

# Discussion of "Yield Curve Premia" by Brooks and Moskowitz

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## summary

- "carry" and "value" predict excess returns on government bonds
- "momentum" is not important/significant
- subsume information in other predictors used in literature
- builds on evidence on gov bonds in Toby's previous work on value & momentum everywhere, carry

## comments

- what are the predictors? how do they relate to what we know?
- factor structure in expected returns?
- do they subsume information in other predictors?
- lessons for economics?
- discussion focuses on US evidence, paper has international data

## what are the predictors?

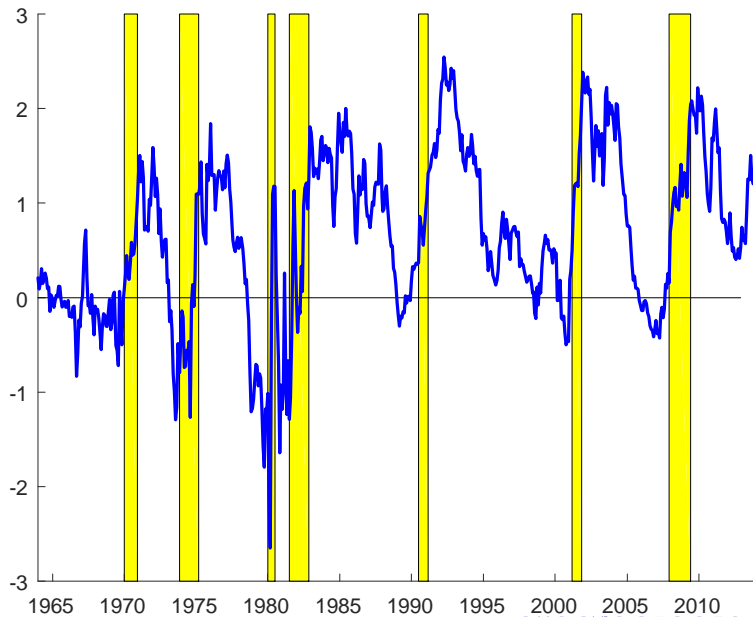
- "carry" = slope = long rate – short rate =  $y_t^{(n)} - y_t^{(1)}$
- each bond  $n$  has its own slope
- classic predictor, Campbell and Shiller (1991)

$$r_{t+1}^{(n)} = \alpha_n + \beta_n \left( y_t^{(n)} - y_t^{(1)} \right)$$

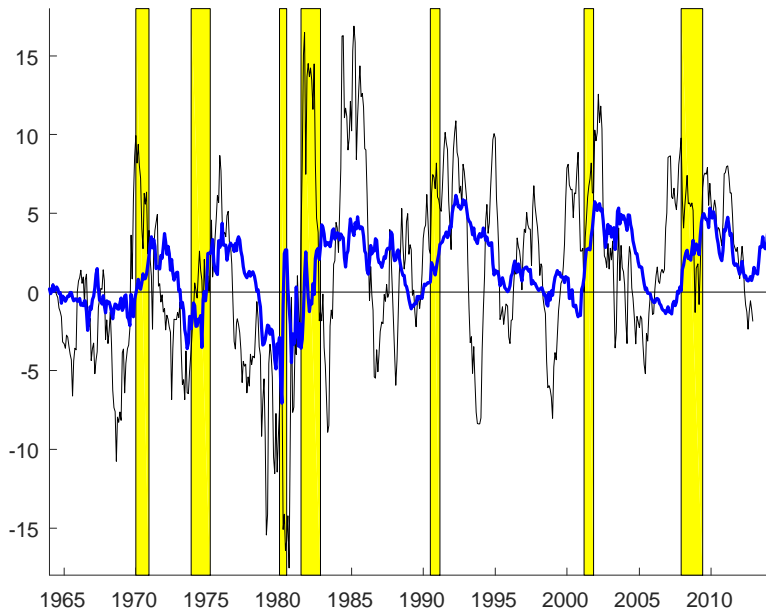
- monthly data 1964-2013

$n$	$\beta_n$	t-stat	$R^2$
2	1.7	3.6	0.12
3	2.1	3.7	0.14
4	2.5	4.1	0.17
5	2.5	3.9	0.15

