

NOMAD: A Distributed Framework for Latent Variable Models

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NIPS 2014 Workshop:
Distributed Machine Learning and Matrix Computations

- Challenges
- Matrix Completion
 - Stochastic Gradient Method
 - Existing Distributed Approaches
 - Our Solution: NOMAD-MF
- Latent Dirichlet Allocation (LDA)
 - Gibbs Sampling
 - Existing Distributed Solutions: AdLDA, Yahoo LDA
 - Our Solution: F+NOMAD-LDA

Large-scale Latent Variable Modeling

- Latent Variable Models: very useful in many applications
 - Latent models for recommender systems (e.g., MF)
 - Topic models for document corpus (e.g., LDA)
- Fast growth of data
 - Almost 2.5×10^{18} bytes of data added each day
 - 90% of the world's data today was generated in the past two year

- *Algorithmic* as well as *hardware* level
 - Many effective algorithms involve fine-grain iterative computation
⇒ hard to parallelize
 - Many current parallel approaches
 - bulk synchronization
⇒ **wasted CPU** power when communicating
 - complicated locking mechanism
⇒ **hard to scale** to many machines
 - asynchronous computation using parameter server
⇒ **not serializable, danger of stale parameters**
- Proposed **NOMAD Framework**
 - access graph analysis to exploit parallelism
 - asynchronous computation, non-blocking communication, and lock-free
 - serializable (or almost serializable)
 - successful applications: MF and LDA

Matrix Factorization: Recommender Systems

Recommender Systems

Rating Matrix

Users

| | Movie 1 | Movie 2 | | | | | | Movie 10 | Movie 11 |
|--|---------|---------|---|---|---|---|---|----------|----------|
|  Hatang-Fu | 1 | | 5 | | | 3 | | 5 | 2 |
|  Choi-Jui | | 2 | 3 | | | 5 | | 2 | 5 |
|  Si Si | | | | 3 | ? | 5 | | 3 | |
|  Inderjit | 2 | | 5 | | 3 | | 4 | | 2 |
|  Kai-Yang | | | | 5 | | 5 | | | 1 |
|  Donghyuk | | 5 | | | 1 | | | 5 | |
|  Kuga | 1 | | | 1 | | | 2 | | 4 |

Matrix Factorization Approach $A \approx WH^T$

H^T

| | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| -0.07 | -0.11 | -0.53 | -0.46 | -0.06 | -0.05 | -0.53 | -0.07 | -0.35 | -0.19 | -0.14 |
| 0.13 | -0.42 | 0.45 | 0.17 | -0.25 | -0.17 | -0.18 | 0.27 | -0.59 | 0.05 | 0.14 |
| -0.21 | -0.43 | -0.23 | 0.16 | 0.08 | 0.17 | 0.57 | -0.39 | -0.37 | -0.08 | -0.15 |

W

| | | |
|-------|-------|-------|
| -8.72 | 0.03 | -1.03 |
| -7.56 | -0.79 | 0.62 |
| -4.07 | -3.95 | 2.55 |
| -3.52 | 3.73 | -3.32 |
| -7.78 | 2.34 | 2.33 |
| -2.44 | -5.29 | -3.92 |
| -1.78 | 1.90 | -1.68 |

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| 1 | | | 5 | | | 3 | | 5 | | 2 |
| | 2 | | 3 | | | 5 | | 2 | 5 | |
| | | | | 3 | | 5 | | 3 | | |
| 2 | | 5 | | | 3 | | 4 | | 2 | |
| | | | 5 | | | 5 | | | | 1 |
| | 5 | | | 1 | | | | 5 | | |
| 1 | | | 1 | | | | 2 | | | 4 |

Matrix Factorization Approach $A \approx WH^T$

H^T

| | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
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| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| 1 | | | 5 | | | 3 | | 5 | | 2 |
| | 2 | | 3 | | | 5 | | 2 | 5 | |
| | | | | 3 | ? | 5 | | 3 | | |
| 2 | | 5 | | | 3 | | 4 | | 2 | |
| | | | 5 | | | 5 | | | | 1 |
| | 5 | | | 1 | | | | 5 | | |
| 1 | | | 1 | | | | 2 | | | 4 |

Matrix Factorization Approach

$$\min_{\substack{W \in \mathcal{R}^{m \times k} \\ H \in \mathcal{R}^{n \times k}}} \sum_{(i,j) \in \Omega} (A_{ij} - w_i^T h_j)^2 + \lambda (\|W\|_F^2 + \|H\|_F^2),$$

- $\Omega = \{(i, j) \mid A_{ij} \text{ is observed}\}$
- Regularized terms to avoid over-fitting

A transform maps users/items to **latent feature space** \mathbb{R}^k

- the i^{th} user $\Rightarrow i^{\text{th}}$ row of W , w_i^T ,
- the j^{th} item $\Rightarrow j^{\text{th}}$ column of H^T , h_j .
- $w_i^T h_j$: measures the interaction.

SGM: Stochastic Gradient Method

SGM update: pick $(i, j) \in \Omega$

- $R_{ij} \leftarrow A_{ij} - w_i^T h_j,$
- $w_i \leftarrow w_i - \eta \left(\frac{\lambda}{|\Omega_i|} w_i - R_{ij} h_j \right),$
- $h_j \leftarrow h_j - \eta \left(\frac{\lambda}{|\Omega_j|} h_j - R_{ij} w_i \right),$

Ω_i : observed ratings of i -th row.

$\bar{\Omega}_j$: observed ratings of j -th column.

An iteration : $|\Omega|$ updates

- Time per update: $O(k)$
- Time per iteration: $O(|\Omega|k),$
better than $O(|\Omega|k^2)$ for ALS

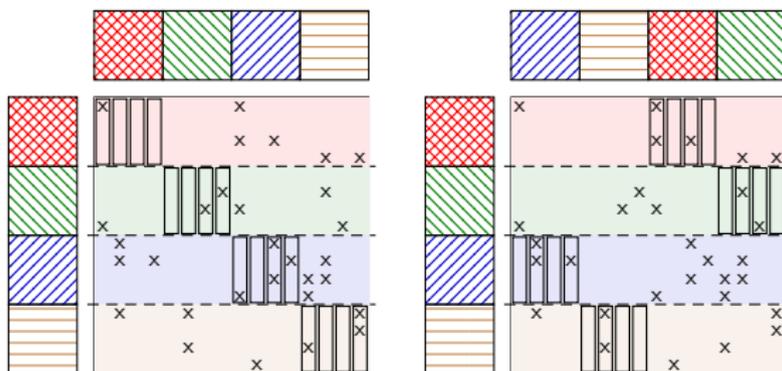
$$\begin{pmatrix} h_1 & h_2 & h_3 \end{pmatrix}$$
$$\begin{pmatrix} w_1^T \\ w_2^T \\ w_3^T \end{pmatrix} \begin{pmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{pmatrix}$$

Parallel Stochastic Gradient Descent for MF

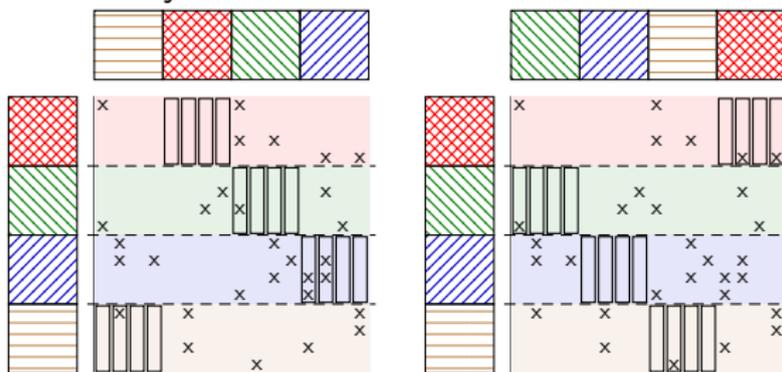
Challenge: direct parallel updates \Rightarrow memory conflicts.

- Multi-core parallelization
 - Hogwild [Niu 2011]
 - Jellyfish [Recht et al, 2011]
 - FPSGD** [Zhuang et al, 2013]
- Multi-machine parallelization:
 - DSGD [Gemulla et al, 2011]
 - DSGD ++ [Teflioudi et al, 2013]

DSGD/JellyFish [Gemulla et al, 2011; Recht et al, 2011]



Synchronize and communicate



Synchronize and communicate

Proposed Asynchronous Approach: NOMAD-MF [Yun et al, 2014]

Most existing parallel approaches require

- **Synchronization** and/or
 - E.g., ALS, DSGD/JellyFish, DSGD++, CCD++
 - Computing power is wasted:
 - Interleaved computation and communication
 - Curse of the last reducer
- **Locking** and/or
 - E.g., parallel SGD, FPSGD**
 - A standard way to avoid conflict and guarantee *serializability*
 - Complicated remote locking slows down the computation
 - Hard to implement efficient locking on a distributed system
- **Computation using stale values**
 - E.g., Hogwild, Asynchronous SGD using parameter server
 - Lack of serializability

Q: Can we avoid both *synchronization* and *locking* but keep CPU from being *idle* and guarantee *serializability*?

