

# CME 193: Introduction to Scientific Python

## Lecture 5: Numpy, Scipy, Matplotlib

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# Contents

- Second part of course
- Numpy
- Scipy
- Matplotlib
- Exercises

# Congrats, we are halfway!

Up to now

- Covered the basics of Python
- Worked on a bunch of tough exercises

From now

- Cover specific topics
- Less exercises
- Time for project

# Feedback

Thanks for the great feedback, very useful

## Remaining topics

- Numpy, Scipy, Matplotlib (today)
- IPython notebooks, Pandas, Statsmodels, SKLearn
- Exception handling, unit testing, recursion
- Brief look at some more modules
  - Flask
  - Regex
  - ... (suggestions welcome)

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- **Numpy**
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# Numpy

- Fundamental package for scientific computing with Python
- N-dimensional array object
- Linear algebra, Fourier transform, random number capabilities
- Building block for other packages (e.g. Scipy)
- Open source

# Numpy

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## import numpy as np

Basics:

```
import numpy as np

A = np.array([[1, 2, 3], [4, 5, 6]])
print A
# [[1 2 3]
#   [4 5 6]]

Af = np.array([1, 2, 3], float)
```

Slicing as usual.

## More basics

```
np.arange(0, 1, 0.2)
# array([ 0. ,  0.2,  0.4,  0.6,  0.8])

np.linspace(0, 2*np.pi, 4)
# array([ 0.0,  2.09,  4.18,  6.28])

A = np.zeros((2,3))
# array([[ 0.,  0.,  0.],
#        [ 0.,  0.,  0.]])
# np.ones, np.diag
A.shape
# (2, 3)
```

## More basics

```
np.random.random((2,3))
# array([[ 0.78084261,  0.64328818,  0.55380341],
#        [ 0.24611092,  0.37011213,  0.83313416]])

a = np.random.normal(loc=1.0, scale=2.0, size=(2,2))
# array([[ 2.87799514,  0.6284259 ],
#        [ 3.10683164,  2.05324587]])

np.savetxt("a_out.txt", a)
# save to file
b = np.loadtxt("a_out.txt")
# read from file
```

## Arrays are mutable

```
A = np.zeros((2, 2))
# array([[ 0.,  0.],
#        [ 0.,  0.]])
C = A
C[0, 0] = 1

print A
# [[ 1.  0.]
#   [ 0.  0.]])
```

# Array attributes

```
a = np.arange(10).reshape((2,5))

a.ndim      # 2 dimension
a.shape     # (2, 5) shape of array
a.size      # 10 # of elements
a.T         # transpose
a.dtype     # data type
```

# Basic operations

Arithmetic operators: **elementwise** application

```
a = np.arange(4)
# array([0, 1, 2, 3])

b = np.array([2, 3, 2, 4])

a * b # array([ 0,  3,  4, 12])
b - a # array([2, 2, 0, 1])

c = [2, 3, 4, 5]
a * c # array([ 0,  3,  8, 15])
```

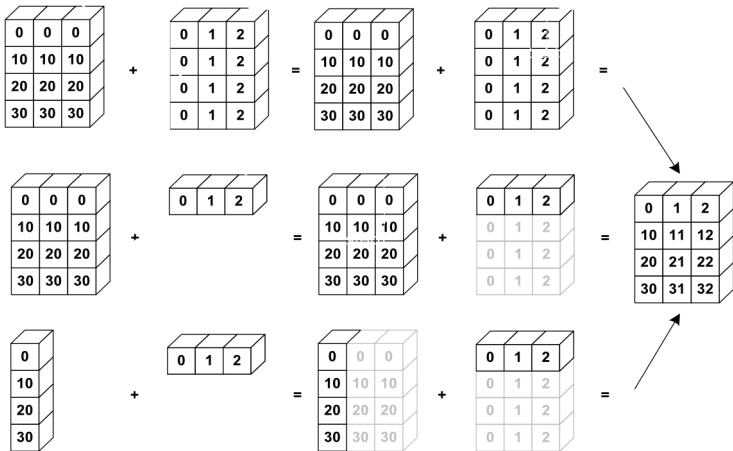
Also, we can use += and \*=.