# slope for 5 year bond



## slope forecast of excess returns on 5 year bond



## what are the predictors?

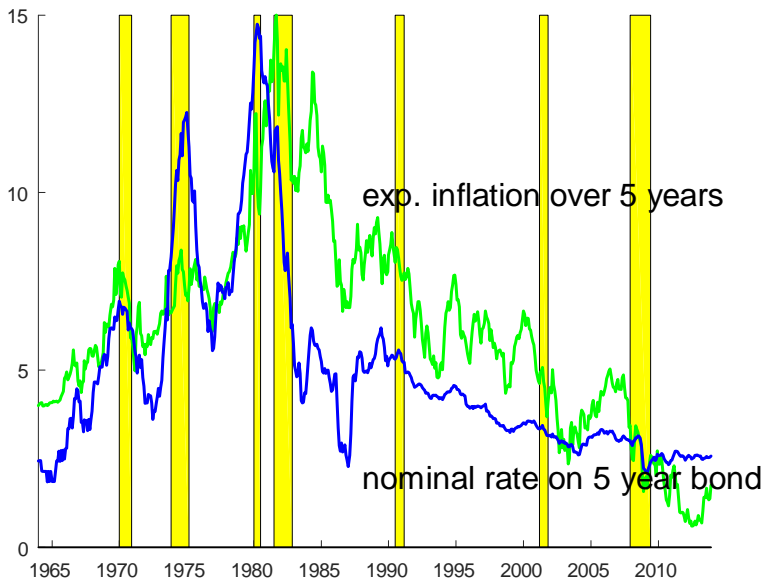
- "value" = real rate  
= nominal rate – exp. inflation over life of the bond  
=  $y_t^{(n)} - E[\pi_{t \rightarrow t+n}]$
- each bond  $n$  has its own real rate
- recent debate about expected inflation as predictor  
one observation: Great Inflation  
54%  $R^2$  in Cieslak and Povala (2015), Bauer and Hamilton (2016),  
Cochrane (2016) gets 62% with a time-trend

monthly data 1985-2013

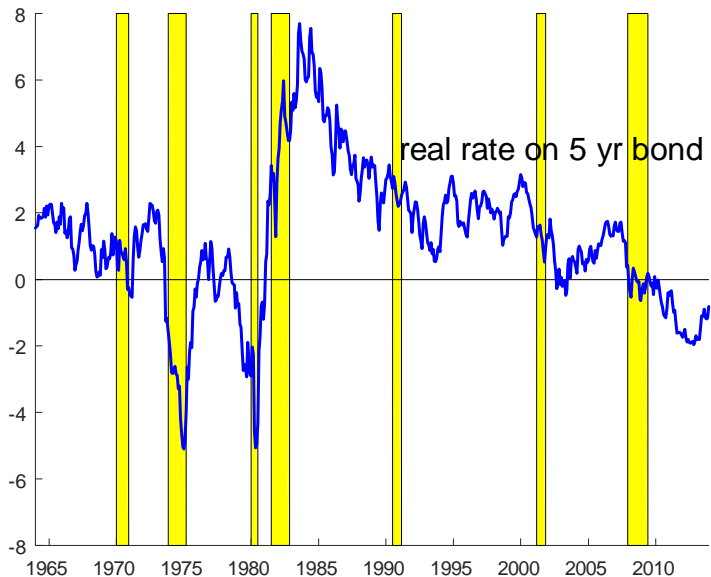
$n$	$R^2$ with all interest rates	include time trend
2	0.17	0.45
3	0.15	0.52
4	0.18	0.58
5	0.17	0.61

- here: exp. inflation over life of the bond, what happens here?