Our answer: NOMAD

A: Yes, NOMAD keeps CPU and network busy simultaneously

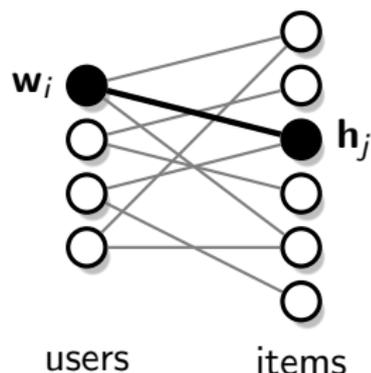
- *Stochastic gradient* update rule
 - only a small set of variables involved
- *Nomadic token passing*
 - widely used in telecommunication area
 - avoids conflict without explicit remote locking
 - Idea: “owner computes”
 - NOMAD: multiple “active tokens” and nomadic passing

Features:

- fully asynchronous computation
- lock-free implementation
- non-blocking communication
- serializable update sequence

Access Graph for Stochastic Gradient

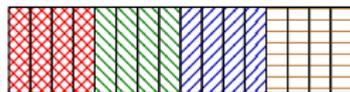
- Access graph $G = (V, E)$:
 - $V = \{\mathbf{w}_i\} \cup \{\mathbf{h}_j\}$
 - $E = \{e_{ij} : (i, j) \in \Omega\}$
- Connection to SG:
 - each e_{ij} corresponds to a SG update
 - only access to \mathbf{w}_i and \mathbf{h}_j
- Parallelism:
 - edges without common node can be updated in parallel
 - identify “matching” in the graph
- Nomadic Token Passing:
 - mechanism s.t. active edges always form a “matching”
 - serializability guaranteed



More Details

Nomadic Tokens for $\{h_j\}$:

- n tokens
- (j, h_j) : $O(k)$ space



Worker:

- p workers
- a computing unit + a concurrent token queue
- a block of W : $O(mk/p)$
- a block row of A : $O(|\Omega|/p)$

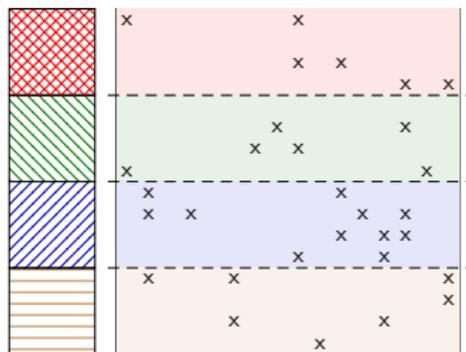


Illustration of NOMAD communication

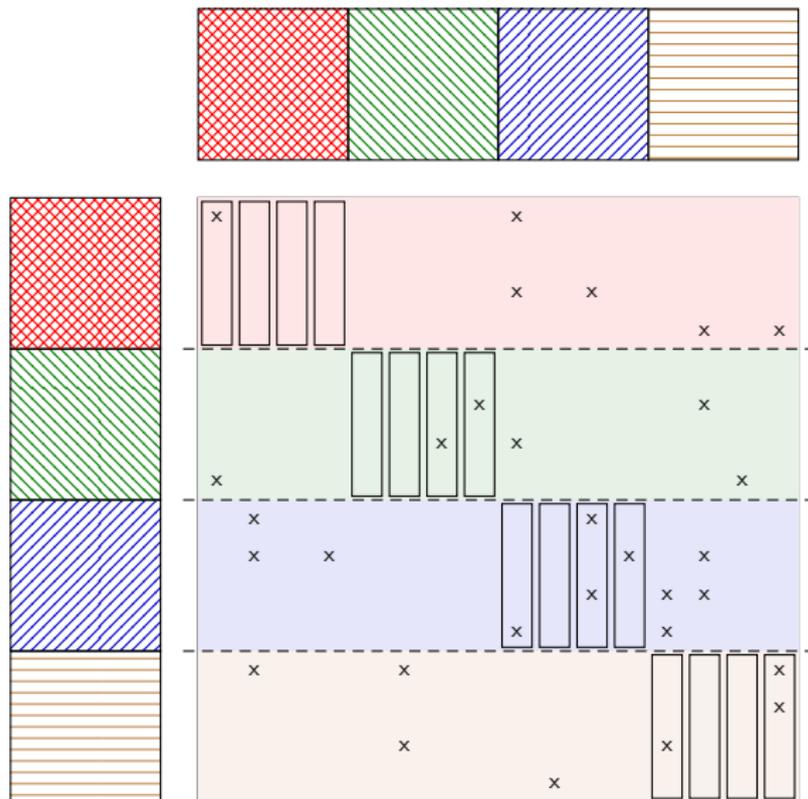


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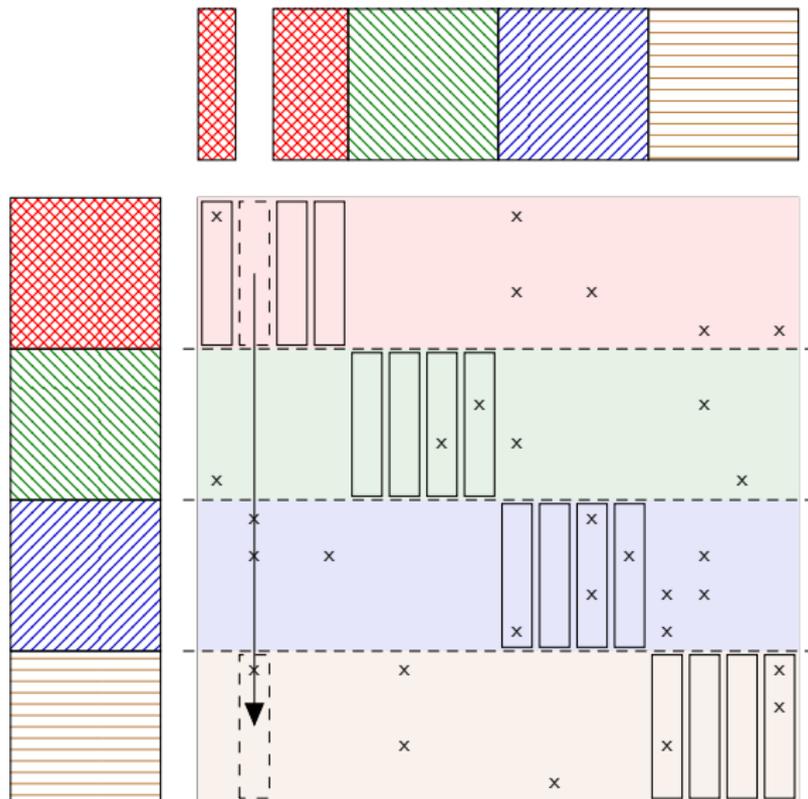


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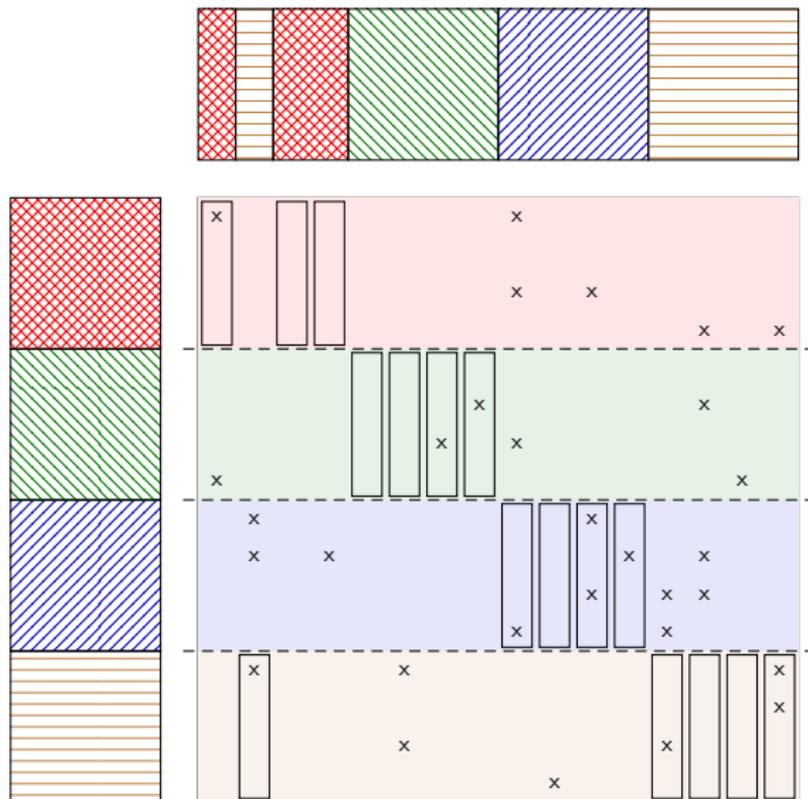


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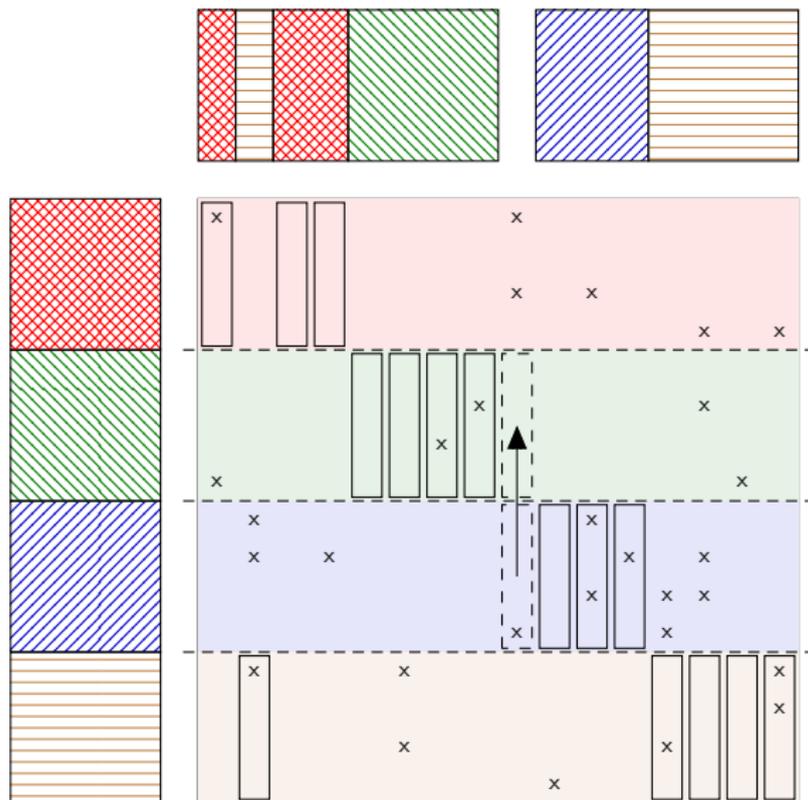