# Array broadcasting

When operating on two arrays, numpy compares shapes. Two dimensions are compatible when

1. They are of equal size
2. One of them is 1

# Array broadcasting





## Array broadcasting with scalars

This also allows us to add a constant to a matrix or multiply a matrix by a constant

```
A = np.ones((3,3))
```

```
print 3 * A - 1
```

```
# [[ 2.  2.  2.]
```

```
# [ 2.  2.  2.]
```

```
# [ 2.  2.  2.]]
```

# Vector operations

- inner product
- outer product
- dot product (matrix multiplication)

```
# note: numpy automatically converts lists
u = [1, 2, 3]
v = [1, 1, 1]

np.inner(u, v)
# 6
np.outer(u, v)
# array([[1, 1, 1],
#        [2, 2, 2],
#        [3, 3, 3]])
np.dot(u, v)
# 6
```

# Matrix operations

First, define some matrices:

```
A = np.ones((3, 2))
# array([[ 1.,  1.],
#        [ 1.,  1.],
#        [ 1.,  1.]])
A.T
# array([[ 1.,  1.,  1.],
#        [ 1.,  1.,  1.]])

B = np.ones((2, 3))
# array([[ 1.,  1.,  1.],
#        [ 1.,  1.,  1.]])
```

# Matrix operations

```
np.dot(A, B)
# array([[ 2.,  2.,  2.],
#        [ 2.,  2.,  2.],
#        [ 2.,  2.,  2.]])

np.dot(B, A)
# array([[ 3.,  3.],
#        [ 3.,  3.]])

np.dot(B.T, A.T)
# array([[ 2.,  2.,  2.],
#        [ 2.,  2.,  2.],
#        [ 2.,  2.,  2.]])

np.dot(A, B.T)
# Traceback (most recent call last):
#   File "<stdin>", line 1, in <module>
# ValueError: shapes (3,2) and (3,2) not aligned: ...
# ... 2 (dim 1) != 3 (dim 0)
```

## Operations along axes

```
a = np.random.random((2,3))
# array([[ 0.9190687 ,  0.36497813,  0.75644216],
#        [ 0.91938241,  0.08599547,  0.49544003]])
a.sum()
# 3.5413068994445549
a.sum(axis=0) # column sum
# array([ 1.83845111,  0.4509736 ,  1.25188219])
a.cumsum()
# array([ 0.9190687 ,  1.28404683,  2.04048899,  2.9598714 ,
#        3.04586687,  3.5413069 ])
a.cumsum(axis=1) # cumulative row sum
# array([[ 0.9190687 ,  1.28404683,  2.04048899],
#        [ 0.91938241,  1.00537788,  1.50081791]])
a.min()
# 0.0859954690403677
a.max(axis=0)
# array([ 0.91938241,  0.36497813,  0.75644216])
```

# Slicing arrays

## More advanced slicing

```
a = np.random.random((4,5))  
  
a[2, :]  
# third row, all columns  
a[1:3]  
# 2nd, 3rd row, all columns  
a[:, 2:4]  
# all rows, columns 3 and 4
```

# Iterating over arrays

- Iterating over multidimensional arrays is done with respect to the first axis: `for row in A`
- Looping over all elements: `for element in A.flat`

# Reshaping

Reshape using `reshape`. Total size must remain the same.

Resize using `resize`, always works: chopping or appending zeros

First dimension has 'priority', so beware of unexpected results

Try it!



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# Reshaping

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First dimension has 'priority', so beware of unexpected results

Try it!

# Matrix operations

```
import numpy.linalg
```

|                                  |                   |
|----------------------------------|-------------------|
| <code>eye(3)</code>              | Identity matrix   |
| <code>trace(A)</code>            | Trace             |
| <code>column_stack((A,B))</code> | Stack column wise |
| <code>row_stack((A,B,A))</code>  | Stack row wise    |

# Linear algebra

```
import numpy.linalg
```

|                           |   |
|---------------------------|---|
| <code>qr</code>           | Computes the QR decomposition                       |
| <code>cholesky</code>     | Computes the Cholesky decomposition                 |
| <code>inv(A)</code>       | Inverse   |
| <code>solve(A,b)</code>   | Solves $Ax = b$ for $A$ full rank                   |
| <code>lstsq(A,b)</code>   | Solves $\arg \min_x \ Ax - b\ _2$                   |
| <code>eig(A)</code>       | Eigenvalue decomposition                            |
| <code>eig(A)</code>       | Eigenvalue decomposition for symmetric or hermitian |
| <code>eigvals(A)</code>   | Computes eigenvalues.                               |
| <code>svd(A, full)</code> | Singular value decomposition                        |
| <code>pinv(A)</code>      | Computes pseudo-inverse of $A$                      |

