td>“The aim of this process is to examine the role that training plays in the tagging process”</td>
</tr>
<tr>
<td>OWN_METHOD</td>
<td>New Knowledge claim, own work: methods</td>
<td>“In order for it to be useful for our purposes, the following extensions must be made:”</td>
</tr>
<tr>
<td>OWN_RESULTS</td>
<td>Measurable/objective outcome of own work</td>
<td>“All the curves have a generally upward trend but always lie far below backoff (51% error rate)”</td>
</tr>
<tr>
<td>USE</td>
<td>Other work is used in own work</td>
<td>“We use the framework for the allocation and transfer of control of Whittaker...”</td>
</tr>
<tr>
<td>GAP_WEAK</td>
<td>Lack of solution in field, problem with other solutions</td>
<td>“Here, we will produce experimental evidence suggesting that this simple model leads to serious overestimates”</td>
</tr>
<tr>
<td>SUPPORT</td>
<td>Other work supports current work or is supported by current work</td>
<td>“Work similar to that described here has been carried out by Merialdo (1994), with broadly similar conclusions.”</td>
</tr>
<tr>
<td>ANTISUPPORT</td>
<td>Clash with other’s results or theory; superiority of own work</td>
<td>“This result challenges the claims of...”</td>
</tr>
</tbody>
</table>

**Figure 23.13** Examples for 7 of the 15 labels from the Argumentative Zoning labelset (Teufel et al., 2009).

Teufel et al. (1999) and Teufel et al. (2009) develop labeled corpora of scientific articles from computational linguistics and chemistry, which can be used as supervision for training standard sentence-classification architecture to assign the 15 labels.

### 23.6 Summary

In this chapter we introduced local and global models for discourse **coherence**.

- Discourses are not arbitrary collections of sentences; they must be **coherent**. Among the factors that make a discourse coherent are coherence relations between the sentences, entity-based coherence, and topical coherence.

- Various sets of **coherence relations** and **rhetorical relations** have been proposed. The relations in Rhetorical Structure Theory (**RST**) hold between spans of text and are structured into a tree. Because of this, shift-reduce and other parsing algorithms are generally used to assign these structures. The Penn Discourse Treebank (**PDTB**) labels only relations between pairs of spans, and the labels are generally assigned by sequence models.

- **Entity-based coherence** captures the intuition that discourses are about an entity, and continue mentioning the entity from sentence to sentence. **Centering Theory** is a family of models describing how salience is modeled for discourse entities, and hence how coherence is achieved by virtue of keeping the same discourse entities salient over the discourse. The **entity grid** model gives a more bottom-up way to compute which entity realization transitions lead to coherence.
Many different genres have different types of global coherence. Persuasive essays have claims and premises that are extracted in the field of argument mining, scientific articles have structure related to aims, methods, results, and comparisons.

Bibliographical and Historical Notes

Coherence relations arose from the independent development of a number of scholars, including Hobbs (1979) idea that coherence relations play an inferential role for the hearer, and the investigations by Mann and Thompson (1987) of the discourse structure of large texts. Other approaches to coherence relations and their extraction include Segmented Discourse Representation Theory (SDRT) (Asher and Lascarides 2003, Baldridge et al. 2007) and the Linguistic Discourse Model (Polanyi 1988, Scha and Polanyi 1988, Polanyi et al. 2004). Wolf and Gibson (2005) argue that coherence structure includes crossed bracketings, which make it impossible to represent as a tree, and propose a graph representation instead. A compendium of over 350 relations that have been proposed in the literature can be found in Hovy (1990).


Another aspect of global coherence is the global topic structure of a text, the way the topics shift over the course of the document. Barzilay and Lee (2004) introduced an HMM model for capturing topics for coherence, and later work expanded this intuition (Soricut and Marcu 2006, Elsner et al. 2007, Louis and Nenkova 2012, Li and Jurafsky 2017).

The relationship between explicit and implicit discourse connectives has been a fruitful one for research. Marcu and Echihabi (2002) first proposed to use sentences with explicit relations to help provide training data for implicit relations, by removing the explicit relations and trying to re-predict them as a way of improving performance on implicit connectives; this idea was refined by Sporleder and Lascarides (2005), (Pitler et al., 2009), and Rutherford and Xue (2015). This rela-
tionship can also be used as a way to create discourse-aware representations. The DisSent algorithm (Nie et al., 2019) creates the task of predicting explicit discourse markers between two sentences. They show that representations learned to be good at this task also function as powerful sentence representations for other discourse tasks.

The idea of entity-based coherence seems to have arisen in multiple fields in the mid-1970s, in functional linguistics (Chafe, 1976), in the psychology of discourse processing (Kintsch and Van Dijk, 1978), and in the roughly contemporaneous work of Grosz, Sidner, Joshi, and their colleagues. Grosz (1977a) addressed the focus of attention that conversational participants maintain as the discourse unfolds. She defined two levels of focus; entities relevant to the entire discourse were said to be in global focus, whereas entities that are locally in focus (i.e., most central to a particular utterance) were said to be in immediate focus. Sidner 1979; 1983 described a method for tracking (immediate) discourse foci and their use in resolving pronouns and demonstrative noun phrases. She made a distinction between the current discourse focus and potential foci, which are the predecessors to the backward- and forward-looking centers of Centering theory, respectively. The name and further roots of the centering approach lie in papers by Joshi and Kuhn (1979) and Joshi and Weinstein (1981), who addressed the relationship between immediate focus and the inferences required to integrate the current utterance into the discourse model. Grosz et al. (1983) integrated this work with the prior work of Sidner and Grosz. This led to a manuscript on centering which, while widely circulated since 1986, remained unpublished until Grosz et al. (1995). A collection of centering papers appears in Walker et al. (1998b). See Karamanis et al. (2004) and Poesio et al. (2004) for a deeper exploration of centering and its parameterizations, and the History section of Chapter 26 for more on the use of centering on coreference.

The grid model of entity-based coherence was first proposed by Barzilay and Lapata (2005) drawing on earlier work by Lapata (2003) and Barzilay, and then extended by them Barzilay and Lapata (2008) and others with additional features (Elsner and Charniak 2008, 2011, Feng et al. 2014, Lin et al. 2011) a model that projects entities into a global graph for the discourse (Guinaudeau and Strube 2013, Mesgar and Strube 2016), and a convolutional model to capture longer-range entity dependencies (Nguyen and Joty, 2017).

Theories of discourse coherence have also been used in algorithms for interpreting discourse-level linguistic phenomena, including verb phrase ellipsis and gapping (Asher 1993, Kehler 1993), and tense interpretation (Lascarides and Asher 1993, Kehler 1994, Kehler 2000). An extensive investigation into the relationship between coherence relations and discourse connectives can be found in Knott and Dale (1994). Useful surveys of discourse processing and structure include Stede (2011) and Webber et al. (2012).

Andy Kehler wrote the Discourse chapter for the 2000 first edition of this textbook, which we used as the starting point for the second-edition chapter, and there are some remnants of Andy’s lovely prose still in this third-edition coherence chapter.
Exercises

23.1 Finish the Centering Theory processing of the last two utterances of (23.30), and show how (23.29) would be processed. Does the algorithm indeed mark (23.29) as less coherent?

23.2 Select an editorial column from your favorite newspaper, and determine the discourse structure for a 10–20 sentence portion. What problems did you encounter? Were you helped by superficial cues the speaker included (e.g., discourse connectives) in any places?
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