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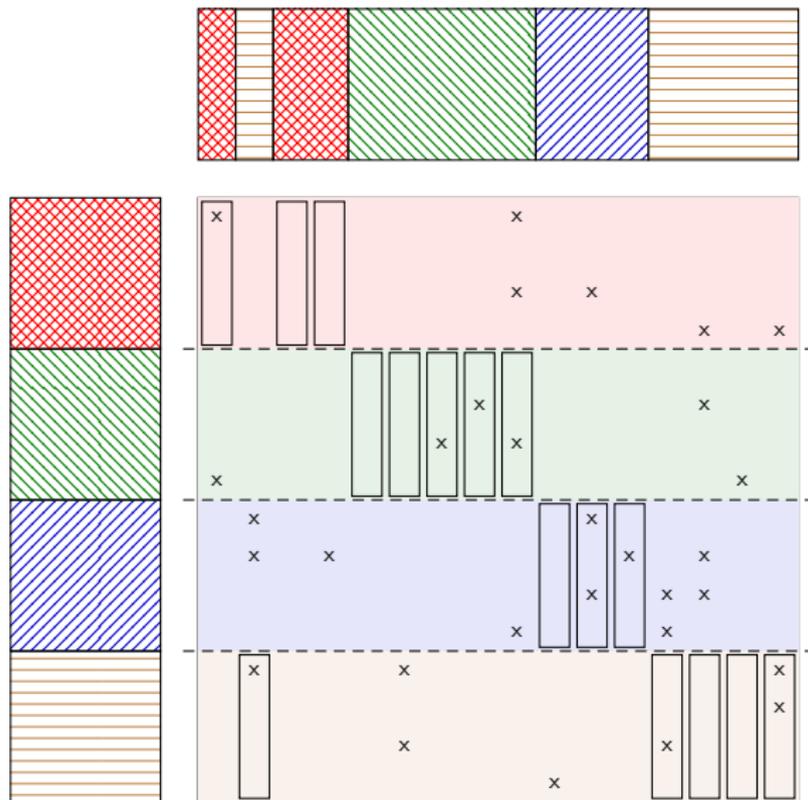


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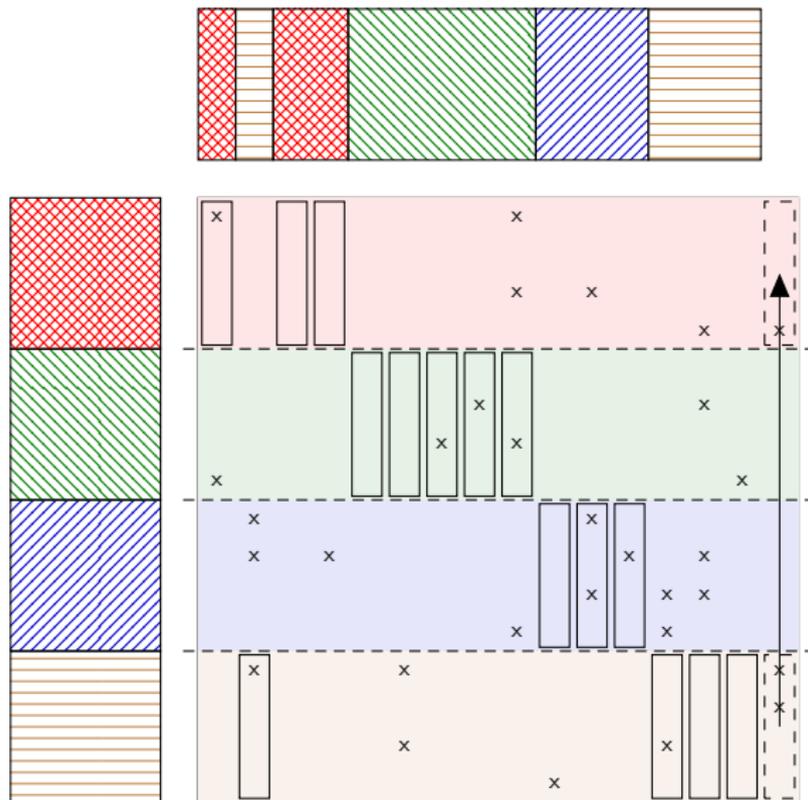