# Fourier transform

```
import numpy.fft
```

- `fft` 1-dimensional DFT
- `fft2` 2-dimensional DFT
- `fftn` N-dimensional DFT
- `ifft` 1-dimensional inverse DFT (etc.)
- `rfft` Real DFT (1-dim)
- `ifft` Imaginary DFT (1-dim)

# Random sampling

```
import numpy.random
```

|                                       |                                |
|---------------------------------------|--------------------------------|
| <code>rand(d0,d1,...,dn)</code>       | Random values in a given shape |
| <code>randn(d0, d1, ...,dn)</code>    | Random standard normal         |
| <code>randint(lo, hi, size)</code>    | Random integers [lo, hi)       |
| <code>choice(a, size, repl, p)</code> | Sample from a                  |
| <code>shuffle(a)</code>               | Permutation (in-place)         |
| <code>permutation(a)</code>           | Permutation (new array)        |

## Distributions in random

```
import numpy.random
```

The list of distributions to sample from is quite long, and includes

- beta
- binomial
- chisquare
- exponential
- dirichlet
- gamma
- laplace
- lognormal
- pareto
- poisson
- power

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# What is SciPy?

SciPy is a library of algorithms and mathematical tools built to work with NumPy arrays.

- linear algebra - *scipy.linalg*
- statistics - *scipy.stats*
- optimization - *scipy.optimize*
- sparse matrices - *scipy.sparse*
- signal processing - *scipy.signal*
- etc.

# Scipy Linear Algebra

Slightly different from `numpy.linalg`. Always uses BLAS/LAPACK support, so could be faster.

Some more functions.

Functions can be slightly different.

# Scipy Optimization

- General purpose minimization: CG, BFGS, least-squares
- Constrained minimization; non-negative least-squares
- Minimize using simulated annealing
- Scalar function minimization
- Root finding
- Check gradient function
- Line search

# Scipy Statistics

- Mean, median, mode, variance, kurtosis
- Pearson correlation coefficient
- Hypothesis tests (ttest, Wilcoxon signed-rank test, Kolmogorov-Smirnov)
- Gaussian kernel density estimation

See also SciKits (or scikit-learn).

# Scipy sparse

- Sparse matrix classes: CSC, CSR, etc.
- Functions to build sparse matrices
- `sparse.linalg` module for sparse linear algebra
- `sparse.csgraph` for sparse graph routines

# Scipy signal

- Convolutions
- B-splines
- Filtering
- Continuous-time linear system
- Wavelets
- Peak finding

# Scipy IO

## Methods for loading and saving data

- Matlab files
- Matrix Market files (sparse matrices)
- Wav files

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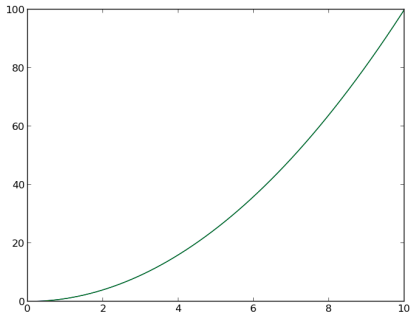
# What is Matplotlib?

- Plotting library for Python
- Works well with Numpy
- Syntax similar to Matlab

# Scatter Plot

```
import numpy as np
import matplotlib.pyplot as plt

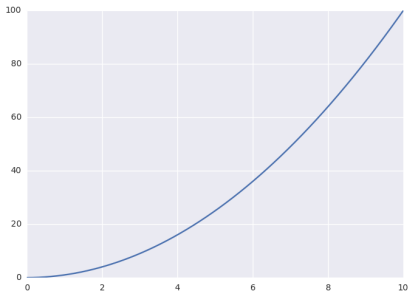
x = np.linspace(0, 10, 1000)
y = np.power(x, 2)
plt.plot(x, y)
plt.show()
```



## Seaborn makes plot pretty

```
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
```

```
x = np.linspace(0, 10, 1000)
y = np.power(x, 2)
plt.plot(x, y)
plt.show()
```