# nominal rate and expected inflation

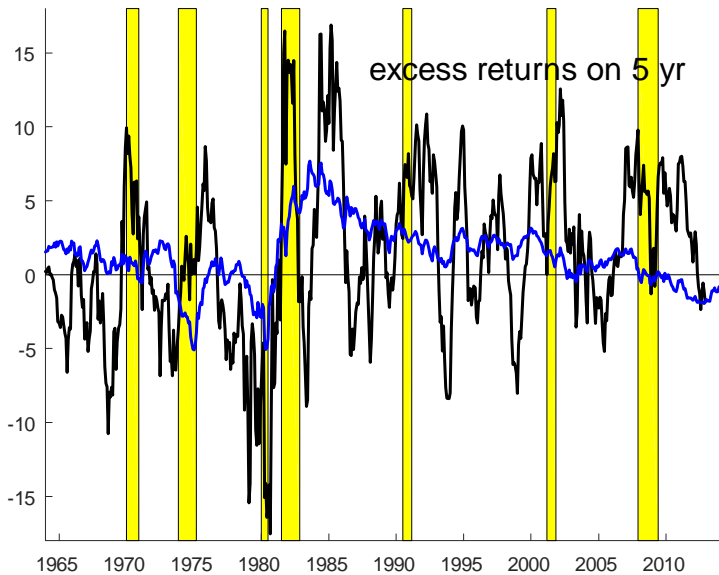


# real rate





# real rate prediction of excess returns



$R^2 = 14\%$ , smaller after 1985

## what are the predictors?

- "momentum" = return of the bond over the last year
- momentum is not important/significant for bonds

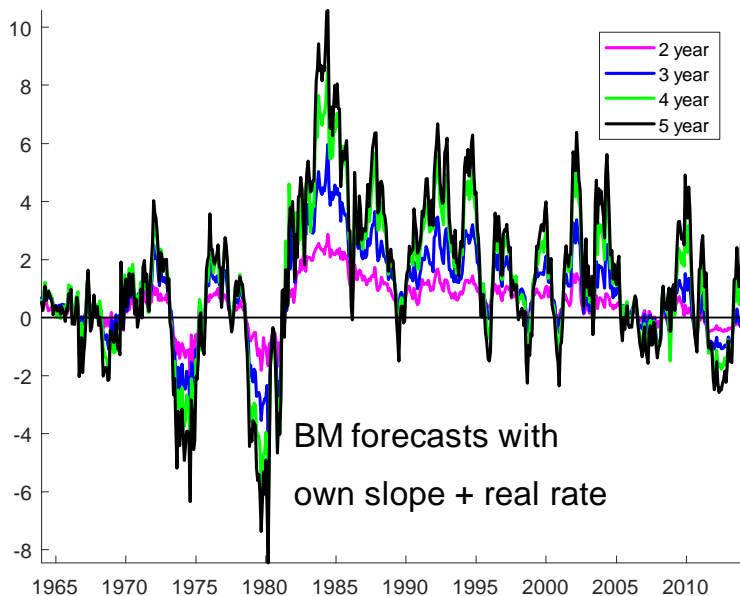
### summary of predictors in Brooks & Moskowitz

- 2 predictors for excess returns: for each bond  $n$ , find
  1. its slope  $y_t^{(n)} - y_t^{(1)}$
  2. its real rate  $y_t^{(n)} - E[\pi_{t \rightarrow t+n}]$
- predictors are nominal rates and exp. inflation over various horizons

## factor structure in expected returns?

- single factor structure in expected returns, Cochrane & Piazzesi 2005
- intuitively: fitted values are linear functions of nominal rates, which have strong factor structure
- does expected inflation over various horizons destroy it?