Illustration of NOMAD communication

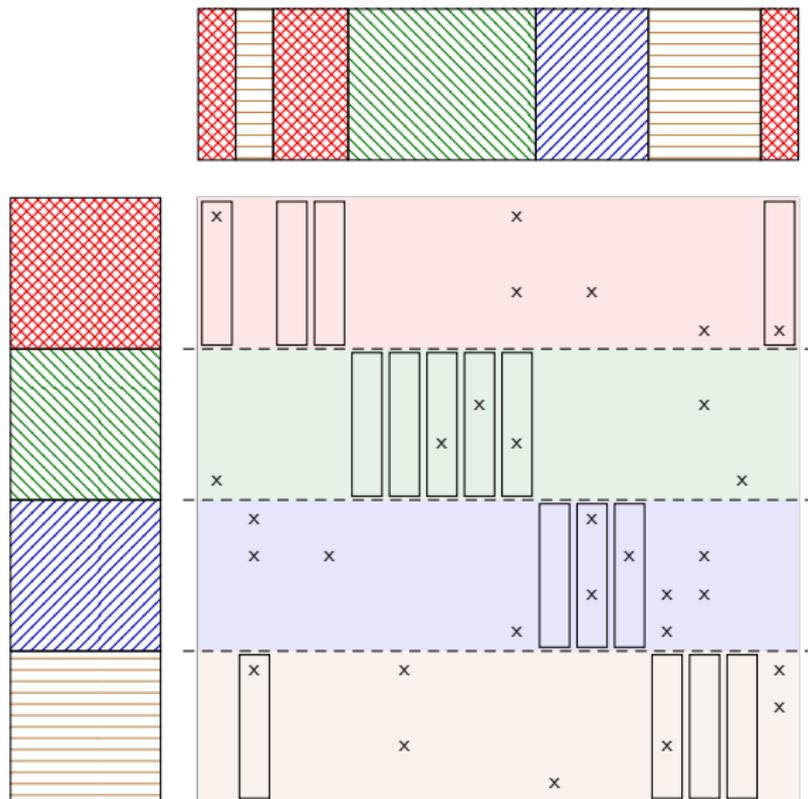


Illustration of NOMAD communication

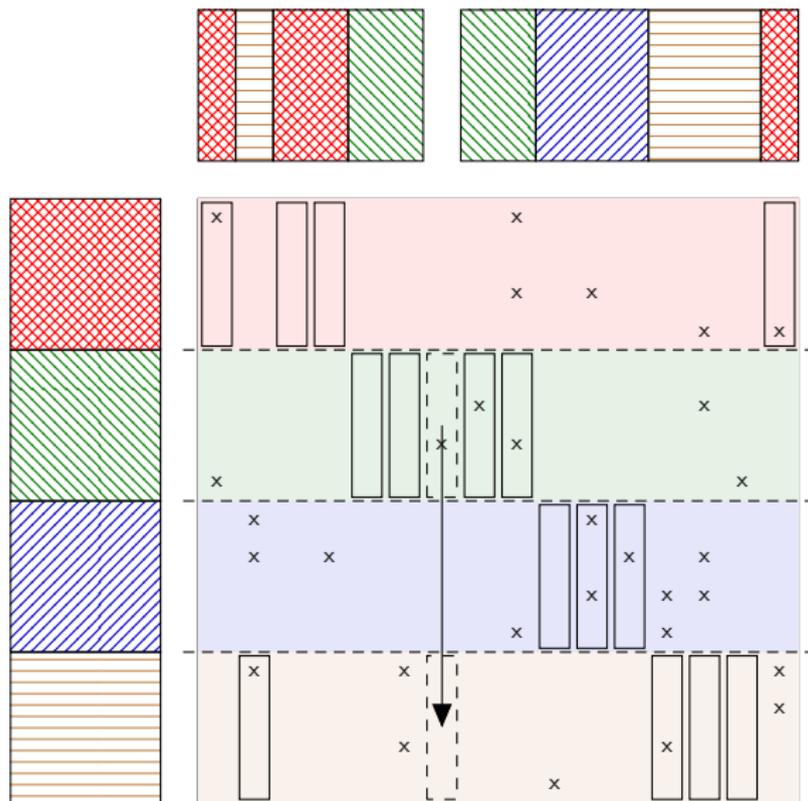


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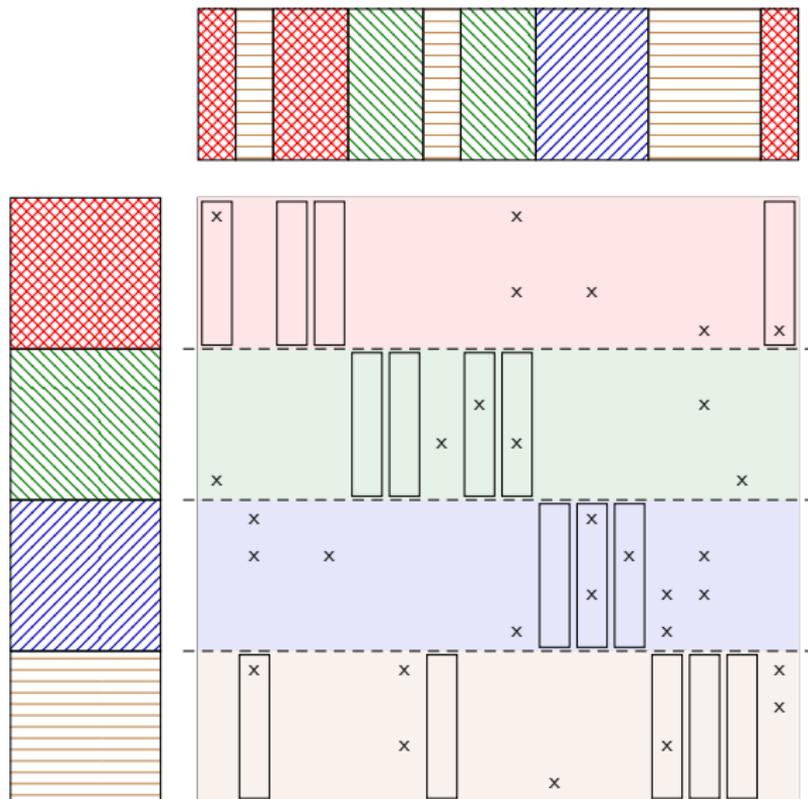


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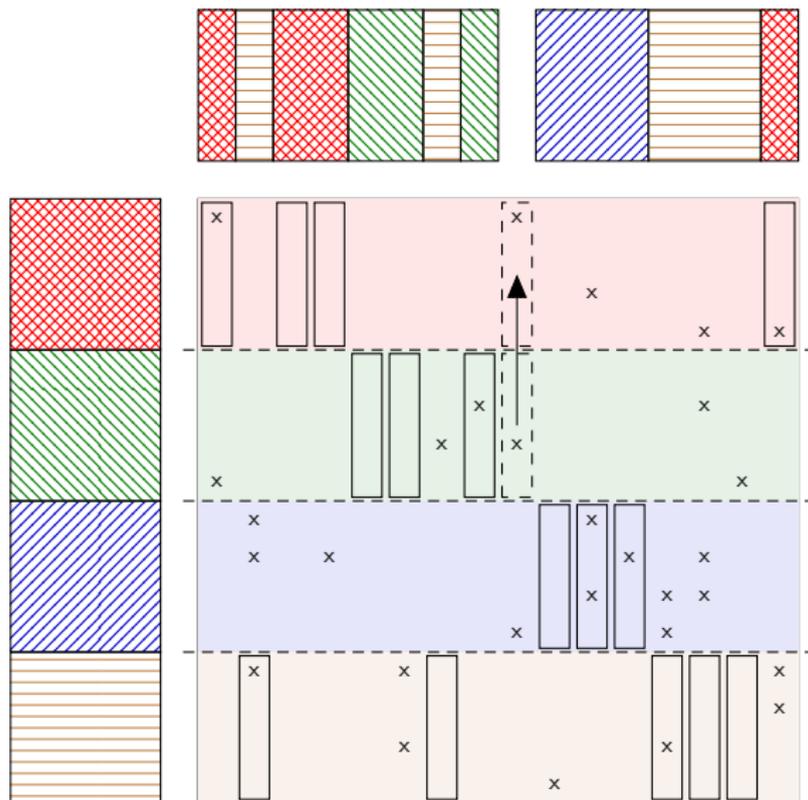
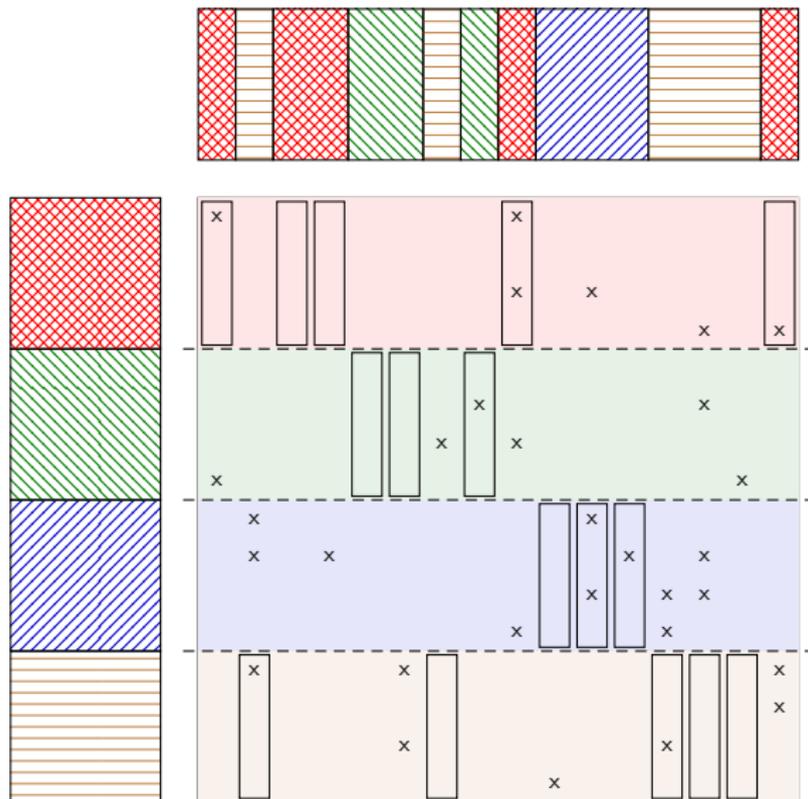


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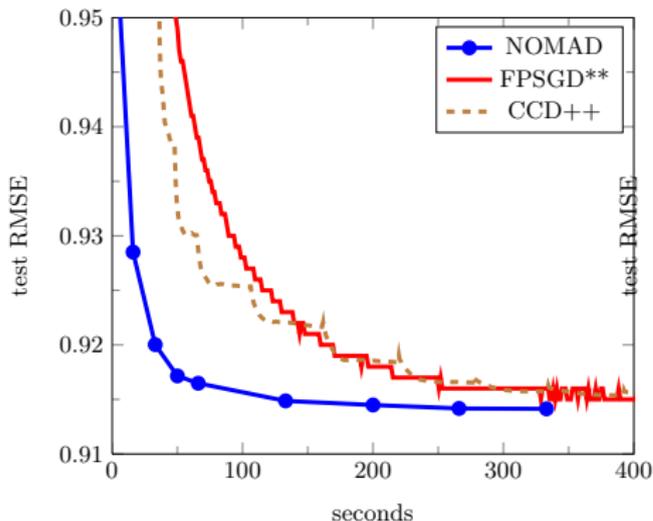


Comparison on a Multi-core System

- On a 32-core processor with enough RAM.
- Comparison: NOMAD, FPSGD**, and CCD++.

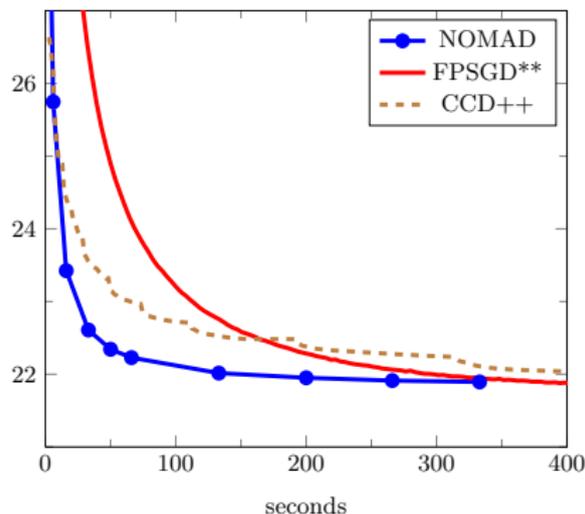
(100M ratings)

Netflix, machines=1, cores=30, $\lambda = 0.05$, $k = 100$



(250M ratings)

Yahoo!, machines=1, cores=30, $\lambda = 1.00$, $k = 100$

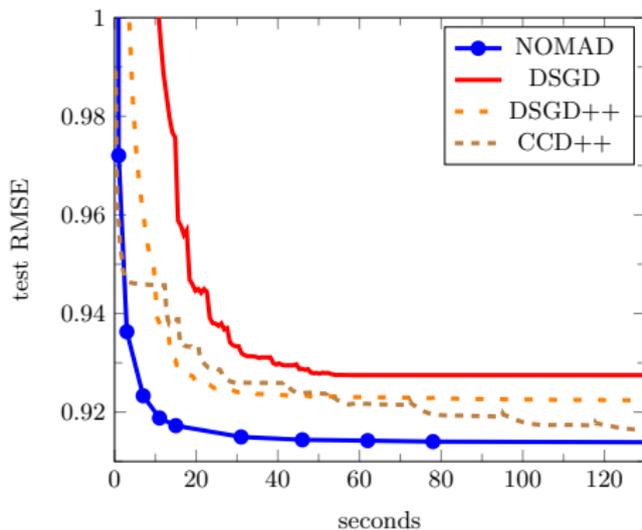


Comparison on a Distributed System

- On a distributed system with 32 machines.
- Comparison: NOMAD, DSGD, DSGD++, and CCD++.