# Scatter Plot

## Adding titles and labels

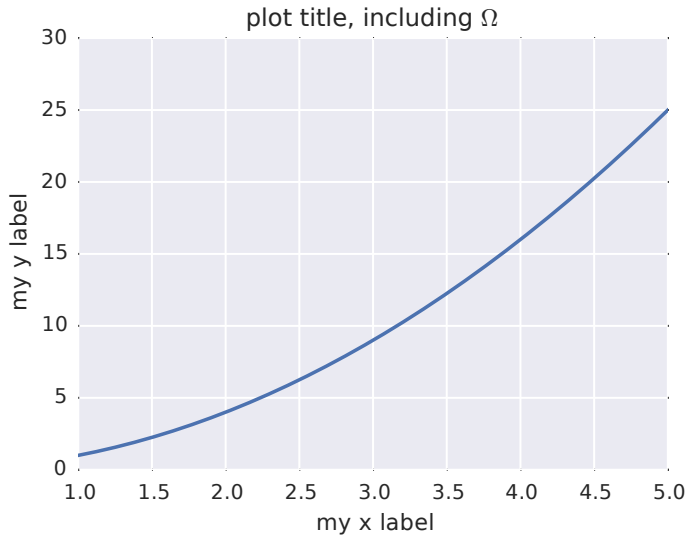
```
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns

f, ax = plt.subplots(1, 1, figsize=(5,4))

x = np.linspace(0, 10, 1000)
y = np.power(x, 2)
ax.plot(x, y)
ax.set_xlim((1, 5))
ax.set_ylim((0, 30))
ax.set_xlabel('my x label')
ax.set_ylabel('my y label')
ax.set_title('plot title, including  $\Omega$ ')

plt.tight_layout()
plt.savefig('line_plot_plus.pdf')
```

# Scatter Plot



# Scatter Plot

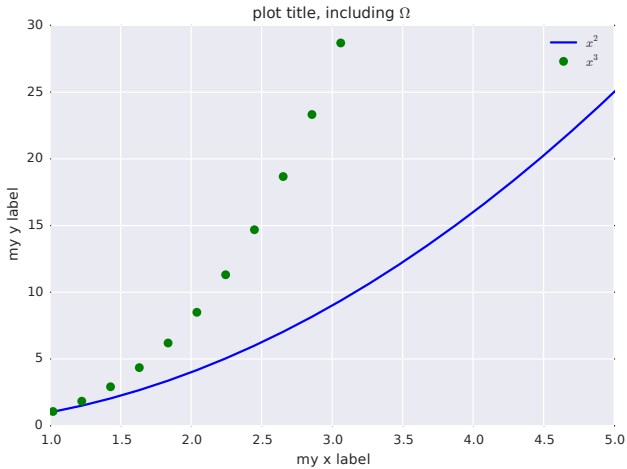
Adding multiple lines and a legend

```
x = np.linspace(0, 10, 50)
y1 = np.power(x, 2)
y2 = np.power(x, 3)

plt.plot(x, y1, 'b-', label='$x^2$')
plt.plot(x, y2, 'go', label='$x^3$')
plt.xlim((1, 5))
plt.ylim((0, 30))
plt.xlabel('my x label')
plt.ylabel('my y label')
plt.title('plot title, including $\Omega$')
plt.legend()

plt.savefig('line_plot_plus2.pdf')
```

# Scatter Plot



# Histogram

```
data = np.random.randn(1000)

f, (ax1, ax2) = plt.subplots(1, 2, figsize=(6,3))

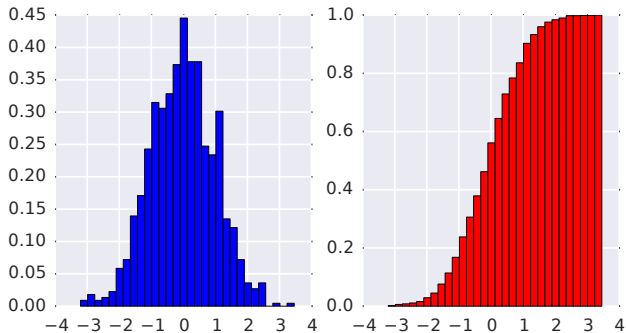
# histogram (pdf)
ax1.hist(data, bins=30, normed=True, color='b')

# empirical cdf
ax2.hist(data, bins=30, normed=True, color='r',
          cumulative=True)

plt.savefig('histogram.pdf')
```