## factor structure in expected excess returns?



## factor structure in expected returns across bonds?

- procedure as in Cochrane & Piazzesi 2005
- collect  $f_t$  = all slopes and real rates for all bonds  $n$
- restricted regression:

1. run regression for cross-sectional average

$$\bar{r}x_{t+1} = \gamma^\top f_t + \varepsilon_{t+1}$$

get fitted value  $\hat{\gamma}^\top f_t$

2. run individual bond regressions on fitted value

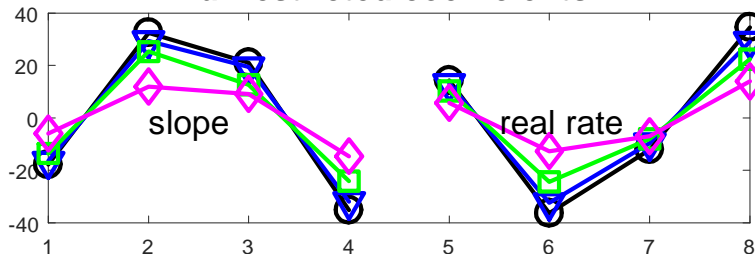
$$rx_{t+1}^{(n)} = \beta_n \left( \hat{\gamma}^\top f_t \right) + \varepsilon_{t+1}^{(n)}$$

$n$	restricted $R^2$	unrestricted $R^2$
2	0.26	0.28
3	0.29	0.30
4	0.33	0.33
5	0.30	0.31

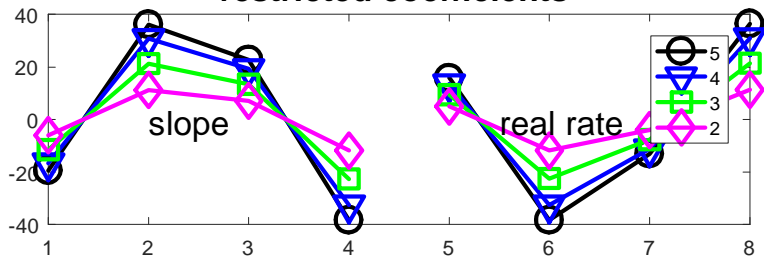
- compare restricted  $\beta_n \hat{\gamma}^\top$  and unrestricted coefficients

# factor structure in expected returns across bonds?

## unrestricted coefficients



## restricted coefficients



## do slope and real rate subsume other factors?

- depends on data and sample
- for example, not in monthly Fama-Bliss data, 1964-2013

$n$	slope	real rate	$R^2$	CP	$R^2$	slope	real rate	CP	$R^2$
2	1.2 (2.1)	0.2 (1.9)	0.20	0.5 (5.3)	0.20	0.03 (0.1)	0.2 (1.6)	0.3 (2.9)	0.25
3	1.9 (2.8)	0.4 (2.0)	0.23	0.9 (5.3)	0.21	0.22 (0.5)	0.3 (1.6)	0.6 (2.8)	0.26
4	2.5 (3.7)	0.6 (2.0)	0.27	1.3 (5.5)	0.25	0.60 (1.0)	0.4 (1.5)	0.9 (2.7)	0.29
5	2.6 (4.0)	0.7 (2.0)	0.26	1.5 (5.2)	0.23	1.5 (1.5)	0.5 (1.6)	0.7 (1.7)	0.28

- yes in quarterly GSW data for 10-year bond, 1972-2016

## lessons for economics?

- evidence for a single factor in expected bond returns
- then bond markets are not segmented much
- standard models that generate time-varying risk premium are fine beliefs (e.g., learning), risk aversion (e.g., habits), risk (e.g., stochastic vol, ambiguity), liquidity risk, etc.
- here, each bond has its own factors: its slope and its real rate
- do we need a model with segmented bond markets?  
QE-style models as Vayanos & Vila?
- how are bond factors related to those in other asset markets, e.g. stocks and foreign exchange?
- hard to interpret the numbers in Table XII, needs more work!