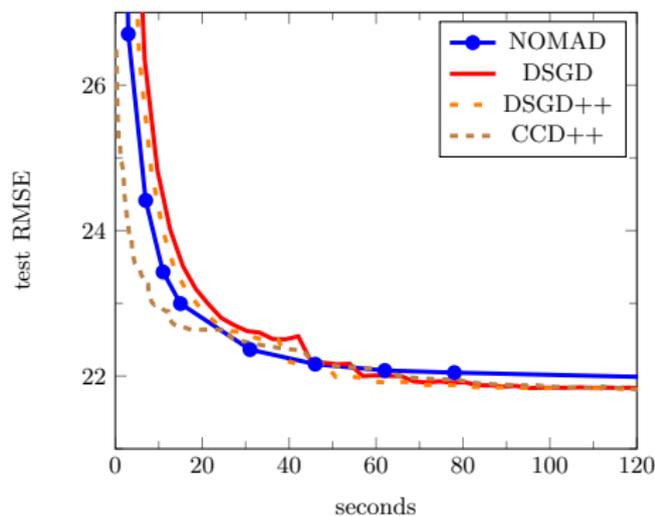
(100M ratings)

Netflix, machines=32, cores=4, $\lambda = 0.05$, $k = 100$



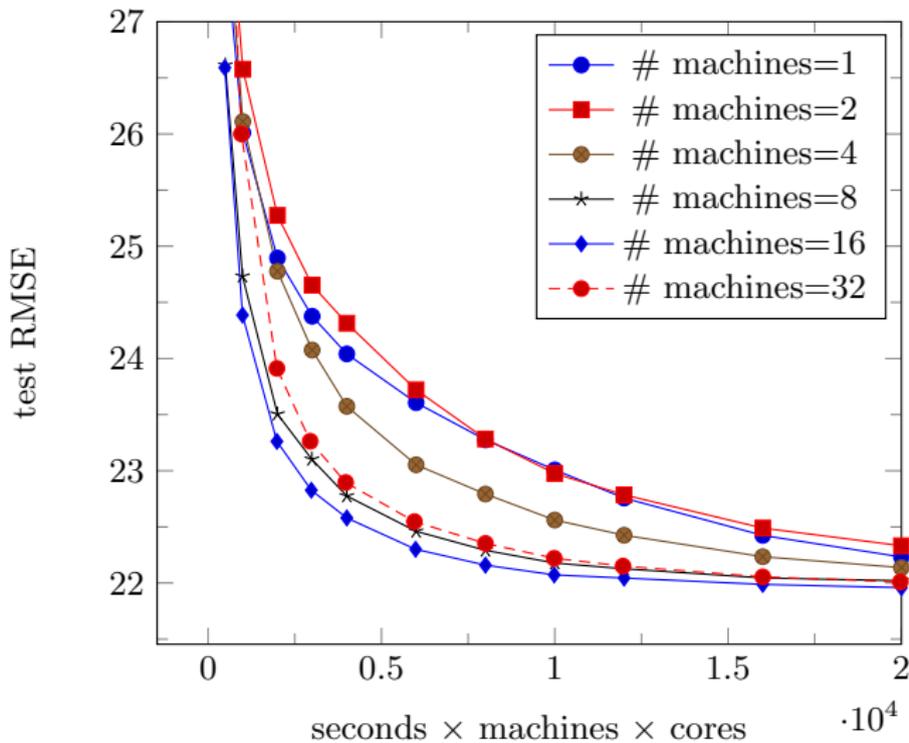
(250M ratings)

Yahoo!, machines=32, cores=4, $\lambda = 1.00$, $k = 100$



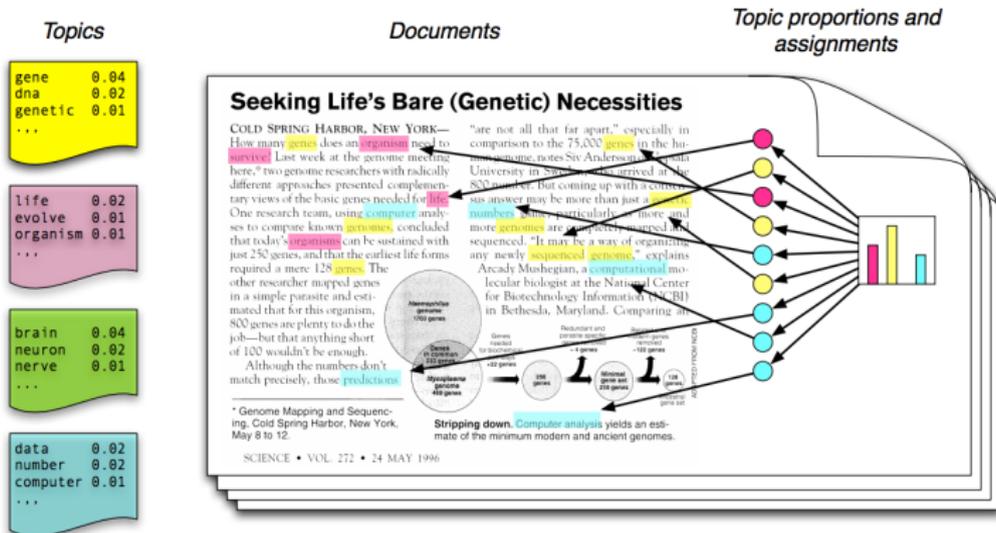
Super Linear Scaling of NOMAD-MF

Yahoo!, cores=4, $\lambda = 1.00$, $k = 100$



Topic Modeling: Latent Dirichlet Allocation

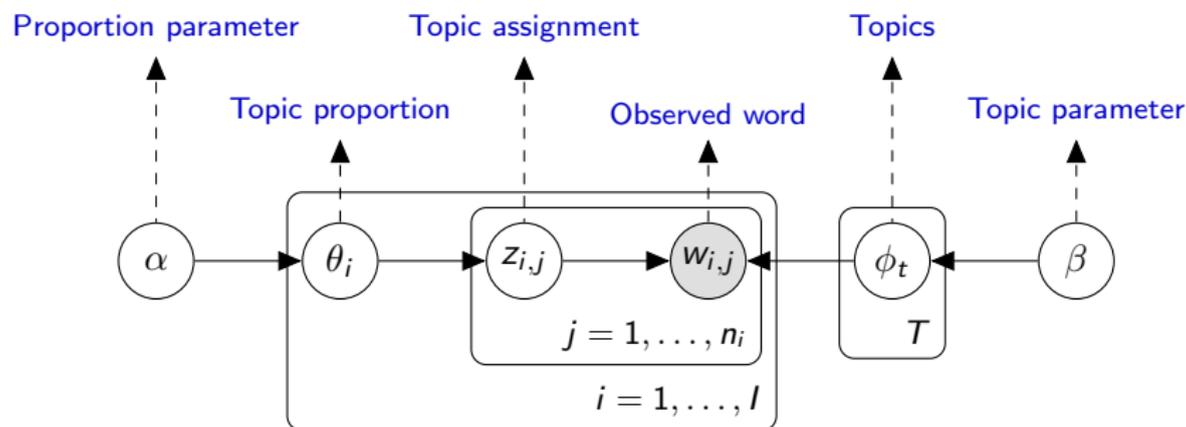
Latent Dirichlet Allocation (LDA)



- Each **topic** is a multinomial distribution over words
- Each **document** is a multinomial distribution over topics
- Each **word** is drawn from one of these topics

¹source: <http://www.cs.columbia.edu/~blei/papers/icml-2012-tutorial.pdf>

Graphical Model for LDA

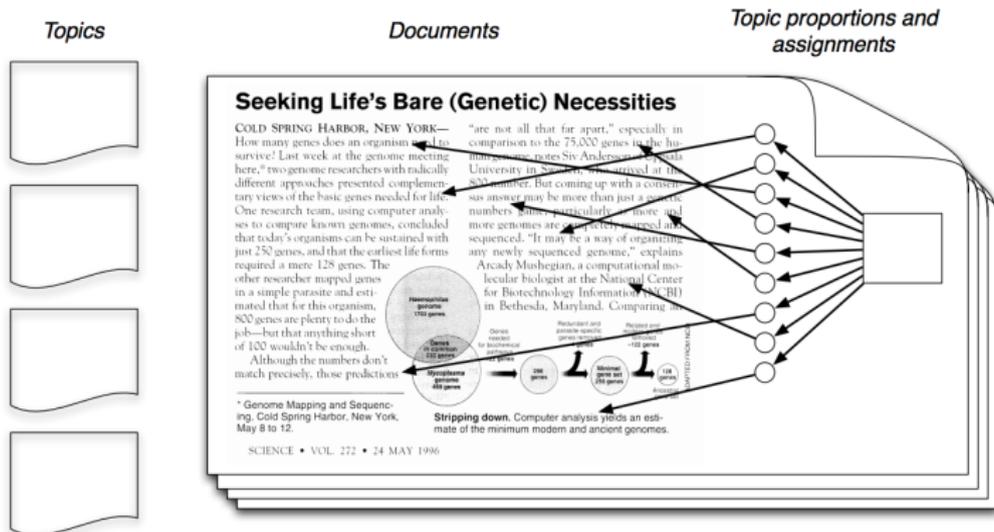


- Joint distribution

$$Pr(\cdot) = \prod_{t=1}^T Pr(\phi_t | \beta) \prod_{i=1}^l Pr(\theta_i | \alpha) \left(\prod_{j=1}^{n_i} Pr(z_{i,j} | \theta_i) Pr(w_{i,j} | \phi_{z_{i,j}}) \right)$$