# Histogram



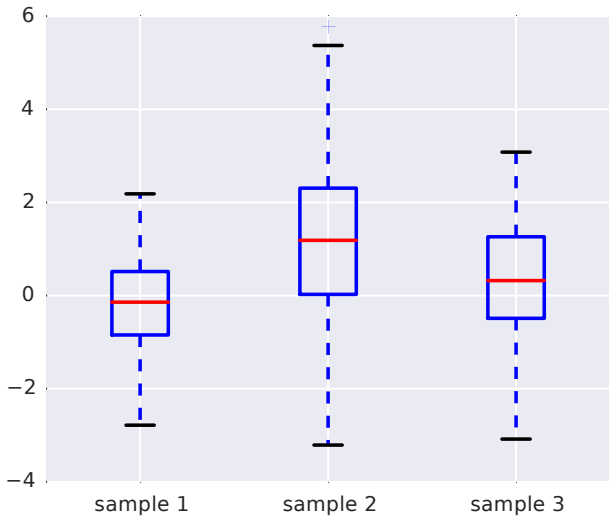
# Box Plot

```
samp1 = np.random.normal(loc=0., scale=1., size=100)
samp2 = np.random.normal(loc=1., scale=2., size=100)
samp3 = np.random.normal(loc=0.3, scale=1.2, size=100)

f, ax = plt.subplots(1, 1, figsize=(5,4))

ax.boxplot((samp1, samp2, samp3))
ax.set_xticklabels(['sample 1', 'sample 2', 'sample 3'])
plt.savefig('boxplot.pdf')
```

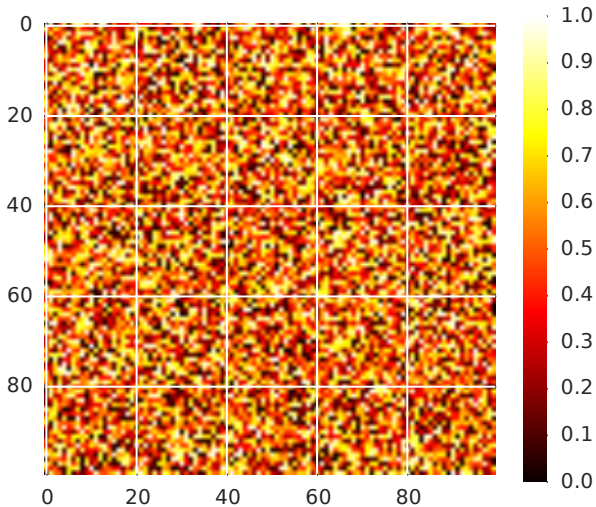
# Box Plot



# Image Plot

```
A = np.random.random((100, 100))  
  
plt.imshow(A)  
plt.hot()  
plt.colorbar()  
  
plt.savefig('imageplot.pdf')
```

# Image Plot



# Wire Plot

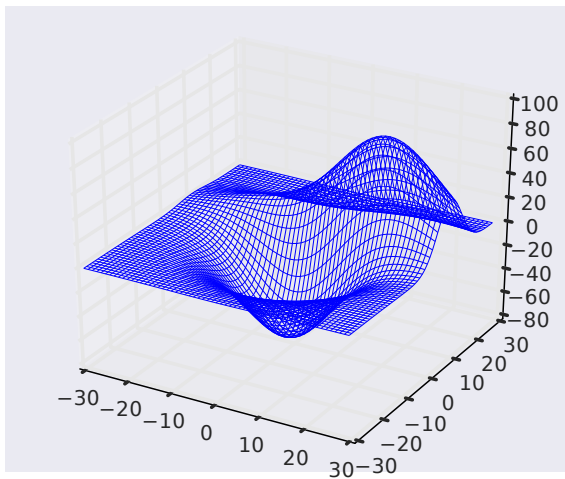
matplotlib toolkits extend functionality for other kinds of visualization

```
from mpl_toolkits.mplot3d import axes3d

ax = plt.subplot(111, projection='3d')
X, Y, Z = axes3d.get_test_data(0.1)
ax.plot_wireframe(X, Y, Z, linewidth=0.1)

plt.savefig('wire.pdf')
```

# Wire Plot







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# Exercises

See course website for exercises for this week.

Get to know the person next to you and do them in pairs!

Let me know if you have any question

Class ends at 5:35pm.