

The Theory of Black Holes

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Course Syllabus for the 2016 CRAQ Summer School on Compact Objects

1. A primer in General Relativity

- a) Motivation for a theory beyond Newtonian gravity
- b) The equivalence principle
- c) Special relativity, Lorentz transformations and spacetime diagrams
- d) Gravity as spacetime curvature
- e) Describing curved spacetimes with differential geometry, 4-vectors and tensors
- f) Motion along geodesics
- g) Observations and measurements as co-ordinate transformations of 4-vectors
- h) The Einstein field equations

2. Black holes in General Relativity

- a) The Schwarzschild metric
- b) Gravitational redshift
- c) Radial and circular motion
- d) Stability of orbits
- e) Gravitational lensing
- f) Event horizons
- g) Spinning black holes and the Kerr metric

3. Accretion physics

- a) Classical Shakura & Sunyaev accretion disks, dynamics and observed thermal emission
- b) Accretion efficiency
- c) Radiatively inefficient accretion flows

4. Theoretical modelling of black hole accretion

- a) Introduction to ideal magnetohydrodynamics
- b) Magnetic pressure and MHD waves
- c) Magnetic flux freezing, viscosity and reconnection
- d) Producing X-ray continuum emission in a Comptonizing corona
- e) The principles of general relativistic magnetohydrodynamics (GRMHD)

5. Jets

- a) Extracting energy from black holes through the Penrose process
- b) The Blandford-Znajek mechanism

6. Observations of black holes and bridging the gap between theory & observations

- a) X-ray reflection from black holes accretion discs
- b) Relativistic blurring of X-ray emission lines
- c) General relativistic ray tracing simulations
- d) X-ray timing and reverberation from accretion discs
- e) Measuring the structure of the corona