- $Pr(\phi_t | \beta)$, $Pr(\theta_i | \alpha)$: Dirichlet distributions
- $Pr(w | \phi_t)$, $Pr(z | \theta_i)$: multinomial distributions

Inference for LDA



- Only documents are observed
- $\theta_t, \phi_t, Z_{i,j}$ are **latent**
- Goal: infer these latent structures

¹source: <http://www.cs.columbia.edu/~blei/papers/icml-2012-tutorial.pdf>

Posterior Inference for LDA

Task: $Pr(\theta_i, \phi_t, z_{i,j} \mid \{d_i\}, \alpha, \beta)$

- Given
 - a corpus of documents $\{d_i : i = 1, \dots, N\}$, α, β
 - each document $d_i = \{w_{i,j} : j = 1, \dots, n_i\}$
- Exact inference for $z_{i,j}, \theta_i, \phi_t$
 - Intractable
 - Latent variables are dependent when conditioned on data

Approximate Inference approaches:

- Variational Methods
 - See [Blei et al, 2003]
 - an optimization approach
 - runs **faster**
 - but generates **biased** results
- Gibbs Samplings
 - See [Griffiths & Steyvers, 2004]
 - an MCMC approach
 - more **accurate**
 - but **slower** with a vanilla implementation

Goal: Design a scalable Gibbs sampler for LDA

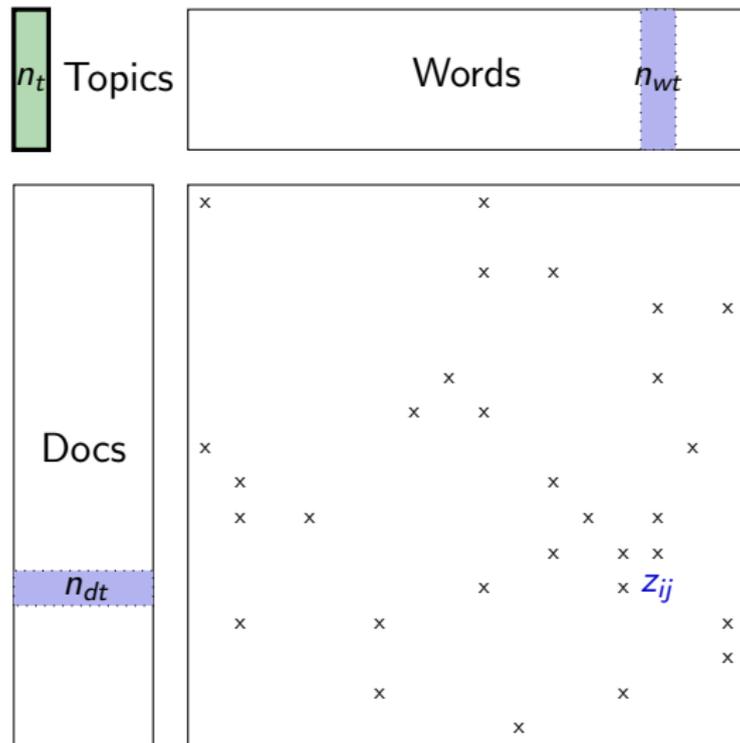
Gibbs Sampling for LDA [Griffiths & Steyvers, 2004]

- Count matrices for topic assignment $\{z_{i,j}\}$:
 - n_{dt} : # words of document d assigned to topic t
 - n_{wt} : # of times word w assigned to topic t
 - $n_t := \sum_w n_{wt} = \sum_d n_{dt}$
- Gibbs Sampling Step
 - 1 choose $w := w_{i,j}$ with old assignment $t_o := z_{i,j}$ of document $d := d_i$
 - 2 Decrease n_{dt_o} , n_{wt_o} , n_{t_o} by 1
 - 3 Resample a new assignment $t_n := z_{i,j}$ according to

$$Pr(z_{i,j} = t) \propto \frac{(n_{dt} + \alpha)(n_{wt} + \beta)}{n_t + \bar{\beta}}, \quad \forall t = 1, \dots, T.$$

- 4 Increase n_{dt_n} , n_{wt_n} , n_{t_n} by 1
- Constants
 - J : vocabulary size
 - $\bar{\beta} = \beta \times J$

Access Pattern for Gibbs Sampling



Multinomial Sampling Techniques for $\mathbf{p} \in R_+^T$

| | Initialization | | Generation | Parameter Update |
|-----------------|----------------|-------------|------------------|------------------|
| | Time | Space | Time | Time |
| LSearch | $\Theta(T)$ | $\Theta(1)$ | $\Theta(T)$ | $\Theta(1)$ |
| BSearch | $\Theta(T)$ | $\Theta(1)$ | $\Theta(\log T)$ | $\Theta(T)$ |
| Alias Method | $\Theta(T)$ | $\Theta(T)$ | $\Theta(1)$ | $\Theta(T)$ |
| F+tree Sampling | $\Theta(T)$ | $\Theta(1)$ | $\Theta(\log T)$ | $\Theta(\log T)$ |

- LSearch

- maintain $c_T = \mathbf{p}^\top \mathbf{1}$
- linear search
- $\Theta(1)$ update

- BSearch

- maintain $\mathbf{c} = \text{cumsum}(\mathbf{p})$
- binary search
- no support for update

- Alias Method

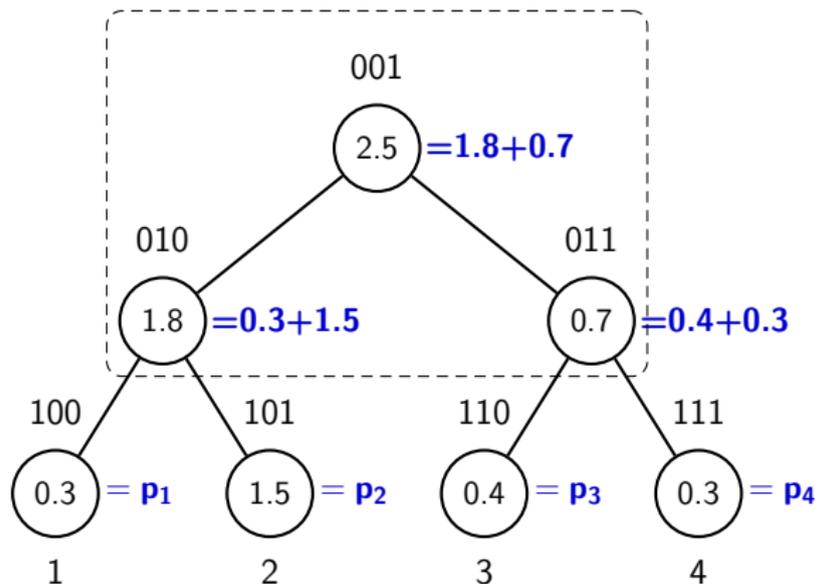
- Alias table
- construction has **some overhead**
- no support for updates

- F+tree

- a variant of Fenwick tree
- construction has **low overhead**
- logarithmic time for sampling and update

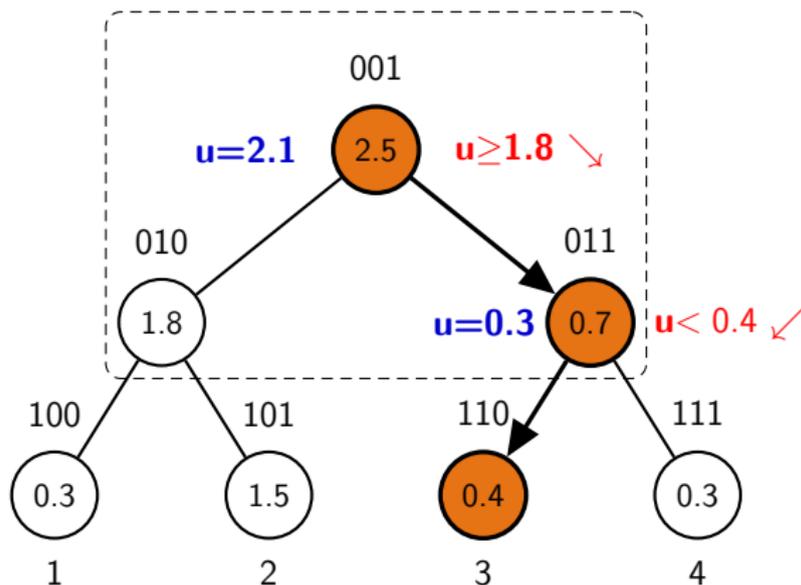
F+Tree: Construction

- Construction in $\Theta(T)$ time
- $\mathbf{p} = [0.3, 1.5, 0.4, 0.3]^T$



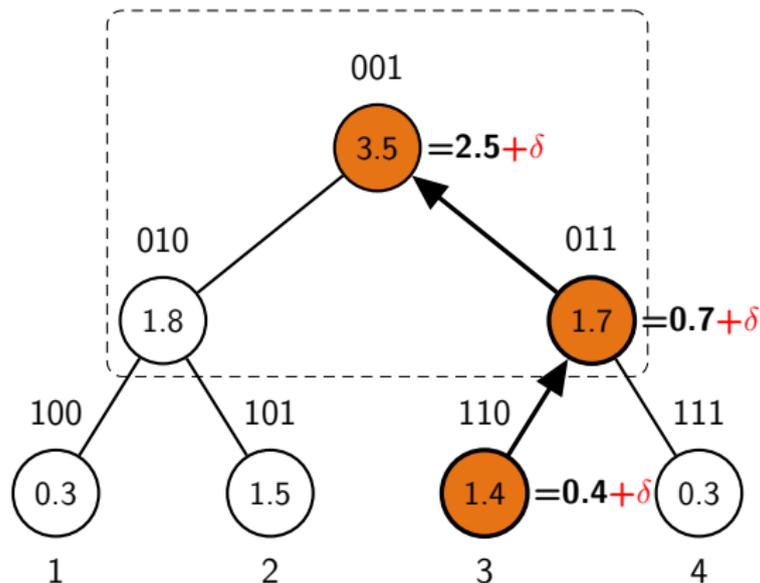
F+Tree: Sampling

- Multinomial sampling in $\Theta(\log T)$ time
- Initial u : a uniformly number drawn from $[0, F[1])$



F+Tree: Update

- Update in $\Theta(\log T)$ time
- $p_3 \leftarrow p_3 + \delta$



F+LDA = LDA with F+tree Sampling

- Decomposition of \mathbf{p}

$$\begin{aligned} p_t &= \frac{(n_{dt} + \alpha)(n_{wt} + \beta)}{n_t + \bar{\beta}}, \quad \forall t = 1, \dots, T. \\ &= \underbrace{\beta \left(\frac{n_{dt} + \alpha}{n_t + \bar{\beta}} \right)}_{q_t} + \underbrace{n_{wt} \left(\frac{n_{dt} + \alpha}{n_t + \bar{\beta}} \right)}_{r_t}. \end{aligned} \quad (1)$$

- $\mathbf{p} = \beta \mathbf{q} + \mathbf{r}$
 - two-level sampling for \mathbf{p}
- \mathbf{q} is dense
 - only 2 entries (q_{t_o}, q_{t_n}) change for each Gibbs step in the same document
 - use F+Tree for \mathbf{q}
- \mathbf{r} is sparse
 - nonzero entries: $T_w := \{t : n_{tw} \neq 0\}$
 - entire \mathbf{r} changes for each Gibbs step
 - use BSearch for \mathbf{r}
- Can also work on word-by-word update sequence

F+LDA: Alternative Decomposition

- Word-by-word Gibbs sampling sequence
- Decomposition of \mathbf{p}

$$\begin{aligned} p_t &= \frac{(n_{dt} + \alpha)(n_{wt} + \beta)}{n_t + \bar{\beta}}, \quad \forall t = 1, \dots, T. \\ &= \underbrace{\alpha \left(\frac{n_{wt} + \beta}{n_t + \bar{\beta}} \right)}_{q_t} + \underbrace{n_{dt} \left(\frac{n_{wt} + \beta}{n_t + \bar{\beta}} \right)}_{r_t}. \end{aligned} \quad (2)$$

- $\mathbf{p} = \alpha \mathbf{q} + \mathbf{r}$
- \mathbf{q} : slight changes for this sequence \Rightarrow use F+Tree
- \mathbf{r} : $|T_d := \{t : n_{dt} \neq 0\}|$ nonzeros \Rightarrow use BSearch

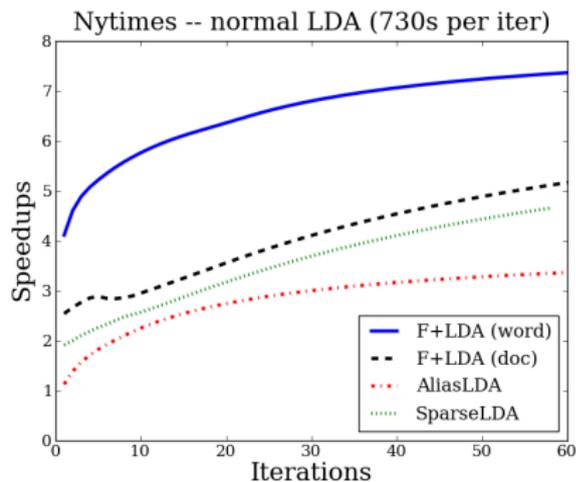
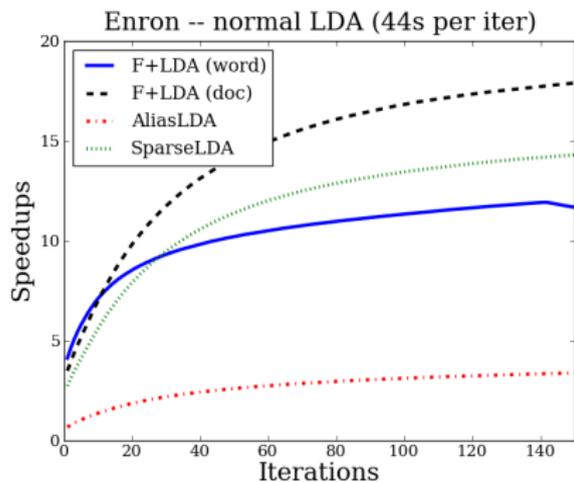
Comparison to Other LDA Sampling

| Sequence Exact? | F+LDA Word-by-Word | | F+LDA Doc-by-Doc | | Sparse-LDA Doc-by-Doc | | | Alias-LDA Doc-by-Doc | |
|-----------------|---|----------------------|--|----------------------|---|-----------------|-----------------|---|-----------------|
| | Yes | | Yes | | Yes | | | No | |
| Decomposition | $\alpha \left(\frac{n_{wt} + \beta}{n_t + \beta} \right) + n_{dt} \left(\frac{n_{wt} + \beta}{n_t + \beta} \right)$ | | $\beta \left(\frac{n_{dt} + \alpha}{n_t + \beta} \right) + n_{wt} \left(\frac{n_{dt} + \alpha}{n_t + \beta} \right)$ | | $\frac{\alpha\beta}{n_t + \beta} + \beta \left(\frac{n_{dt}}{n_t + \beta} \right) + n_{wt} \left(\frac{n_{dt} + \alpha}{n_t + \beta} \right)$ | | | $\alpha \left(\frac{n_{wt} + \beta}{n_t + \beta} \right) + n_{dt} \left(\frac{n_{wt} + \beta}{n_t + \beta} \right)$ | |
| Structure | F+tree | BSearch | F+tree | BSearch | LSearch | LSearch | LSearch | Alias | Alias |
| Fresh samples | Yes | Yes | Yes | Yes | Yes | Yes | Yes | No | Yes |
| Initialization | $\Theta(\log T)$ | $\Theta(T_d)$ | $\Theta(\log T)$ | $\Theta(T_w)$ | $\Theta(1)$ | $\Theta(1)$ | $\Theta(T_w)$ | $\Theta(1)$ | $\Theta(T_d)$ |
| Sampling | $\Theta(\log T)$ | $\Theta(\log T_d)$ | $\Theta(\log T)$ | $\Theta(\log T_w)$ | $\Theta(T)$ | $\Theta(T_d)$ | $\Theta(T_w)$ | $\Theta(\#MH)$ | $\Theta(\#MH)$ |

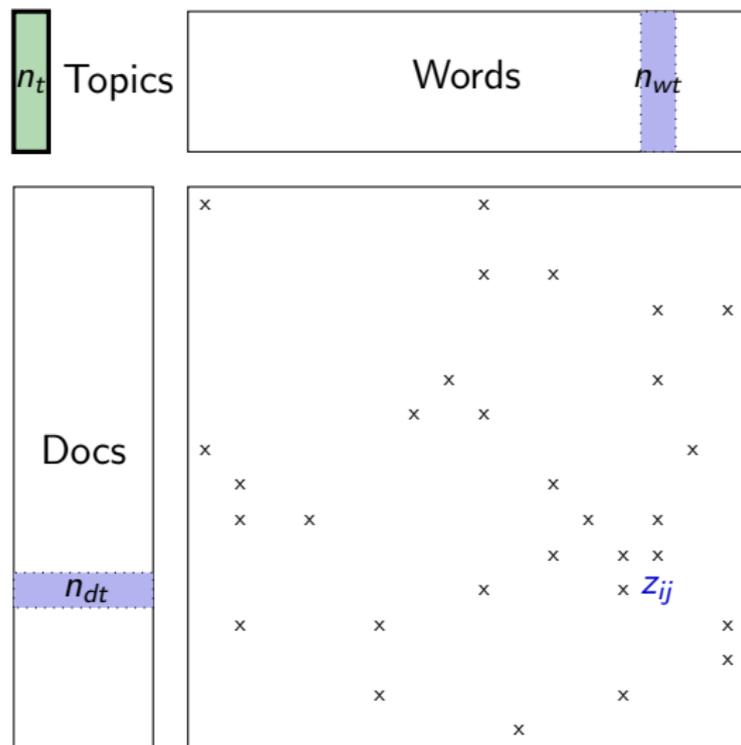
- F+LDA: word-by-word faster than doc-by-doc for large I
 - $|T_d|$ bounded by n_i , but $|T_w|$ approaches to T
 - per Gibbs step cost: $\rho_F \log T + \rho_B |T_d|$
- SparseLDA:
 - per Gibbs step cost: $\Theta(T + |T_d| + |T_w|)$
 - the first $\Theta(T)$ rarely happens but $|T_w| \rightarrow T$ for large I
- AliasLDA:
 - per Gibbs step cost: $\rho_A |T_d| + \#MH$
 - $\rho_A \approx 3 \times \rho_B$: construction overhead of Alias table
 - If $(\rho_A - \rho_B) |T_d| > \rho_F \log T \Rightarrow$ AliasLDA slower than F+LDA
 - say $|T_d| \approx 100$, F+LDA still faster for $T < 2^{50}$

Comparison of various sampling methods

- Single machine, single thread
- y-axis: speedup over normal $O(T)$ multinomial sampling
- Enron: 38K docs with 6M tokens
- NyTimes: 0.3M docs with 100M tokens



Access Pattern for Gibbs Sampling



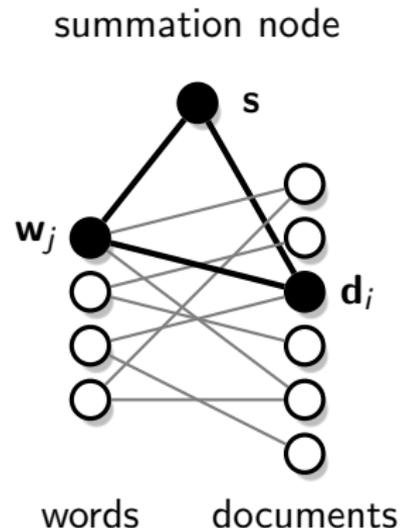
Access Graph for Gibbs Sampling

- $G = (V, E)$: a hyper graph

$$V = \{\mathbf{d}_i\} \cup \{\mathbf{w}_j\} \cup \{\mathbf{s}\}$$

$$E = \{e_{ij} = (\mathbf{d}_i, \mathbf{w}_j, \mathbf{s})\}$$

- Connection to Gibbs sampling
 - $(\mathbf{d}_i)_t := n_{d_i t}$, $(\mathbf{w}_j)_t := n_{w_j t}$, $(\mathbf{s})_t := n_t$
 - each e_{ij} : a Gibbs step for word w_j in d_i access to $(\mathbf{d}_i, \mathbf{w}_j, \mathbf{s})$
- Parallelism: more challenging
 - all edges incident to \mathbf{s}
 - all $(\mathbf{s})_t$ are large in general
 \Rightarrow slightly stale \mathbf{s} is fine for accuracy
 - duplicate \mathbf{s} for parallelism

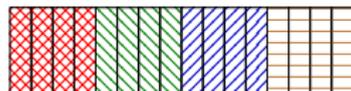


Nomadic Tokens for \mathbf{w}_j

Nomadic Tokens for

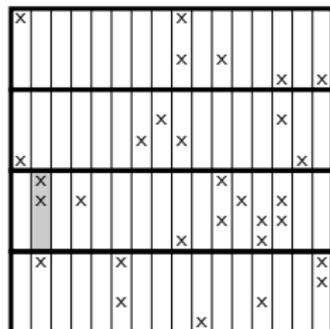
$\{\mathbf{w}_j : j = 1, \dots, J\}$:

- J tokens
- (j, \mathbf{w}_j) : $O(T)$ space



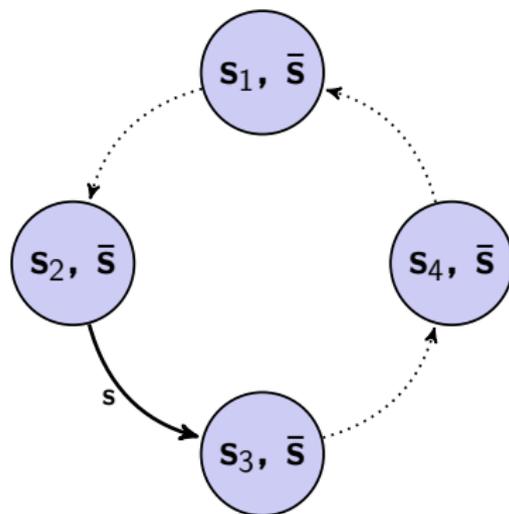
Worker:

- p workers
- a computing unit + a concurrent token queue
- a subset of $\{\mathbf{d}_i\}$: $O(IT/p)$
- "x": an occurrence of a word
- bigger rectangle: a subset of corpus
- smaller rectangle: a unit subtask



Nomadic Token for s : Circular Delta Update

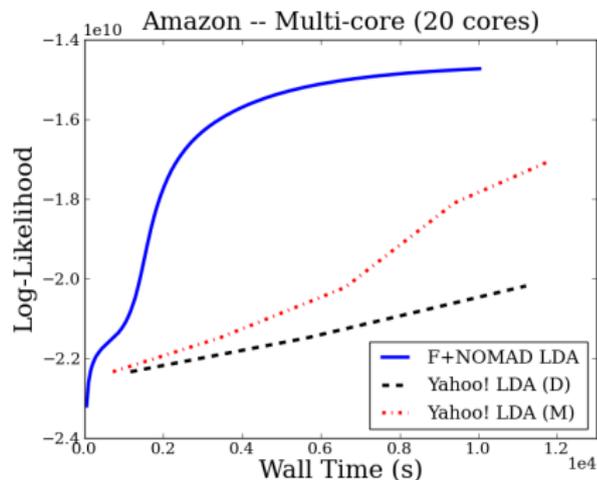
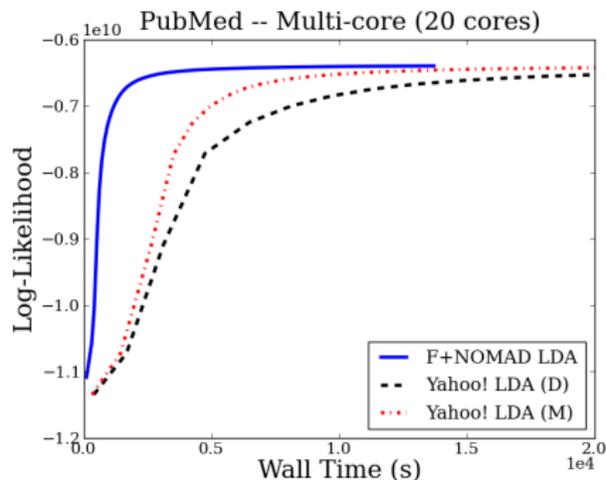
- Single global s
 - travels among machines as a messenger
 - broadcasts local delta updates
- Every machine p : (s_p, \bar{s})
 - s_p : local working copy
 - \bar{s} : snapshot version of global s



$$\begin{aligned} s &\leftarrow s + (s_3 - \bar{s}) \\ \bar{s} &\leftarrow s \\ s_3 &\leftarrow s \end{aligned}$$

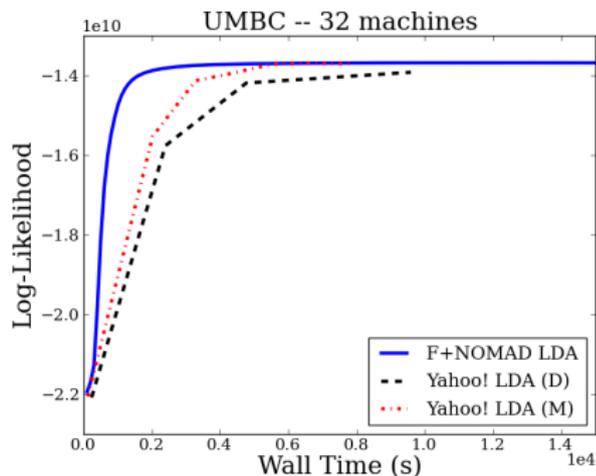
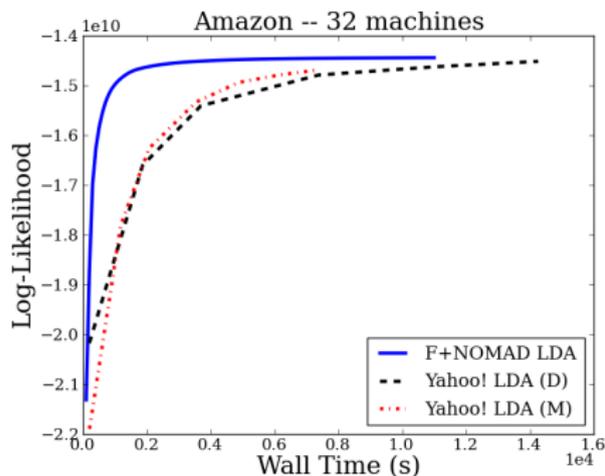
Comparison on a single multi-core machine

- On a machine with a 20-core processor
- Comparison: F+NOMAD LDA, Yahoo! LDA
- PubMed: 9M docs with 700M tokens
- Amazon: 30M docs with 1.5B tokens



Comparison on a Multi-machine System

- 32 machines, each with a 20-core processor.
- Comparison: F+NOMAD LDA, Yahoo! LDA
- Amazon: 30M docs with 1.5B tokens
- UMBC: 40M docs with 1.5B tokens



Conclusions

- NOMAD framework uses nomadic tokens to provide
 - Asynchronous computation
 - Non-blocking communication
 - Lock-free implementation
 - Serializable or near Serializable
- Recommender System: Matrix factorization
 - scalable parallel stochastic gradient
 - Serializability guarantee
- Topic Modeling: Latent Dirichlet Allocation
 - Logarithmic F+tree sampling
 - Efficient Gibbs Sampling
 - Duplicated nomadic tokens for the common node
 - Outperforms Yahoo! LDA